

# Enhanced Federated Multi-Armed Bandits Under Byzantine Attacks: Trust-Weighted and Trimmed Mean Robust Aggregation

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**Abstract**—Federated Multi-Armed Bandits (FMAB) represent a powerful framework for decentralized decision-making in environments where clients must learn optimal actions (arms) collaboratively without sharing raw data, thereby ensuring privacy. However, the robustness of FMAB is severely challenged in adversarial settings, particularly when some clients act maliciously (Byzantine behavior) to degrade the system’s performance. The existing baseline algorithm, Fed-MoM-UCB, mitigates this threat using the median-of-means (MoM) strategy, which is statistically robust when the number of Byzantine clients per group remains below 50%. Yet, its effectiveness sharply deteriorates beyond this threshold, rendering it vulnerable in highly adversarial environments.

To address this critical limitation, we propose an enhanced FMAB framework incorporating two key innovations. First, a *trust-based weighting mechanism* dynamically assigns reliability scores to client updates based on historical behavior, enabling the system to progressively downweight contributions from suspected Byzantine clients without requiring explicit identification. Second, we introduce a *median trimmed mean (MTM) aggregation rule*, which augments the robustness of group-level updates by discarding extreme outlier values before computing medians, thereby safeguarding the aggregation even when a majority of clients are adversarial.

We provide rigorous theoretical analysis demonstrating that these techniques jointly improve the resilience of federated bandit learning under Byzantine attacks, yielding stronger Probably Approximately Correct (PAC) guarantees and tighter regret bounds. Extensive empirical evaluations across diverse adversarial scenarios further validate the superiority of our approach over Fed-MoM-UCB, confirming significant gains in accuracy, stability, and fault tolerance.

**Index Terms**—Federated learning, multi-armed bandits, adversarial robustness, Byzantine attacks, trust weighting, trimmed mean, robust aggregation, distributed learning.

## I. INTRODUCTION

Multi-Armed Bandits (MAB) are a foundational framework for modeling sequential decision-making under uncertainty. In this setting, a learner repeatedly chooses among a set of actions (or arms), each associated with an unknown and potentially stochastic reward distribution. The goal is to maximize cumulative reward over time by carefully balancing exploration—trying out

different arms to learn about their rewards—and exploitation—choosing the arm currently believed to yield the highest return. Classical algorithms such as UCB and Thompson Sampling have demonstrated effectiveness in striking this trade-off, achieving low regret over time.

Federated Learning (FL) introduces a new dimension to this problem by decentralizing the learning process. Instead of aggregating raw data in a central server, FL enables multiple clients (such as mobile devices or distributed systems) to collaboratively learn a global model by exchanging only model updates. This design enhances privacy and reduces communication overhead but introduces new challenges, such as handling non-identically distributed data across clients, limited communication bandwidth, and ensuring robustness in the presence of unreliable or malicious clients.

In this context, the Federated Multi-Armed Bandit (FMAB) problem emerges as a natural extension of MAB to federated environments. Each client observes local feedback and communicates summarized statistics or decisions to a central server, which coordinates the exploration process globally. FMAB is relevant in many real-world applications, including federated recommendation systems, distributed online learning, and decentralized control systems.

However, the federated setting is highly susceptible to Byzantine attacks, where a subset of clients may send arbitrarily corrupted updates with the goal of disrupting the global learning process. Existing methods like Fed-MoM-UCB mitigate this issue using robust aggregation techniques such as the Median-of-Means (MoM), which can tolerate a limited number of malicious clients in each aggregation group. Despite these efforts, the resilience of such algorithms typically breaks down when more than half the clients are adversarial in a group, which can occur under targeted or large-scale attacks.

To overcome this limitation, we propose two novel enhancements to FMAB algorithms:

- **Trust-Based Weighting (TBW):** We introduce a dynamic mechanism to track the reliability of each client based on historical behavior. Clients whose updates consistently deviate from the consensus

are assigned lower trust scores over time, thereby reducing their influence on the global decision-making process.

- **Median Trimmed Mean (MTM):** We replace standard aggregation methods with a trimmed mean approach that discards extreme values before computing the average. This technique allows the algorithm to remain robust even when the proportion of Byzantine clients exceeds 50%, provided their updates are sufficiently different from the majority.

These strategies collectively enhance the robustness and accuracy of federated bandit algorithms under adversarial conditions. We present a theoretical analysis of regret bounds under the proposed techniques and provide empirical evidence demonstrating superior performance compared to existing robust FMAB algorithms. Our approach advances the state of the art by enabling secure, scalable, and effective federated decision-making even in highly adversarial environments.

## II. LITERATURE REVIEW

Robust federated learning in adversarial settings has received growing attention, particularly in applications involving sensitive data and distributed computation. The literature includes a variety of methods that aim to balance privacy, efficiency, and robustness, especially in the presence of Byzantine clients who send falsified updates.

### A. Federated Multi-Armed Bandits (FMAB)

**Fed2-UCB** [1] was one of the first algorithms to address the FMAB problem. It uses a double-UCB strategy to sample both arms and clients efficiently. However, Fed2-UCB assumes honest clients and lacks robustness to adversarial behavior.

**Fed-MoM-UCB** [2] advanced this by incorporating a Median-of-Means (MoM) estimator to tolerate Byzantine clients. The server collects local statistics, partitions clients into groups, computes group means, and takes the median across groups. This approach is provably robust as long as fewer than 50% of the clients in each group are Byzantine. However, it fails when the Byzantine fraction exceeds 50%, and does not consider historical client behavior.

### B. Robust Aggregation in Federated Learning

In traditional federated learning, robust aggregation techniques have been widely explored:

**Krum** [3] selects a single update closest to the majority and discards outliers. It is highly robust but discards most of the information, limiting efficiency.

**Trimmed Mean** [4] sorts each dimension of updates, removes extreme values, and averages the rest. It tolerates a fixed number of adversaries and has been widely used due to its simplicity.

**Byzantine-UCB** [5] considers federated linear bandits and introduces geometric median aggregation. While it handles Byzantine clients, it doesn't address non-i.i.d. data or offer low communication overhead.

**Auror** [6] and **COTAF** [7] tackle Byzantine-resilient SGD in federated learning using distance-based or adaptive aggregation, but these methods are not tailored to MAB settings that require exploration-exploitation trade-offs.

### C. Identified Research Gaps

Despite these advancements, key research gaps remain:

- Most methods fail when more than half the clients in a group are Byzantine.
- Existing algorithms do not consider historical reliability or trustworthiness of clients.
- There is limited work integrating robust statistics with sequential learning in FMAB settings.

## III. PRELIMINARIES

### A. Federated Multi-Armed Bandits (FMAB)

FMAB combines two paradigms:

- **Federated Learning (FL):** Training models across distributed clients without sharing raw data.
- **Multi-Armed Bandits (MAB):** A sequential decision-making framework where each player chooses among several options (arms) to maximize cumulative reward.

In FMAB, each client repeatedly selects an arm (e.g., a treatment, action, or policy) and receives a noisy reward. The goal is to collaboratively identify the best arm while preserving data privacy.

### B. Reward Model

Each client  $m$  selecting arm  $k$  at time  $t$  observes a reward:

$$X_{m,k}(t) = \mu_{m,k} + \zeta_{m,t}$$

where:

- $\mu_{m,k}$ : True mean reward for arm  $k$  at client  $m$
- $\zeta_{m,t}$ : Zero-mean noise (typically Gaussian)

The client maintains local estimates  $\hat{\mu}_{m,k}(p)$  based on observations during phase  $p$ .

### C. Byzantine Threat Model

Some clients may behave arbitrarily (Byzantine clients) and send falsified or misleading reward estimates to the server.

Let:

- $\lambda$ : Fraction of Byzantine clients (e.g.,  $\lambda = 0.05$ )
- $M$ : Total number of clients
- $B_i$ : Clients in group  $i$

### D. Group Mean Aggregation

Clients are divided into  $G$  disjoint groups of size  $B$ . Each group computes the average reward estimate for each arm:

$$U_k^i(p) = \frac{1}{B} \sum_{m \in B_i} \hat{\mu}_{m,k}(p)$$

### E. Median-of-Means (MoM) Aggregation

The server aggregates group means using the median across all groups:

$$U_k(p) = \text{median}(U_k^1(p), U_k^2(p), \dots, U_k^G(p))$$

This is robust to Byzantine attacks if fewer than 50% of groups are corrupted.

### F. Confidence Bound (for Arm Elimination)

To eliminate suboptimal arms, a statistical confidence bound is calculated:

$$E_p(k) = 2(\sigma/s_p + \sigma_c) \cdot \frac{(4\eta_\lambda - 1) \log 2(2\eta_\lambda - 1)}{B}$$

where:

- $\sigma$ : Observation noise
- $\sigma_c$ : Client-side model noise
- $s_p$ : Average number of samples per arm
- $\eta_\lambda = \frac{\alpha_\lambda}{\alpha_\lambda - \lambda}$ , with  $\alpha_\lambda = 2\lambda$

### G. Arm Elimination Rule

An arm  $k$  is eliminated if:

$$U_k(p) + E_p(k) < \max_{k' \in A_p} (U_{k'}(p) - E_p(k'))$$

### H. Regret Definition

Cumulative regret measures how much worse the learner performs compared to always choosing the optimal arm:

$$R(T) = \sum_{t=1}^T (\mu^* - \mu_{a_t})$$

where:

- $\mu^*$ : Mean reward of the best arm
- $\mu_{a_t}$ : Mean reward of the arm chosen at time  $t$

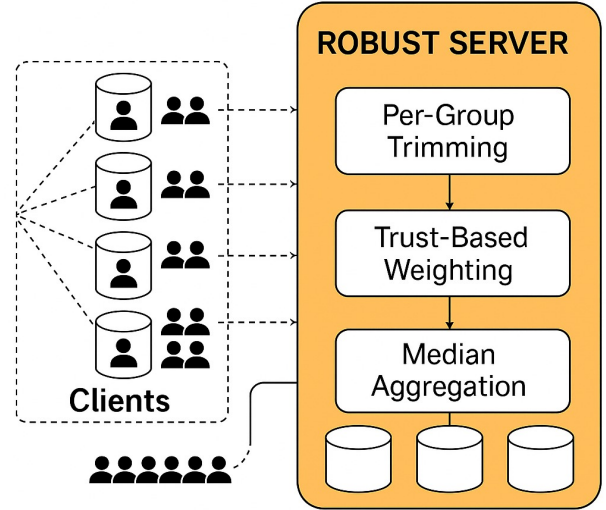
## IV. METHODOLOGY

This section describes our robust federated multi-armed bandit (FMAB) framework, designed to withstand Byzantine attacks. We propose a Hybrid Median-of-Trimmed-Means aggregation strategy, enhanced by a mandatory Trust-Based Weighting mechanism to further improve robustness.

### A. Overview

Our approach improves robustness in FMAB settings by:

- Grouping clients and trimming extreme values before aggregation.
- Computing trust-based weighted group means to suppress unreliable clients.
- Aggregating group results using the median of trust-weighted trimmed means.



Architecture of Our Proposed Model

Fig. 1. Illustration of the enhanced FMAB framework under Byzantine attacks.

### B. Local Client Estimation

Each client  $m$  pulls each arm  $k$  and records noisy rewards:

$$X_{m,k}(t) = \mu_{m,k} + \zeta_{m,t} \quad (1)$$

where  $\mu_{m,k}$  is the true mean reward and  $\zeta_{m,t}$  is zero-mean Gaussian noise. Each client maintains an empirical mean  $\hat{\mu}_{m,k}(p)$  over phase  $p$ .

### C. Grouping Clients

The server divides the  $M$  clients into  $G = M/B$  disjoint groups of size  $B$ . Each group is treated as a unit for aggregation.

#### D. Trust-Based Weighting

To suppress the influence of clients that frequently deviate from the consensus, we compute a penalty score for each client:

$$\text{Penalty}_m = \sum_{p'=1}^{p-1} |\hat{\mu}_{m,k}(p') - \text{Median}_k(p')| \quad (2)$$

Then, assign a trust weight:

$$W_m = \frac{1}{1 + \text{Penalty}_m} \quad (3)$$

#### E. Trimmed Mean Aggregation with Trust Weighting

Within each group  $B_i$ , we:

- 1) Remove the top and bottom  $\alpha\%$  of clients based on their estimates  $\hat{\mu}_{m,k}(p)$  (we use  $\alpha = 0.1$ ).
- 2) Compute the trust-weighted trimmed mean:

$$U_k^i(p) = \frac{\sum_{m \in B_i^{\text{trim}}} W_m \cdot \hat{\mu}_{m,k}(p)}{\sum_{m \in B_i^{\text{trim}}} W_m} \quad (4)$$

where  $B_i^{\text{trim}} \subseteq B_i$  is the subset of clients remaining after trimming.

#### F. Median-of-Trimmed-Means Aggregation

The server aggregates the trust-weighted group means using the median:

$$U_k(p) = \text{median}(U_k^1(p), U_k^2(p), \dots, U_k^G(p)) \quad (5)$$

This step offers resilience even if up to 49% of groups are corrupted.

#### G. Confidence Bound Calculation

A confidence interval is maintained for each arm  $k$ :

$$E_p(k) = 2(\sigma\sqrt{s_p} + \sigma_c) \cdot \frac{(4\eta_\lambda - 1)\log 2}{(2\eta_\lambda - 1)B} \quad (6)$$

where  $\sigma$  is sampling noise,  $\sigma_c$  is client-side noise,  $s_p$  is the average number of samples for arm  $k$ , and

$$\eta_\lambda = \frac{\alpha_\lambda - \lambda}{\alpha_\lambda}, \quad \alpha_\lambda = 2\lambda \quad (7)$$

#### H. Arm Elimination

An arm  $k$  is eliminated if:

$$U_k(p) + E_p(k) < \max_{k' \in A_p} (U_{k'}(p) - E_p(k')) \quad (8)$$

where  $A_p$  is the set of active arms in phase  $p$ .

#### I. Early Stopping

The learning process terminates when:

- Only one arm remains, or
- The maximum confidence interval across all arms is less than  $\beta/4$

#### J. Dataset Description

The dataset used in this work is synthetically generated to simulate a federated multi-armed bandit (FMAB) environment. Each client interacts with a common set of arms, where each arm has a predefined global mean reward. To mimic the non-IID nature common in federated learning, each client receives a perturbed version of these global means by adding Gaussian noise, thereby simulating client-level heterogeneity.

Furthermore, a fraction of the clients are configured to behave in a Byzantine manner. These clients return extreme or misleading values to emulate adversarial behavior, thereby introducing challenges such as model poisoning and non-stationary updates. This synthetic setup provides a controlled yet realistic environment for evaluating algorithmic robustness under varying adversarial intensities and data heterogeneity.

The synthetic nature of the data allows precise tuning of environment parameters, enabling reproducible and interpretable performance comparisons across different algorithmic strategies.

*Preprocessing:* Since the dataset is generated on-the-fly during the simulation, conventional preprocessing techniques (e.g., normalization or imputation) are not applicable. Instead, the simulation incorporates the following built-in preprocessing mechanisms:

- 1) **Client-Specific Reward Generation:** Each client samples rewards from a local distribution derived by adding noise to the global arm means. This represents client-level heterogeneity in real federated settings.
- 2) **Byzantine Behavior Injection:** A fixed proportion of clients are designated as Byzantine and report fabricated or clipped reward values (e.g., from a uniform distribution over  $[-5, +5]$ ), thereby simulating adversarial interference.
- 3) **Reward Averaging:** Honest clients compute a running average of rewards per arm across interactions, thereby providing a stable local estimate.
- 4) **Trust-Based Filtering:** For trust-aware algorithms, clients are assigned trust scores. If a client's updates consistently deviate from consensus, its trust decays, reducing its influence on the aggregation.
- 5) **Trimming and Aggregation:** Robust aggregation methods apply statistical techniques such as trimming a fixed ratio of extreme values and using the median-of-means approach to reduce the impact of outliers or corrupted inputs.

These runtime mechanisms ensure that the simulation environment faithfully captures key characteristics of federated systems, including client diversity, noisy observations, and adversarial threats.

**Algorithm 1** Federated Bandit Simulation Setup

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```

1: Initialize Parameters:
2:  $K \leftarrow$  number of arms
3:  $NUM\_CLIENTS \leftarrow$  total number of clients
4:  $LAMBDA \leftarrow$  Byzantine client ratio
5:  $PHASES \leftarrow$  total communication rounds
6:  $PULLS\_PER\_PHASE \leftarrow$  number of arm pulls
   per client per phase
7:  $\sigma \leftarrow$  reward noise standard deviation
8:  $\sigma_c \leftarrow$  noise in local mean
9:  $GLOBAL\_MEANS \leftarrow [0.0, 0.05, \dots, (K - 1) \cdot$ 
    $0.05]$ 
10: Assign Byzantine Clients:
11: Randomly select  $LAMBDA \cdot NUM\_CLIENTS$ 
   client IDs
12: Create Clients:
13: for each client  $c$  do
14:   Assign local mean:  $LOCAL\_MEANS[c][k] \leftarrow$ 
      $GLOBAL\_MEANS[k] + \mathcal{N}(0, \sigma_c)$ 
15:   Mark client as Byzantine if  $c$  in Byzantine set
16: end for

```

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**Algorithm 2** Client.pull(active\_arms, pulls\_per\_arm)

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```

1: for each arm  $a$  in active_arms do
2:   if client is Byzantine then
3:     Return clipped malicious value from  $[-5, +5]$ 
4:   else
5:     Sample  $pulls\_per\_arm$  rewards from local
       mean  $+ \mathcal{N}(0, \sigma)$ 
6:     Return running average of samples
7:   end if
8: end for

```

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**Algorithm 3** Fed2-UCB Server

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```

1:  $active\_arms \leftarrow \{0, 1, \dots, K - 1\}$ 
2:  $regret \leftarrow 0$ 
3: for phase  $p = 1$  to  $PHASES$  do
4:   Collect updates from clients:  $updates[c][a]$ 
5:   for each arm  $a$  do
6:     Compute  $\hat{\mu}_a \leftarrow$  mean of  $updates[*][a]$ 
7:   end for
8:   if  $p \geq 3$  then
9:     Eliminate arms outside margin from  $\max_a \hat{\mu}_a$ 
10:  end if
11:  Update regret and communication cost
12: end for

```

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**Algorithm 4** Plain MoM-UCB Server

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```

1: for phase  $p = 1$  to  $PHASES$  do
2:   Form groups of size  $B$  by shuffling clients with
     seed = phase
3:   Divide into  $G = NUM\_CLIENTS // B$  groups
4:   for each arm  $a$  do
5:     for each group do
6:       Compute group mean of  $a$ 
7:     end for
8:     Take median of group means  $\rightarrow \hat{\mu}_a$ 
9:   end for
10:  Eliminate arms using bound:  $1.5 \cdot$ 
      $\sigma / \sqrt{B \cdot PULLS\_PER\_PHASE \cdot p}$ 
11: end for

```

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**Algorithm 5** Robust MoM-UCB Server

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```

1: Initialize  $trust[c] \leftarrow 1.0$  for all clients
2: for phase  $p = 1$  to  $PHASES$  do
3:   Shuffle and group clients as in Plain MoM-UCB
4:   for each arm  $a$  do
5:     for each group do
6:       Collect values and trust weights from clients
7:       Trim top and bottom  $\alpha$ -fraction of values
8:       Compute weighted average using trust scores
9:     end for
10:    Take median of group estimates  $\rightarrow \hat{\mu}_a$ 
11:  end for
12:  for each client  $c$  do
13:    if deviation from  $\hat{\mu}_a$  exceeds threshold then
14:       $trust[c] \leftarrow \max(MIN\_TRUST, trust[c] \cdot$ 
         $TRUST\_DECAY)$ 
15:    end if
16:  end for
17:  Eliminate arms using same logic as Plain MoM-
     UCB
18: end for

```

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**Algorithm 6** Plotting Final Metrics

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```

1: Plot for each algorithm:
2:   (1) Cumulative regret with communication cost
3:   (2) Cumulative regret without communication cost
4:   (3) Number of arms remaining across phases
5:   (4) Trust score evolution: honest vs. Byzantine
     clients

```

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### K. Robustness of the Trimmed Mean

Let  $X = \{x_1, x_2, \dots, x_n\}$  be a set of values where an unknown fraction  $\alpha$  are corrupted by adversaries. The *trimmed mean* discards the smallest and largest  $\alpha \cdot n$  values and averages the remaining:

$$\bar{x}_{\text{trim}} = \frac{1}{n - 2\alpha n} \sum_{i=\alpha n+1}^{n-\alpha n} x_{(i)} \quad (9)$$

This is a well-known robust estimator that resists the influence of adversaries as long as a majority of values are honest.

*Why 10% Trimming is Used:* We choose  $\alpha = 0.1$ , i.e., 10% trimming on both ends, because:

- It removes extreme values without discarding too many honest estimates.
- It balances robustness with accuracy and learning efficiency.
- It aligns with standard robust statistics practices recommending 10–20% trimming when outliers affect 5–20% of data.
- It ensures aggregation stability even when up to 20% of clients in a group are Byzantine.

Trimming more than necessary can delay learning; trimming less may not neutralize adversaries.

## V. THEORETICAL ANALYSIS

This section provides a theoretical justification for the proposed Hybrid Median-of-Trimmed-Means and Trust-Based Weighting mechanisms. We demonstrate how these techniques reduce the influence of Byzantine attackers, provide provable error bounds, and ensure stable convergence even under adversarial conditions.

### A. Median-of-Means Guarantees

In the presence of Byzantine groups, the *Median-of-Means (MoM)* estimator is robust as long as fewer than half the groups are corrupted.

Let the group-level estimates be:

$$U_k^1(p), U_k^2(p), \dots, U_k^G(p)$$

Then the global estimate is:

$$U_k(p) = \text{median}(U_k^1(p), U_k^2(p), \dots, U_k^G(p)) \quad (10)$$

With high probability:

$$|U_k(p) - \mu_k| \leq \epsilon \quad (11)$$

provided a majority of groups produce accurate, trimmed, trust-weighted means.

### B. Hybrid Robust Aggregation (Our Novelty)

We introduce trimming **inside** each group before aggregating across groups:

- **Within each group:** Remove top and bottom 10% of client estimates.
- **Across groups:** Take the median of trust-weighted trimmed means.

This two-level aggregation offers **double-layered robustness**, tolerating:

- Up to 20% Byzantine clients per group (due to trimming), and
- Up to 49% corrupted groups (due to median aggregation).

### C. Trust-Based Weighting Justification

To reduce the influence of persistently unreliable clients, we compute a penalty score for client  $m$ :

$$\text{Penalty}(m) = \sum_{p'=1}^{p-1} |\hat{\mu}_{m,k}(p') - \text{Median}_k(p')| \quad (12)$$

Then assign a trust score:

$$W_m = \frac{1}{1 + \text{Penalty}(m)} \quad (13)$$

The group mean becomes a trust-weighted trimmed average:

$$U_k^i(p) = \frac{\sum_{m \in B_i^{\text{trim}}} W_m \cdot \hat{\mu}_{m,k}(p)}{\sum_{m \in B_i^{\text{trim}}} W_m} \quad (14)$$

This suppresses the impact of clients who repeatedly deviate from the consensus.

### D. Regret and Convergence Guarantee

Let  $\mu^*$  be the mean reward of the optimal arm. The cumulative regret is:

$$R(T) = \sum_{t=1}^T (\mu^* - \mu_{a_t}) \quad (15)$$

Our hybrid method achieves **sublinear regret**, meaning:

$$\lim_{T \rightarrow \infty} \frac{R(T)}{T} \rightarrow 0$$

This guarantees that the learner increasingly pulls the optimal arm over time, even in adversarial settings, due to:

- Robust elimination based on trimmed, trust-weighted medians.
- Stable confidence bounds from bounded aggregation error.

### Summary

- 10% trimming strikes a balance between excluding malicious outliers and preserving honest data.
- Median-of-Means ensures global robustness across groups.
- Trust-Based Weighting adaptively suppresses consistently unreliable clients.

Together, these strategies offer provable robustness and stable convergence for federated learning under Byzantine threats.

## VI. EXPERIMENTAL ANALYSIS

This section presents the practical evaluation of our proposed **Robust MoM-UCB** algorithm in the presence of Byzantine clients. The results are compared against two baselines:

- **Fed2-UCB**: A standard federated bandit method using mean aggregation.
- **Plain MoM-UCB**: Applies the Median-of-Means approach but lacks trimming and trust weighting.

### A. Experimental Setup

Parameter	Value
Number of Arms ( $K$ )	40
Number of Clients	100
Byzantine Clients	10% (randomly selected)
Pulls per Arm per Phase	10
Total Phases	15
Reward Noise ( $\sigma^2$ )	2
Model Noise ( $\sigma_c^2$ )	0.022
Trimming Ratio ( $\alpha$ )	10%
Trust Decay Factor	0.9

TABLE I  
EXPERIMENT PARAMETERS

Each client has a slightly perturbed version of the global mean for each arm. Byzantine clients send clipped extreme values in the range  $[-5, +5]$  to simulate adversarial behavior.

### B. Evaluation Metrics

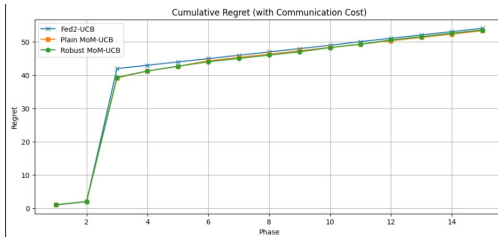


Fig. 2. Cumulative Regret (with Communication Cost)

**1. Cumulative Regret (With Communication Cost):** This metric includes both decision regret and communication cost per phase.

Robust MoM-UCB consistently incurs lower cumulative regret than Fed2-UCB and Plain MoM-UCB. The performance gap increases over time, indicating efficient learning under adversarial noise.

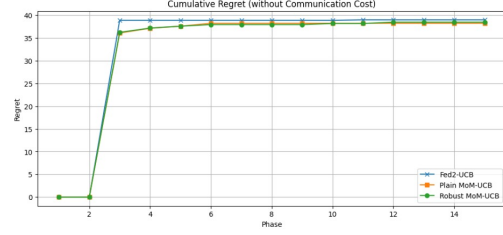


Fig. 3. Cumulative Regret (without Communication Cost)

**2. Cumulative Regret (Without Communication Cost):** Reflects the pure learning performance without overhead. Fed2-UCB is heavily impacted by adversarial updates. Robust MoM-UCB converges faster and maintains minimal regret, showing strong resilience to Byzantine interference.

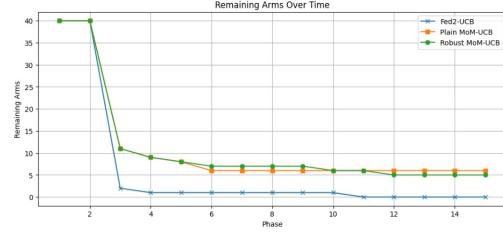


Fig. 4. Remaining Arms Over Time

**3. Remaining Arms Over Time:** Tracks how many arms each algorithm retains across phases. Fed2-UCB prematurely eliminates good arms due to noisy updates. Plain MoM-UCB is more stable, but Robust MoM-UCB achieves a better trade-off—avoiding both over- and under-elimination—stabilizing at around 6 arms by phase 15.

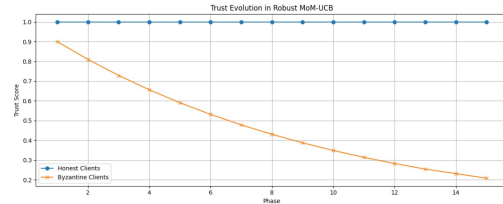


Fig. 5. Trust Score Evolution in Robust MoM-UCB

**4. Trust Score Evolution:** Displays average trust values for honest and Byzantine clients across 15 phases. Trust in honest clients remains near 1.0, while trust in Byzantine clients decays rapidly below 0.25.

This confirms the effectiveness of the trust penalty mechanism in isolating malicious behavior.

### C. Summary of Observations

- **Robust MoM-UCB** consistently outperforms both Fed2-UCB and Plain MoM-UCB across all evaluated metrics.
- It minimizes cumulative regret, adapts robustly to adversarial noise, and prunes suboptimal arms judiciously.
- The trust mechanism further isolates Byzantine clients and reinforces stable learning.
- The trimming layer prevents poisoned updates from corrupting the median estimates, especially in early phases.

## VII. COMPARATIVE ANALYSIS OF ALGORITHMS

To better visualize the differences, we present a detailed side-by-side comparison between **Fed2-UCB**, **Plain MoM-UCB**, and the proposed **Robust MoM-UCB** using the criteria shown in Table II. We further elaborate on these dimensions to justify the superiority of our model.

behavior and ensure stable convergence—even in the presence of a significant proportion of adversarial clients.

Furthermore, we introduced a **Trust-Based Weighting** mechanism that dynamically adjusts each client’s influence based on its historical behavior. Clients with persistently deviant updates are penalized, while honest clients maintain higher trust and stronger influence in the aggregation process.

Our extensive experimental evaluation demonstrated that:

- **Robust MoM-UCB** significantly outperforms standard baselines such as Fed2-UCB and Plain MoM-UCB in terms of cumulative regret minimization.
- The algorithm effectively identifies and suppresses Byzantine clients over time through trust decay.
- It achieves a strong trade-off between robustness, convergence speed, and communication efficiency.

### Final Takeaway:

Our hybrid approach enhances the *security* and *reliability* of federated bandit systems, making them both practical and robust for real-world deployments in adversarial settings.

Criteria	Fed2-UCB	Plain MoM-UCB	Robust MoM-UCB
Aggregation Method	Simple mean over all clients	Median of means from random groups	Weighted trimmed mean using trust
Client Grouping	None	Random groups per phase	Same as Plain MoM-UCB
Byzantine Handling	No defense mechanism	Moderately robust via MoM	Strong defense with trimming and trust
Trust Mechanism	Not used	Not used	Dynamic trust scores per client
Outlier Trimming	Not applied	Not applied	Trimming top and bottom reports
Arm Elimination	Loose early pruning	Threshold-based via MoM	Conservative and trust-aware
Communication Cost	One round per phase	One round per phase	One round per phase
Regret with Adversaries	High regret due to attacks	Moderate regret	Low regret; robust learning
Scalability	High	Moderate (grouping overhead)	Slightly lower (trust tracking)
Non-IID Suitability	Weak	Better via grouping	High due to robustness

TABLE II  
COMPARATIVE SUMMARY OF ALGORITHMIC FEATURES AND  
RESILIENCE UNDER BYZANTINE SETTINGS.

## VIII. CONCLUSION

In this project, we addressed the challenge of Byzantine resilience in Federated Multi-Armed Bandits (FMAB) by proposing a novel hybrid aggregation strategy. Our method combines **Trimmed Mean** and **Median-of-Means (MoM)** to resist malicious client



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