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## CS/IT-224 B.E., III Semester

Examination, December 2016

## Choice Based Credit System (CBCS) Discrete Structure

Time: Three Hours

Maximum Marks: 60

- Note: i) Attempt any five questions.
  - ii) All questions carry equal marks.
- 1. a) Let A, B, C be any three sets, then prove that  $A \times (B \cap C) = (A \times B) \cap (A \times C)$ 
  - b) Show that if  $R_1$  and  $R_2$  are equivalence relations on A, then  $R_1 \cap R_2$  is an equivalence relation on A.
- 2. a) Let  $f: \mathbb{R} \to \mathbb{R}$  be defined by f(x) = 3x + 4, show that f is one-one and onto. Give a formula that defines  $f^{-1}$ .
  - b) Prove by the method of mathematical induction that  $7^{2n} + 2^{3n-3} \cdot 3^{n-1}$  is divisible by 25 for all  $n \in \mathbb{N}$ .
- 3. a) Show that the algebraic structure  $(\{a+b\sqrt{2}:a,b\in I\},+)$  forms a group.
  - b) Prove that every field is an integral domain.
- 4. a) Obtain disjunctive normal form of  $P \lor (\sim P \rightarrow (q \lor (q \rightarrow \sim r)))$ 
  - b) Show that  $((p \lor q) \land \sim (\sim p \land (\sim q \lor \sim r))) \lor (\sim p \land \sim q) \lor (\sim p \land \sim r)$  is a tautology.
- a) Find a deterministic Finite-State Machine that recognizes the set:

$$L = \left\{ (01)^{i} 1^{2j} \mid i \ge 1, j \ge 1 \right\}$$

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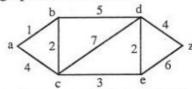
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b) For the finite state machine shown below, find all equivalent states and obtain an equivalent finite state machine with the smallest number of states:

State	Input		Output
	0	1	77.2
A	F	В	0
В	D	C	0
C	G	В	0
D	E	A	1
E	D	A	0
F	A	G	1
G	C	H	1
H	A	H	1

- 6. a) Write a short note on:
  - i) Isomorphism of groups
  - ii) Universal and existential quantifiers
  - b) Explain:
    - i) Hamiltonian paths and circuits
    - ii) Graph coloring
- a) Determine shortest path between vertices 'a' and 'z' in the graph shown below:



- b) Prove that every chain is a distributive lattice.
- 8. a) Find total solution for the recurrence relation

$$a_r - 4a_{r-1} + 4a_{r-2} = (r+1)2^r$$

Given  $a_0 = 1, a_1 = 2, a_2 = 3$ 

- b) Describe:
  - i) Hasse diagram
- ii) Binomial theorem

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