

$$\frac{\partial \mathbf{U}}{\partial t} + \frac{\partial \mathbf{E}}{\partial x} + \frac{\partial \mathbf{F}}{\partial y} + \frac{\partial \mathbf{G}}{\partial z} = 0$$

$$\frac{\partial \mathbf{U}_1}{\partial t} + \frac{\partial \mathbf{E}_1}{\partial \xi} + \frac{\partial \mathbf{F}_1}{\partial \eta} + \frac{\partial \mathbf{G}_1}{\partial \zeta} = 0$$

$$\begin{aligned}\mathbf{U}_1 &= \frac{\mathbf{U}}{J} \\ \mathbf{E}_1 &= \frac{1}{J} (\mathbf{E}\xi_x + \mathbf{F}\xi_y + \mathbf{G}\xi_z) \\ \mathbf{F}_1 &= \frac{1}{J} (\mathbf{E}\eta_x + \mathbf{F}\eta_y + \mathbf{G}\eta_z) \\ \mathbf{G}_1 &= \frac{1}{J} (\mathbf{E}\zeta_x + \mathbf{F}\zeta_y + \mathbf{G}\zeta_z)\end{aligned}$$

$$\begin{aligned}J &= \frac{\partial(\xi, \eta, \zeta)}{\partial(x, y, z)} = \begin{vmatrix} \xi_x & \xi_y & \xi_z \\ \eta_x & \eta_y & \eta_z \\ \zeta_x & \zeta_y & \zeta_z \end{vmatrix} \\ &= \xi_x(\eta_y\zeta_z - \eta_z\zeta_y) - \xi_y(\eta_x\zeta_z - \eta_z\zeta_x) + \xi_z(\eta_x\zeta_y - \eta_y\zeta_x)\end{aligned}$$

$$\begin{aligned}\mathbf{E} &= (\mathbf{E}_i - \mathbf{E}_v) \\ \mathbf{F} &= (\mathbf{F}_i - \mathbf{F}_v) \\ \mathbf{G} &= (\mathbf{G}_i - \mathbf{G}_v)\end{aligned}$$

$$\begin{aligned}&\frac{\partial}{\partial t} \left(\frac{\mathbf{U}}{J} \right) + \\ &\frac{\partial}{\partial \xi} \left\{ \frac{1}{J} [\xi_x (\mathbf{E}_i - \mathbf{E}_v) + \xi_y (\mathbf{F}_i - \mathbf{F}_v) + \xi_z (\mathbf{G}_i - \mathbf{G}_v)] \right\} + \\ &\frac{\partial}{\partial \eta} \left\{ \frac{1}{J} [\eta_x (\mathbf{E}_i - \mathbf{E}_v) + \eta_y (\mathbf{F}_i - \mathbf{F}_v) + \eta_z (\mathbf{G}_i - \mathbf{G}_v)] \right\} + \\ &\frac{\partial}{\partial \zeta} \left\{ \frac{1}{J} [\zeta_x (\mathbf{E}_i - \mathbf{E}_v) + \zeta_y (\mathbf{F}_i - \mathbf{F}_v) + \zeta_z (\mathbf{G}_i - \mathbf{G}_v)] \right\} = 0\end{aligned}$$

$$\mathbf{A} = \begin{bmatrix} \text{Continuity} \\ \text{x-Momentum} \\ \text{y-Momentum} \\ \text{z-Momentum} \\ \text{Energy} \end{bmatrix}$$

$$\mathbf{U} = \begin{bmatrix} \rho \\ \rho u \\ \rho v \\ \rho w \\ E_t \end{bmatrix}$$

$$E_t = \rho \left(e + \frac{u^2 + v^2 + w^2}{2} \right)$$

$$p = \rho RT$$

$$(p + a\rho^2) \left(\frac{1}{\rho} - b \right) = RT$$

$$\mathbf{E}_i = \begin{bmatrix} \rho u \\ \rho u^2 + p \\ \rho uv \\ \rho uw \\ (E_t + p)u \end{bmatrix} \quad \mathbf{F}_i = \begin{bmatrix} \rho v \\ \rho uv \\ \rho v^2 + p \\ \rho vw \\ (E_t + p)v \end{bmatrix} \quad \mathbf{G}_i = \begin{bmatrix} \rho w \\ \rho uw \\ \rho vw \\ \rho w^2 + p \\ (E_t + p)w \end{bmatrix}$$

$$\mathbf{E}_v = \begin{bmatrix} 0 \\ \tau_{xx} \\ \tau_{xy} \\ \tau_{xz} \\ u\tau_{xx} + v\tau_{xy} + w\tau_{xz} - q_x \end{bmatrix}$$

$$\mathbf{F}_v = \begin{bmatrix} 0 \\ \tau_{xy} \\ \tau_{yy} \\ \tau_{yz} \\ u\tau_{xy} + v\tau_{yy} + w\tau_{yz} - q_y \end{bmatrix}$$

$$\mathbf{G}_v = \begin{bmatrix} 0 \\ \tau_{xz} \\ \tau_{yz} \\ \tau_{zz} \\ u\tau_{xz} + v\tau_{yz} + w\tau_{zz} - q_z \end{bmatrix}$$

$$\begin{aligned}
\tau_{xx} &= \frac{2}{3}\mu [2(\xi_x u_\xi + \eta_x u_\eta + \zeta_x u_\zeta) - (\xi_y v_\xi + \eta_y v_\eta + \zeta_y v_\zeta) - (\xi_z w) \xi + \eta_z w_\eta + \zeta_z w_\zeta] \\
\tau_{yy} &= \frac{2}{3}\mu [2(\xi_y v_\xi + \eta_y v_\eta + \zeta_y v_\zeta) - (\xi_x u_\xi + \eta_x u_\eta + \zeta_x w_\zeta) - (\xi_z w) \xi + \eta_z w_\eta + \zeta_z w_\zeta] \\
\tau_{zz} &= \frac{2}{3}\mu [2(\xi_z w_\xi + \eta_z w_\eta + \zeta_z w_\zeta) - (\xi_x u_\xi + \eta_x u_\eta + \zeta_x w_\zeta) - (\xi_y v_\xi + \eta_y v_\eta + \zeta_y v_\zeta)]
\end{aligned}$$

$$\begin{aligned}
\tau_{xy} &= \mu (\xi_y u_\xi + \eta_y u_\eta + \zeta_y u_\zeta + \xi_x v_\xi + \eta_x v_\eta + \zeta_x v_\zeta) \\
\tau_{xz} &= \mu (\xi_z u_\xi + \eta_z u_\eta + \zeta_z u_\zeta + \xi_x w_\xi + \eta_x w_\eta + \zeta_x w_\zeta) \\
\tau_{yz} &= \mu (\xi_z v_\xi + \eta_z v_\eta + \zeta_z v_\zeta + \xi_y w_\xi + \eta_y w_\eta + \zeta_y w_\zeta)
\end{aligned}$$

$$\begin{aligned}
q_x &= -k(\xi_x T_\xi + \eta_x T_\eta + \zeta_x T_\zeta) \\
q_y &= -k(\xi_y T_\xi + \eta_y T_\eta + \zeta_y T_\zeta) \\
q_z &= -k(\xi_z T_\xi + \eta_z T_\eta + \zeta_z T_\zeta)
\end{aligned}$$