

[4]

OR

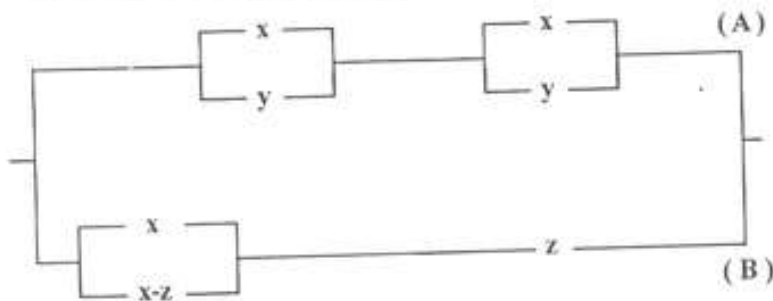
Find the eigen values of A and using Cayley - Hamilton theorem, find A^n (n is a positive integer); given that

$$A = \begin{bmatrix} 1 & 2 \\ 4 & 3 \end{bmatrix}$$

7

Unit - V

5. a) What do you mean by logical equivalence and prove that the statement $(p \vee q) \wedge (\neg p \wedge \neg q)$ is a contradiction. 2
- b) For a simple graph of n vertices, the number of edges is $\frac{1}{2}n(n-1)$. 2
- c) Simplify the following circuit 3



- d) A simple graph with n vertices and k components can have at most $\frac{(n-k)(n-k+1)}{2}$ edges. 7

OR

Express the following functions into disjunctive normal form $f(x, y, z) = x \cdot y' + x \cdot z + x \cdot y$. 7

Total No. of Questions : 5]

[Total No. of Printed Pages : 4

Roll No

BE - 102

B.E. I & II Semester

Examination, June 2014

Engineering Mathematics-I

Time : Three Hours

Maximum Marks : 70

- Note : i) Answer five questions. In each question part A, B, C is compulsory and D part has internal choice.
- ii) All parts of each question are to be attempted at one place.
- iii) All questions carry equal marks, out of which part A and B (Max. 50 words) carry 2 marks, part C (Max. 100 words) carry 3 marks, part D (Max. 400 words) carry 7 marks.
- iv) Except numericals, Derivation, Design and Drawing etc.

Unit - I

- a) Expand $\log \frac{1+x}{1-x}$ in powers of x using Maclaurin's theorem. 2
- b) Define homogeneous functions and composite function and establish the Euler's theorem on homogeneous function. 2
- c) Find the extreme values of the function $x^3 + y^3 - 3axy$. 3
- d) If the sides and angles of a triangle ABC vary in such a way that its circum radius remains constant, prove that

[2]

$$\frac{da}{\cos A} + \frac{db}{\cos B} + \frac{dc}{\cos C} = 0.$$

OR

Prove that the radius of curvature for the catenary $Y = c \cosh\left(\frac{x}{c}\right)$ is equal to the portion of the normal intercepted between the curve and the x-axis and that it varies as the square of the ordinate.

Unit - II

2. a) Define Gamma function and Beta function and also establish the symmetry of Beta function. 2
- b) Evaluate the following integral by changing the order of integration $\int_0^1 \int_0^x \frac{dy dx}{\log y}$ 2
- c) Evaluate by definition of definite integral as the limit of a sum $\int_0^{\pi} \sin x dx$. 3
- d) Find the volume bounded by the cylinder $x^2 + y^2 = 4$ and the planes $y + z = 4$ and $z = 0$. 7

OR

Prove that 7

$$\lim_{n \rightarrow \infty} \left[\left(1 + \frac{1}{n^2}\right) \left(1 + \frac{2^2}{n^2}\right) \left(1 + \frac{3^2}{n^2}\right) \dots \left(1 + \frac{n^2}{n^2}\right) \right]^{\frac{1}{4}} = 2e^{\left(\frac{\pi-4}{2}\right)}$$

Unit - III

3. a) Define the order and degree of a differential equation with one example also explain that the elimination of n arbitrary constants from an equation leads us to which order derivative and hence a differential equation of which order. 2

[3]

- b) Solve $-y dx + x dy = \sqrt{x^2 + y^2} dx$. 2
- c) A bacterial population β is known to have a rate of growth α to β itself. If between noon and 2 pm the population triples, at what time, no controls being exerted should β become 100 times what it was at noon. 3
- d) Solve $x^3 \frac{d^3 y}{dx^3} + 3x^2 \frac{d^2 y}{dx^2} + x \frac{dy}{dx} + y = x + \log x$. 7

OR

Solve the following differential equation by using the method of variation of parameters

$$\frac{d^2 y}{dx^2} - 2 \frac{dy}{dx} + 2y = e^x \tan x$$

Unit - IV

4. a) Determine the rank of the following matrix $\begin{bmatrix} 4 & 2 & 3 \\ 8 & 4 & 6 \\ -2 & -1 & -1.5 \end{bmatrix}$. 2
 - b) Solve the system of equations using matrix method. 2
- $$\begin{aligned} x + 3y - 2z &= 0 \\ 2x - y + 4z &= 0 \\ x - 11y + 14z &= 0 \end{aligned}$$
- c) If A is a non-singular matrix, prove that the eigen values of A^{-1} are the reciprocals of the eigen values of A. 3
 - d) Find the eigen values and eigen vectors of the matrix

$$A = \begin{bmatrix} -2 & 2 & -3 \\ 2 & 1 & -6 \\ -1 & -2 & 0 \end{bmatrix}$$