

# MLP (Multi-Layer Perceptron)

- Neural Networks

- Computing systems vaguely inspired by the biological neural networks that constitute animal brains
- **Function approximators that stack affine transformations followed by nonlinear transformations.**

- Linear Neural Networks

- Data:  $\mathcal{D} = \{(x_i, y_i)\}_{i=1}^N$
- Model:  $\hat{u} = wx + b$
- Loss:  $\text{loss} = \frac{1}{N} \sum_{i=1}^N (y_i - \hat{y}_i)^2$

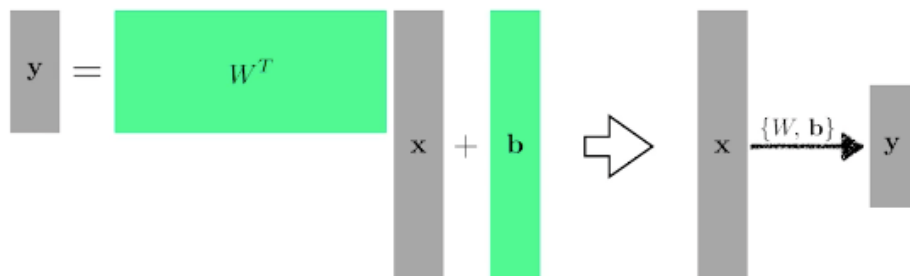
$$\begin{aligned} \frac{\partial \text{loss}}{\partial w} &= \frac{\partial}{\partial w} \frac{1}{N} \sum_{i=1}^N (y_i - \hat{y}_i)^2 \\ &= \frac{\partial}{\partial w} \frac{1}{N} \sum_{i=1}^N (y_i - wx_i - b)^2 \\ &= \frac{1}{N} \sum_{i=1}^N -2(y_i - wx_i - b)x_i \end{aligned}$$

$$\begin{aligned} \frac{\partial \text{loss}}{\partial b} &= \frac{\partial}{\partial b} \frac{1}{N} \sum_{i=1}^N (y_i - \hat{y}_i)^2 \\ &= \frac{\partial}{\partial b} \frac{1}{N} \sum_{i=1}^N (y_i - wx_i - b)^2 \\ &= \frac{1}{N} \sum_{i=1}^N -2(y_i - wx_i - b) \end{aligned}$$

$$w \leftarrow w - \eta \frac{\partial \text{loss}}{\partial w}$$

$$b \leftarrow b - \eta \frac{\partial \text{loss}}{\partial b}$$

- $\eta$  (Stepsize) 적절하게 잡는 것 중요



$$y = W_3^T h_2 = W_3^T \rho(W_2^T X h_1) = W_3^T \rho(W_2^T \rho(W_1^T X))$$

- Non-linear transform ( $\rho$ ), activation functions(활성함수)이 들어야 네트워크를 깊게 쌓았을 때 의미 있음

- Activation functions

- ReLU (Rectified Linear Unit)
- sigmoid
- tanh (Hyperbolic Tangent)

- Universal approximation theory
  - 히든 레이어가 1개 있는 신경망의 표현력은 일반적인 continuous function들을 포함함
  - 존재성에 대한 증명 (어떻게 찾는지까지에 대한 이론은 아님)
- Loss functions

- Regression Task

$$\text{MSE} = \frac{1}{N} \sum_{i=1}^N \sum_{d=1}^D \left( y_i^{(d)} - \hat{y}_i^{(d)} \right)^2$$

- Classification Task

$$\text{CE} = -\frac{1}{N} \sum_{i=1}^N \sum_{d=1}^D y_i^{(d)} \log \hat{y}_i^{(d)}$$

- Probabilistic Task

$$\text{MLE} = \frac{1}{N} \sum_{i=1}^N \sum_{d=1}^D \log \mathcal{N} \left( y_i^{(d)}; \hat{y}_i^{(d)}, 1 \right) \quad (= \text{MSE})$$