CS/IT 302

B.E. III Semester

Examination, December 2012

Discrete Structure

Time: Three Hours Maximum Marks: 70/100

Nok: 1. Attempt any one question from each unit.

2. All questions carry equal marks. Rgpv online question papers

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Unit- I

- 1. a) Out of 120 students sun/eyed, it was found that 20 students have studied French, 50 students have studied English, 70 students have studied Hindi, 5 have studied English and French, 20 have studied English and Hindi, 10 have studied Hindi and French. Only 3 students have studied all the three languages. Find how many students have studied.
- (i) Hindi alone (ii) French alone (iii) English but not Hindi (iv) Hindi but not French.
- b) If n pigeons are assigned to m pigeonhole and m<n show that some pigeonholes contain at least two pigeon also show that among 13 people, there are at least two people. who were born in the same month.

Or

- 2. a) Write the principle of mathematical induction and by using this prove that n(n2+5) is an integer multiple of 6 for all positive integer n.
- b) Define equivalence relation and prove that the relation a b (mod m); i.e., m divides (a-b) in the set of all integers 1 is an equivalence relation.

- 3. a) Let (A, *) be a monoid such that for every x in A, x*x -= e where e is the identity element. Show that (A, *) is an abelian group.
- b) Define Ring and show that in a ring R (i) (-a)(-b) = -ab
- (ii) (-1)(-1) 1. If R has an identity element.

Or

- 4. Let (H, .) be a subgroup of (0, .). $N = \{x \mid x \in G, xHx^{-1} = H\}$ Let Show that (N, .) is a subgroup of G
- b) Let S he the set of real numbers of the form $a \pm b$,h; where a and b are rational numbers. Show that S is a field with respect to addition and multiplication.

Unit-III

5. a) Define tautology and contradiction and show that

$$P \Rightarrow (q \Rightarrow r) \equiv (p \land q) \Rightarrow r$$

b) Construct the state diagram for the finite state machine with the state table as given below.

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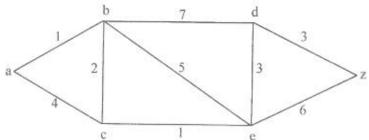
State	f Input		g Output	
	0	1	0	1
S_o	S_1	So	1	0
S_1	S ₂	S,	0	1
S_2	S_3	S	1	1
S_3	S,	S,	0	0

- 6. a) State and prove De Morgan's Laws.
- b) For the finite state machine shown below, find all equivalent states and obtain an equivalent finite state machine with the smallest number of states.

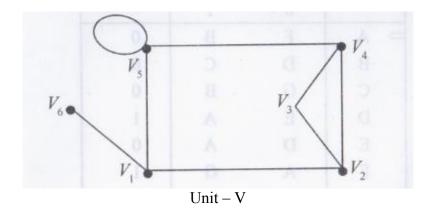
State	Input		Output
	0	1	
⇒ A	F	В	0
В	D	C	0
C	G	В	0
D	E	Α	1
E	D	A	0
F	Α	G	1
G	C	H	1
Н	A	H	1

Unit IV

7. a) Write an algorithm for shortest path in weighted graph and use it to find shortest path from a to z in the graph shown in the following figure where numbers associated with the edges are the weights.



- b) Define Chromatic polymial. Show that a graph with n vertices is a tree if and only if
- 8. a) Prove that a graph G with N vertices always has a Hamiltonian path if the sum of the degrees of every pair of vertices V, V; in G satisfies the condition d(V1) + d(k) > (n-1).
- b) Explaining need of the matrix representation of the graph write the adjacency matrix of the following graph.



- 9. a) Let L be the set of all factors of 12 and 1 be the divisibility relation on L, show that (L,1) is a lattice.
- b) Determine the discrete Numeric function corresponding to the following generating functions.

i)
$$A(z) = \frac{(1+z)^2}{(1+z)^4}$$
 ii) $A(z) = \frac{1}{1-z^3}$

Or

- 10. a) Define any three of the following.
 - i) Hasse diagram of partially ordered set
 - ii) Well ordered set (iii) Complemented lattice
- b) Solve by the method of generating functions the recurrence relation dfasds ssdf