

### Example 1

It is known that 12% of the calculators shipped from a particular factory are defective.  $n=6$   
 $p=0.12$   
 $1-p=0.88$

- a. What is the probability that exactly three of six chosen calculators are defective?

$${}^6C_3 (0.12)^3 (0.88)^3 = 0.0236$$

- b. What is the probability that none in a random sample of six calculators is defective?

$${}^6C_0 (0.12)^0 (0.88)^6 = 0.4644$$

- c. What is the probability that at least one in a random sample of six calculators is defective?

$$A = 1, 2, 3, 4, 5, \text{ or } 6$$

$$A' = 0$$

$$\begin{aligned} P(A) &= 1 - P(A') \\ &= 1 - 0.4644 \\ &= 0.5356 \end{aligned}$$

### Example 2

Twenty-five percent of the CFA candidates have a degree in economics. A random sample of four CFA candidates is selected.  $n=4$   $p=0.25$   $1-p=0.75$

- a. What is the probability that none of them has a degree in economics?

$${}^4C_0 (0.25)^0 (0.75)^4 = 0.3164$$

- b. What is the probability that at least one of them has a degree in economics?

$$A = 1, 2, 3, \text{ or } 4 \quad P(A) = 1 - P(A') = 1 - 0.3164 = 0.6836$$

### Example 3

On a particular production line, the likelihood that a light bulb is defective is 8%. Fifteen light bulbs are randomly selected.  $n=15$   $p=0.08$   $1-p=0.92$

- a. What is the probability that two light bulbs will be defective?

$${}^{15}C_2 (0.08)^2 (0.92)^{13} = 0.2273$$

- b. What is the probability that none of the light bulbs will be defective?

$${}^{15}C_0 (0.08)^0 (0.92)^{15} = 0.2863$$

- c. What are the mean and variance of the number of defective bulbs?

$$E(x) = np = (15)(0.08) = 1.2$$

$$V(x) = np(1-p) = (15)(0.08)(0.92) = 1.104$$

#### Example 4

For a particular clothing store, a marketing firm finds that 22% of \$10-off coupons delivered by mail are redeemed. Suppose ten customers are randomly selected and are mailed \$10-off coupons.  $n = 10$   $p = 0.22$

- a. What is the probability that three of the customers redeem the coupon?

$${}^{10}C_3 (0.22)^3 (0.78)^7 = 0.2244$$

- b. What is the probability that no more than one of the customers redeems the coupon?

$$\begin{array}{l} 0 \text{ or } 1 \\ {}^{10}C_0 (0.22)^0 (0.78)^{10} + {}^{10}C_1 (0.22)^1 (0.78)^9 = 0.3185 \\ 0.0834 + 0.2351 \end{array}$$

- c. What is the probability that at least two of the customers redeem the coupon?

$$\begin{array}{l} 2, 3, 4, \dots, 10 \\ \text{(not 0 or 1)} \end{array} \quad 1 - 0.3185 = 0.6815$$

- d. What is the expected number of coupons that will be redeemed?

$$E(x) = np = (10)(0.22) = 2.2$$

#### Example 5

According to a Department of Labor report, the city of Detroit had a 18% unemployment rate in May of 2011. Five working-age residents were chosen at random.

$$n = 5 \quad p = 0.18 \quad 1 - p = 0.82$$

- a. What is the probability that exactly one of the residents was unemployed?

$${}^5C_1 (0.18)^1 (0.82)^4 = 0.4069$$

- b. What is the probability that at least two of the residents were unemployed?

$$\begin{array}{l} 2, 3, 4, \text{ or } 5 \\ \text{(not 0 or 1)} \end{array} \quad 1 - {}^5C_0 (0.18)^0 (0.82)^5 + 0.4069 = 1 - 0.7776 = 0.2224$$

- c. What is the probability that exactly four residents were unemployed?

$${}^5C_4 (0.18)^4 (0.82)^1 = 0.0043$$

- d. What was the expected number of unemployed residents when five working-age residents were randomly selected?

$$E(x) = np = (5)(0.18) = 0.9$$

### Example 6

Chauncey Billups, a current shooting guard for the Los Angeles Clippers, has a career free-throw percentage of 89.4%. Suppose he shoots four free throws in tonight's game.

- $n=4$     $p=0.894$     $1-p=0.106$   
a. What is the probability that Billups makes all four free throws?

$$4C4 (0.894)^4 (0.106)^0 = 0.6388$$

- b. What is the probability that Billups makes three or more of his free throws?

3 or 4

$$4C3 (0.894)^3 (0.106)^1 + 0.6388 = 0.9417$$

- c. What is the expected number of free throws that Billups will make?

$$E(x) = np = (4)(0.894) = 3.576$$

- d. What is the standard deviation of the number of free throws that Billups will make?

$$SD(x) = \sqrt{np(1-p)} = \sqrt{4(0.894)(0.106)} = 0.6157$$

### Answers

1. 0.0236, 0.4644, 0.5356
2. 0.3164, 0.6836
3. 0.2273, 0.2863, 1.2, 1.104
4. 0.2244, 0.3185, 0.6815, 2.2
5. 0.4069, 0.2224, 0.0043, 0.9
6. 0.6388, 0.9417, 3.576, 0.6157