Roll No

Unit - V

- What is FEM? Write some application of FEM.
- Find the extremal of $I = \int_{x_0}^{x_1} (16y^2 y^{1/2} + x^2) dx$

OR

- Find the curve on which the functional $\int_0^1 (y')^2 + 2xy dx \text{ with y } (0) = 0 \text{ and y}(1) = 1 \text{ can be}$ extremised?
 - Write short note on
 - i) Ritz method
 - ii) Galerkin's method

RGPVONLINE.COM

MMTP/MMCM/MMIE/MMMD/MMPD-101

M.E./M.Tech., 1 Semester

Examination, July 2015

Advanced Mathematics

Time: Three Hours

Maximum Marks: 70

Note: Attempt one question from each unit. All questions carry equal marks.

Unit - I

- 1. a) Show that the mapping $T: V_2(R) \to V_3(R)$ defined by T(a, b) = (a + b, a - b, b) is a linear transformation from $V_2(R)$ into $V_3(R)$?
 - b) Show that the vectors (1, 0, 0) (1, 1, 0) (1, 1, 1) form a basis for R³?

OR

- 2. a) Prove that four vectors $\alpha_1 = (1,2,3), \alpha_2 = (1,0,0)$ $\alpha_3 = (0,1,0), \ \alpha_4 = (0,0,1) \text{ in } V_3(R) \text{ form a linearly}$ dependent set.
 - b) What are Hermite polynomials explain briefly?

Unit - II

3. a) Use the method of separation of variables to solve the equations:

$$\frac{\partial^2 u}{\partial x^2} = \frac{\partial u}{\partial y} + \partial t$$

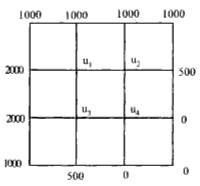
- b) Write short note on
 - i) FT

ii) DFT

OR

 a) Given the values of u (x, y) on the boundary of the square in the following figure:

Evaluate the function u(x, y) satisfying the Laplace equation $\nabla_{\alpha}^2 = 0$ at the pivotal points of this figured by:



b) Explain the wavelet transform, explain briefly?

Unit - III

- A can hit a target 4 times in 5 shots B can hit three times in 4 shots and C can hit twice in 3 shots. They fire a volley what is the probability that two shots at least hit? Write short note on
- i) Hypothesis
- ii) Recurred relation

OR

The probability that a valve manufactured by a company will be defective is 1/10. If 12 such valves are manufactured find the probability with the help of binomial distribution

- Exactly two will be defective
- ii) At least two will be defective

RGPVONLINE.COM

b) Write short note on

RGPVONLINE.COM

- i) Poisson distribution
- Normal distribution

Unit - IV

7. a) Find the probability for queuing model

 $(M/M/1 : \infty/\infty / FCFS)$

- b) A self service store employs one cashier at its counter. Nine customers arrive on an average every 5 minutes while the cashier can serve 10 customers in 5 minutes. Assuming Poisson distribution for arrival rate and exponential distribution for service rate find:
 - i) Average number of customers in the system.
 - ii) Average number of customer in queue

(average queue length)

OR

- 8. a) Write short note on
 - i) Maslov process
 - ii) Transient and steady state for queuing system
 - b) A person repairing radio's find that the time spent on the radio sets has been exponential distributed with mean 20 minutes. If the radios are repaired in the order in which they come in and their arrival is approximately poisson with an average rate of 15 for 8 hour day. What is the repairman's expected idle time each day.