

2014 AMC 10A Problems

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Problem 1

What is $10 \cdot \left(\frac{1}{2} + \frac{1}{5} + \frac{1}{10}\right)^{-1}$?

- (A) 3 (B) 8 (C) $\frac{25}{2}$ (D) $\frac{170}{3}$ (E) 170

Solution

Problem 2

Roy's cat eats $\frac{1}{3}$ of a can of cat food every morning and $\frac{1}{4}$ of a can of cat food every evening. Before feeding his cat on Monday morning, Roy opened a box containing 6 cans of cat food. On what day of the week did the cat finish eating all the cat food in the box?

- (A) Tuesday (B) Wednesday (C) Thursday (D) Friday (E) Saturday

Solution

Problem 3

Bridget bakes 48 loaves of bread for her bakery. She sells half of them in the morning for \$2.50 each. In the afternoon she sells two thirds of what she has left, and because they are not fresh, she charges only half price. In the late afternoon she sells the remaining loaves at a dollar each. Each loaf costs \$0.75 for her to make. In dollars, what is her profit for the day?

- (A) 24 (B) 36 (C) 44 (D) 48 (E) 52

Solution

Problem 4

Walking down Jane Street, Ralph passed four houses in a row, each painted a different color. He passed the orange house before the red house, and he passed the blue house before the yellow house. The blue house was not next to the yellow house. How many orderings of the colored houses are possible?

- (A) 2 (B) 3 (C) 4 (D) 5 (E) 6

Solution

Problem 5

On an algebra quiz, 10% of the students scored 70 points, 35% scored 80 points, 30% scored 90 points, and the rest scored 100 points. What is the difference between the mean and median score of the students' scores on this quiz?

- (A) 1 (B) 2 (C) 3 (D) 4 (E) 5

Solution

Problem 6

Suppose that a cows give b gallons of milk in c days. At this rate, how many gallons of milk will d cows give in e days?

- (A) $\frac{bde}{ac}$ (B) $\frac{ac}{bde}$ (C) $\frac{abde}{c}$ (D) $\frac{bcde}{a}$ (E) $\frac{abc}{de}$

Solution

Problem 7

Nonzero real numbers x , y , a , and b satisfy $x < a$ and $y < b$. How many of the following inequalities must be true?

(I) $x + y < a + b$

(II) $x - y < a - b$

(III) $xy < ab$

(IV) $\frac{x}{y} < \frac{a}{b}$

- (A) 0 (B) 1 (C) 2 (D) 3 (E) 4

Solution

Problem 8

Which of the following numbers is a perfect square?

- (A) $\frac{14!15!}{2}$ (B) $\frac{15!16!}{2}$ (C) $\frac{16!17!}{2}$ (D) $\frac{17!18!}{2}$ (E) $\frac{18!19!}{2}$

Solution

Problem 9

The two legs of a right triangle, which are altitudes, have lengths $2\sqrt{3}$ and 6. How long is the third altitude of the triangle?

- (A) 1 (B) 2 (C) 3 (D) 4 (E) 5

Solution

Problem 10

Five positive consecutive integers starting with a have average b . What is the average of 5 consecutive integers that start with b ?

- (A) $a + 3$ (B) $a + 4$ (C) $a + 5$ (D) $a + 6$ (E) $a + 7$

Solution

Problem 11

A customer who intends to purchase an appliance has three coupons, only one of which may be used:

Coupon 1: 10% off the listed price if the listed price is at least \$50

Coupon 2: \$20 off the listed price if the listed price is at least \$100

Coupon 3: 18% off the amount by which the listed price exceeds \$100

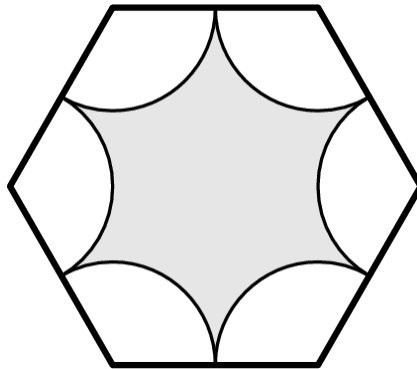
For which of the following listed prices will coupon 1 offer a greater price reduction than either coupon 2 or coupon 3?

- (A) \$179.95 (B) \$199.95 (C) \$219.95 (D) \$239.95 (E) \$259.95

Solution

Problem 12

A regular hexagon has side length 6. Congruent arcs with radius 3 are drawn with the center at each of the vertices, creating circular sectors as shown. The region inside the hexagon but outside the sectors is shaded as shown. What is the area of the shaded region?

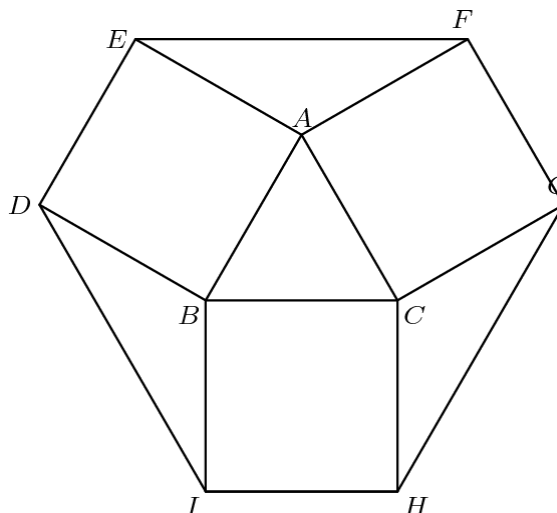


- (A) $27\sqrt{3} - 9\pi$ (B) $27\sqrt{3} - 6\pi$ (C) $54\sqrt{3} - 18\pi$ (D) $54\sqrt{3} - 12\pi$
 (E) $108\sqrt{3} - 9\pi$

Solution

Problem 13

Equilateral $\triangle ABC$ has side length 1, and squares $ABDE$, $BCHI$, $CAFG$ lie outside the triangle. What is the area of hexagon $DEFGHI$?



- (A) $\frac{12 + 3\sqrt{3}}{4}$ (B) $\frac{9}{2}$ (C) $3 + \sqrt{3}$ (D) $\frac{6 + 3\sqrt{3}}{2}$ (E) 6

Solution

Problem 14

The y -intercepts, P and Q , of two perpendicular lines intersecting at the point $A(6, 8)$ have a sum of zero. What is the area of $\triangle APQ$?

- (A) 45 (B) 48 (C) 54 (D) 60 (E) 72

Solution

Problem 15

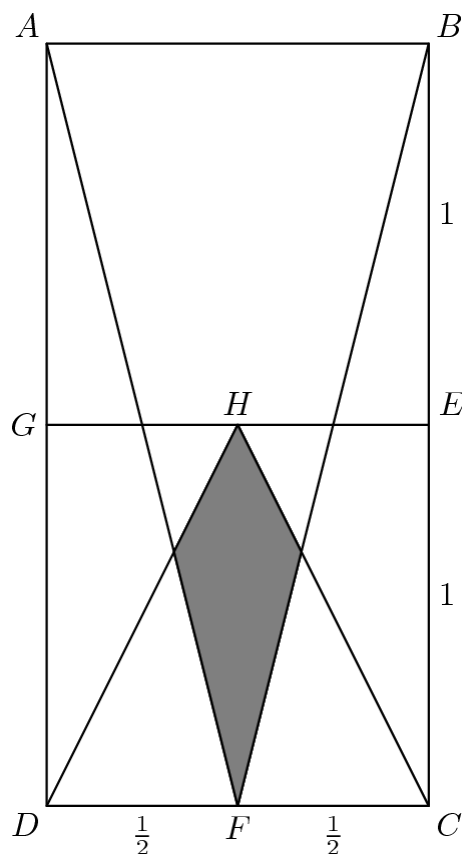
David drives from his home to the airport to catch a flight. He drives 35 miles in the first hour, but realizes that he will be 1 hour late if he continues at this speed. He increases his speed by 15 miles per hour for the rest of the way to the airport and arrives 30 minutes early. How many miles is the airport from his home?

- (A) 140 (B) 175 (C) 210 (D) 245 (E) 280

Solution

Problem 16

In rectangle $ABCD$, $AB = 1$, $BC = 2$, and points E , F , and G are midpoints of \overline{BC} , \overline{CD} , and \overline{AD} , respectively. Point H is the midpoint of \overline{GE} . What is the area of the shaded region?



- (A) $\frac{1}{12}$ (B) $\frac{\sqrt{3}}{18}$ (C) $\frac{\sqrt{2}}{12}$ (D) $\frac{\sqrt{3}}{12}$ (E) $\frac{1}{6}$

Solution

Problem 17

Three fair six-sided dice are rolled. What is the probability that the values shown on two of the dice sum to the value shown on the remaining die?

- (A) $\frac{1}{6}$ (B) $\frac{13}{72}$ (C) $\frac{7}{36}$ (D) $\frac{5}{24}$ (E) $\frac{2}{9}$

Solution

Problem 18

A square in the coordinate plane has vertices whose y -coordinates are 0, 1, 4, and 5. What is the area of the square?

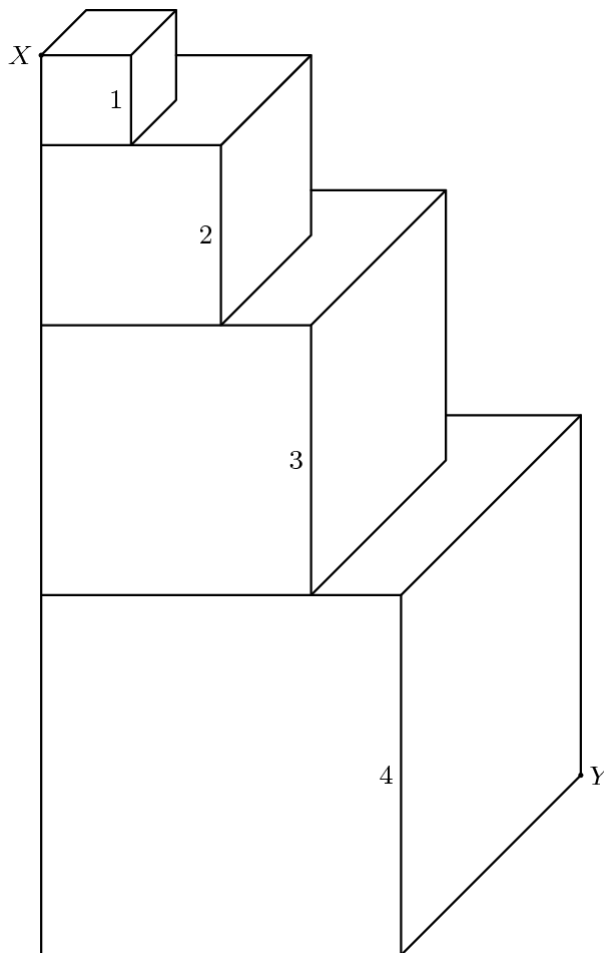
- (A) 16 (B) 17 (C) 25 (D) 26 (E) 27

Solution

Problem 19

Four cubes with edge lengths 1, 2, 3, and 4 are stacked as shown. What is the length of the portion of \overline{XY} contained in the cube with edge length 3?

- (A) $\frac{3\sqrt{33}}{5}$ (B) $2\sqrt{3}$ (C) $\frac{2\sqrt{33}}{3}$ (D) 4 (E) $3\sqrt{2}$



Solution

Problem 20

The product $(8)(888 \dots 8)$, where the second factor has k digits, is an integer whose digits have a sum of 1000. What is k ?

- (A) 901 (B) 911 (C) 919 (D) 991 (E) 999

Solution

Problem 21

Positive integers a and b are such that the graphs of $y = ax + 5$ and $y = 3x + b$ intersect the x -axis at the same point. What is the sum of all possible x -coordinates of these points of intersection?

- (A) -20 (B) -18 (C) -15 (D) -12 (E) -8

Solution

Problem 22

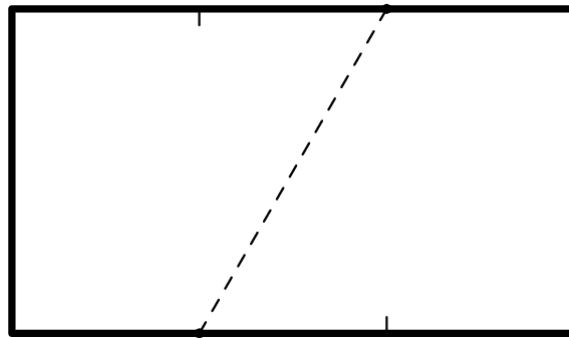
In rectangle $ABCD$, $AB = 20$ and $BC = 10$. Let E be a point on \overline{CD} such that $\angle CBE = 15^\circ$. What is AE ?

- (A) $\frac{20\sqrt{3}}{3}$ (B) $10\sqrt{3}$ (C) 18 (D) $11\sqrt{3}$ (E) 20

Solution

Problem 23

A rectangular piece of paper whose length is $\sqrt{3}$ times the width has area A . The paper is divided into three equal sections along the opposite lengths, and then a dotted line is drawn from the first divider to the second divider on the opposite side as shown. The paper is then folded flat along this dotted line to create a new shape with area B . What is the ratio $B : A$?



- (A) $1 : 2$ (B) $3 : 5$ (C) $2 : 3$ (D) $3 : 4$ (E) $4 : 5$

Solution

Problem 24

A sequence of natural numbers is constructed by listing the first 4, then skipping one, listing the next 5, skipping 2, listing 6, skipping 3, and, on the n th iteration, listing $n + 3$ and skipping n . The sequence begins 1, 2, 3, 4, 6, 7, 8, 9, 10, 13. What is the 500,000th number in the sequence?

- (A) 996,506 (B) 996,507 (C) 996,508 (D) 996,509 (E) 996,510

Solution

Problem 25

The number 5^{867} is between 2^{2013} and 2^{2014} . How many pairs of integers (m, n) are there such that $1 \leq m \leq 2012$ and

$$5^n < 2^m < 2^{m+2} < 5^{n+1}?$$

- (A) 278 (B) 279 (C) 280 (D) 281 (E) 282

Solution

See also

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