## **UNIVERSITY OF SOUTHAMPTON**

Faculty of Physical Engineering and Science School of Electronics and Computer Science

A project report submitted for the award of MEng Computer Science

Supervisor: Dr Timothy Norman Examiner: Dr Nicholas Harris

Reinforcement Learning agents for Online Flexible Resource allocation in Mobile Edge Computing

by Mark Towers

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#### University of Southampton

#### **Abstract**

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Mobile Edge Computing enables computational tasks to be completed at the edge of the network reducing network congestion and latency compared to traditional Cloud Computing. A key challenge of these settings is that servers have limited computational resources that need to be allocated to many self-interested users. Existing resource allocation approaches assume that tasks have fixed resource requirements (i.e. a fixed amount of computation, bandwidth and storage) that results in inefficient resource usage and even bottlenecks. This project expands on Flexible resource allocation to Online settings such that tasks arrive over time where auction bids and resource allocation are determined by agents trained using Reinforcement Learning. Using Flexible resource allocation, significantly more tasks are completed than Fixed resource allocation solutions however Flexible resource allocations causes ~5% of tasks to be not completed within their deadline. Along with this a range of training hyperparameters, Reinforcement Learning algorithms and Network Architectures were explored and compared.

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## **Declaration of Authorship**

I declare that this thesis and the work presented in it is my own and has been generated by me as the result of my own original research.

#### I confirm that:

- 1. This work was done wholly or mainly while in candidature for a degree at this University;
- 2. Where any part of this thesis has previously been submitted for any other qualification at this University or any other institution, this has been clearly stated;
- 3. Where I have consulted the published work of others, this is always clearly attributed;
- 4. Where I have quoted from the work of others, the source is always given. With the exception of such quotations, this thesis is entirely my own work;
- 5. I have acknowledged all main sources of help;
- 6. Where the thesis is based on work done by myself jointly with others, I have made clear exactly what was done by others and what I have contributed myself;
- 7. Parts of this work have been published as: S.R. Gunn. Pdflatex instructions, 2001. URL http://www.ecs.soton.ac.uk/~srg/softwaretools/document/
  - C. J. Lovell. Updated templates, 2011
  - S.R. Gunn and C. J. Lovell. Updated templates reference 2, 2011

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To Professor Timothy Norman for his constant guidance over the project and for surviving my bad spelling and grammar.

# Chapter 1

# Introduction

Cloud computing is a rapidly growing technology with competition from Google, Amazon, Microsoft and others that aims to allow users to run computer programs that are too large, difficult or time consuming to run locally. These services provide the computational resources, e.g. CPU cores, RAM, hard drive space, bandwidth, etc to be able to run such programs. However, as these resources are limited, if users request an unbalance quantity of resources, bottlenecks can occur limiting the number of tasks <sup>1</sup> that can be run on servers simultaneously.

For Google Cloud Services (GCP), Microsoft Azure or Amazon Web Services, their cloud computing facilities contain huge server nodes limiting the probability that such a bottleneck occurs. Therefore this work considers a developing paradigm (Mao et al., 2017) called Mobile Edge Computing (Hu et al., 2015) referred to as MEC. MEC aims to provide users with the ability to run their tasks with greater proximity to them in the network, reducing latency, network congestion and providing better application performance.

Currently Disaster Response (Guerdan et al., 2017), Smart Cities (Alazawi et al., 2014) and the Internet-of-Things (Corcoran and Datta, 2016) are all areas that utilise MECs due to its ability to process computationally small tasks locally with low latency. For example, in Smart Cities, this allows smart intersection systems with road-side sensors or smart traffic lights to minimise cars waiting times at traffic lights and reduce overall congestion (Mustapha et al., 2018). Or for the police to analyse CCTV footage to spot suspicious

<sup>&</sup>lt;sup>1</sup>Tasks, Programs and Jobs will be used interchangeable to refer to the same idea of a computer programs that has a fixed amount of resources required to compute.

behaviour and to track people between cameras (Sreenu and Saleem Durai, 2019). In the case of Disaster Response, maps can be produced using data from autonomous vehicles' sensors that can support in the search for potential victims and support responders in planning rescues (Alazawi et al., 2014).

With MECs, the problem of bottlenecks is of particular relevant as instead of large server farms that can be geographically distant from the users. Servers are significantly smaller, possibly just high powered desktop computers or single server nodes. This results in greater demand on individual server resources, meaning that efficient allocation of these resources is of growing importance, particularly as more technologies begin to utilise MECs.

However it is believed that there are shortcomings in existing research about resource allocation within MEC (Farhadi et al., 2019; Bi et al., 2019) due to the nature of how task resource usage is determined. Traditionally, a user would submit a request for a fixed amount of resources, i.e. 2 CPU cores, 8GB of RAM, 20GB of storage, that would be allocated to the user. As a result, these resources can't be redistributed until the user finishes with them. But there are good reasons for this form of resource allocation to be used and effective within cloud computing. Primarily, it is simple for the user to decide resource requirements, Cloud Computing companies can use simple linear pricing mechanisms and as it is rare for servers with large resource capacity to have bottlenecks. However it is believed that the problem of bottlenecks within MEC systems, warrant the investigation of an alternative resource allocation mechanisms.

In previous work a novel resource allocation mechanism was proposed (Towers et al., 2020) to allow for significantly more flexibility in determining resource usage with the aims of reducing possible bottlenecks. The mechanism is based on the principle that the time taken for an operation to complete is generally proportional to the resources provided for the operation. An example for this is downloading an image, the time taken is proportional to the bandwidth allocated. This sort of flexibility is similarly true for computing of most tasks <sup>2</sup> or sending back results to the user.

Based on this principle, a modified resource allocation mechanism can be reconstructed such that the users provide the task's total resource usage over its lifetime instead of the task's requested resource usage. This allows for each task's resource usage to be determined by the server rather than

<sup>&</sup>lt;sup>2</sup>It is well known that some algorithms are not linearly scalable making this principle incompatible with those tasks. Therefore this work considers the case for algorithms that can be scalable linearly and leaves case of non-linearly scalable tasks to future research.

the user increasing a server's flexibility and control. Using this flexible resource allocation mechanism, algorithms proposed achieved 20% better social welfare than a fixed inflexible resource allocation mechanisms in one-shot cases investigated by Towers et al. (2020). This is due to the ability of the algorithms to properly balance task resources, preventing bottlenecks occurring as often, which in turn allowed for more tasks to run simultaneously and to reduce the price.

However that work only considered the proposed mechanism within a one-shot case where all tasks were presented at the first time step, where in all tasks would be auctioned and resource allocated. As a result, in practice the proposed algorithms would require tasks to be processed in batches, such that servers would bid on all tasks submitted every 5 minutes for example. This also meant that while resources could be dynamically allocated at the first time step, they would not change during future batches until the task was completed. This work aims to address these problems.

This was achieved by introducing time into the optimisation problem (outlined in Section 3.1). As a result, tasks now arrive over time and servers can redistribute resources at each time step. However, all previous mechanisms proposed in Towers et al. (2020) are incompatible with this modified online flexible optimisation problem. Therefore this work investigates Reinforcement Learning methods that train agents to optimally bid on tasks based on their resource requirements and efficiently allocate resources to tasks running on a server.

This report is set out in the following chapters. Chapter 2 investigates previous research that this project builds upon within both resource allocation in Cloud Computing and Reinforcement Learning. Chapter 3 proposes a solution to the problem outline in Chapter 1. The solution is implemented in Chapter 4 with testing and evaluation in Chapter 5. Chapter 6 presents the conclusion along with future work for the project.

In addition to this report, the paper referred to as Towers et al. (2020) was written within this academic year and thus considered part of this project's work. A copy of the paper can be found in Appendix A. The paper was also presented at SPIE Defense and Commercial Sensing 2020 as a recorded digital presentation. A copy of the slides can be found in Appendix B with a link to the recording.

# **Chapter 2**

# Literature Review

There is a considerable amount of research in the area of resource allocation and task pricing in cloud computing, where auction mechanisms are used to deal with competition. Section 2.1 presents the different approaches to resource allocation and pricing mechanisms in Cloud Computing.

The proposed solution of the project (presented in chapter 3) uses a form of machine learning, called Reinforcement Learning to train agents. Section 2.2 covers the current state-of-the-art algorithms in Q learning and policy gradient research.

# 2.1 Resource Allocation and Pricing Mechanisms in Cloud Computing

A majority of approaches taken for task pricing and resource allocation in Cloud Computing uses a fixed resource allocation mechanism, such that each user requests a fixed amount of resources for a task from a server. However this mechanism, as previously explained, provides no control for the server over the quantity of resource allocated to a task, only determining the task's price. As a result, a majority of approaches don't consider the server's management of resource allocation. Thus research has focused on designing efficient and incentive compatible auction mechanisms.

Work by Kumar et al. (2017) provides a systematic study of double auction mechanisms that are suitable for a range of distributed systems like Grid

computing, Cloud computing, Inter-Cloud systems. The work reviewed 21 different proposed auction mechanisms over a range of important auction properties like Economic Efficiency, Incentive Compatibility and Budget-Balance. In a majority of the proposed auction mechanisms, truthfulness was only considered for the user, thus a Truthful Multi-Unit Double auction mechanism was presented as such that both users and server should act truthfully.

Deep Reinforcement Learning was implemented by Bingqian Du (2019) to learn resource placement and pricing in order to maximise cloud profits. Deep neural network models with Long/Short Term Memory units enabled state-of-the-art online cloud resource allocation and task pricing algorithms that had significantly better results than traditionally online mechanisms with that profit made and number of users accepted. The system considered both the pricing and placement of virtual machines in the system to maximise the profits of cloud providers through the use of Deep Deterministic Policy Gradient (Silver et al., 2014) to train agents. Users would request a type of virtual machine from the system that a server would allocate to a user. The price and placement of the virtual machine is determined by agents with neural networks. To train the agent, real-world Cloud Computing workloads were utilised and allow it to achieve significantly high profits even in worst-case scenarios compared to previous research.

Some approaches have been taken to increase flexibility within Fog Cloud Computing (Bi et al., 2019) through efficient distribution of data centers and connections to maximise social welfare. A truthful online mechanism was proposed that was incentive compatible and individually rational, to allow tasks to arrive over time by solving an integer programming optimisation problem. Similar research in Farhadi et al. (2019), considers the placement of code/data needed to run specific tasks over time where the demands change over time while also considering the operational costs and system stability. An approximation algorithm achieved 90% of the optimal social welfare by converting the problem to a set function optimisation problem.

Previous work proposed the novel resource allocation mechanism and optimisation problem that this project works to expand (Towers et al., 2020). The paper presents three mechanisms for the optimisation problem, one to maximise the social welfare and two auction mechanisms for self-interested users. The Greedy algorithm presented allows for quick approximation of

a solution through the use of several heuristics in order to maximise the social welfare. Results found that the algorithm achieved over 90% of the optimal solution given certain heuristics compared to a fixed resource allocation solution that achieved 70%. The algorithm has polynomial time complexity with a lower bound of  $\frac{1}{n}$  however in practice achieves significantly better results.

The work also presented a novel decentralised iterative auction mechanism inspired by the VCG mechanism (Vickrey, 1961; Clarke, 1971; Groves, 1973) in order to iteratively increase a task's price. As a result, a task doesn't reveal its private task value that has particular interest within military tactical networks where countries do not need to reveal the importance of a task to another coalition country but can still allow them to run the task. The auction mechanism achieves over 90% of the optimal solution due to iteratively solving of a specialised server optimisation problem. The third algorithm is an implementation of a single parameter auction (Nisan et al., 2007) using the greedy algorithm to find the critical value for each task. Using the greedy algorithm with a monotonic value density function means the auction is incentive compatible and inherits the social welfare performance and polynomial time complexity of the greedy mechanism.

## 2.2 Reinforcement Learning

A key characteristic of humans is the ability to learn from experiences that for computers must be programmed in and so researchers have invented a variety of ways for computers to do this. These are broadly grouped into three categories: Supervised, Unsupervised and Reinforcement Learning. Supervised learning uses inputs that are mapped to known outputs, an example is image classification. Unsupervised learning in comparison doesn't have a known output for a set of inputs, instead algorithms try to find links between similar data, for example data clustering.

However both of these techniques are not applicable for cases where agents must interact with an environment making a series of actions that result in rewards over time. Algorithms designed for these problems fall into the category of Reinforcement Learning where agents select actions based on an environment state that generates the result state and reward from the action as shown in Figure 2.1.

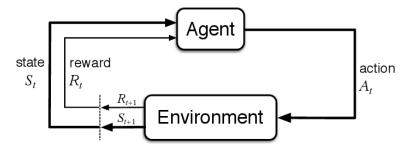


FIGURE 2.1: Reinforcement learning model (Source: Sutton and Barto (2018))

Q-learning (Watkins and Dayan, 1992) is a learning method used for estimating an action-value function, called the Q value, that forms the basis of modern Reinforcement Learning algorithms. The Q value represents the estimated discounted reward in the future given an action in a particular state. Equation (2.1) gives a mathematically description where rewards in the future are discounted. A recursive version of this equation can be formulated as equation (2.2) where the next state is the max Q value of the next state-action. Agents can be trained to approximate the Q value using equation (2.3) through the use of a table of state-action pairs by finding the difference of the best next action and the current Q value.

$$Q(s_t, a_t) = \mathbb{E}\left[R_{t+1} + \gamma R_{t+2} + \gamma^2 R_{t+2} + \cdots\right]$$
 (2.1)

$$Q(s_{t}, a_{t}) = r_{t} + \gamma \max_{a}' Q(s_{t+1}, a')$$
(2.2)

$$Q(s_t, a_t) = Q(s_t, a_t) + \alpha \cdot (r_t + \gamma \cdot \max_a Q(s_{t+1}, a) - Q(s_t, a_t))$$
(2.3)

However the curse of dimensionally was found to be a major problem for using Q-learning as the number of states or actions increase, the table of state-action pairs grows exponentially. This makes the method impractical for problems with large state spaces due to both the table size and the required training time for agents.

Therefore function approximators are used to circumvent this problem, typically this is done using neural networks due to their ability to approximate any function (Csáji, 2001) and to be trained using gradient descent. Work by Mnih et al. (2013), implemented a deep Q network (DQN) to achieve state-of-the-art performance in six of seven games tested as part of the Atari game engine, with three of these scores being superhuman. This was done using two different neural networks, a model and target network in which the target

network is slowly updated by the model network to act as a slowly updating target Q value. An experience replay buffer was also implemented to enable the agent to learn from previous actions.

Follow up work by Mnih et al. (2015) found that with no modifications to the hyperparameters, neural network or training method; state-of-the-art results were achieved in almost all 49 Atari games with superhuman results in 29 of these games. The work showed that deep neural networks could be trained through observing just the raw game pixels and of the game score over time to achieve scores better than those humanly possibly.

Due to this research, a large number of heuristics have been proposed to the loss function (van Hasselt et al., 2015), network architecture (Wang et al., 2015), experience replay buffer (Schaul et al., 2015) and more to improve the algorithm. A combined agent (Hessel et al., 2017) applying a range of heuristics enabling it to achieved over 200% of the original DQN algorithm in score.

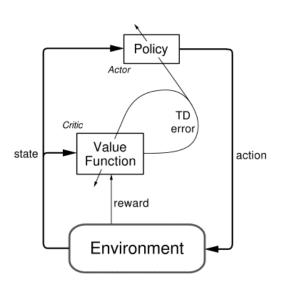


FIGURE 2.2: Actor Critic model (Source: Sutton and Barto (2018))

Policy gradient agents, Figure 2.2, using the base of Q-learning separate the action selection policy from the Q-value function known as the critic. In deep Q networks, actions are selected on the maximum Q-value for all of the actions, however this requires actions to be discretized. By splitting the actions from the Q values, an actor chooses an action based on the environment state allowing for both discrete and continuous action space to be utilised. The critic network is trained almost identically to the Dqn agent except for the use of a soft target

update. While the actor network is trained through gradient ascent and the critic evaluation to increase the value. This has the advantage of the action policy being trained directly compare to Dqn agents that use an epsilon greedy action selection policy. However it is well known that Ddpg agents can also get stuck in local maxima's (Matheron et al., 2020). As a result policy gradient has been used to master the game of Go (Silver et al., 2017) and achieved the top 1% ranking in both Dota 2 (OpenAI, 2018) and Starcraft 2 (Vinyals et al., 2017) video games.

# Chapter 3

# **Optimising Resource Allocation in MEC**

In Chapter 1, the problem that this project aims to address was outlined along with a short description of the proposed solution. This chapter builds upon that, giving a formal mathematical model for the problem in Section 3.1. Section 3.2 proposes an auction mechanism in order to pay servers for their resources in order to deal with self-interested users and as servers are normally paid for use of their services.

Using the optimisation problem and auction mechanism from the previous sections, agents for both auction and resource allocation are proposed, in Section 3.3, that learn together to maximise a server's profits over time.

## 3.1 Resource Allocation Optimisation Problem

Using the flexible resource principle, the time taken for a operation to occur, e.g. loading of data, computing a program and sending back results, etc, is proportional to the amount of resources allocated to complete the operation. A modified version of a resource allocation optimisation model can be designed by building upon the formulation in Towers et al. (2020).

A sketch of the whole system is in Figure 3.1. The system is assumed to contain a set of  $I = \{1, 2, ..., |I|\}$  servers that are heterogeneous in all characteristics. Each server has a fixed resource capacity: storage for the code/data needed

to run a task, measured in GB, computation capacity in terms of CPU cycles per time interval, measured in GHz, and communication bandwidth to receive the data and to send back the results of the task after execution measured in Mbit/s. An example of a task could be the analysis of CCTV images with 2GB of data, 5GHz of CPU cycles and 5MB of results data. The resources for a server i are denoted:  $S_i$  for storage capacity,  $W_i$  for computation capacity, and  $R_i$  for communication capacity. The system occurs over discrete time steps that are defined as the set  $T = \{1, 2, ..., |T|\}$ .

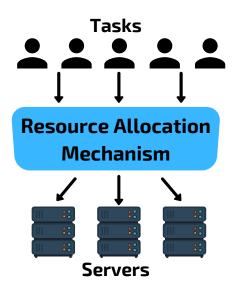


FIGURE 3.1: System model

The system is assumed to contain a set of  $J = \{1, 2, ..., |J|\}$  heterogeneous tasks that require services from one of the servers in set I. To run any of these tasks on a server requires storing the appropriate code/data on the same server. This could be, for example, a set of images, videos or neural network layers used in identification tasks.

The storage size of task j is denoted as  $s_j$  with the rate at which the program is transferred to a server at time t being  $s'_{i,t}$ . For a task to be computed

successfully, it must fetch and execute instructions on a CPU. We consider the total number of CPU cycles required for the program to be  $w_j$ , where the number of CPU cycles assigned to the task at time t is  $w'_{j,t}$ . Finally, after the task is run and the results obtained, the latter needs to be sent back to the user. The size of the results for task j is denoted by  $r_j$ , and the rate at which they are sent back to the user is  $r'_{j,t}$  on a server at time t.

The allocation of tasks to a server is denoted by  $x_{i,j}$  for each task,  $j \in J$ , and server,  $i \in I$ . This is constrained by equation (3.1) meaning that a task can only be allocated to a single server at any point in time.

$$\sum_{i \in I} x_{i,j} \le 1 \qquad \forall j \in J \tag{3.1}$$

$$x_{i,j} \in \{0,1\} \qquad \forall i \in I, j \in J \tag{3.2}$$

As the task must complete each stage in series, additional variables are required to track the progress of each task stage.  $\hat{s}_{j,t}$  denotes the loading progress (equation (3.3)),  $\hat{w}_{j,t}$  denotes the compute progress (equation (3.4)) and  $\hat{r}_{j,t}$  denotes the sending progress (equation (3.5)) of the task. Each of these variables are updated recursively depending on the progress at the previous time step with the resources allocated. For the compute and sending progress constraints, the resources allocated are clipped so that the previous stage finishes before the next stage starts. For each task stage, progress is limited to the total resource required to prevent unneeded resource allocation (constraints (3.6), (3.7) and (3.8)).

$$\hat{s}_{j,t+1} = \hat{s}_{j,t} + s'_{j,t}$$
  $\forall j \in J, t \in T$  (3.3)

$$\hat{w}_{j,t+1} = \hat{w}_{j,t} + w'_{j,t} \lfloor \frac{\hat{s}_{j,t}}{s_j} \rfloor \qquad \forall j \in J, t \in T$$
(3.4)

$$\hat{r}_{j,t+1} = \hat{r}_{j,t} + r'_{j,t} \lfloor \frac{\hat{w}_{j,t}}{w_i} \rfloor \qquad \forall j \in J, t \in T$$
(3.5)

$$\hat{s}_{j,t} \le s_j \qquad \forall j \in J, t \in T \tag{3.6}$$

$$\hat{w}_{j,t} \le w_j \qquad \forall j \in J, t \in T \tag{3.7}$$

$$\hat{r}_{j,t} \le r_j \qquad \forall j \in J, t \in T \tag{3.8}$$

Every task has an auction time, denoted by  $a_j$  and a deadline, denoted by  $d_j$ . This is the time step when the task is auctioned and the last time for which the task can be completed successfully. Using this deadline constraint can be constructed such that the sending results progress is equal to the required results data at the deadline time step (equation (3.9)).

$$\hat{r}_{j,d_j} = r_j \qquad \forall j \in J \tag{3.9}$$

As servers have limited capacity, the total resource usage for all tasks running on a server must be capped. The storage constraint (equation (3.10)) is the sum of the loading progress for each task allocated to the server. While the computation capacity (equation (3.11)) is the sum of compute resources used by all of the tasks on a server i at time t and the bandwidth capacity

(equation (3.12)) being less than the sum of resources used to load and send results back by all allocated tasks.

$$\sum_{i \in I} \hat{s}_{j,t} x_{i,j} \le S_i \qquad \forall i \in I, t \in T$$
 (3.10)

$$\sum_{i \in I} w'_{j,t} x_{i,j} \le W_i \qquad \forall i \in I, t \in T$$
 (3.11)

$$\sum_{j \in J} \hat{s}_{j,t} x_{i,j} \leq S_i \qquad \forall i \in I, t \in T \qquad (3.10)$$

$$\sum_{j \in J} w'_{j,t} x_{i,j} \leq W_i \qquad \forall i \in I, t \in T \qquad (3.11)$$

$$\sum_{j \in J} (s'_{j,t} + r'_{j,t}) x_{i,j} \leq R_i \qquad \forall i \in I, t \in T \qquad (3.12)$$

## **Auctioning of Tasks**

While the mathematically description of the problem presented in the previous section doesn't consider any auctions occurring. In real life servers are normally paid for the use of their resources through auctions as discussed in Section 2.1. However the modifications that this project has made, all of the auction mechanisms discussed in the previous Chapter are incompatible due to users not requesting a fixed amount of resources. Nor can the available resources be easily computed as this is dynamic, depending on the different stages of tasks allocated to a server. The modifications also effect the algorithms presented in Towers et al. (2020) as they assume that all of the task stages can occur concurrently that this project does not. Because of this, an outline of the most common auctions is presented in Table 3.1 with their respective properties in Table 3.2 for selecting an auction mechanism to use.

Auction type	Description
English Auction	A traditional auction where all participants can bid on
	a single item with the price slowly ascending till only a
	single participant is left who pays the final bid price. Due
	to the number of rounds, this requires a large amount of
	communication.

Dutch Auction	The reverse of the English auction, where the starting price
	is higher than anyone is willing to pay with the price slowly
	dropping till the first participant "jumps in". This can
	result in sub-optimal pricing if the starting price is not high
	enough or possibly a large number of rounds until anyone
	bids. Plus due the auctions occurring over the internet,
	latency can have a large effect on the winner.
Japanese Auction	Similar to the English auction, the Japanese auction is
	instead over a set period of time lets bids increasing with
	the last bid being the winner. Because of this, there is
	no guarantee that the price will converge to the maximum
	price like the English but the auction has a fixed time length.
	However factors like latency can have a large effect on the
	winner and resulting price like the Dutch auction.
Blind Auction	Also known as a First-price sealed-bid auction, all
	participants submit a single secret bid for an item with the
	highest bid winning. As a result, no dominant strategy exist
	as an agent would wish to bid only a small amount more
	than the next highest price in order to not overpay for an
	item. But due to there being only a single round of biding,
	latency doesn't affect the winner and can occur over a fixed
	period of time.
Vickrey	Also known as a second-price sealed-bid auction,
Auction (Vickrey,	participants each submit a single secret bid for an item with
1961)	the highest bid winning like the blind auction. However
	the winner only pays the price of the second highest bid.
	Because of this, the dominant strategy (referred to as
	incentive compatibility) for an agent to bid its true value as
	even if the bid is much higher than all other participants its
	doesn't matter as they pay the minimum required for them
	to win.
L	I

TABLE 3.1: Table of Auction mechanisms

The auction properties that this project considers most important are if the fixed time length, which enables fast auctions for processing large numbers of tasks quickly, and Incentive Compatibility such that an optimal strategy actually exists. Because of these two properties, the Vickrey Auction (Vickrey,

Auction	Incentive compatible	Fixed time length
English	False	False
Dutch	False	False
Japanese	False	True
Blind	False	True
Vickrey	True	True

TABLE 3.2: Table of Auction Properties

1961) is selected over the alternatives. An additional advantage of incentive compatibility, is that agents don't need to learn how to outbid another agents, they only need to learn to accurately evaluate each task allowing agents to learn purely through self-play.

However a modification must be made to the auction as servers generate the prices for tasks rather than the task suggesting a price to the servers. Because of this, the auction is reversed, such that the bid with the minimum price wins the task instead of the maximum price. The auction therefore works by allowing all servers to submit their bids for a task with the winner being the server with the lowest price, but as this is a Vickrey auction, the server actually gains second lowest price.

#### 3.3 Server Agents

Using the optimisation formulation and auction mechanism from the previous two sections, the problem can be modelled as Markov Decision Process (Bellman, 1957) as shown in Figure 3.2. This has the advantage of separating out the auction and resource allocation parts of the problem with separate agents acting for each. Subsection 3.3.1 and 3.3.2 proposes agents for each of the auction and resource allocation environments respectively.

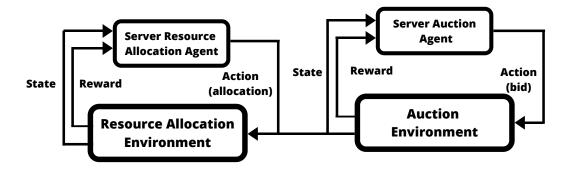


FIGURE 3.2: Markov Decision process system model

Due to the exploratory nature of the project, a range of reinforcement learning algorithms and neural network architectures will be implemented and compared to evaluate the effectiveness of each. These are outlined in Table 3.3 for proposed algorithms and Table 3.4 for networks architectures.

Algorithm	Description
Dqn (Mnih et al., 2015)	A standard deep Q network (Dqn) agent that
	discretizes the action space with a target neural
	network and experience replay buffer.
Double Dqn (van Hasselt	A heuristic for the Dqn that modifies the loss function
et al., 2015)	using the target network actions index but the model
	network value.
Dueling Dqn (Wang et al.,	A heuristic for the Dqn that modifies the network to
2015)	separates the state value and action advantages that
	can help understand the environment.
Categorical	DQN represents the Q value as a scalar value,
Dqn (Bellemare et al.,	the Categorical DQN agent outputs probability
2017)	distribution over values which is helpful for
	environments that are stochastic.
Deep Deterministic Policy	Deep Deterministic Policy Gradient (DDPG) allows
Gradient (Silver et al.,	for continuous actions space, compared to DQN
2014)	agents that must discretize the action space. This is
	done through the use of an actor and critic network
	with target networks for each that are updated with a
	soft target update method.

Twin	Delay	Like the Double Dueling DQN agents, Twin delay
DDPG (Fujimoto	,	DDPG (TD3) includes a couple heuristics for the
2018)		DDPG algorithm. A critic twin is used to prevent
,		the actor network from tricking the critic network in
		evaluating a state's Q value. Another heuristic is the
		delaying the updates for actor network compared to
		the critic network to allow the critic to out learn the
		actor to prevent being tricked.
Td3 Central critic		As there are multiple agents working together, the
		critic used for all of the agents can be same, this
		is inspired by Lowe et al. (2017) which the critic
		only evaluates the agents private observation not with
		complete information of all agents.

TABLE 3.3: Table of the Reinforcement Learning algorithms

Neural Network	Description
Artificial Neural	Originally developed as a theoretically approximation for the
Networks	brain, it was found that for networks with at least one hidden
(McCulloch and	layer, networks could approximate any function (Csáji, 2001).
Pitts, 1943)	This made neural networks extremely helpful for cases where
	it would normally be too difficult for a human to specify the
	exact function, neural networks can be used to find a close
	approximation to the true function through gradient descent.
Recurrent Neural	A major weakness of artificial neural networks is in its use of
Network (Elman,	a fixed number of inputs and outputs making them unusable
1990)	with text, sound or video where previous inputs are important
	for understanding a current input. Therefore recurrent neural
	network's (RNN) extend artificial neural networks to allow
	for connections to previous neurons to "pass on" information.
	However this was found to struggle from vanishing or exploding
	gradient during training such that gradients would tended either
	to zero or infinity over long sequences.

I on a /Ch out	Long/Chart Torm momenty (LCTM) sime to remade DNING
Long/Short Town Moments	Long/Short Term memory (LSTM) aims to remedy RNNs
Term Memory	problem of vanishing and exploding gradient problems. This is
(Hochreiter and	done by using forget gates that determine how much information
Schmidhuber,	from the last state would get, allowing for more complex
1997)	information to be remembered over time compared to RNNs.
Gated Recurrent	Gated recurrent unit (GRU) are very similar to LSTMs, except
unit (Chung et al.,	for the use of different wiring mechanisms with one less gate, an
2014)	update gate instead of two forget gates. These changes mean that
	GRUs run faster and are easier to code than LSTMs. However
	are not as expressive meaning that less complex functions can be
	encoded.
Bidirectional	With RNNs, LSTMs and GRUs, inputs are passed through
(Schuster and	forward however in understanding an input the subsequent
Paliwal, 1997)	inputs are also required. Bidirectional neural network fixed this
	by passes in an input twice, once forwards normally and then a
	second time in reverse. This allows networks to understand the
	context around an input from both before it and after it.
Neural Turing	Inspired by computers, Neural Turing Machines build on
Machine (Graves	long/short term memory by using an external memory module
et al., 2014)	instead of memory being inbuilt to the network. This allows for
	external observers to understand what is going on much better
	than other networks due to their black-box nature.
Differentiable	An expansion to the Neural Turing Machine that allows the
Neural	memory module to be scalable in size allowing for additional
Computer (Graves	memory to be added if needed.
et al., 2016)	
Sequence to	All networks considered above allow for sequences to be passed
Sequence	in while outputting a single output vector. Sequence to sequence
Network	(Seq2Seq) networks utilise two sub-networks; an encoder and
(Sutskever et al.,	decoder. The encoder takes a sequence that is encoded which
2014)	is outputted to the decoder that then outputs another sequence
	by continually passing in the decoders last input.
	1

Table 3.4: Table of Neural network layers

#### 3.3.1 Auction Agents

Traditionally pricing mechanisms (Al-Roomi et al., 2013) rely on mixture of metrics: resource availability, resource demand, quality of service, task resource allocation quantity, etc to determine a price. However these values are difficult to approximate during the auction for this project. So, due to the complexity of deriving this function, reinforcement learning will be used to learn an optimal policy for a server to maximise its profits over time.

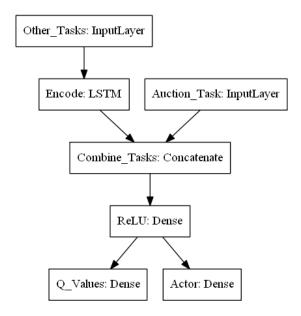


FIGURE 3.3: Task pricing network architecture

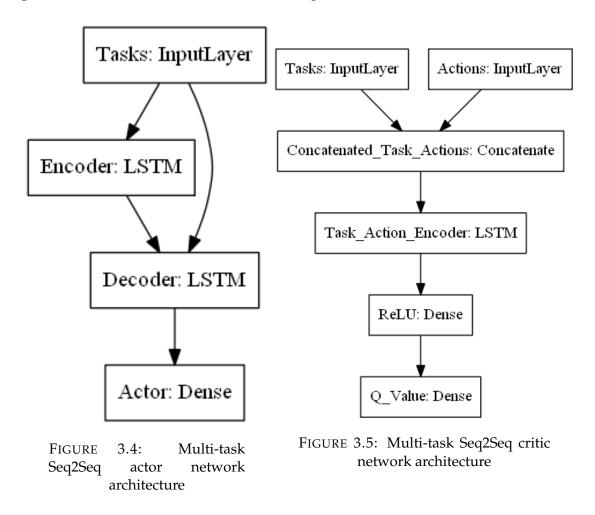
The network used for the auction must take into account a server's current tasks and the attributes of the task being auctioned. Because of this, a recurrent network must be used like the RNN, GRU, LSTM and Bidirectional as the number of tasks allocated to a server is unknown. For the DDPG, a single ReLU output will be used while a linear Q value output for DQN agent must be used as shown in Figure 3.3.

#### 3.3.2 Resource Allocation Agents

When a new task is allocated to the server or a task completes a stage, the server will need to redistributed its resources to its tasks. But while the problem of how to allocate resources isn't as complex as the task pricing policy in Section 3.3.1, no obvious heuristics exist. This is because allocation of resources

to a single task must take into account other tasks that it will affect in order to balance resources between allocated tasks. Because of this, reinforcement learning agents are proposed to learn this with two different network structures and a weighting heuristic to simplify the optimal function for agents.

The heuristic proposes that a weighted value for the task's resources is used instead of the raw resource usage of a task. While simpler, this approach still has the same expressiveness as the exact resource usage while avoiding the problem of either over or under allocating resources to tasks.



To allocate resources to a single task requires also being aware of the resource requirements of other tasks. Because of this, two different neural network structures are proposed, one using a Sequence to Sequence network to allow all tasks actions to be determined simultaneously and the other structure weights a single task at a time. For the Sequence to Sequence network, all tasks are passed in to the encoder that allows the task's attributes to be compressed before passing its output the decoder as shown in Figure 3.4. However Dqn

can't be used to train the network therefore a critic network, Figure 3.5, is required for policy gradient training.

The alternative network uses a simple recurrent neural networks but due to having to output a fixed shape, only a single task can be weighted at a time, as shown in Figure 3.6. Because of this, each task is required to pass through the network. However this network structure can be trained with both Dqn and policy gradient algorithms unlike the Sequence to Sequence network. The Neural Machine Machine and Differentiable Neural Computer were not implemented due to there complexity.

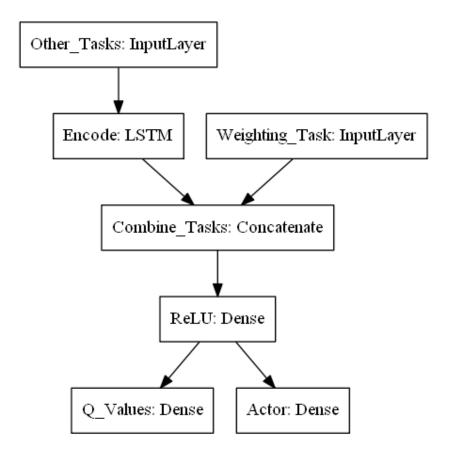


FIGURE 3.6: Single task resource weighting network architecture

# Chapter 4

# Implementing Flexible Resource Allocation Environment and Server Agents

To test the effectiveness of the proposed optimisation problem and agents from Chapter 3 a Mobile Edge Cloud (MEC) computing network must be simulated for both training and evaluation of agents. However as this is impractical to physically setup such a network to train agents in parallel and offline such a system must be simulated.

This chapter implements a simulation of MEC networks (Section 4.1), server auction and resource allocation agents (Section 4.2) and the training of agents (Section 4.3).

The implementation discussed below is written in Python and available to download from Github <sup>1</sup>.

# 4.1 Simulating MEC Networks

While the aim of the environment is to accurately simulate MEC servers, the implementation of the environment must allow agents to interact and train on the environment efficiently. Therefore it has been implemented as an OpenAI gym (Brockman et al., 2016), the de facto standard for implementing reinforcement learning environments by researchers. However the standard

<sup>1</sup>https://github.com/stringtheorys/Online-Flexible-Resource-Allocation

specification must be modified due to the problem being multi-agent and multistep as shown in Listing 4.1.

```
# Load the environment with a setting
   env = OnlineFlexibleResourceAllocationEnv('settings.env')
2
   # Generate the environment state
4
   server_state = env.reset()
5
6
   done = False
   while not done:
        # Check if auction and resource allocation steps
9
10
        if server_state.auction_task:
           # Auction actions
11
            actions = {
12
13
                server: auction_agent.bid(state)
                for server, state in server_state
14
15
            }
        else:
16
17
           # Resource allocation actions
18
            actions = {
19
                server: resource_allocation_agent.weights(state)
20
                for server, state in server_state
21
            }
22
        # Take environment step
23
        server_state , reward , done , info = env.step(actions)
24
```

LISTING 4.1: Example running of the Online Flexible Resource allocation environment

## 4.1.1 Weighted Server Resource Allocation

A particular complication of the environment is to distribute server resources due to the fact that the resource allocation agents provide a resource weighting for a task rather than a task's actual resource usage. Originally, the weighting was converted to the actual resource usage by just allocating each task with the weighted resources from the server capacity. However this was found to be inefficient for when a task completed a stage, they would not use all of the resources that were allocated to them. As a result, a large amount of server resources were wasted using this method. Therefore an alternative novel algorithm was implemented to convert the weighting to the actual resources of each task that wasted zero resources.

This was done by checking if any of the tasks would finish a stage given the weighted resources that could be allocated. If this was true, the task was allocated just the resources required for the task to finish the current stage, with the resources removed from the servers available resources. This was then repeated, with the resource weightings being recalculated each time, until no task could finish its current stage with the weighted resources. For the remaining tasks, the standard algorithm was applied with their weighted resources.

For allocating storage and bandwidth resources, servers must be aware of simultaneously allocating resource to task either loading or sending results. Because of this, a tension exists between allocating bandwidth and storage resources for all of the tasks fairly. The algorithm thus chosen to give priority when allocating resources to the tasks sending results as these tasks are more likely to finish, not penalising the server by failing to complete the task within its deadline.

# 4.2 Server Auction and Resource Allocation Agents

For the server, two policies are required, one for bidding on auction tasks and the other for allocating resources. Subsections 3.3.1 and 3.3.2 propose server agents that use a variety of Reinforcement Learning algorithms (outlined in Table ??) along with a range of neural networks to learn the agent policy.

The Reinforcement Learning algorithms were originally attempted to be implemented using Tf-Agent (Hafner et al., 2017) and a range of frameworks however due to numerous issues, due to modifying the OpenAI gym specification, that was not possible. Therefore all of the algorithms have been handcrafted, using tensorflow (Abadi et al., 2015) a Python module developed by Google designed for machine learning.

Both deep Q networks and policy gradient algorithms are based on the Q value function (explained in Section 2.2)) which tries to approximate the reward at the next time step. To do this requires a reward function and the agent's next observation to train these agents. The reward function and training observations are detailed in Subsections 4.2.1 and 4.2.2.

A particular problem that this project encountered was using recurrent neural networks with different lengths of data inputs during training. This is as the number of inputs to the networks are dependant on the number of tasks allocated to the server at the time for both the auction and resource allocation

## 4.2.1 Agent Rewards Functions

As explained in the background review for Reinforcement Learning (Section 2.2), the Q value is the estimated discounted reward in the future for an action given a particular state. Therefore the rewards that an agent receives for taking an action is extremely important to enable the agent to learn a predictable reward function.

For the auction, the reward is based on the winning price of the task. If the task fails, the reward is instead multiplied by a negative constant in order to discourage the auction agent from bidding on tasks that it wouldn't be able to complete. As the price of zero is treated as a non-bid in the auction, the agent gets a reward of zero in order to not penalise the agent. However, if the agent does bid on a task and doesn't win, the agent's reward is set just below zero at -0.05 as a way of encouraging the agent to change their bid but not large enough to force it to.

$$R(j) = \begin{cases} p_{j}, & \text{if } \hat{r}_{j,d_{j}} = d_{j} \\ -p_{j}, & \text{else if } \hat{r}_{j,d_{j}} < d_{j} \\ 0, & \text{else if } p = 0 \\ -0.05, & \text{otherwise} \end{cases}$$
(4.1)

For resource allocation, the reward function is much simpler than the auction agent's reward function, as it only needs to consider the task being weighted at

the time and rewards from other tasks allocated at the same time step. This is because a task must consider its actions in conjunction with the resource requirements of other allocated tasks.

When the task is successfully finished, the reward is set to 1 while the reward is set to -1.5 if the task fails. This makes failing a task more costly than completing a task. But when a task's action is not under consideration, this reward is multiplied by 0.4, as while this rewards impact the task, their value is not as impactful as the reward for the action on a particular task.

These rewards don't consider the price paid for the task instead valuing each task equally for the aim of finishing all tasks not just the valuable ones. Using this information, the reward function is simply the sum of the rewards of the finished tasks in the next time step.

$$R(j') = \sum_{j \in j'} \begin{cases} 1, & \text{if } \hat{r}_{j,d_j} = d_j \\ -1.5 & \text{otherwise} \end{cases}$$
 (4.2)

## 4.2.2 Agent Training Observations

In order to update both Dqn and Ddpg critic networks, the loss function used in training (Equation (4.3)) requires the next observation to evaluate the next Q value. However the next observation for an agent is not clear as shown in Figure 4.1. For both the auction and resource allocation agents, there is an unknown number of actions taken by the other agents before its next observation is known.

$$L_{\theta} = \mathbb{E}_{s,a \sim p(s)} \left[ (r + \gamma \max_{a'} Q_{\theta'}(s', a') - Q_{\theta}(s, a))^2 \right]$$

$$(4.3)$$

For the resource allocation agent, a trick is implemented such that the next observation for the agent is not the actual next resource allocation observation as shown in Figure 4.1. Instead a generated observation from the resulting server state is used. This is identical to the last case in the figure where no auction occurs between resource allocation steps. The resource allocation Q value is therefore able to approximate the reward from its actions no matter the number of auctions that occur between resource allocation steps.

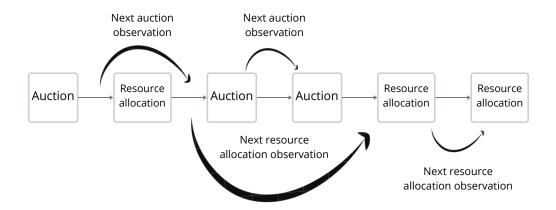


FIGURE 4.1: Environment server agents observations

For the auction agent, the agent's observations require an auction task to select an action (the task bidding price). Therefore a trick like the one implemented for the resource allocation agent can't be used in this case. Thus during training, each server's last observation is recorded, to be used with the next auction observation. But this is a suboptimal solution for the agent as the next observation has an unknown number of resource allocation steps between them. A possible solution that has not been implement in this project is n step prediction (Sutton, 1988). This heuristic modifies the discounted reward to be n steps in the future. This approach could help reduce the amount of randomness in the server's observations and improve bidding performance.

## 4.3 Training Agents

The first section of this chapter implementation simulations for MEC servers (section 4.1) as a Reinforcement Learning environment. While the second section implements auction and resource allocation agents that can interact with the proposed environment. This allows for the training of agents using a range of algorithms outlined in Table ??.

Neural networks, the basis of the Reinforcement Learning agents implemented, often require huge amounts of data and high powered Graphical Processing Unit (GPU) to run efficiently. Because of this, Iridis 5, University of Southampton's supercomputer was utilised with GTX1050 GPUs to train these agents for long periods of time and en mass. During training, for each episode

29

a random environment was generated from a list of possible environment settings.

After every 10 episodes, the agents would be evaluated using a set of environments that are pre-generated and saved at the beginning of training. This allowed the same environments to be used between training agents in order to have a consistent basis to compare the agents over time.

To ensure that agents explored the state space as much as possible, during training actions are taken randomly to allow the agents to "explore". This is a key problem within Reinforcement learning, the exploration vs exploitation dilemma (Sutton and Barto, 2018). For the Dqn agents, including the Double Dqn, Dueling Dqn and Categorical Dqn, epsilon greedy actions were taken such that a percentage of the actions are taken random. The exploration factor (epsilon) is initially set at 1 and ending at 0.1 with it linearly decreasing over 100,000 actions. For the Ddpg and Td3 agents, initially Gaussian distribution was used to add randomness to actions (Silver et al., 2014). However this was found to be ineffective, due to half of the actions added a negative value to the action which is unhelpful as actions must be positive. As a result, agents were found to only bid zero in all auctions. Therefore Gamma distribution (Stacy, 1962) was used with a constant shape parameter of 1 and the scale parameter linearly decreasing from 4.5 to 0.5 over 100,000 actions. However further research is required as agents are found to instead bid on every task.

A table of agent hyperparameters used in training can be found in Appendix C.

# Chapter 5

# **Testing and Evaluation**

To test and evaluate the effectiveness of the proposed solution and implementation, both functional unit tests and agent training evaluation have been used. To confirm that the environment, agents and training all work as intended, Unit testing has been implemented in Section 5.1.

Section 5.2 compares both Flexible and Fixed resource allocation problems in Subsection 5.2.1 and agents with different training hyperparameters (subsection 5.2.2), Reinforcement Learning algorithms (subsection 5.2.3) and Neural Network Architectures (subsection 5.2.4).

# 5.1 Functional Testing

To confirm that the implementation of the agents and environment correctly, PyTest, a Python module, has been used. These tests are split into three families: agent, environment and training that are explained in their respective Tables 5.1, 5.2 and 5.3.

Unit Test name	Description					
Building agents	Constructs all of the agents with any arguments to confirm					
	agents can accept of all its attributes due to multi-					
	inheritance means that only certain arguments are valid for					
	each superclass.					
Saving agents	Confirms that agents can successfully save their neural					
	networks and load the network again.					

Agent actions	Confirms that all agents can generate valid actions for			
	both bidding and weighting of tasks for both training and			
	evaluation.			
Gin config file	Gin is used to set agent and function arguments during			
	training. To test that the file can be successfully parsed and			
	arguments set.			
Building	Constructs all of the neural networks to confirm that the			
networks	network accept and return valid inputs and outputs.			
Agent epsilon	While training agents randomly select actions in order to			
policy	explore the state space. To tests that the random actions			
	selected are valid and that the exploration factor (epsilon)			
	reduces at a linear rate over time correctly.			

TABLE 5.1: Table of Unit tests for Auction and Resource Allocation Agents

<b>Unit Test name</b>	Description
Saving and	The online flexible resource allocation environment can be
loading of	saved to a file in its current state: server allocations, future
environments	task auctions, time steps and total time steps. This tests that
	the environment can save and loaded again.
Loading	Tests that environment settings can be loaded correctly
environment	generating a new random environment.
settings	
Random action	Tests that inputs to the auction and resource allocation steps
environment	work, random actions are generated to check for unknown
steps	edge cases.
Auction step	To confirm the Vickrey auction mechanism is correctly
	implemented, a range of edges cases are tested to confirm
	that right price is set and the task is allocated to the correct
	server in all cases.
Resource	To confirm the resource allocation step is correct generate
allocation	the updated state and reward tasks in all cases.
step	
Allocation of	Checks that the servers correctly allocates computational
computational	resources to allocated tasks given resource weightings.
resources	

Allocation of	Checks that the servers correctly allocates storage and
storage and	bandwidth resources to allocated tasks given resource
bandwidth	weightings.
resources	
Allocation of all	Checks that resources are allocated by the servers correctly
resources	given a weighting input for storage, computation and
	bandwidth resources.

TABLE 5.2: Table of Unit tests for the Online Flexible Resource Allocation Environment

<b>Unit Test name</b>	Description				
Task pricing	Tests that the task pricing reinforcement learning agents				
training	correctly learning and train with different auction				
	observations.				
Resource	Tests that resource allocation reinforcement learning agents				
allocation	correctly learn and train with different resource allocation				
training	observations.				
Agent	Tests that the agent evaluation function during training				
evaluation	correctly captures information from the actions taken.				
Agent training	Tests that agents correctly train over an environment with				
	different actions and observations.				
Random actions	Tests random action agents using the environment training				
training	function to confirm that the function work as intended.				

TABLE 5.3: Table of Unit tests for Agent training

## 5.2 Agent evaluation

Subsection 5.2.1, compares the proposed Online Flexible Resource Allocation environment to an Online Fixed Resource Allocation environment using a linear programming solver to evaluate the effectiveness of the proposed optimisation problem.

In order to compare the implemented agents from Chapter 4, a range of performance metrics are recorded each time the agents are evaluated during training. These metrics are: number of failed tasks, number of completed tasks,

percentage of tasks attempted and a histogram of actions taken which together are used to compare the performance between different agents. Differences in Server agents are compared over training environment settings and number of agents, Reinforcement Learning algorithms and network architectures within Subsections 5.2.2, 5.2.3 and 5.2.4 respectively.

# 5.2.1 Fixed Vs Flexible Resource Allocation Optimisation Problems

Due to tasks containing only the required resources for their lifetime instead of the proposed resource usage as in a fixed resource allocation scheme. It is difficult to convert the Flexible Resource Allocation Optimisation problem from Section 3.1. Appendix D describes the conversation process for tasks and the Fixed Resource Allocation Optimisation problem with solutions found using an integer programming solver. However due to the complexity a time limit of 2.5 minutes were used meaning that all solution are not optimal. For the flexible environment, a Dqn agent for both auctions and resource allocation were used.

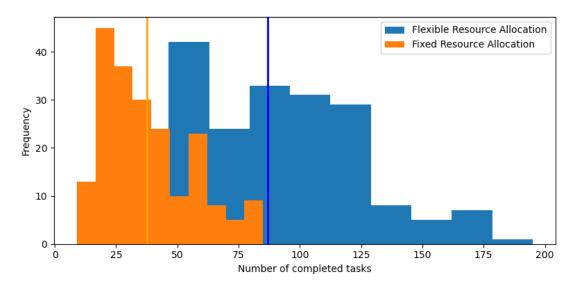


FIGURE 5.1: Number of Tasks completed with Fixed and Flexible resource allocation

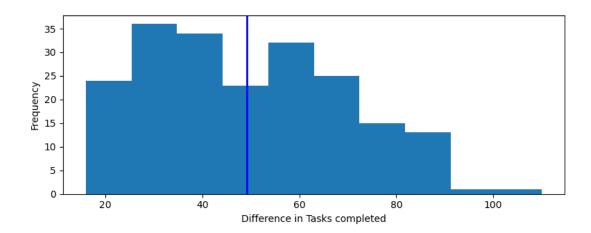


FIGURE 5.2: Difference in number of tasks completed in environment by the Fixed and the Flexible resource allocation agents

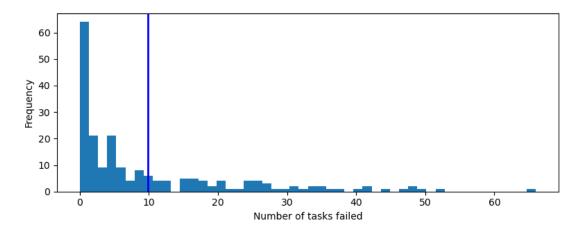


FIGURE 5.3: Number of tasks failed by the Flexible resource allocation agents

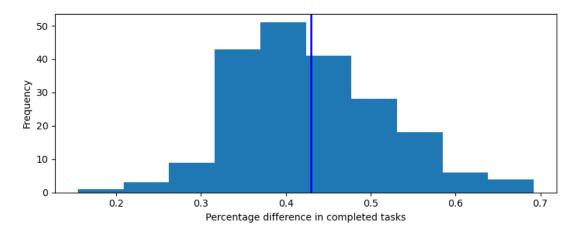


FIGURE 5.4: Percentage difference between the number of Completed tasks by the Fixed and Flexible resource allocation

A histogram of the number of tasks completed by the Fixed and Flexible resource allocation in Figure 5.1 shows that using flexible resource allocation on average over twice the number of tasks can be completed per environment, 35 to 81. Figure 5.2 shows the difference in the number of tasks completed per environment, with on average 51 more tasks being completed by the flexible resource allocation. However on average the flexible resource allocation also fails 10 tasks per environment, as shown in Figure 5.3 with in some cases significantly more.

While these results show that the Flexible resource allocation has significantly better results than the Fixed resource allocation. The results need further analyse to confirm as the fixed resource allocation is not a perfect conversation from the flexible environment and as the solution is found are not optimal.

## 5.2.2 Environment and Agent number training

This subsection analyses two qualities used by the following two subsections when training agents with different Reinforcement Learning algorithms or neural network architectures. These are the training and evaluation environments and number of agents trained concurrently.

Agents trained must able to adapt to a range of environment settings due to the unpredictability of real-life environments, agent generality is an important measure. In particular that agents do not overfit to particular environments used during training thus making them unreliable with unseen environments. An advantage of the Vickrey auction, over alternative auctions is that it is incentive compatible, meaning that the dominant strategy for all agents is to bid truthfully. As a result, agents do not need to learn how to "out bid" each other and can train through purely self-play. However single agents may struggle with a lack of "genetic" diversity therefore making the number of agents an important hyperparameter to investigate.

This subsection compares the results of agents that are trained on a single environment setting and those trained on multi-environment settings as well as when multiple or single agents are trained together. These are compared using a set of pre-generated environments, 5 from the single environment setting in Figures 5.8, 5.9 and 5.10 and 20 from the multi-environment settings, in Figures 5.5, 5.6 and 5.7 to evaluate all agents.

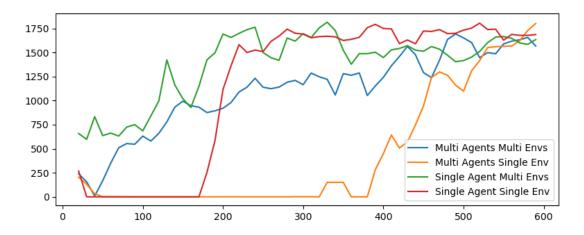


FIGURE 5.5: Environment and number of Agents - Number of completed tasks (Multi-env settings)

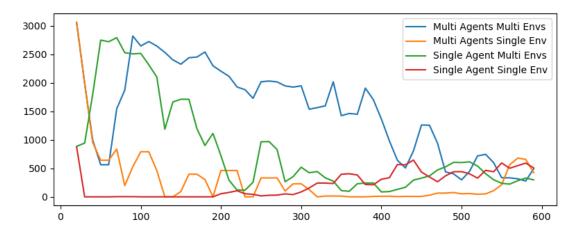


FIGURE 5.6: Environment and number of Agents - Number of failed tasks (Multi-env settings)

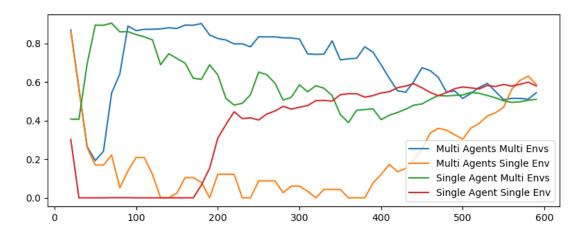


FIGURE 5.7: Environment and number of Agents - Percentage of tasks attempted (Multi-env settings)

In Figure 5.5, agents trained using only a single environment settings, both single and multiple agents variations, took a relatively long time (150 and 350 episodes) for the agents to achieve 25% of its final total tasks completed. In comparison, both multi-environment agents achieved similar results within 50 episodes.

Despite the training speed of the single environment agents, after 600 episodes of training time, all agents no matter the training environments or number of agents trained together achieve very similar results in all metrics (figure 5.5, 5.6 and 5.7. This is surprising that despite single environment agents not being trained on the multi-environment settings, they achieve similar results as multi-environment agents. This means agents are able to generalised to unknown environment effectively alas not as quickly. However more training is required to check if overfitting affects the performance as the agent over learns a particular setting.

This also shows that single agent trained to the same level as multiple agents training together achieve similar results. Meaning that showing that single agent can learn the optimal strategy without needing a diverse "genetic" pool of the multiple agents to train quickly.

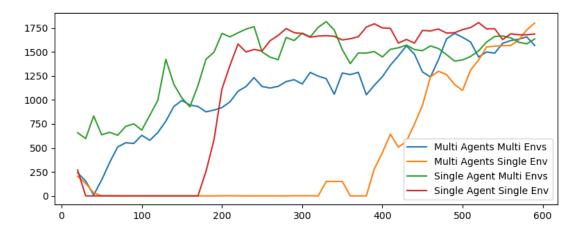


FIGURE 5.8: Environment and number of Agents - Number of completed tasks (Single env settings)

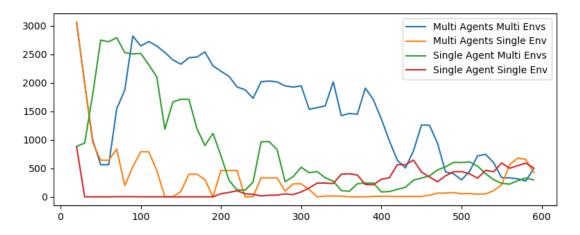


FIGURE 5.9: Environment and number of Agents - Number of failed tasks (Single env settings)

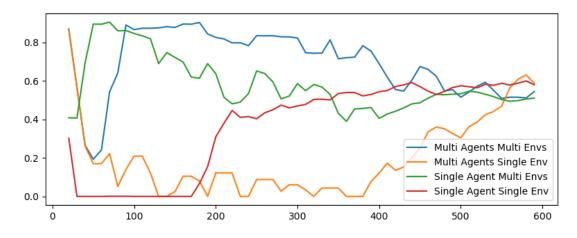


FIGURE 5.10: Environment and number of Agents - Percentage of tasks attempted (Single env settings)

During training, all agents were simultaneously evaluated on the single environment setting as well as the multi-environment settings, shown in Figures 5.8, 5.9 and 5.10. For the single environment agents, they achieve 10% more completed tasks than the multiple environment agents. This is understandable due to single environment being more "specialised" for the single environment than multi-environment agents. As a result, this allows the single environment agents to maximise profits in specialised environments compared to the multi-environment agents that have learnt to maximise profit over more environments being less "specialised" for a single environment.

## 5.2.3 Training Reinforcement Learning Algorithms

To compare Reinforcement Learning algorithms, set out in Table 3.3, each were trained using the algorithms for both auctioning and resource allocation. During training, multiple environments were used for both training and evaluation with three task pricing agents and a single resource allocation agents. This was done because of the analyse in in Subsection 5.2.2.

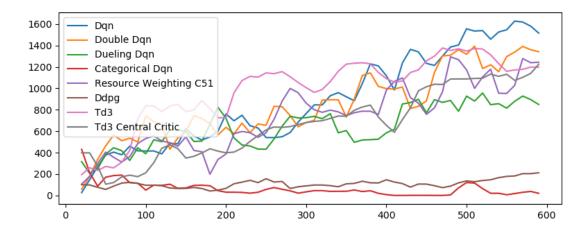


FIGURE 5.11: Reinforcement Learning algorithms - Number of completed tasks

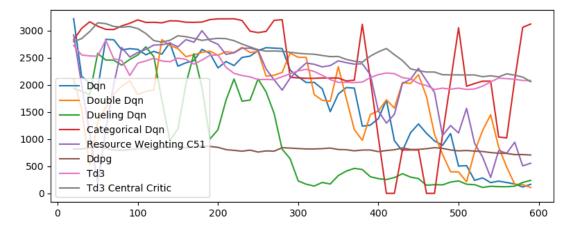


FIGURE 5.12: Reinforcement Learning algorithms - Number of failed tasks

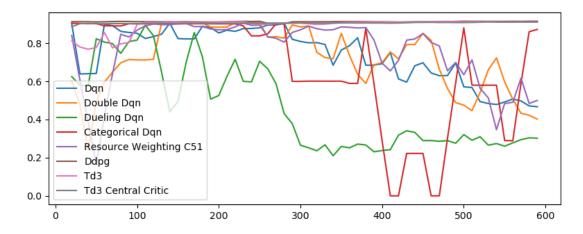


FIGURE 5.13: Reinforcement Learning algorithms - Percentage of tasks attempted

For the Dqn agents, the results did not match expectation as the heuristic Dqn agents achieved fewer completed tasks, Figure 5.11, compared to the standard Dqn agent. This is surprising as previous research (van Hasselt et al., 2015; Wang et al., 2015; Hessel et al., 2017) have found they to achieve better results than the standard Dqn, despite no changes being made to the agents hyperparameters. Possible reasons for this is due to an incorrect implementation, training time or initial network weights. While it is possible to be an incorrect implementation, this is unlikely due to the code matching other implementation. The initial network weights could be a problem, as when the best action is not the optimal actions can cause the network to be trained incorrect at the start but this will self-correct given enough time. Therefore training time is believed to be the primary reason for the heuristic Dqn agents achieving worse result. For future works, doubling the number of training episodes is proposed because of this.

The Categorical Dqn agent struggled to achieving over 50 completed tasks during evaluation after 600 episodes of training. However the reason for this is unknown as a separate training was done using a Dqn for the task pricing and a Categorical Dqn agent for the resource allocation, referred to as 'Resource Weighting C51'. This agent was able to achieve similar results to the other Dqn agent meaning that the task pricing agent fails to work with the Categorical Dqn agent. The reason for this is believed to be due to agent min and max value hyperparameters not due to the implementation. But further research is required to explore Categorical Dqn agents fully and understand why for task pricing this has not worked.

Figure 5.13 shows that the Ddpg agents (Ddpg, Td3, Td3 Central critic) attempted over 80% of auctioned tasks compared to the Dqn agents with only 60%. As a result, agent's can't distributed resource to each of its tasks meaning that the agents have a significantly higher number of failed tasks (Figure 5.12) in comparison to Dqn agent. In terms of completed tasks, the Td3 and Td3 central critic (where all task pricing agents use the same critic and twin critic) are able to achieve results as good as the Dqn agent. This is in comparison to the Ddpg agent which struggled to complete 25% of the amount achieved by the other agents showing that the twin critic heuristics are highly effective for the Ddpg agents.

## 5.2.4 Training Neural Network Architectures

There are a wide-range of compatible neural network architectures that agents can use, as outlined in Table 3.4. To compare these architectures, five different network architectures are trained: RNN, LSTM, GRU, Bidirectional using an LSTM network and a Seq2Seq network. These networks are trained using the Dqn algorithm due to its constant performance compared to the Ddpg agents as shown in the previous section. The Seq2Seq network used a Dqn Agent with a LSTM network for the task pricing agent and the Seq2Seq network with a Td3 agent for resource allocation. This is as the network architecture is only applicable for the resource weighting agent and requires a policy gradient algorithm to train.

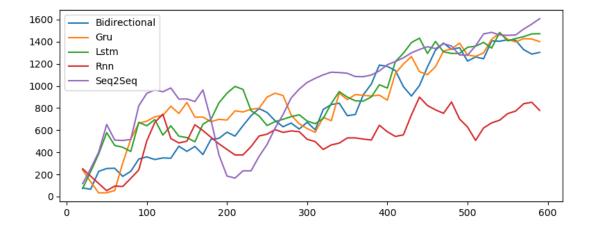


FIGURE 5.14: Network Architecture - Number of completed tasks

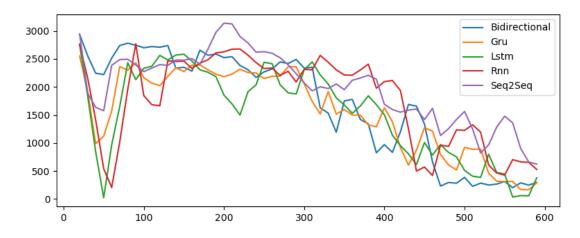


FIGURE 5.15: Network Architecture - Number of failed tasks

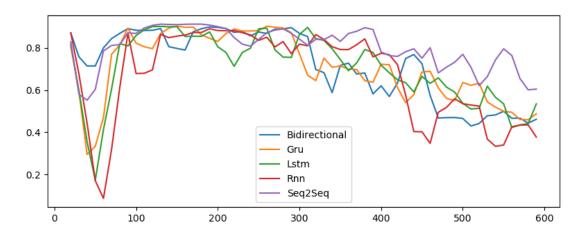


FIGURE 5.16: Network Architecture - Percent of tasks attempted

Figure 5.14 shows that the LSTM, GRU, Bidirectional and Seq2Seq networks all achieved a similar score in the number of tasks completed while the RNN network achieves 30% less. RNNs have a known problem of vanishing or exploding gradients as explained in Table 3.4 making it understandable why the network struggled.

These results are slightly surprising that the heuristic advantages of LSTM and Bidirectional over GRU are not required for agents to approximate the optimal strategy. While ability for the Seq2Seq to learn the task policies together is not a large advantage for the agents in comparison to the other network that weighted tasks individually. However more training time is required till all agents plateau in training which could allow the more complex networks to accel.

# Chapter 6

# Conclusion and future work

The aim of this project was to expand previous research to fix flaws in the elastic resource allocation optimisation problems for Mobile Edge Computing. This was achieved by introducing the notion of time into the optimisation model. As a result, a new optimisation problem was presented in Section 3.1 along with an auction mechanism to deal with self-interested users (Section 3.2).

Due to the complexity of the problem, Reinforcement learning was applied to learn how to bid on auctioned tasks and allocation the server's resources. By implementing an MEC environment and numerous Reinforcement Learning algorithms, agents were able to be train that learnt the optimal strategy for both task pricing and resource allocation.

The evaluation and testing of the implementation, in Chapter 5, found that agents could efficiently learn the policy achieving significantly more tasks completed than the Fixed Resource Allocation mechanisms. However around  $\sim 5\%$  of all tasks were not completed within their time frame. As a result, this project has been viewed as a success however more research and analysis of agents are required before such systems can be implemented into real-life environments.

For future work into this project, this author believes that several additions to the proposed agents could greatly improve their performance like n-step rewards (Sutton, 1988) and distributional ddpg agents (Bellemare et al., 2017; Barth-Maron et al., 2018) that would improve agents due to the environment stochastic nature for agents. An additional heuristic for the policy gradient, would be to use a centralised critic (Lowe et al., 2017) that has been proposed in mix competitive-cooperative environment to help multiple agents working together.

The word count of the Project can be found in Appendix E.

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# Appendix A: Paper

This paper was been produced with the authors being myself, Dr Sebastian Stein, Professor Tim Norman from Southampton University, Dr Fidan Mehmeti, Professor Tom La Porta, Caroline Rubein from Pennsylvania State University and Dr Geeth Demel from IBM and within this project is referred to as Towers et al. (2020).

# Auction-based Mechanisms for Allocating Elastic Resources in Edge Clouds

Paper #1263

#### **ABSTRACT**

Edge clouds enable computational tasks to be completed at the edge of the network, without relying on access to remote data centres. A key challenge in these settings is the limited computational resources that need to be allocated to many self-interested users. Here, existing resource allocation approaches usually assume that tasks have inelastic resource requirements (i.e., a fixed amount of compute time, bandwidth and storage), that may result in inefficient resource use due to unbalanced requirements. To address this, we propose a novel approach that takes advantage of the elastic nature of some of the resources, e.g., to trade-off computation speed with bandwidth allowing a server to execute more tasks by their deadlines. We describe this problem formally, show that it is NPhard and then propose a scalable approximation algorithm. To deal with the self-interested nature of users, we show how to design a centralized auction that incentives truthful reporting of task requirements and values. Moreover, we propose novel auction-based decentralized approaches that are not always truthful, but that limit the information required from users and that can be adjusted to trade off convergence speed with solution quality. In extensive simulations, we show that considering the elasticity of resources leads to a gain in utility of around 20% compared to existing fixed approaches and that our novel auction-based approaches typically achieve 95% of the theoretical optimal.

#### **KEYWORDS**

Edge clouds; elastic resources; auctions

#### 1 INTRODUCTION

In the last few years, cloud computing [2] has become a popular solution to run data-intensive applications remotely. However, in some application domains, it is not feasible to rely a remote cloud, for example when running highly delay-sensitive and computationally-intensive tasks, or when connectivity to the cloud is intermittent. To deal with such domains, *mobile edge computing* [13] has emerged as a complementary paradigm, where computational tasks are executed at the edge of mobile networks at small data-centers, known as *edge clouds*.

Mobile edge computing is a key enabling technology for the Internet-of-Things (IoT) [6] and in particular applications in smart cities [19] and disaster response scenarios [9]. In these applications, low-powered devices generate computational tasks and data that have to be processed quickly on local edge cloud servers. More

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© 2020 International Foundation for Autonomous Agents and Multiagent Systems (www.ifaamas.org). All rights reserved. https://doi.org/doi specifically, in smart cities, these devices could be smart intersections that collect data from road-side sensors and vehicles to produce an efficient traffic light sequence to minimize waiting times [14]; or it could be CCTV cameras that analyse video feeds for suspicious behaviour, e.g., to detect a stabbing or other crime in progress [20]. In disaster response, sensor data from autonomous vehicles (including video, sonar and LIDAR) can be aggregated in real time to produce maps of a devastated area, search for potential victims and help first responders in focusing their efforts to save lives [1].

To accomplish these tasks, there are typically several types of resources that are needed, including communication bandwidth, computational power and data storage resources [7], and tasks are generally delay-sensitive, i.e., have a specific completion deadline. When accomplished, different tasks carry different values for their owners (e.g., the users of IoT devices or other stakeholders such as the police or traffic authority). This value will depend on the importance of the task, e.g., analysing current levels of air pollution may be less important than preventing a large-scale traffic jam at peak times or tracking a terrorist on the run. Given that edge clouds are often highly constrained in their resources [12], we are interested in allocating tasks to edge cloud servers to maximize the overall social welfare achieved (i.e., the sum of completed task values). This is particularly challenging, because users in edge clouds are typically self-interested and may behave strategically [3] or may prefer not to reveal private information about their values to a central allocation mechanism [18].

An important shortcoming of existing work of resource allocation in edge clouds, e.g., [3, 7], is that it assumes tasks have strict resource requirements - that is, each task consumes a fixed amount of computation (CPU cycles per time), takes up a fixed amount of bandwidth to transfer data and uses up a fixed amount of storage on the server. However, in practice, edge cloud servers have some flexibility in how they allocate limited resources to each task. In more detail, to execute a task, the corresponding data and/or code first has to be transferred to the server it is assigned to, requiring some bandwidth. This then takes up storage on the server. Next, the task needs computing power from the server in terms of CPU cycles per time. Once computation is complete, the results have to be transferred back to the user, requiring further bandwidth. Now, while the the storage capacity at the server for every task is strict, since the task cannot be run unless all the data is stored, the bandwidth and compute speed allocated to the task can be elastic. This allows flexibility in the resource allocation process enabling resources to be shared evenly, prevent resource self-interested users and for more task to receive service simultaneously.

Against this background, we make the following novel contributions to the state of the art:

 We formulate an optimization problem for assigning the tasks to the servers, whose objective is to maximize total

- social welfare, taking into account resource limitations and elastic allocation of resources.
- We prove that the problem is NP-hard and propose an approximation algorithm with a performance guarantee of  $\frac{1}{n}$ , where n is the number of tasks, and a linearithmic computational complexity, i.e.,  $O(n \log(n))$ .
- We propose a range of auction-based mechanisms to deal with the self-interested nature of users. These offer various trade-offs regarding truthfulness, optimality, scalability, information requirements from users, communication overheads and decentralization.
- Using extensive realistic simulations, we compare the performance of our algorithm against other benchmark algorithms, and show that our algorithm outperforms all of them, while at the same time being within 95% to the optimal solution.

The paper is organized as follows. In the next section we discuss related work. This is followed by the problem formulation in Section 3. Our novel resource allocation mechanisms are presented in Section 4. In Section 5, we evaluate the performance of our mechanisms and compare them against the optimal solution and other benchmarks. Finally, Section 6 concludes the work.

#### 2 RELATED WORK

There is a considerable amount of research in the area of resource allocation and pricing in cloud computing, some of which use auction mechanisms to deal with competition [3, 4, 11, 22]. However, these approaches assume that users request a fixed amount of resources system resources and processing rates, with the cloud provider having no control over the speeds, only the servers that the task was allocated to. In our work, tasks' owners report deadlines and overall data and computation requirements, allowing the edge cloud server to distribute its resources more efficiently based on each task's requirements.

Our problem is related to multidimensional knapsack problems. In particular, Nip et al. [15] consider flexibility in the allocation, with linear constraints that are used for elastic weights. The paper provides a pseudo-polynomial time complexity algorithm for solving this problem to maximize the values in the knapsack. Our problem case is similar to their problem, but our problem has nonlinear constraints due to the deadline constraint, so their algorithm cannot be applied here.

Other closely related work on resource allocation in edge clouds [7] considers both the placement of code/data needed to run a specific task, as well as the scheduling of tasks to different edge clouds. The goal there is to maximize the expected rate of successfully accomplished tasks over time. Our work is different both in the setup and the objective function. Our objective is to maximize the value over all tasks. In terms of the setup, they assume that data/code can be shared and they do not consider the elasticity of resources.

## 3 PROBLEM FORMULATION

In this section we first describe the system model. Then, we present the optimization problem and prove its NP-hardness.



Figure 1: System Model

## 3.1 System model

A sketch of the system is shown in Fig. 1. We assume that in the system there is a set of servers  $I=\{1,2,\ldots,|I|\}$  servers, which could be edge clouds that can be accessed either through cellular base stations or WiFi access points (APs). Servers have different types of resources: storage for the code/data needed to run a task (e.g., measured in GB), computation capacity in terms of CPU cycles per time interval (e.g., measured in FLOP/s), and communication bandwidth to receive the data and to send back the results of the task after execution (e.g., measured in Mbit/s). We assume that the servers are heterogeneous in all their characteristics. More formally, we denote the storage capacity of server i with  $S_i$ , computation capacity with  $W_i$ , and the communication capacity with  $R_i$ .

There is a set  $J = \{1, 2, ..., |J|\}$  of different tasks that require service from one of the servers. Every task  $j \in J$  has a value  $v_j$  that represents the value of running the task to its owner. To run any of these tasks on a server requires storing the appropriate code/data on the same server. These could be, for example, a set of images, videos or CNN layers in identification tasks. The storage size of task j is denoted as  $s_j$  with the rate at which the program is transferred to the server being  $s_i$ . For a task to be computed successfully, it must fetch and execute instructions on a CPU. We consider the total number of CPU cycles required for the program to be  $w_i$ , where the rate at which the CPU cycles are assigned to the task per unit of time is  $w'_{i}$ . Finally, after the task is run and the results obtained, the latter need to be sent back to the user. The size of the results for task j is denoted with  $r_j$ , and the rate at which they are sent back to the user is  $r'_{i}$ . Every task has its deadline, denoted by  $d_{i}$ . This is the maximum time for the task to be completed in order for the user to derive its value. This time includes: the time required to send the data/code to the server, run it on the server, and get back the results. We assume that there is an all or nothing task execution reward scheme, meaning that for the task value to be awarded the entire task must be run and the results sent back within the deadline.

<sup>&</sup>lt;sup>1</sup>We focus on a single-shot setting in this paper. In practice, an allocation mechanism would repeat the allocation decisions described here over regular time intervals, with longer-running tasks re-appearing on consecutive time intervals. We leave a detailed study of this to future work.

#### 3.2 **Optimization problem**

Given the aforementioned assumptions, the optimal assignment of tasks to servers and optimal allocation of resources in a server to the tasks assigned to that server is obtained as a solution to the following optimization problem. Here, the decision variables are  $x_{i,j} \in \{0,1\}$  (whether to run task j on server i) as well as  $s_{i}^{'}, r_{i}^{'}$  and  $w_{i}^{'}$  (indicating the bandwidth rates for transferring the code, for returning the results and the CPU cycles per unit of time, respectively).

$$\max \sum_{\forall j \in J} v_j \left( \sum_{\forall i \in I} x_{i,j} \right)$$
s.t. (1)

t. 
$$\sum_{\forall j \in J} s_j x_{i,j} \leq S_i, \qquad \forall i \in I, \qquad (2)$$

$$\sum_{\forall j \in J} w'_j x_{i,j} \leq W_i, \qquad \forall i \in I, \qquad (3)$$

$$\sum_{\forall j \in J} (r'_j + s'_j) \cdot x_{i,j} \leq R_i, \qquad \forall i \in I, \qquad (4)$$

$$\sum_{\forall j \in I} w_j^{\prime} x_{i,j} \le W_i, \qquad \forall i \in I, \qquad (3)$$

$$\sum_{\forall i \in I} (r_j^{'} + s_j^{'}) \cdot x_{i,j} \le R_i, \qquad \forall i \in I, \qquad (4)$$

$$\frac{s_j}{s_i'} + \frac{w_j}{w_i'} + \frac{r_j}{r_i'} \le d_j, \qquad \forall j \in J, \qquad (5)$$

$$0 \le s_{j}^{'} \le \infty,$$
  $\forall j \in J,$  (6)

$$0 \le w_j^{'} \le \infty, \qquad \forall j \in J, \qquad (7)$$

$$0 \le r_j^{'} \le \infty,$$
  $\forall j \in J,$  (8)

$$\sum_{\forall i \in I} x_{i,j} \le 1, \qquad \forall j \in J, \qquad (9)$$

$$x_{i,j} \in \{0,1\}, \qquad \forall i \in I, \forall j \in J. \tag{10}$$

The objective (Eq.(1)) is to maximize the total value over all tasks (i.e., the social welfare). Task j will receive the full value  $v_i$ only if it is executed entirely and the results are obtained within the deadline for that task. Constraint (Eq.(2)) relates to the finite storage capacity of every server to store code/data for the tasks that are to be run. The finite computation capacity of every server is expressed through Eq.(3), whereas Eq.(4) denotes the constraint on the communication capacity of the servers. As can be seen, the communication bandwidth comprises two parts: one part to send the data/code or request to the server, and the other part to get the results back to the user.<sup>2</sup> Constraint Eq.(5) is the deadline associated with every task, where the total time of the task in the system is the sum of the time to send the request and code/data to the server, time to run the task, and the time it takes the server to send all the results to the user. Note that if a task is not run on any server, this constraint can be satisfied by choosing arbitrarily high bandwidth and CPU rates (without being constrained by the resource limits of any server). The rates at which the code is sent, run and the results are sent back are all positive and finite (Eqs. (6), (7), (8)). Further, every task is served by at most one server (Eq.(9)). Finally, a task is either served or not (Eq.(10)).

**Complexity:** In the following we show that this optimization problem is NP-hard.

THEOREM 3.1. The optimization problem (1)-(10) is NP-hard.

PROOF. The optimization problem without constraint (5) is a 0-1 multidimensional knapsack problem [10], which is a generalization of a simple 0-1 knapsack problem. The latter is an NP-hard problem [10]. Given this, it follows that the 0-1 multidimensional knapsack problem is also NP-hard. Since optimization problem (1)-(10) is a generalization of a 0-1 multidimensional knapsack problem, it follows that it is NP-hard as well.

Before we propose our novel allocation mechanisms for the allocation problem with elastic resources, we briefly outline an example that illustrates why considering this elasticity is important. In this example, there are 12 potential tasks and 3 servers (the exact settings can be found in table 2 for the tasks and table 1 for the

Figure 2 shows the best possible allocation if tasks have fixed resource requirements. The resource speeds were chosen such to the minimum total resource usage that the task would require from the deadline. Here, 9 of the tasks are run, resulting in a total social welfare of 980 due to the limitation of the server's computation and the task requirement not being balanced.

In contrast to this, Figure 3 depicts the optimal allocation if elastic resources are considered. Here, it is evident that all of the resources are used by the servers whereas the fixed (in figure 2) cant do this. In total, the elastic approach manages to schedule all 12 tasks within the resource constraints, achieving a total social welfare of 1200 (an 19% improvement over the fixed approach).

The figures represent resource usage of the servers by the three bars relating to each of this resources (storage, CPU and bandwidth). For each task that is allocated to the server, the percentage of the resource's used is bar size. Then, for the tasks that are assigned to corresponding servers, the percentage of used resources are also depicted.

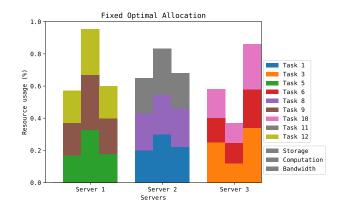


Figure 2: Optimal solution with fixed resources. Due to not being able to balance out the resources, bottlenecks on the server 1 and 2's computation have occurred

<sup>&</sup>lt;sup>2</sup>Not that sending and receiving data will not always overlap, but for tractability we assume they deplete a common limited bandwidth resource per time step. This ensures that the bandwidth constraint is always satisfied in practice.

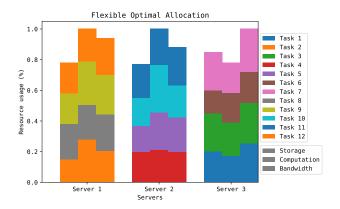


Figure 3: Optimal solution with elastic resources. Compared to the fixed allocation, the elastic allocation is able to fully use all of its resources

Name	$S_i$	$W_i$	$R_i$	
Server 1	400	100	220	
Server 2	450	100	210	
Server 3	375	90	250	

Table 1: Servers - Table of server attributes

Name	$v_j$	$s_j$	$w_j$	$r_j$	$d_j$	$s_{j}^{'}$	$w_{j}^{'}$	$r_{j}^{'}$
Task 1	100	100	100	50	10	30	27	17
Task 2	90	75	125	40	10	22	32	15
Task 3	110	125	110	45	10	34	30	17
Task 4	75	100	75	35	10	27	21	13
Task 5	125	85	90	55	10	24	28	17
Task 6	100	75	120	40	10	20	32	16
Task 7	80	125	100	50	10	31	30	19
Task 8	110	115	75	55	10	30	22	20
Task 9	120	100	110	60	10	27	29	24
Task 10	90	90	120	40	10	25	30	17
Task 11	100	110	90	45	10	30	26	16
Task 12	100	100	80	55	10	24	24	22

Table 2: Tasks - Table of task attributes, the columns for resource speeds  $(s'_j, w'_j, r'_j)$  is for fixed speeds which the flexible allocation does not take into account. The fixed speeds is the minimum required resources to complete the task within the deadline constraint.

# 4 FLEXIBLE RESOURCE ALLOCATION MECHANISMS

In this section, we propose several mechanisms for solving the resource allocation problem with elastic resources. First, we discuss a centralized greedy algorithm (detailed in Section 4.1) with a  $\frac{1}{|J|}$  performance guarantee and polynomial run-time. Then, we consider settings where task users are self-interested and may either report their task values and requirements strategically or may

wish to limit the information they reveal to the mechanism. To deal with such cases, we propose two auction-based mechanisms, one of which can be executed in a decentralized manner (in Sections 4.2 and 4.3).

## 4.1 Greedy Mechanism

As solving the allocation problem with elastic resources is NP-hard, we here propose a greedy algorithm (Algorithm 1) that considers tasks individually, based on an appropriate prioritisation function.

More specifically, the greedy algorithm does this in two stages; the first sorts the tasks and the second allocates them to servers. A value density function is applied to each of the task based on its attributes: value, required resources and deadlines. Stage one uses this function to sort the list of tasks. The second stage then iterates through the tasks in the given order, applying two heuristics to each task: one to select the server and another to allocate resources. The first of these heuristics, called the server selection heuristic, works by checking if a server could run the task if all of its resources were to be used for meeting the deadline constraint (eq 5) then calculating how good it would be for the job to be allocated to the server. The second heuristic, called the resource allocation heuristic, finds the best permutations of resources to minimise a formula, i.e., the total percentage of server resources used by the task.

In this paper we prove that the lower bound of the algorithm is  $\frac{1}{|J|}$  (where |J| is the number of jobs) using the value of a task as the value density function and using any feasible server selection and resource allocation heuristic. However we found that the task value heuristic is not the best heuristic as it does not consider the effect of the deadline or resources used for a job. In practice, the following heuristic often works better:  $\frac{v_j \cdot (s_j + w_j + r_j)}{d_j}$ . For the server selection heuristic we use  $argmin_{\forall i \in I} S_i' + W_i' + R_i'$ , where  $S_i'$ ,  $W_i'$ ,  $R_i'$  are the server's available storage, computation and bandwidth resources respectively. While for the resource allocation heuristic we use  $min \frac{W_i'}{w_i'} + \frac{R_i'}{s_i' + r_i'}$ .

Theorem 4.1. The lower bound of the greedy mechanism is  $\frac{1}{n}$  of the optimal social welfare

PROOF. Taking the value of a task as the value density function, the first task allocated will have a value of at least  $\frac{1}{n}$  total values of all jobs. As the allocation of resources for a task is not optimal, allocation of subsequent tasks is not guaranteed. Therefore, as the optimal social welfare must be the total values of all jobs or lower then the lower bound of the mechanism must be  $\frac{1}{n}$  of the optimal social welfare.

In figure 4, an example allocation using the algorithm is shown using the model from tables 1 and 2. The algorithm uses the recommend heuristic proposed above and allows for all tasks to be allocated achieving 100% of the flexible optimal in figure 3.

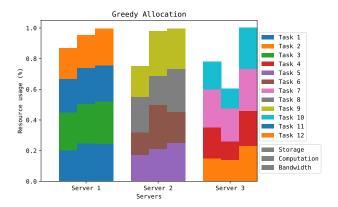


Figure 4: Example Greedy allocation using model from table 2 and 1

#### Algorithm 1 Greedy Mechanism

**Require:** J is the set of tasks and I is the set of servers

**Require:**  $S_i', W_i'$  and  $R_i'$  is the available resources (storage, computation and bandwidth respectively) for server *i*.

**Require:**  $\alpha(j)$  is the value density function of a task

**Require:**  $\beta(j, I)$  is the server selection function of a task and set of servers returning the best server, or  $\emptyset$  if the task is not able to be run on any server

**Require:**  $\gamma(j, i)$  is the resource allocation function of a task and server returning the loading, compute and sending speeds

**Require:** sort(X, f) is a function that returns a sorted list of elements in descending order, based on a set of elements and a function for comparing elements

```
\begin{split} & f' \leftarrow sort(J,\alpha) \\ & \textbf{for all } j \in f' \textbf{ do} \\ & i \leftarrow \beta(j,I) \\ & \textbf{if } i \neq \emptyset \textbf{ then} \\ & s_j',w_j',r_j' \leftarrow \gamma(j,i) \\ & x_{i,j} \leftarrow 1 \\ & \textbf{end if} \\ & \textbf{end for} \end{split}
```

Theorem 4.2. The time complexity of the greedy algorithm is O(|J||I|), where |J| is the number of tasks and |I| is the number of servers. Assuming that the value density and resource allocation heuristics have constant time complexity and the server selection function is O(|I|).

PROOF. The time complexity of the stage 1 of the mechanism is  $O(|J|\log(|J|))$  due to sorting the tasks and stage 2 has complexity O(|J||I|) due to looping over all of the tasks and applying the server selection and resource allocation heuristics. Therefore the overall time complexity is  $O(|J||I| + |J|\log(|J|) = O(|J||I|)$ .

#### 4.2 Critical Value Auction

Due to the problem case being non-cooperative, if the greedy mechanism was used to allocate resources such that the value is the

price paid. This is open to manipulation and misreporting of task attributes like the value, deadline or resource requirements. Therefore in this section we propose an auction that is weakly-dominant for tasks to truthfully report it attributes.

Single-Parameter domain auctions are extensively studied in mechanism design [16] and are used where an agent's valuation function can be represented as single value. The task price is calculated by finding the task's value such that if the value were any smaller, the task could not be allocated. This value is called the critical value. This has been shown to be a strategyproof [17] (weakly-dominant incentive compatible) auction so it is a weakly-dominant strategy for a task to honestly reveal its value.

The auction is implemented using the greedy mechanism from section 4.1 to find an allocation of tasks using the reported value. Then for each task allocated, the last position in the ordered the task list such that the task would still allocated is found. The critical value of the task is then equal to the inverse of the value density function where the density is the density of the next task in the list after that position.

In order that the auction is strategy proof, the value density function is required to be monotonic so that misreporting of any task attributes will result in the value density decreasing. Therefore a value density function of the form  $\frac{v_j d_j}{\alpha(s_j, w_j, r_j)}$  must be used so that the auction is strategy proof.

Theorem 4.3. The value density function  $\frac{v_j d_j}{\alpha(s_j, w_j, r_j)}$  is monotonic for task j assuming the function  $\alpha(s_j, w_j, r_j)$  is monotonic decreasing.

PROOF. In order to misreport the task private value and deadline must be less than the true value. The opposite is true for the required resources (storage, compute and result data) with the misreported value being greater than the true value. Therefore the  $\alpha$  function will increase as the resource requirements increase as well, meaning that density will decrease.

## 4.3 Decentralised Iterative Auction

VCG (Vickrey-Clark-Grove) auction [21] [5] [8] is proven to be economically efficient, budget balanced and incentive compatible. A task's price is found by the difference of the social welfare for when the task exists compared to the social welfare when the task doesn't exist. Our auction uses the same principle for pricing by finding the difference between the current server revenue and the revenue when the task is allocated (at £0).

The auction iteratively lets a task advertise its requirements to all of the servers who respond with their price for the task. This price is equal to the server's current revenue minus the solution to the the problem in section 4.3.1 plus a small value called the price change variable. Being the reverse of the VCG mechanism, such that the price is found for when the task exists rather than when it doesn't exist. The price change variable allows for the increase in the revenue of the server and is can be chosen by the server. Once all of the server have responded, the task can compare the minimum server price to its private value. If the price is less then the task will accept the servers with the minimum price offer, otherwise the task will stop looking as the price for the task to run on any server is greater than its reserve price.

To find the optimal revenue for a server *m* given a new task *p* and set of currently allocated tasks N has a similar formulation to section 3.2. With an additional variable is considered, a task's price being  $p_n$  for task n.

### 4.3.1 Server problem case.

$$\max_{\forall n \in N} p_n x_n \tag{11}$$
s.t. (12)

$$\sum_{n \in S} s_n x_n + s_p \le S_m,\tag{13}$$

$$\sum_{\forall n \in N} w_n' x_n + w_p \le W_m, \tag{14}$$

$$\sum_{\forall n \in N} s_{n} x_{n} + s_{p} \leq S_{m},$$

$$\sum_{\forall n \in N} w'_{n} x_{n} + w_{p} \leq W_{m},$$

$$\sum_{\forall n \in N} (r'_{n} + s'_{n}) \cdot x_{n} + (r'_{p} + s'_{p}) \leq R_{m},$$
(13)

$$\frac{s_n}{s_n'} + \frac{w_n}{w_n'} + \frac{r_n}{r_n'} \le d_n, \qquad \forall n \in \mathbb{N} \cup \{p\}, \tag{16}$$

$$0 \le s_n' \le \infty, \qquad \forall n \in N \cup \{p\}$$
 (17)

$$0 \le w_n' \le \infty, \qquad \forall n \in N \cup \{p\} \quad (18)$$

$$0 \le r_n^{'} \le \infty, \qquad \forall n \in N \cup \{p\}$$
 (19)

$$x_n \in \{0, 1\}, \qquad \forall n \in N \quad (20)$$

The objective (Eq.(11)) is to maximize the price of all tasks (not including the new task as the price is zero). The server resource capacity constraints are similar to the constraints in the standard model set out in section 3.2 however with the assumption that the task k is running so there is no need to consider if the task is running or not. The deadline and non-negative resource speeds constraints (5, 6, 7 and 8) are all the same equation with the new task included with all of the other tasks. The equation to check that a task is only allocated to a single server is not included as only server *i* considers the task *k*'s price.

In auction theory, four properties are considered: Incentive compatible, budget balanced, economically efficient and individual ra-

- Budget balanced Since the auction is run without an auctioneer, this allows for the auction to be run in a decentralised way resulting in no "middlemen" taking some money so all revenue goes straight to the servers from the tasks
- Individually Rational As the server need to confirm with the task if it is willing to pay an amount to be allocated, the task can check this against its secret reserved price preventing the task from ever paying more than it is willing
- Incentive Compatible Misreporting can give a task as if the task can predict the allocation of resources from server to tasks then tasks can misreport so to be allocate to a certain server that otherwise would result in the task being unallocated.
- · Economic efficiency At the begin then task are almost randomly assigned in till server become full and require kicking tasks off, this means that allocation can fall into a local price maxima meaning that the server will sometime not be 100% economically efficient.

### Algorithm 2 Decentralised Iterative Auction

**Require:** *I* is the set of servers

**Require:** *J* is the set of unallocated tasks, which initial is the set of all tasks to be allocated

**Require:** P(i, k) is solution to the problem in section 4.3.1 using the server *i* and new task *k*. The server's current tasks is known to itself and its current revenue from tasks so not passed as arguments.

**Require:** R(i, k) is a function returning the list of tasks not able to run if task k is allocated to server i

```
Require: \leftarrow_R will randomly select an element from a set
  while |J| > 0 do
```

```
j \leftarrow_R J
    p, i \leftarrow argmin_{i \in I} P(i, j)
    if p \le v_i then
        p_j \leftarrow p
         x_{i,j} \leftarrow 1
         for all j' \in R(i, j) do
             x_{i,j'} \leftarrow 0
p_{j}^{'} \leftarrow 0
J \leftarrow J \cup j^{'}
         end for
    end if
    J \leftarrow J \setminus \{j\}
end while
```

The algorithm 2 is a centralised version of the decentralised iterative auction. It works through iteratively checking a currently unallocated job to find the price if the job was currently allocated on a server. This is done through first solving the program in section 4.3.1 which calculates the new revenue if the task was forced to be allocated with a price of zero. The task price is equal to the current server revenue – new revenue with the task allocated + a price change variable to increase the revenue of the server. The minimum price returned by P(i, k) is then compared to the job's maximum reserve price (that would be private in the equivalent decentralised algorithm) to confirm if the job is willing to pay at that price. If the job is willing then the job is allocated to the minimum price server and the job price set to the agreed price. However in the process of allocating a job then the currently allocated jobs on the server could be unallocated so these jobs allocation's and price's are reset then appended to the set of unallocated jobs.

### 4.4 Attributes of proposed algorithms

In table 3, the important attributes for the proposed algorithm

Attribute	GM	CVA	DIA
Truthfulness		Yes	No
Optimality	No	No	No
Scalability	Yes	Yes	No
Information	All	All	Not the re-
requirements			serve value
from users			
Communication	Low	Low	High
over heads			
Decentralisation	No	No	Yes

Table 3: Attributes of the proposed algorithms: Greedy mechanism (GM), Critical Value auction(CVA) and Decentralised Iterative auction (DIA)

#### 5 EMPIRICAL EVALUATION

To test the algorithms presented in section 4, synthetic models have been used to generate a list of tasks and servers.

The synthetic models have been handcrafted with each attribute being generated from a gaussian distribution with a mean and standard deviation.

To compare the greedy algorithm to the optimal elastic allocation, a branch and bound was implemented to solve the problem in section 3.2. In order to compare to fixed speed equivalent models, the minimum total resource required to run the job is found and set as the resource speeds for all of the tasks, with the optimal solution for running the job with the fixed speeds is found as well. To implement the greedy mechanism, the value density function was  $\frac{v_j}{s_j + w_j + r_j}$ , server selection was  $argmin_{\forall i \in I} S_i' + W_i' + R_i'$  and the resource allocation was  $mins_i' + w_i' + r_i'$  for job j and servers I.

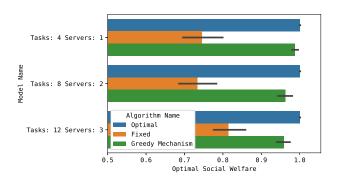


Figure 5: Comparison of the social welfare for the greedy mechanism, optimal, relaxed problem, time limited branch and bound

As figure 5 shows, the greedy mechanism achieves 98% of the optimal solution for the small models, the mechanism achieves within 95% for larger models. In comparison, the fixed allocation achieves 80% of the optimal solution and always does worse than the social welfare of the greedy mechanism.

Figure 6 compares the social welfare of the auction mechanisms: vcg, fixed resource speed vcg, critical value auction and the decentralised iterative auction with different price change variables.

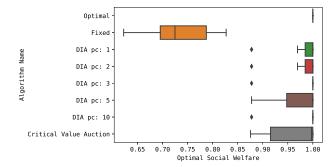


Figure 6: Comparison of the social welfare for the auction mechanisms

VCG is an economically efficient auction that requires the optimal solution to the problem in section 3.2.

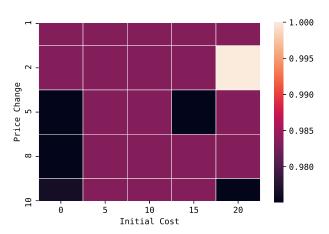


Figure 7: Average number of rounds with a price change variables and task initial cost

Within the context of edge cloud computing, the number of rounds for the decentralised iterative auction is important to making it a feasible auction as it is proportional to the time required to run. We investigated the effect of two heuristic on the number of rounds and social welfare of the auction; the price change variable and initial cost heuristic. With an auction using as minimum heuristic values for the price change and initial cost, figure 7, on average 400 rounds were required for the price to converge while an auction using a price change of 10 and initial cost of 20 means that only on average 80 rounds are required, 5x less. But by using high initial cost and price change heuristics, this can prevent tasks from being allocated, figure 8, shows that the difference in social welfare is only 2% from minimum to maximum heuristics.

### 6 CONCLUSIONS

In this paper, we studied a resource allocation problem in edge clouds, where resources are elastic and can be allocated to tasks at varying speeds to satisfy heterogeneous requirements and deadlines.

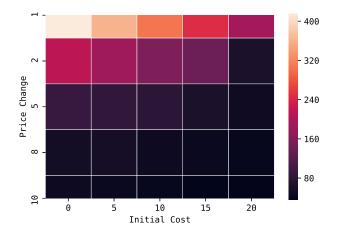


Figure 8: Average social welfare with a price change variables and task initial cost

To solve the problem, we proposed a centralized greedy mechanism with a guaranteed performance bound, and a number of auction-based mechanisms that also consider the elasticity of resources and limit the potential for strategic manipulation. We show that explicitly taking advantage of resource elasticity leads to significantly better performance than current approaches that assume fixed resources.

In future work, we plan to consider the dynamic scenario where tasks arrive and depart from the system over time, and to also consider the case where task preemption is allowed.

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### **Appendix B: SPIE Presentation**

The research of Towers et al. (2020) was presented at SPIE Defense + Commercial Sensing to the conference on Artificial Intelligence and Machine Learning for Multi-Domain Operations Applications II under the title "Analytical agility at the edge of the network through auction mechanisms". Link to the recorded presentation.

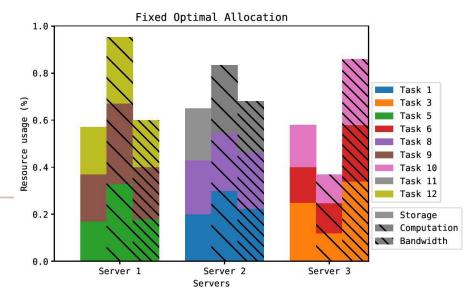


By Mark Towers, Fidan Mehmeti, Sebastian Stein, Tim Norman, Tom La Porta, Caroline Rublein and Geeth De Mel



## Motivation

- Edge cloud computing allows coalitions to run computationally demanding analytical tasks in military tactical networks that couldn't be run locally by the user.
- However, edge cloud computing servers have significantly fewer resources than traditional cloud computing servers.
- They therefore require efficient and effective allocation of these resources to maximise the number of tasks that can be run concurrently
- Previous research considered a fixed allocation scheme where task requested a fixed resource usage
- However, resource bottleneck can easy occur when numerous users over request particular resources, limit the number of tasks that can be run

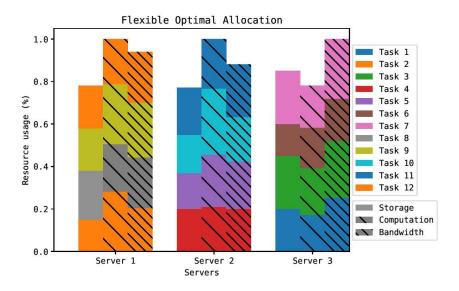


- Here servers are described with three resources (storage, computation and bandwidth).
- Each task uses a percentage of these resources in order to run being the coloured bars.



# Flexible resource allocation mechanism

- Principle That the time taken for an operation to complete is proportional to the amount of resources allocated
- Instead task submit their resource requirement over their lifetime and a deadline to be computed by
- This is used by servers to determine how resources are allocated to individual tasks
- Algorithm aims is to maximise the social welfare (sum of task values' that are computed within the deadline)
- This proposes research challenges as no previous algorithms exist that are compatible with this mechanism and to deal with self-interested task owners who may wish to misreport their task values and requested resources.



### Deadline Constraint

$$\frac{s_j}{s_j'} + \frac{w_j}{w_j'} + \frac{r_j}{r_j'} \le d_j$$

Sj	Required Storage	s <sub>j</sub> '	Loading task speed
w <sub>j</sub>	Required computation	s <sub>j</sub> '	Compute speed
r <sub>j</sub>	Required results data	r <sub>j</sub> '	Sending results speed
dj	Deadline		3



# Optimisation problem

$$\max \sum_{\forall j \in I} v_j \left( \sum_{\forall i \in I} x_{i,j} \right) \tag{1}$$

s.t.

$$\sum_{\forall j \in J} s_j x_{i,j} \le S_i, \qquad \forall i \in I, \qquad (2)$$

$$\sum_{\forall j \in J} w'_{j} x_{i,j} \le W_{i}, \qquad \forall i \in I, \qquad (3)$$

$$\sum_{\forall i \in I} (r'_j + s'_j) \cdot x_{i,j} \le R_i, \qquad \forall i \in I, \qquad (4)$$

$$\frac{s_j}{s_i'} + \frac{w_j}{w_i'} + \frac{r_j}{r_i'} \le d_j, \qquad \forall j \in J, \qquad (5)$$

$$0 \le s_{j}^{'} \le \infty, \qquad \forall j \in J, \qquad (6)$$

$$0 \le w_{j}^{'} \le \infty, \qquad \forall j \in J, \qquad (7)$$

$$0 \le r_{j}^{'} \le \infty,$$
  $\forall j \in J,$  (8)

$$\sum_{\forall i \in I} x_{i,j} \le 1, \qquad \forall j \in J, \qquad (9)$$

$$x_{i,j} \in \{0,1\},$$
  $\forall i \in I, \forall j \in J.$  (10)

- Using this flexibility principle, an optimisation problem can be mathematically described
- The aim is to maximise the sum of task value that can be computed within the task deadline (equation 1)
- Constraints 2-4 limit the resource usage to be within server capacity
- Constraint 5 forces the task to be completed within its deadline
- Constraints 6-8 force the resource speeds to be positive
- Constraints 9-10 limit a task be allocated to only a single server
- This problem is NP-Hard due to being a knapsack problem

s <sub>j</sub>	Required Storage for task j	s <sub>j</sub> ′	Loading task speed for task j
w <sub>j</sub>	Required computation for task j	s <sub>j</sub> '	Compute speed for task j
rj	Required results data for task j	r <sub>j</sub> ′	Sending results speed for task j
d <sub>j</sub>	Deadline for task j	Vj	Value of task j
S <sub>i</sub>	Storage capacity of server i	Wi	Computational capacity of server i
R <sub>i</sub>	Bandwidth capacity of server i	$X_{i,j}$	Allocation of task j to server i



## Approaches

Properties	Greedy mechanism	Critical value auction	Decentralised Iterative auction
Strategyproof	No	Yes	No
Optimal	No	No	No (however this does occur a majority of the time)
Scalability	High	High	Medium
Information requirements from users	All information	All information	All information except the reserved private value
Communications overhead	Low	Low	High
Decentralisation	No	No	Yes

## Greedy mechanism

- The algorithm has a lower-bound of 1/n of the optimal welfare. This is as it unknown after the first task is allocated if any subsequent tasks can be allocated. However in practice, this case almost never occurs.
- Algorithm steps:
  - 1. The list of tasks are sorted in descending order by a value density function.
  - 2. For each task in the sorted list, a server is selected from the list of available servers using the server selection function.
  - Then the resource allocated is determined by a resource allocation function for the task on the server
- As a results, the algorithm has polynomial time complexity
- The algorithm however assumes that tasks are not lying about their attributes like value or required resources. This problem is addressed by the critical value auction.

### Algorithm 1 Greedy Mechanism

**Require:** *J* is the set of tasks and *I* is the set of servers

**Require:**  $S_{i}^{'}$ ,  $W_{i}^{'}$  and  $R_{i}^{'}$  is the available resources (storage, computation and bandwidth respectively) for server i.

**Require:**  $\alpha(j)$  is the value density function of a task

**Require:**  $\beta(j, I)$  is the server selection function of a task and se of servers returning the best server, or  $\emptyset$  if the task is not able to be run on any server

**Require:**  $\gamma(j, i)$  is the resource allocation function of a task and server returning the loading, compute and sending speeds

**Require:** sort(X, f) is a function that returns a sorted list of elements in descending order, based on a set of elements and a function for comparing elements

```
J' \leftarrow sort(J, \alpha)

for all j \in J' do

i \leftarrow \beta(j, I)

if i \neq \emptyset then

s'_j, w'_j, r'_j \leftarrow \gamma(j, i)

x_{i,j} \leftarrow 1

end if

end for
```



## • Single parameter domain auctions are a well-researched area in mechanism design, with the critical value being the minimum value a buyer must report such that the item is still sold to them.

- Using the critical value, strategyproof (weakly-dominant incentive compatible) auctions can be created using the greedy mechanism previously explained as the method of calculating each task's critical value.
- Auction steps:

Critical value

auction

- 1. The greedy mechanism is run with the reported task values to find the task that would be allocated
- 2. For each task that would be allocated, we find the critical value for the task, the user then pays this value instead of the reported value as in the greedy mechanism. The critical value is found by:
  - a. Removing the task from the list of sorted tasks (greedy mechanism step 1)
  - b. Running the greedy mechanism normally except after each task is allocated checking if the task can still be allocated on any server
  - c. Once the task is unable to be allocated to any server, the critical value density is equal to the value density of last task allocated
  - d. The critical value is equal to the inverse of the value density function using the critical value density
- Due to the use of the greedy mechanism, the auction inherits the same social welfare performance as the greedy mechanism
- The auction's time complexity is still polynomial as well, as it just computes the greedy mechanism multiple times, up to number of tasks + 1.
- While any value density function can be used, in order for the auction to be strategyproof, the value density function used must be monotonic meaning that if the user misreports a task attribute, the value density must decrease.



# Decentralised iterative auction

- While the critical value auction is incentive compatible, it requires the revelation of a task's value.
- However, for some users, e.g., in tactical networks, they may not wish to reveal this information to other coalition partners.
- The VCG mechanism works by calculating the price of an auction item by finding the difference in social welfare when the task exists and doesn't exist
- We modify this mechanism to be decentralised instead of centralised such that each server calculates the difference. To do this requires a modified optimisation problem for the server to maximise task prices instead of task values.
- Auction steps:
  - 1. Unallocated tasks is equal to a initial list of tasks
  - 2. While unallocated tasks has tasks
    - A. Select a random task from the list of unallocated tasks
    - B. The task price is the minimum price from all of the servers which calculates its price using the modified optimisation problem
    - C. If the task price is greater than the minimum price then the task is disregard otherwise allocate the task to the server
    - D. However by allocated the task to the server, other tasks may be kicked off. These task are added back to the unallocated tasks list

### Algorithm 2 Decentralised Iterative Auction

Require: I is the set of servers

Require: J is the set of unallocated tasks, which initial is the set of all tasks to be allocated

Require: P(i, k) is solution to the problem in section 4.3.1 using the server i and new task k. The server's current tasks is known to itself and its current revenue from tasks so not passed as arguments.

**Require:** R(i, k) is a function returning the list of tasks not able to run if task k is allocated to server i

```
Require: \leftarrow_R will randomly select an element from a set
```

```
while |J| > 0 do

j \leftarrow_R J

p, i \leftarrow argmin_{i \in I} P(i, j)

if p \leq v_j then

p_j \leftarrow p

x_{i,j} \leftarrow 1

for all j' \in R(i, j) do

x_{i,j'} \leftarrow 0

p'_j \leftarrow 0

J \leftarrow J \cup j'

end for

end if

J \leftarrow J \setminus \{j\}

end while
```



# Modified server optimisation problem

- A task's price is equal to the difference in the server revenue (the task doesn't exist) to when the task is included with a price of zero (plus a small value)
- This modifications to the general optimisation problem is that it is only for single server with the new task referred to as n'.
- The resulting constraints are extremely similar except that the new task is forced to be allocated to the server.
  - Objective function is to maximise the sum of computed task prices (Equation 11)
  - Constraints 12-14 limit the resource usage to be within server capacity
  - Constraint 15 forces the task to be completed within its deadline including the new task.
  - Constraints 16-18 force the resource allocation to be positive for all tasks
  - Constraints 19 limits task allocation to be binary

$$\max \sum_{\forall n \in N} p_n x_n \tag{11}$$

s.t.

$$\sum_{\forall n \in N} s_n x_n + s_{n'} \le S_m, \tag{12}$$

$$\sum_{\forall n \in N} w'_n x_n + w_{n'} \le W_m, \tag{13}$$

$$\sum_{\forall n \in N} (r_{n}^{'} + s_{n}^{'}) \cdot x_{n} + (r_{n^{'}}^{'} + s_{n^{'}}^{'}) \le R_{m}, \tag{14}$$

$$\frac{s_n}{s_n'} + \frac{w_n}{w_n'} + \frac{r_n}{r_n'} \le d_n, \qquad \forall n \in N \cup \{n'\}$$

$$\tag{15}$$

$$0 < s_{n}^{'} < \infty, \qquad \forall n \in N \cup \{n^{'}\}$$
(16)

$$0 < w_n' < \infty, \qquad \forall n \in N \cup \{n'\}$$

$$\tag{17}$$

$$0 < r_{n}^{'} < \infty, \qquad \forall n \in N \cup \{n'\}$$

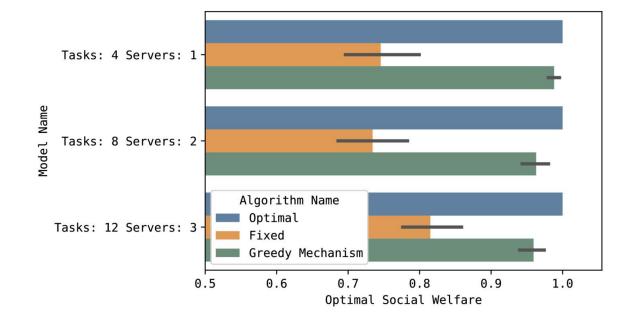
$$\tag{18}$$

$$x_n \in \{0, 1\} \qquad \forall n \in N \tag{19}$$



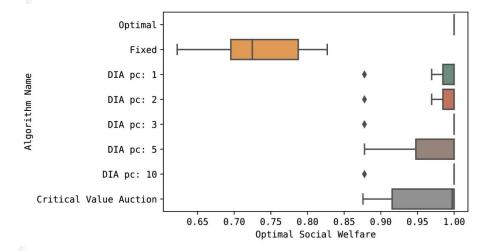
# Greedy mechanism and critical value auction results

- To compare our algorithm, we implemented a time-limited optimal solver and a fixed resource allocation mechanism where the task resource usage is fixed between the server preventing any flexibility.
- These results compare the proportion of the optimal social welfare (sum of the computed task values).
- We compared results over a range of environments with different levels of supply and demand.
- With environment that have extremely high demand over a single resources, our system is extremely advantageous as it can deal with this type of pressure that normally is not possible. In cases where server resources are well distributed then this mechanism achieves similar results as the fixed version.



# Decentralised Iterative auction

- The VCG auction is an economically efficient auction that finds the optimal allocation to calculate prices. We therefore use the VCG for the optimal flexible and fixed results.
- We found that a majority of the time, the DIA achieves the optimal social welfare however sometimes falls into a local optima
- We also found that the value of the price change doesn't effect the social welfare of the solution much.



### Conclusion and future work

- In this work, we have presented a novel resource allocation optimisation problem along with a greedy mechanism to maximise social welfare. Along with two auction mechanisms: critical value auction for strategyproof auctions and a novel decentralised iterative auctions for users who don't wish to reveal their private task value.
- Future work is to consider an online case of this work as tasks arrive over time instead resources being allocated in batches.

### **Appendix C: Agent hyperparameters**

During training there are a range of hyperparameters for each agent, table 1 provides an explanation for the values for each hyperparameter used in the project.

Agent	Properties name	Value	Explanation
RL Agent	batch_size	32	The number of trajectories from
			the experience replay buffer that
			are used each time to train an
			agent.
RL Agent	error_loss_fn	tf.losses.	The loss function used in
		huber_loss	calculating a network's error.
RL Agent	initial_training_	5000	The number of trajectories in
	replay_size		the experience replay buffer
			required before the agent begins
			training.
RL Agent	training_freq	2	For every trajectory added to
			the experience replay buffer, for
			each 2, the agent tries to be
			trained.
RL Agent	discount_factor	0.9	Within the Q learning function
			(equation (2.3)), the discount
			factor determines how
			important the rewards in
			the future impact the Q value.
RL Agent	replay_buffer_	25000	The length of the circular
	length		experience replay buffer.
RL Agent	save_frequency	25000	The agent networks are saved
			after 25000 time that agent has
			been trained
RL Agent	training_loss_	250	Tensorboard allows for data to
	log_freq		be saved using training, after
			every the agent has been trained
			250 time, the agents loss is
			logged for future analysis.

Task	reward_scaling	1	
Pricing RL			
Agent			
Task	failed_auction_	-0.05	The reward for when the agent
Pricing RL	reward		bids on a task but fails to win the
Agent			auctioned task.
Task	failed_multiplier	-1.5	A multiplier applied to the
Pricing RL			winning price is the task fails
Agent			to be computed within its
			deadline.
Resource	other_task_discount	0.4	The multiplier to tasks not
weighting			under consideration for a
RL Agent			weighting action.
Resource	success_reward	1	The reward when the agent
weighting			successfully completes a task
RL Agent			
Resource	failed_reward	-1.5	The reward when the agent fails
weighting			to complete a task within its
RL Agent			deadline.
Dqn	target_update_tau	1.0	The update tau value for use in
Agent			the target update frequency.
Dqn	target_update_freq	2500	The target network in the DQN
Agent			agent is updated after the agent
			has been updated 2500 times.
Dqn	initial_epsilon	1	The initial exploration factor
Agent			during training
Dqn	final_epsilon	0.1	The final exploration factor
Agent			during training
Dqn	epsilon_steps	10000	The number of training step
Agent			for linear exploration to move
			between the initial_epsilon and
			the final_epsilon factor.
Dueling	double_loss	True	If to use the double dqn loss
Dqn			function
Agent			

Categorical min_value	Categorical	max_value	-20.0	The maximum value for the
Categorical Dqn Agent	Dqn			value distribution
Dqn Agent	Agent			
Categorical Dqn Agent	Categorical	min_value	25.0	The minimum value for the
Categorical Dqn Agent Ddpg actor_learning_rate 0.0001 The learning rate for the optimiser for the actor network. Ddpg critic_learning_rate 0.0005 The learning rate for the optimiser for the critic network. Ddpg initial_epsilon_std Agent Ddpg final_epsilon_std Agent Ddpg actor_target_ update_freq update_freq Ddpg upper_action_ bound Task min_value for the actor network action.  The number of atoms for each actions.  The learning rate for the optimiser for the critic network.  The learning rate for the optimiser for the critic network.  The initial exploration standard deviation of the normal distribution used during training.  The final exploration standard deviation of the normal distribution used during training.  The actor target network update frequency  The critic target network update frequency  The critic target network update frequency  The upper action bound for the actor network  Task min_value -100.0 The minimum value for the critic network to estimate for an action  Task max_value 100.0 The maximum value for the critic network to estimate for an action  The pricing Ddpg action action bound for the critic network to estimate for an action	Dqn			value distribution
Dqn Agent  Ddpg Actor_learning_rate Agent  Ddpg Critic_learning_rate Agent  Ddpg Initial_epsilon_std Agent  Ddpg  Ddpg Agent  Ddpg  Ddpg  Agent  Ddpg	Agent			
Agent Ddpg actor_learning_rate 0.0001 The learning rate for the optimiser for the actor network.  Ddpg critic_learning_rate 0.0005 The learning rate for the optimiser for the critic network.  Ddpg initial_epsilon_std 0.8 The initial exploration standard deviation of the normal distribution used during training  Ddpg final_epsilon_std 0.05 The final exploration standard deviation of the normal distribution used during training  Ddpg actor_target_ update_freq update_freq update_freq 1500 The critic target network update frequency  Ddpg upper_action_ 30.0 The upper action bound for the actor network  Task min_value -100.0 The minimum value for the critic network to estimate for an action  Ddpg Agent  Task max_value 100.0 The maximum value for the critic network to estimate for an action	Categorical	num_atoms	21	The number of atoms for each
Ddpg critic_learning_rate deviation of the normal distribution used during training deviation of the normal distribution used during	Dqn			actions.
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Agent Ddpg initial_epsilon_std 0.8 The initial exploration standard deviation of the normal distribution used during training  Ddpg final_epsilon_std 0.05 The final exploration standard deviation of the normal distribution used during training  Ddpg actor_target_ update_freq Update	Agent			optimiser for the actor network.
Ddpg   initial_epsilon_std   0.8   The initial exploration standard deviation of the normal distribution used during training    Ddpg   final_epsilon_std   0.05   The final exploration standard deviation of the normal distribution used during training    Ddpg   actor_target_ update_freq   3000   The actor target network update frequency    Ddpg   critic_target_ update_freq   1500   The critic target network update frequency    Ddpg   upper_action_ bound   30.0   The upper action bound for the actor network    Task   min_value   -100.0   The minimum value for the critic network to estimate for an action    Task   max_value   100.0   The maximum value for the critic network to estimate for an action    Task   critic_target_ action_ bound   The maximum value for the critic network to estimate for an action    Task   max_value   100.0   The maximum value for the critic network to estimate for an action	Ddpg	critic_learning_rate	0.0005	The learning rate for the
Agent deviation of the normal distribution used during training  Ddpg final_epsilon_std 0.05 The final exploration standard deviation of the normal distribution used during training  Ddpg actor_target_ 3000 The actor target network update frequency  Ddpg critic_target_ 1500 The critic target network update frequency  Ddpg update_freq frequency  Ddpg upper_action_ 30.0 The upper action bound for the actor network  Task min_value -100.0 The minimum value for the critic network to estimate for an action  Task max_value 100.0 The maximum value for the critic network to estimate for an action  Ddpg Agent The maximum value for the critic network to estimate for an action  Ddpg Agent The maximum value for the critic network to estimate for an action	Agent			optimiser for the critic network.
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Ddpg Agent  Task pricing Ddpg  Agent  Touch  Task pricing Ddpg  The maximum value for the critic network to estimate for an action	Task	min_value	-100.0	The minimum value for the
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Task max_value 100.0 The maximum value for the critic network to estimate for an action				
Ddpg action		max_value	100.0	The maximum value for the
Ddpg action	pricing			critic network to estimate for an
	1			action
Agent				

Resource	min_value	-20	The minimum value for the
allocation			critic network to estimate for an
Ddpg			action
Agent			
Resource	max_value	15	The maximum value for the
allocation			critic network to estimate for an
Ddpg			action
Agent			
TD3	actor_update_freq	3	The actor network update
Agent			frequency for each critic
			network update.

TABLE 1: Agent hyperparameters

## Appendix D: Fixed Resource Allocation Optimisation Problem

Using the Flexible Resource Allocation Optimisation problem from Section 3.1, to convert the problem to a Fixed Resource Allocation Optimisation problem requires two stages.

The first of these is to convert the flexible task specification to a fixed task specification, by solving the linear programming equations 1 and 2. The equations forces the resource usage speeds  $(s'_j, w'_j \text{ and } r'_j)$  to be within the deadline (equation 2) and that the objective function is to minimise the total resources used. The reason for speeds being raise to the power is to prevent over use of a single resources (e.g. 5 loading speeds, 3 compute speed, 10 sending speed).

minimise 
$$1.2^{s'_j} + 1.2^{w'_j} + 1.2^{r'_j}$$
 (1)

s.t

$$\frac{s_j}{s_j'} + \frac{w_j}{w_j'} + \frac{r_j}{r_j'} \le d_j - a_j \tag{2}$$

(3)

The second stage is using the Fixed task specifications, to construct the server resource allocation optimisation problem. The objective function (equation 4) is to maximise the number of tasks that are completed. The updated fixed tasks are denoted I'. Due to there being a fixed resource allocation, the server allocates all of the required resources over the tasks whole lifetime. As a result, the server computational and bandwidth capacity constraints (equations 6 and 7) allocates a task's resources over its whole lifetime. The server's storage constraint is similar except with a task's storage increasing till the whole task's required storage is included.

$$\max \sum_{i \in I, j \in J'} x_{i,j} \tag{4}$$

s.t.

$$\sum_{\substack{\{j \in J' \mid a_j \le t \le d_j\}}} \min(s_j, s_j' \cdot (t+1-a_j)) \cdot x_{i,j} \le S_i \qquad \forall i \in I$$

$$\sum_{\substack{\{j \in J' \mid a_j \le t \le d_j\}}} w_j' x_{i,j} \le W_i \qquad \forall i \in I$$

$$\sum_{\substack{\{j \in J' \mid a_j \le t \le d_j\}}} (s_j' + r_j') \cdot x_{i,j} \le R_i \qquad \forall i \in I$$

$$\{j \in J' \mid a_j \le t \le d_j\} \qquad \forall i \in I$$

$$\{j \in J' \mid a_j \le t \le d_j\} \qquad (7)$$

$$\sum_{\substack{(j \in J' | a_i \le t \le d_i\}}} w_j' x_{i,j} \le W_i$$
  $\forall i \in I$  (6)

$$\sum_{\{j \in J' \mid a_j \le t \le d_j\}} (s'_j + r'_j) \cdot x_{i,j} \le R_i \qquad \forall i \in I$$
 (7)

$$\sum_{i \in I} x_{i,j} \le 1 \tag{8}$$

$$x_{i,j} \in \{0,1\} \qquad \forall i \in I, j \in J' \qquad (9)$$

### **Appendix E: Project management**

To management this project has been difficult due to splitting my time between writing the academic paper at the start of the year (plus creating the recorded presentation) and the programming and write up the expanded research. Because of this, a risk assessment (Table 2) to understand possible risks during the project. The project was also planned using a grantt chart (figure 2) to understand the progress of the project over time and to plan how the project would run. The project brief is submitted in October 2019 is included at the end of this report as well. The word count of the project generated by texcount for chapters 1 to 6 is included.

The general plan for the project in the project briefing was kept to with very small changed like the real-world data from the Google data center was found to be incompatible with the resource requirements therefore dropped.

### Risk assessment

Risk	Severity	Possibility	Explanation
Rejected paper	1	4	The paper (Appendix A) was
submission			submitted to the AAMAS 2020
			conference in December that could
			be rejected. While this was be
			disappointing if this happened,
			the paper can still be submitted to
			another conference at a later time.
Iridis failure	5	1	In order to train the agent in
			this project, the University of
			Southampton supercomputer, Iridis
			5 was utilised so if this could not
			be used anymore. This was cause
			massive issues to be able to train all
			of the agents for both long enough.
Agent Training	4	2	Reinforcement learning agents can
time			take several million actions to achieve
			effective results which takes days or
			weeks to learn. This project doesn't
			have such resources or time to spend
			training agents to do this therefore
			making it a large problem.
Personal Illness	4	1	Physical illness or injury could
or Injury			prevent the project from being both
			programmed or written.
Pandemic	4	1	While Pandemic will not prevent the
			project from being completed due
			to all work being digital, it would
			prevent talking with my supervisor in
			person or for University to be open.

TABLE 2: Risk Assessment

### **Progress Grantt Chart**

For the expected progress grantt chart (figure 1), most of the time scales are accurate expect didn't allocate enough time to write the report. However this was realised during the project and so report was started another month early due to the required work to rewrite the background literature and write the solution and implementation. This is shown in the updated actual progress grantt chart in Figure 2.

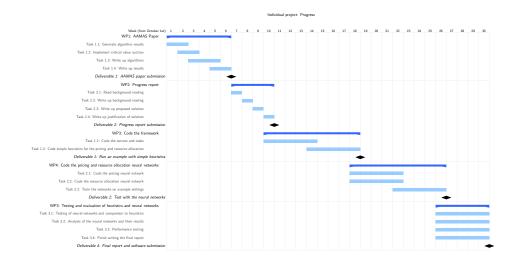


FIGURE 1: Expected Progress Grantt chart

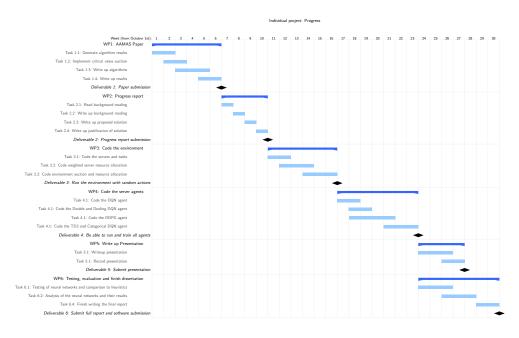


FIGURE 2: Actual Progress Grantt chart

### Project Brief

Mark Towers

October 2019

### 1 Problem

When computer programs are too large, difficult or time consuming to be run on a normal computer, these programs are often offloaded to cloud providers like Google Cloud Platform, Amazon Web Service, Microsoft Azure and many more. These providers all allow customers to individually request a set of resources to compute their program with. However, this can create a bottleneck on certain resource preventing other jobs from running with this fixed requirement model. This project considers the case where users don't request a set amount of resources but rather the user details the total requirements for the program and a deadline for when the program must be finished. This then means that the cloud provider can effectively balances resource demands as it has complete knowledge of its different user's requirements, allowing more jobs to run simultaneously and lower price as there can be a lower overall demand of individual resources.

This research is being done in conjunction with the DAIS ITA project with previous work done by myself, Dr Sebastian Stein and a team from Pennsylvania State University. The difference between the prior work done and this proposed work is to introduce the idea of time more fully into the problem case. Where previously, all jobs would arrive at the beginning of the program and the resources speeds allocated would be fixed for the rest of the program, in this work, jobs will arrive over time and at each time step then the resource speeds allocated can change.

To do this, I believe that I will have to create two algorithms, the first to evaluate a price to charge jobs for running on the cloud provider and second to know how to allocate resources for each jobs currently allocated to the cloud provider at a given time step.

### 2 Goals

The goal of the project is to apply reinforcement learning to solve the two problem stated above. This is because to the two functions above are too complex for humans to describe effectively and I believe that a universal function approximation will be able to learn them over time through the use of a reward function based on the revenue caused by finishing a job.

### 3 Scope

The scope of this project is to investigate the use of reinforcement learning in solving this program and if time allows compare to greedy or handcrafted algorithms. We will test the effectiveness of these algorithms through synthetic data and real world data from a google data center.

### Word count

```
File: chapters/1_introduction.tex
Encoding: ascii
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Words in text: 977
Words in headers: 1
Words outside text (captions, etc.): 69
Number of headers: 1
Number of floats/tables/figures: 0
Number of math inlines: 0
Number of math displayed: 0
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Number of headers: 3
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Number of math displayed: 1
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 76+2+0 (1/0/0/0) Chapter: Literature Review
 667+8+0 (1/0/1/0) Section: Resource Allocation and Pricing Mechanisms
        in Cloud Computing
 724+2+8 (1/1/0/1) Section: Reinforcement Learning
File: chapters/3_solution.tex
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Number of headers: 6
Number of floats/tables/figures: 4
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1847+29+8 (7/1/0/3) File(s) total: chapters/4\_implementation.tex
2092+27+188 (7/16/0/0) File(s) total: chapters/5\_evaluation.tex
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