Examination, June 2016

Information Theory and Coding (Elective-I)

Time: Three Hours

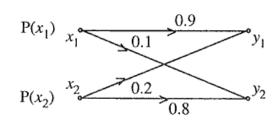
Maximum Marks: 70

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Note: i) Attempt any five questions out of eight.

- ii) All questions carry equal marks.
- 1. a) Write down the comparison between binary memory less channel and discrete memory less channel.
 - b) A discrete source emits one of five symbols once every millisecond with probabilities $\frac{1}{2}$, $\frac{1}{4}$, $\frac{1}{8}$, $\frac{1}{16}$ and $\frac{1}{32}$ respectively. Determine the source entropy and information rate.
- 2. a) State and explain Shannon's capacity theorem.
 - b) Given a binary channel shown in figure.



- i) Find the channel matrix of the channel.
- ii) Find $P(y_1)$ and $P(y_2)$ when $P(x_1) = P(x_2) = 0.5$
- iii) Find the joint probability $P(x_1, y_2)$ and $P(x_2, y_1)$ when $P(x_1) = P(x_2) = 0.5$

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- 3. Define following terms: Code word, Block length, Code rate, Channel data rate, Code vector.
 - State and explain channel coding theorem in detail.
- Describe syndrome decoding method to correct errors with suitable diagram and description.
 - b) For a (7, 4) block code generated by [G] below, explain how the error syndrome helps in correcting single error.

$$G = \begin{bmatrix} 1 & 0 & 0 & 0 & 1 & 1 & 0 \\ 0 & 1 & 0 & 0 & 0 & 1 & 1 \\ 0 & 0 & 1 & 0 & 1 & 0 & 1 \\ 0 & 0 & 0 & 1 & 1 & 1 & 1 \end{bmatrix}$$

- Draw the block diagram of encoder for systematic (n, k)cyclic codes and explain briefly.
 - For the (7, 4) Hamming code, the parity check matrix H is given by

$$\mathbf{H} = \begin{bmatrix} 1 & 0 & 1 & 1 & 1 & 0 & 0 \\ 1 & 1 & 0 & 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 1 & 0 & 0 & 1 \end{bmatrix}$$

- i) Construct the generator matrix.
- ii) The code word that begins with 1010.
- iii) If the received code word Y is 0111100, then decode this received code word.
- What do you mean by Cyclic codes? Write down the basic properties of cyclic codes.
 - Describe Viterbi algorithm for decoding convolutional codes.

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- What are BCH codes? Discuss its encoding and decoding procedures.
 - Explain code tree, Trellis and state diagram for a convolutional encoder with suitable example.

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- Write short notes (any two):
 - Hamming code and their applications
 - Fading channel
 - Huffman coding
 - Advantages and disadvantages of convolutional codes.
