

1. Academic Honesty.

- An permissible and honest work means that one finish the work by their own. without copying from others or other not-permitted resources. for collaboration work, carefully clarify how partners collaborate in the project and cite every related resource that helped.
- Copying from others, collaborating an assignment without permission, use of views or opinions from others without acknowledgement.

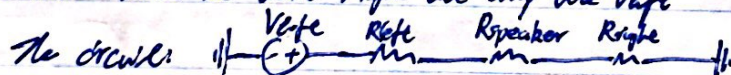
2. Island Karaoke Machine.

$$R_{\text{left}} = R_{\text{right}} = 3\Omega, R_{\text{speaker}} = 4\Omega$$

$$V_{\text{left}} = V_{\text{vocals}}, V_{\text{right}} = V_{\text{vocals}} + V_{\text{instrument}}, V_{\text{vocal}} = 120.524 \text{ mV}, V_{\text{instrument}} = 50 \text{ mV}$$

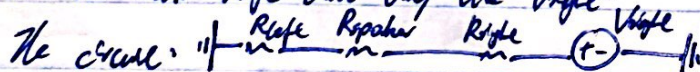
- Since, $V_{\text{right}} = V_{\text{left}} + V_{\text{instrument}}, |V_{\text{right}}| > |V_{\text{left}}|$

Use superposition: when we short V_{right} and only use V_{left}



$$\text{Thus } V_{\text{speaker},1} = V_{\text{left}} \times \frac{R_{\text{speaker}}}{\Sigma R} = V_{\text{vocal}} \times \frac{4\Omega}{3\Omega + 4\Omega} = 0.4 V_{\text{vocals}}$$

- When we short V_{left} and only use V_{right} :



$$\text{Thus } V_{\text{speaker},2} = V_{\text{right}} \times \frac{R_{\text{speaker}}}{\Sigma R} = (V_{\text{vocals}} + V_{\text{instrument}}) \times \frac{4\Omega}{10\Omega} = 0.4(V_{\text{vocals}} + V_{\text{instrument}})$$

since $|V_{\text{right}}| > |V_{\text{left}}|$, we see the current as from V_{right} to V_{left} .

$$\text{Thus } V_{\text{speaker}} = V_{\text{speaker},2} - V_{\text{speaker},1} = 0.4 \times V_{\text{instrument}} = 20 \text{ mV}$$

Not depend on V_{vocals} .

(Hear Instrument only)

$$b) P_{\text{speaker}} = V_{\text{speaker}} I_{\text{speaker}} = \frac{V_{\text{speaker}}^2}{R_{\text{speaker}}} = \frac{(20 \text{ mV})^2}{4 \Omega} = \frac{400}{4} \times 10^{-6} \text{ W} = 1 \times 10^{-4} \text{ W}$$

c) As discussed in part a), we know that $V_{\text{speaker}} = V_{\text{speaker},2} - V_{\text{speaker},1}$

If we use amplifiers, then it's same that we amplify $V_{\text{speaker},2,1}$, thus it equals that

$$V_{\text{speaker}} = 100 \times (-1)^i \times 0.4 (V_{\text{out},i} + V_{\text{in},i}) - 100 \times (-1)^j (V_{\text{out},j}) \times 0.4 \\ = 40 V_{\text{in},i} ((-1)^i - (-1)^j) + 40 \times (-1)^j V_{\text{in},i}$$

Since we drive using $V_{\text{in},i}$, then $(-1)^i - (-1)^j = 0$ thus $i=j$ thus the two amplifiers must be the same kind, and since $i=0$ or 1 and here in order to make $(-1)^i$ be positive, we use $i=j=0$, which means non-inverting amplifiers.

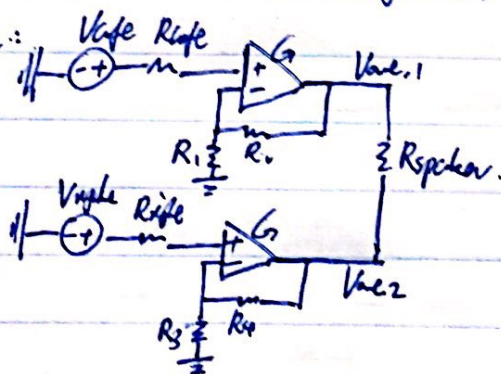
$$\text{Thus } V_{\text{speaker}} = 100 \times V_{\text{speaker, original}} = 200 \text{ mV} = 2 \text{ V} \quad \leftarrow (\text{not } V_{\text{in},i} \times 0.4) \\ \text{Difference} = 100 \times (V_{\text{in},1} - V_{\text{in},2}) = 100 \times V_{\text{in},i}$$

$$d) P_{\text{speaker}} = 1 \text{ W} = 10^4 \times P_{\text{speaker, original}} = 10^4 \times \frac{V_{\text{speaker, original}}^2}{R_{\text{speaker}}}$$

$$\text{Thus } V_{\text{speaker, new}} = 10^2 \times V_{\text{original}} = 100 \times 20 \text{ mV} = 2 \text{ V.}$$

As stated in c), we use both non-inverting amplifiers.

Thus the circuit:



$$\text{Thus } |V_{\text{out},1} - V_{\text{out},2}| = 2 \text{ V}$$

$$= G(V_{\text{in},1} - V_{\text{in},2})$$

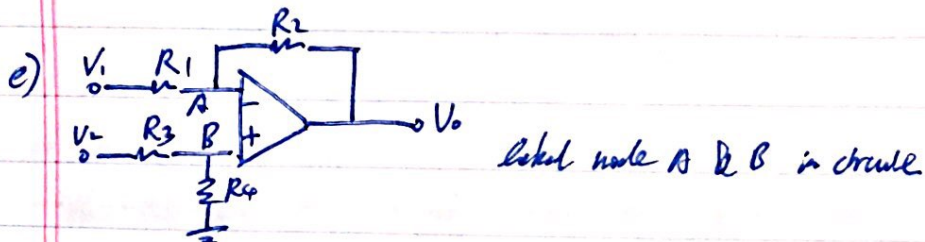
$$= G \cdot V_{\text{in},i}$$

$$= G \times 50 \times 10^{-3} \text{ V}$$

$$\Rightarrow G = 40$$

$$\text{And since } V_{\text{out}} = (1 + \frac{R_2}{R_1}) V_{\text{in}} \text{ for non-inverting amplifier, } 1 + \frac{R_2}{R_1} = 40 \Rightarrow R_2 = 39 R_1$$

$$\text{thus, } R_2 = 39 R_1 \text{ and } R_2 = 39 R_1$$



then when $V_2 = 0$ $V_B = 0 = V_+ = V_-$ (Golden Rule) $= V_A$

thus analyse node A: $(-\frac{V_A - V_1}{R_1}) = \frac{V_A - V_0}{R_2} \Rightarrow \frac{-V_1}{R_1} = \frac{V_0}{R_2}$, then $V_0 = -\frac{R_2}{R_1} V_1$

f) when $V_1 = 0$, thus $V_+ = \frac{R_4}{R_3 + R_4} \times V_2 = V_- = V_A$

when we analyse A node: $\frac{V_A - 0}{R_1} + \frac{V_A - V_0}{R_2} = 0 \Rightarrow \frac{V_A}{R_1} + \frac{V_A}{R_2} = \frac{V_0}{R_2}$

thus $V_0 = \frac{R_2}{R_1} V_A + V_A = V_A (1 + \frac{R_2}{R_1}) = \frac{R_4}{R_3 + R_4} \times \frac{R_2 + R_1}{R_1} \times V_2$

g) $V_0 = V_{0(0)} + V_{0(f)} = \frac{R_4}{R_3 + R_4} \times \frac{R_2 + R_1}{R_1} \times V_2 - \frac{R_2}{R_1} V_1$

Take V_1 as V_{diff} and V_2 as V_{ref}

thus $\frac{R_2}{R_1} = \frac{R_4}{R_3 + R_4} \times \frac{R_2 + R_1}{R_1} = 40$, then $R_2 = 40 R_1 \Rightarrow \frac{R_2 + R_1}{R_1} = 41 \Rightarrow \frac{R_4}{R_3 + R_4} = \frac{40}{41} \Rightarrow R_4 = 40 R_3$

thus $V_0 = 40 V_2 - 40 V_1 = 40(V_2 - V_1)$ and for example $R_1 = R_3 = 1\Omega$ and $R_2 = R_4 = 40\Omega$

3. Jumped.

a) Because of the Golden Rule $V_+ = V_- = 0V$

~~thus we get $\frac{V_- - V_0}{R_1} + C \frac{dV_-}{dt} = 0 \Rightarrow \frac{V_- - V_0}{R_1} = C \times (V_- - V_0) \Rightarrow V_- = CR_1 V_- - CR_1 V_0 + V_0$~~

thus $\frac{V_- - V_0}{R_1} = C \frac{dV_-}{dt} = 0 \Rightarrow \frac{V_0}{R_1} = C \frac{dV_-}{dt} \Rightarrow \frac{V_0}{R_1} dt = C dV_-$ (integrate both sides)

$\int \frac{V_0}{R_1} dt = \int C dV_- \Rightarrow C V_- = \frac{V_0}{R_1} t \Rightarrow V_- = \frac{V_0}{R_1 C} t = V_- - V_1$

$\Rightarrow V_1 = -\frac{V_0 t}{R_1 C}$

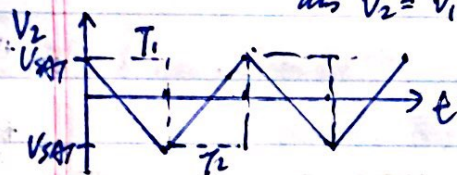
b) Since $V_1 = -\frac{V_0 t}{R_1 C} = -\left(\frac{V_0}{R_1 C}\right)t$

~~but by calculating over $\frac{1}{2} \times T_1 \times (2V_{sat}) =$~~

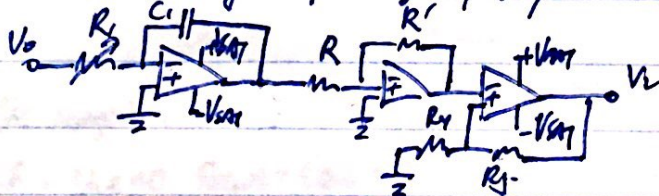
Slope $= \frac{2 \times V_{sat}}{T_1} = \frac{V_{sat}}{R_1 C} \Rightarrow T_1 = \frac{2V_{sat} R_1 C}{V_{sat}} = T_2$

c) Since Coulter Rule: $V_1 = V_- = V_+ = V_2 \times \frac{R_4}{R_3 + R_4} = -\frac{V_0}{R_1 C} t$

thus $V_2 = V_1 \times \frac{R_3 + R_4}{R_4}$ (slope doesn't change) . thus the graph is a amplified version for V_1 graph in b)



d) We add an inverting amp to give polarity



e) Since $1/f_0 = 15 \Rightarrow 1/f_0 = 10^{-3} s$, $T = \frac{2V_{sat} R_1 C}{V_{sat}} = \frac{2 \times 10 \times R_1 \times 10^{-5} F}{10V} = 10^{-5} R_1 F$

Since $2T$ is a period then $10^{-3} = 2 \times 10^{-5} R_1 F \Rightarrow$ thus $R_1 = 50 \Omega$

thus $V_{TH} = \frac{R_4}{R_3 + R_4} V_{sat} = 5V = \frac{10k\Omega}{10k\Omega + R_3} \times 10V \Rightarrow 20 = 10 + R_3 \Rightarrow R_3 = 10k\Omega$

4. Rain Sensor v2.0

a) $C = \frac{\epsilon A}{d}$. $C_{\text{empty}} = \frac{\epsilon \cdot w \cdot h_{\text{air}}}{w} = \epsilon \cdot h_{\text{air}}$

$$C_{\text{tot}} = C_{\text{empty}} + C_{\text{water}} = \frac{\epsilon \cdot w \cdot (h_{\text{air}} + h_{\text{water}})}{w} + \frac{81\epsilon \cdot w \cdot h_{\text{water}}}{w} = \epsilon(h_{\text{air}} + h_{\text{water}}) + 81\epsilon \cdot h_{\text{water}}$$

$$= \epsilon h_{\text{air}} + 80\epsilon h_{\text{water}} = C_{\text{empty}} + 80\epsilon h_{\text{water}}$$

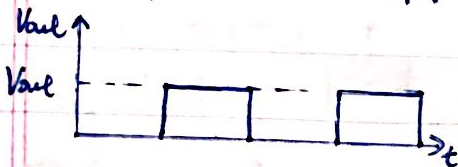
b) When Φ_1 is on and Φ_2 is off:

C_{in} is charged. $Q_{\text{cin}} = C_{\text{in}} \cdot V_{\text{in}}$. C_f is discharged. thus $V_{\text{out}} = V_{\text{cf}} = 0$

When Φ_2 is on and Φ_1 is off:

$$Q_{\text{cf}} = -Q_{\text{cin}} = -C_{\text{in}} V_{\text{in}} = -C_f V_{\text{cf}} \Rightarrow V_{\text{out}} = V_{\text{cf}} = \frac{C_{\text{in}} V_{\text{in}}}{C_f}$$

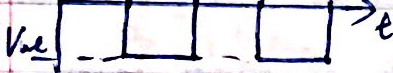
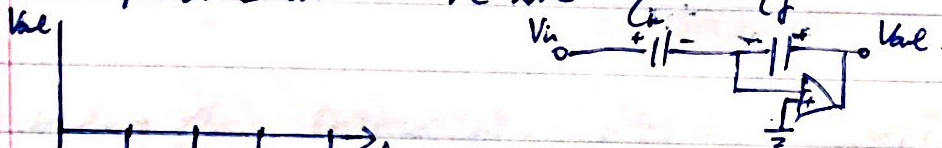
charges are transferred through amp and this voltage is printed



c) In Φ_1 open and Φ_2 close:

C_{in} is discharged. $Q_{\text{cf}} = Q_{\text{in}} = Q_{\text{out}} = 0$. and thus $V_{\text{out}} = 0$

When Φ_1 open and Φ_2 closed: we have



$$\text{and } C_f V_{\text{cf}} = C_{\text{in}} V_{\text{in}} \Rightarrow V_{\text{out}} = \frac{C_{\text{in}} V_{\text{in}}}{C_f}$$

d) Use superposition

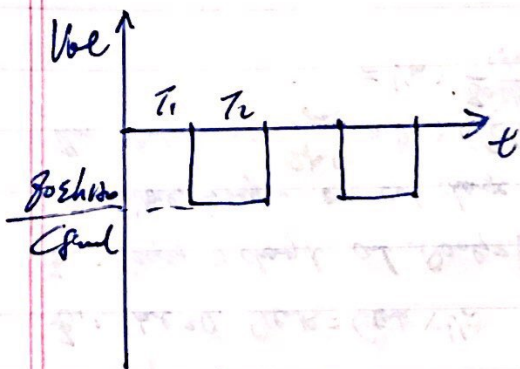
Φ_1 : $V_{\text{in}} \neq 0$. $Q_{\text{out}} = C_{\text{tot}} \times V_{\text{in}}$

Φ_2 : C_{empty} is charged. and $Q_{\text{empty}} = V_{\text{in}} \times C_{\text{empty}}$

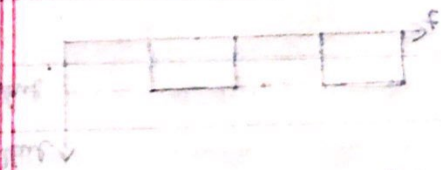
Since $V_{\text{out}} \neq 0$ register the total charge on $Q_{\text{tot}} = Q_1 - Q_2 = C_{\text{tot}} \times V_{\text{in}} - V_{\text{in}} \times C_{\text{empty}}$

$$\text{Thus if } V_{\text{out}} = V_{\text{out}} = \frac{Q_{\text{tot}}}{C_{\text{tot}}} = V_{\text{in}} \times (C_{\text{tot}} - C_{\text{empty}}) \times \frac{1}{C_{\text{tot}}} = (C_{\text{empty}} + 80\epsilon h_{\text{water}} - C_{\text{empty}}) \times V_{\text{in}} \times \frac{1}{C_{\text{tot}}}$$

$$= V_{\text{in}} \times \frac{80\epsilon h_{\text{water}}}{C_{\text{tot}}}$$



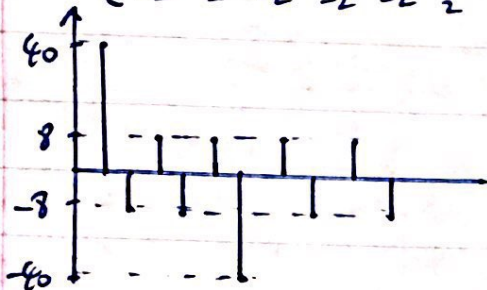
- e) This problem's full formula looks simpler than I will prefer this one since it can help avoiding too much calculation.



5. Mechanical Correlation

a) First:

$$\begin{bmatrix}
 2 & -2 & 2 & -2 & -2 & -2 & 2 & -2 & 2 & 2 \\
 2 & 2 & -2 & 2 & -2 & -2 & -2 & 2 & -2 & 2 \\
 2 & 2 & 2 & -2 & 2 & -2 & -2 & -2 & 2 & -2 \\
 -2 & 2 & 2 & 2 & -2 & 2 & -2 & -2 & -2 & 2 \\
 2 & -2 & 2 & 2 & 2 & -2 & 2 & -2 & -2 & -2 \\
 -2 & 2 & -2 & 2 & 2 & 2 & -2 & 2 & -2 & -2 \\
 -2 & 2 & 2 & -2 & 2 & 2 & 2 & -2 & 2 & -2 \\
 -2 & -2 & -2 & 2 & -2 & 2 & 2 & 2 & -2 & 2 \\
 2 & -2 & -2 & -2 & 2 & -2 & 2 & 2 & 2 & -2 \\
 -2 & 2 & -2 & -2 & -2 & 2 & -2 & 2 & 2 & 2
 \end{bmatrix}
 \begin{bmatrix}
 2 \\
 -2 \\
 2 \\
 -2 \\
 -2 \\
 2 \\
 -2 \\
 2 \\
 2 \\
 2
 \end{bmatrix}
 =
 \begin{bmatrix}
 40 \\
 40-24 \times 2 \\
 40-16 \times 2 \\
 40-14 \times 2 \\
 40-16 \times 2 \\
 -40 \\
 40-16 \times 2 \\
 40-24 \times 2 \\
 40-16 \times 2 \\
 40-14 \times 2
 \end{bmatrix}
 =
 \begin{bmatrix}
 40 \\
 -8 \\
 -8 \\
 -8 \\
 -8 \\
 -40 \\
 -8 \\
 -8 \\
 -8 \\
 -8
 \end{bmatrix}$$



Second:

[Use Matlab]

b) [Use Matlab]

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We rarely really meet but we communicate if we have problems with concepts or methods.

⇒ I, Wayne Li, affirm that all of my solutions are entirely my work and that I have properly credited and acknowledged any sources or work that I have consulted.

```

1 function [result,result_b] = part_a_second()
2     close all
3     x = [0 1 2 3 4 5 6 7 8 9];
4     y = [1 2 3 4 5 6 7 6 5 4];
5     the_y = zeros(10,10);
6     the_y(1,:) = y;
7     for i = 2:10
8         index = i - 1;
9         the_y(i,:) = [y(i:end), y(1:index)];
10    end
11    result = the_y * y';
12    figure(1);
13    plot (x,result);
14    y_of_first = [2 -2 2 -2 -2 -2 2 -2 2 2];
15    figure(2);
16    result_b = the_y * y_of_first';
17    plot(x, result_b);
18 end
19

```

