

一、选择题

1.B

2.C

二、选择题

1.  $F(b, c) - F(a, c)$

2.3

3.  $\frac{10!}{1! \cdot 5! \cdot 3! \cdot 1!} (7\%) (43\%)^5 (35\%)^3 (15\%) \approx 3.34\%$ .

三、解答题

1.  $X_1, X_2$  的取值只能是 0, 1. 于是

$$P(X_1 = 0, X_2 = 0) = P(Y \leq 1, Y \leq 2) = P(Y \leq 1) = 1 - e^{-1}$$

$$P(X_1 = 0, X_2 = 1) = P(Y \leq 1, Y > 2) = 0$$

$$P(X_1 = 1, X_2 = 0) = P(Y > 1, Y \leq 2) = P(1 < Y \leq 2) = e^{-1} - e^{-2}$$

$$P(X_1 = 1, X_2 = 1) = P(Y > 1, Y > 2) = P(Y > 2) = e^{-2}$$

于是分布律为

$X_1 \backslash X_2$	0	1
0	$1 - e^{-1}$	0
1	$e^{-1} - e^{-2}$	$e^{-2}$

2.  $X = 0, 1, 2, 3, Y = 0, 1, 2$ . 于是

$$\begin{aligned}
 P(X=0, Y=0) &= 0 & P(X=0, Y=1) &= 0 & P(X=0, Y=2) &= \frac{C_2^2 C_2^2}{C_4^4} \\
 P(X=1, Y=0) &= 0 & P(X=1, Y=1) &= \frac{C_3^1 C_2^1}{C_7^4} & P(X=1, Y=2) &= \frac{C_3^1 C_2^2 C_2^1}{C_{74}^4} \\
 P(X=2, Y=0) &= \frac{C_3^2 C_2^2}{C_4^4} & P(X=2, Y=1) &= \frac{C_3^2 C_2^1 C_2^1}{C_7^4} & P(X=2, Y=2) &= \frac{C_3^2 C_2^2 C_2^1}{C_7^4} \\
 P(X=3, Y=0) &= \frac{C_3^3 C_2^1}{C_7^4} & P(X=3, Y=1) &= \frac{C_3^3 C_2^1}{C_7^4} & P(X=3, Y=2) &= 0
 \end{aligned}$$

Y \ X	0	1	2	3
0	0	0	$\frac{C_3^2 C_2^2}{C_4^4}$	$\frac{C_3^3 C_2^1}{C_7^4}$
1	0	$\frac{C_3^1 C_2^1}{C_7^4}$	$\frac{C_3^2 C_2^1 C_2^1}{C_7^4}$	$\frac{C_3^2 C_2^1}{C_7^4}$
2	$\frac{C_3^2 C_2^2}{C_7^4}$	$\frac{C_3^1 C_2^2 C_2^1}{C_7^4}$	$\frac{C_3^2 C_2^2 C_2^1}{C_7^4}$	0

3.(1)

$$\begin{aligned}
 \iint f(x, y) dx dy &= 1. \\
 \Rightarrow c \int_0^\infty e^{-2x} dx \int_0^\infty e^{-4y} dy &= 1 \\
 \Rightarrow c &= 8.
 \end{aligned}$$

(2)

$$\begin{aligned}
 P(X > 2) &= \int_2^\infty \int_0^\infty 8e^{-(2x+4y)} dx dy = e^{-4} \\
 P(X > Y) &= \int_0^\infty \int_0^x 8e^{-(2x+4y)} dx dy = \frac{2}{3}. \\
 P(X + Y < 1) &= \int_0^1 \int_0^{1-x} 8e^{-(2x+4y)} dy dx = 1 - 2e^{-2} + e^{-4}.
 \end{aligned}$$

(3)

$$F(x, y) = \begin{cases} (1 - e^{-2x})(1 - e^{-4y}) & x < 0, y > 0, \\ 0, & \text{其它} \end{cases}$$