Total No. of Questions :5]

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## BE - 301

## **B.E. III Semester**

Examination, June 2014

## **Engineering Mathematics - II**

(Common for all Branches)

Time: Three Hours

Maximum Marks: 70

**Note:** i) Answer five questions. In each question part A, B, C is compulsory and D part has internal choice.

- ii) All parts of each question are to be attempted at one place.
- iii) All questions carry equal marks, out of which part A and B (Max. 50 words) carry 2 marks, part C (Max. 100 words) carry 3 marks, part D (Max. 400 words) carry 7 marks.
- iv) Except numericals, Derivation, Design and drawing etc.
- 1. a) Write Dirichlet's conditions for Fourier series.
  - Write linear property and change of scale property four Fourier transform.
  - c) Find the Fourier sine transform of  $e^{-|x|}$ . Hence show that

$$\int_0^\infty \frac{x \sin mx}{1+x^2} dx = \frac{\pi e^{-m}}{2}, m > 0$$
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d) Expand the function  $f(x)=x\sin x$  as a Fourier series in the interval  $-\pi \le x \le \pi$ . Deduce that

$$\frac{1}{1.3} - \frac{1}{3.5} + \frac{1}{5.7} - \frac{1}{7.9} + \dots = \frac{\pi - 2}{4}$$

OR

Obtain a half-range cosine series for

$$f(x) = \begin{cases} kx \text{ for } 0 \le x \le \frac{l}{2} \\ k(l-x) \text{ for } \frac{l}{2} \le x \le l \end{cases}$$

Deduce the sum of the series  $\frac{1}{1^2} + \frac{1}{3^2} + \frac{1}{5^2} + \dots$ .

- 2. a) If  $L\{f(t)\} = \overline{f}(s)$  then prove that  $L\{e^{at}f(t)\} = \overline{f}(s-a)$ .
  - b) Find the inverse L.T of  $\overline{f}(s) = \log \frac{s+2}{s+3}$ .
  - Using convolution theorem, find the inverse Laplace transform of  $\overline{f}(s) = \frac{1}{(s+1)(s^2+1)}$ .
  - d) Solve the following differential equation by Laplace transform:  $\frac{d^2y}{dt^2} + \frac{5dy}{dt} + 6y = 5e^t$ , given y(0) = 2, y'(0) = 1.

OR

Find the Laplace transform of

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(i) 
$$f(t) = \int_0^t e^{-t} \frac{\sin t}{t} dt$$
 (ii)  $f(t) = t^2 e^{-2t} \cos 3t$ 

- 3. a) In the differential equation  $\frac{d^2y}{dx^2} + P\frac{dy}{dx} + Qy = R$ , satisfies the equation 1 P + Q = 0, then find the one part of complimentary function of the differential equation.
  - b) Write a part of C.F of the differential equation  $(3-x)\frac{d^2y}{dx^2} (9-4x)\frac{dy}{dx} + (6-3x)y = 0$
  - c) Prove that  $J_1(x) = \sqrt{\frac{2}{\pi x}} \sin x$
  - d) Solve in series the differential equation  $(1-x^2)\frac{d^2y}{dx^2} + 2x\frac{dy}{dx} + y = 0.$

OR

Solve the differential equation

$$x\frac{d^2y}{dx^2} - \frac{dy}{dx} - 4x^3y = 8x^3\sin x^2.$$

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- 4. a) Solve the p.d.e. xp + yq = 3z.
  - b) Find the particular integral of the p.d.e.

$$\frac{\partial^2 z}{\partial x^3} - 7 \frac{\partial^3 z}{\partial x \partial y^2} - 6 \frac{\partial^3 z}{\partial y^3} = \sin(x + 2y)$$

- c) Solve  $p^2 q^2 = x y$ .
- d) Solve the p.d.e  $(D-D'-1)(D-D'-2)z = e^{3x-y} + x$ .

OR

Use the method of separation of variables to solve the

equation 
$$\frac{\partial^2 u}{\partial x^2} - 2 \frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} = 0$$
.

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5. a) Find the grad  $\phi$  when  $\phi$  is given by  $\phi = 3x^2y - y^3z^2$  at the point (1, -2, -1).

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- b) Write the statement of Gauss divergence theorem .
- c) A vector field is given by  $\overline{A} = (x^2 + xy^2)i + (y^2 + x^2y)j$ . Show that the field is irrotational.
- d) Find the work done when a force  $\overline{F} = (x^2 y^2 + x)i (2xy + y)j$  moves a particle in the xy plane from (0,0) to (1,1) along the parabola  $y^2 = x$ . Is the work done different when the path is the straight line y = x?

OR

Verify stoke's theorem for  $\overline{F} = (x^2 - y^2)i + 2xyj$  over the box bounded by the planes x = 0, x = a; y = 0, y = b; z = 0, z = c; if the face z = 0 is cut.

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