[2]

Roll No

BE-3001 (EC) (CBGS)

B.E., IV Semester

Examination, May 2018

Choice Based Grading System (CBGS)

Mathematics - III

Time: Three Hours

Maximum Marks: 70

Note: i) Attempt any five questions out of eight.

- ii) All questions carry equal marks.
- 1. a) Find the Fourier series to represent the function $f(x) = x^2 \text{ in } (-\pi, \pi).$
 - b) Expand $f(x) = \pi x x^2$, $0 < n < \pi$ in a half range sine series. http://www.rgpvonline.com
- 2. a) Find Fourier sine transform of $\frac{e^{-ax}}{x}$.
 - b) Find the cosine transform of $\frac{1}{x^2 + a^2}$

- 3. a) Find Laplace transform of the followings:
 - i) $2\sin t \cos t$
 - ii) $\left(t^2+1\right)^2$
 - b) Find Laplace transform of the followings:
 - i) t sin at
 - ii) $t^n e^{at}$
- 4. a) Evaluate the followings:

i)
$$L^{-1}\left\{\frac{3s+7}{s^2-2s-3}\right\}$$

ii)
$$L^{-1}\left\{\frac{3s-2}{s^2-4s+20}\right\}$$

b) Using convolution theorem, evaluate

$$L^{-1}\left\{\frac{1}{(s-1)(s-2)}\right\}$$

5. a) Find the value of k for which the function

$$f(x) = \begin{cases} kx^2 & \text{if } 0 \le n \le 3\\ 0 & \text{otherwise} \end{cases}$$

is a probability density function. Also, compute $p(1 \le n \le 2)$.

- b) A coin is tossed 4 times. What is the probability of getting
 - i) two heads
 - ii) atleast two heads
- a) Use Poisson distribution to find the probability of at most 5 detective fuses in a box of 200 fuses. Experience shows that 2% of such fuses are defective.
 - b) Find mean and variance of binomial distribution.

http://www.rgpvonline.com

7. a) Use least square method to Dot a straight line to the data

х	1	2	3	4
у	3	7	13	21

b) Dot a Poisson distribution to the set of observations.

x	0	1	2	3	4
у	122	60	15	2	1

- 8. a) If there are 3 misprints in a book of 1000 pages, find the probability that a given page will contain
 - i) No misprint
 - ii) More than 2 misprints

b) Find
$$L\left\{\frac{1-e^t}{t}\right\}$$
