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## EC-603

## B. E. (Sixth Semester) EXAMINATION, June, 2012 (Electronics & Communication Engg. Branch)

## DIGITAL SIGNAL PROCESSING

(EC-603)

Time: Three Hours

Maximum Marks: 100

Minimum Pass Marks: 35

Note: Attempt all the *five* questions. Choice is provided within every question.

. (a) Given the sequence:

$$x(n) = (6-n)[u(n) - u(n-6)]$$

Make a sketch of:

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- (i)  $y_1(n) = x(4-n)$
- (ii)  $y_2(n) = x(2n-3)$
- (b) Determine whether the following system is periodic or not:
  - (i)  $x(n) = \cos(0.125 \pi n)$
  - (ii)  $x(n) = \sin(\pi + 0.2 n)$

Or

Find the solution to the difference equation: 20

$$y(n) = y(n-1) - y(n-2) + 0.5x(n) + 0.5x(n-1)$$

Input  $x(n) = (0.5)^n u(n)$  with initial conditions y(-1) = 0.75 and y(-2) = 0.25.

P. T. O.

2. (a) Find the z-transform of the following sequences: 10

(i) 
$$x(n) = \left(\frac{1}{3}\right)^n \cos(n\omega_0) u(n)$$

- (ii)  $x(n) = \alpha^{|n|}$
- (b) Find the inverse of the following z-transform: 10

(i) 
$$X(z) = \log \left(1 - \frac{1}{2}z^{-1}\right) |z| > \frac{1}{2}$$

(ii)  $X(z) = e^{1/2}$  with x(n) a right side sequence.

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Evaluate the following integral:

$$\frac{1}{2\pi j} \oint_{C} \frac{1 + 2z^{-1} - z^{-2}}{\left(1 - 0.5z^{-1}\right) \left(1 - \frac{2}{3}z^{-1}\right)} \times z^{3} dz$$

where contour of integration 'C' is unit circle.

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3. (a) Find the discrete time Fourier transform of the two-sided sequence:

$$x\left(n\right) = \left(\frac{1}{4}\right)^{\left|n\right|}$$

(b) Find the frequency response of a linear shift invariant system whose input and output satisfy the difference equation:

$$y(n) - 0.5y(n-1) = x(n) + 2x(n-1) + x(n-2)$$
Or

Find a difference equation to implement a system that has a unit sample response:

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$$h(n) = \left(\frac{1}{4}\right)^n \cos\left(\frac{n\pi}{3}\right) u(n)$$

4. Describe decimation in time algorithm for fast Fourier transformation.

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What do you understand by Decimation in frequency algorithm for FFT? Also discuss FFT algorithm for composite N.

5. Write notes on any two of the following:

10 each

- (i) FIR filter
- (ii) IIR filter
- (iii) Various kinds of windows
- (iv) Bilinear transformation