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Roll No

MCA-102**M.C.A. I Semester**

Examination, November 2018

Mathematical Foundation of Computer Science**Time : Three Hours****Maximum Marks : 70**

- Note:** i) Attempt any five questions.
ii) All questions carry equal marks.

1. a) If A, B, C are any three sets, then prove that:
 - i) $A - (B \cup C) = (A - B) \cap (A - C)$
 - ii) $A \times (B \cup C) = (A \times B) \cup (A \times C)$
- b) For the two mappings $f: R \rightarrow R$ defined by $f(x) = x^2 \forall x \in R$, and $g: R \rightarrow R$ defined by $g(x) = \sin x \forall x \in R$. Then show that $(g \circ f)x \neq (f \circ g)x$.
2. a) Let $A = \{1, 2, 3\}$, $B = \{a, b, c\}$ and $C = \{x, y, z\}$ be three sets. Let R and S be the relations from A to B and B to C respectively defined by $R = \{(1, b), (2, a), (2, c)\}$ and $S = \{(a, y), (b, x), (c, y), (c, z)\}$. Then find matrices M_R , M_S and M_{SOR} .
- b) Prove that $5^{2n} - 1$ is divisible by 24, where n is any positive integer.

[2]

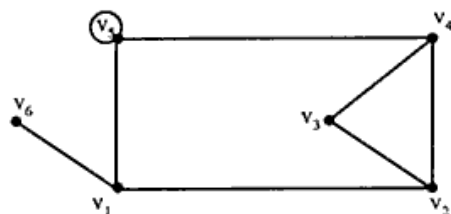
3. a) i) Prove that $p \wedge q \Rightarrow q \vee p$ is a Tautology.
ii) Write converse, inverse and contrapositive of the conditional statement $p \Rightarrow q$.
- b) Let $L = \{1, 2, 3, 4, 6, 8, 9, 12, 18, 24\}$ be ordered by the relation ' $|$ ' where $x | y$ means x divides y. Then show that D_{24} the set of all divisors of the integer 24 is a sub lattice of the lattice $(L, |)$.
4. a) Draw the simplified switching circuit of the function:
 $F(x, y, z) = x \cdot y' \cdot z + (z + y) \cdot x'$
- b) If (A, \leq) and (B, \leq) are two posets, then show that $(A \times B, \leq)$ is a poset where the ordering \leq on $A \times B$ defined by $(a, b) \leq (a', b') \Leftrightarrow a \leq a' \text{ in } A \text{ and } b \leq b' \text{ in } B$.
5. a) Prove that intersection of two subgroups of a group G is a subgroup of G but union of two subgroups is not necessarily a subgroup of G.
- b) Show that the set of numbers of the form $a + b\sqrt{2}$ with a and b as rational numbers, is a field.
6. a) Explain the following:
 - i) Connected graph
 - ii) Complete graph
 - iii) Spanning tree
 - iv) Binary tree

[3]

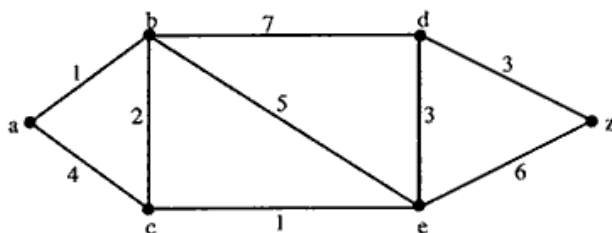
- b) Prove that the maximum number of edges in a simple graph

with n vertices is $\frac{n(n-1)}{2}$.

7. a) Write the adjacency matrix of the graph:



- b) Find shortest path from a to z for the following weighted graph:



8. a) Define numeric function. Find the generating function corresponding to numeric function $a_r = 2^r + 3^r$.

- b) Solve the recurrence relation:

$$a_r - 6a_{r-1} + 8a_{r-2} = 0 \text{ given } a_0 = 3 \text{ and } a_1 = 2.$$

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