

Roll No.

MVSE-102**M. E. (First Semester) EXAMINATION, Dec., 2010****STRENGTH OF MATERIAL AND THEORY OF ELASTICITY****(MVSE-102)***Time : Three Hours**Maximum Marks : 100**Minimum Pass Marks : 40***Note :** Attempt any five questions.

- 1 (a) State the assumptions made in the theory of elasticity. 6

- (b) Derive the following equations : 14

$$\sigma_x = \lambda_e + 2 G \epsilon_x$$

$$\sigma_y = \lambda_e + 2 G \epsilon_y$$

$$\sigma_z = \lambda_e + 2 G \epsilon_z$$

$$\text{where, } \lambda = \frac{\mu E}{(1 + \mu)(1 - 2\mu)}$$

2. In a 2-D problem, derive the following equations : 20

(i) Compatibility equations

(ii) Differential equations

Using the above explain how a problem in elasticity can be solved.

3. (a) Derive the equations of equilibrium in polar co-ordinates. 8

- (b) For the case of axially symmetric stress distribution taking the general solution of the compatibility equation in the form :

$$Q = A \log r + B r^2 \log r + C r^2 + D$$

calculate the maximum circumferential stress in a thick cylinder of internal radius r_i and external radius r_o subjected to uniform pressure p_i and p_o at the inner and outer surface.

4. Find out the expression for vertical and horizontal deformations of a circular ring of radius
- R
- , subjected to diametrical opposite loads
- P
-
- P
- , using energy method. 20

5. Why do we use polar co-ordinate systems ? Derive equations of equilibrium and compatibility in polar co-ordinates. 20

6. (a) What do you understand by membrane analogy ? How is it useful in torsional analysis ? 10

- (b) Derive the expressions for shear stress, angle of twist and twisting moments in case of a thin rectangular section. 10

7. (a) What are the rectangular components of stress in three dimensions ? 10

- (b) Establish equation of equilibrium in three dimension. 10

8. Write short notes on any four of the following : 5 each

(i) Boundary conditions

(ii) Strain energy in torsion

(iii) Torsional analysis of rolled sections

(iv) Saint-Venant's principle

(v) Pure bending of prismatic bars