

Find the lines of regression and coefficient of correlation from the following table: 7

| | | | | | |
|---|---|----|----|----|----|
| X | 3 | 4 | 6 | 7 | 10 |
| Y | 9 | 11 | 14 | 15 | 16 |

5. a) The probability density function $p(x)$ of a random variable is given by $p(x) = y_0 e^{-|x|}$, $-\infty \leq x \leq \infty$. Find the value of y_0 . 2
- b) If the 10 percent of the bolts produced by a machine are defective, find the probability that out of 5 bolts chosen at random at least two will be defective. 2
- c) Write the procedure to test significance and goodness of fit using χ^2 method. 3
- d) Prove that the mean deviation from mean of a normal distribution is approximately $\frac{4}{5}$ times of standard deviation. 7

OR

The nine items of a sample have the values: 45, 47, 50, 52, 48, 47, 49, 53, 51. Does the mean of these differ significant from the assumed mean 47.5. ($t_{0.05} = 2.31$ for $\nu = 8$). 7

B.E. - 401

B.E. IV Semester

Examination, June 2014

Engineering Mathematics - III

(Common for all Branches)

Time : Three Hours

Maximum Marks : 70

- Note:** i) Answer five questions. In each question part A, B, C is compulsory and D part has internal choice.
- ii) All parts of each question are to be attempted at one place.
- iii) All questions carry equal marks, out of which part A and B (Max. 50 words) carry 2 marks, part C (Max. 100 words) carry 3 marks, part D (Max. 400 words) carry 7 marks.
- iv) Except numericals, Derivation, Design and Drawing etc.

1. a) Show that the function $\frac{1}{2} \log(x^2 + y^2)$ is harmonic. 2
- b) Evaluate the integral $\int_C \frac{z^2 - z + 1}{z - 1} dz$, where C is the circle $|z| = 1$. 2
- c) Find Cauchy - Riemann equations in polar form. 3
- d) Find the analytic function $f(z) = u + iv$ if $u - v = (x - y)(x^2 + 4xy + y^2)$ 7

OR

Evaluate the integral $\int_0^{\infty} \frac{\cos ax}{x^2+1} dx$. 7

2. a) Determine the Newton - Raphson iterative formula to find the k^{th} root of N. 2
- b) Find a real root of the equation $x \log_{10} x = 1.2$ by regula - falsi method correct to one decimal place. 2
- c) Find a real root of the equation $3x = \cos x + 1$ by iterative method correct to two decimal places. 3
- d) Apply Crout's factorization method to solve the system of equations: 7

$$\begin{aligned} x - y &= 0 \\ -2x + 4y - 2z &= -1 \\ -y + 2z &= 1.5 \end{aligned}$$

OR

Apply Gauss-Seidel iteration method to solve the system of equations: 7

$$\begin{aligned} 20x + y - 2z &= 17 \\ 3x + 20y - z &= -18 \\ 2x - 3y + 20z &= 1.5 \end{aligned}$$

3. a) Prove that: $e^x = \left(\frac{\Delta^2}{E} \right) e^x \cdot \frac{Ee^x}{\Delta^2 e^x}$ 2
- b) Derive Newton's forward interpolation formula. 2
- c) Evaluate the integral $\int_0^{0.6} e^{-x^2} dx$ by Simpson $\frac{1}{3}$ rule. 3

- d) Apply Newton's divided difference formula to find the value of $f(9)$ from the following table: 7

| | | | | | |
|--------|-----|-----|------|------|------|
| x | 5 | 7 | 11 | 13 | 17 |
| $f(x)$ | 150 | 392 | 1452 | 2368 | 5202 |

OR

Find $\frac{dy}{dx}$ at $x = 1.1$ from the following table: 7

| | | | | | | |
|-----|-----|-------|-------|-------|-------|-------|
| x | 1.0 | 1.2 | 1.4 | 1.6 | 1.8 | 2.0 |
| y | 0 | 0.128 | 0.544 | 1.296 | 2.432 | 4.000 |

4. a) Find by Taylor's series method the value $y(0.1)$ correct to three decimal places from the differential equation:

$$\frac{dy}{dx} = x^2 y - y, y(0) = 1. \quad 2$$

- b) Write the working rule of Runge-Kutta method of fourth order for the numerical solution of differential equation. 2

- c) If θ is the angle between the two regression lines show that: 3

$$\tan \theta = \frac{1-r^2}{r} \cdot \frac{\sigma_x \sigma_y}{\sigma_x^2 + \sigma_y^2}.$$

- d) Using modified Euler's method, find the value of $y(0.3)$ from the equation: 7

$$\frac{dy}{dx} = x + y, y(0) = 1.$$

OR