Total No. of Questions: 8]

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Roll No

BE-3001 (CS/IT) (CBGS)

B.E., III Semester

Examination, December 2017

Choice Based Grading System (CBGS) **Mathematics - III**

Time: Three Hours

Maximum Marks: 70

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Note: i) Attempt any five questions.

All questions carry equal marks.

1. a) Prove that

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$$x^{2} = \frac{\pi^{2}}{3} + 4 \sum_{n=1}^{\infty} (-1)^{n} \frac{\cos nx}{n^{2}}, -\pi < x < \pi$$

- Obtain half-range sine series for e^x in 0 < x < 1
- 2. a) Find the Fourier transform of $f(x) = \begin{cases} 1 x^2, & |x| \le 1 \\ 0, & |x| > 1 \end{cases}$

Hence evaluate
$$\int_0^\infty \frac{x \cos x - \sin x}{x^3} \cos \frac{x}{2} dx$$

[2]

Using Laplace transform to solve the diff. equation

$$\frac{d^2x}{dt^2} - 2\frac{dx}{dt} + x = e^t$$

When
$$x = 2$$
, $\frac{dx}{dt} = -1$ at $t = 0$

- 3. a) Find the Laplace transform of $\frac{1-\cos t}{t^2}$

b) Using the convolution theorem, find
$$L^{-1}\left\{\frac{s}{\left(s^2+1\right)\left(s^2+4\right)}\right\}$$

- Define:
 - Probability density function for continuous random variables.
 - ii) Mean and variance of random variables.
 - Find the mean and variance for Binomial distribution.
- Fit Poisson's distribution to the following and calculate theoretical frequencies ($e^{-0.5} = 0.61$)

Deaths:

Frequency: 122

Show that the mean deviation from the mean of the normal distribution is $\frac{4}{5}$ times its standard deviation.

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By the method of least squares. Find the straight line that best fits the following data:

x	1	2	3	4	5
y	14	27	40	55	68

The profit of certain company in the xth year of its life are given by:

x	1	2	3	4	5
у	1250	1400	1650	1950	2300

Taking u = x - 3 and 50v = y - 1650, show that the parabola of second degree of y on x is

$$y = 1140.05 + 72.1x + 32.15x^2$$
.

7. a) Find the Fourier series for $f(x) = \begin{cases} -\pi, & -\pi < x < 0 \\ x, & 0 < x < \pi \end{cases}$

and deduce that
$$\frac{1}{12} + \frac{1}{3^2} + \frac{1}{5^2} + \dots = \frac{\pi^2}{8}$$

b) Find the Fourier cosine transform of $f(x) = \frac{1}{1+x^2}$ and

hence find Fourier sine transform of
$$F(x) = \frac{x}{1+x^2}$$

For a Poisson distribution with mean m, show that

$$\mu_{r+1} = mr.\mu_{r-1} + m\frac{d\mu r}{dm}$$

Where
$$\mu_r = \sum_{x=0}^{\infty} (x-m)^r e^{-m} \frac{m^x}{|x|}$$

Evaluate by using Laplace transform

i)
$$\int_0^\infty t \ e^{-4t} \sin t \ dt$$

ii)
$$\int_0^\infty e^{-t} \frac{\sin t}{t} dt$$

[4]

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