

- d) Explain the procedure for designing a FIR filter using the Kaiser window.

OR

What is impulse invariant technique? Obtain the mapping formula for the impulse invariant transformation.

Roll No

EC-603

B.E. VI Semester

Examination, December 2016

Digital Signal Processing

Time : Three Hours

Maximum Marks : 70

- Note:** i) Answer five questions. In each question part A, B, C is compulsory and D part has internal choice.
ii) All parts of each question are to be attempted at one place.
iii) All questions carry equal marks, out of which part A and B (Max. 50 words) carry 2 marks, part C (Max. 100 words) carry 3 marks, part D (Max. 400 words) carry 7 marks.
iv) Except Numericals, Derivation, Design and Drawing etc.

Unit-I

1. a) Define and explain discrete time linear time invariant system.
b) Determine if the following system is time invariant or time variant $y(n) = x(n) \cos \omega_0 n$
c) Explain and differentiate the following :
i) Causal versus noncausal system
ii) Linear Versus nonlinear system
d) Show that for a linear time invariant system, if the input sequence is $x(n)$ and impulse response is $h(n)$, then the

output $y(n)$ is given by $y(n) = \sum_{k=-\infty}^{\infty} x(k)h(n-k)$

[2]

OR

Determine the output $y(n)$ of a relaxed linear time invariant system with impulse response $h(n) = a^n u(n)$, $|a| < 1$ when the input is a unit step sequence that is $x(n) = u(n)$

Unit-II

2. a) Define Z-transform and explain its use.
- b) Define Region of convergence and explain the significance of ROC in Z-plane.
- c) Determine the Z-transform of the signal

$$x(n) = \left(\frac{1}{2}\right)^n u(n).$$

- d) State and prove the following properties of Z-transform.
 - i) Time shifting
 - ii) Convolution

OR

Determine the system function and the unit sample response of the system described by the difference equation $y(n) = \frac{1}{2} y(n-1) + 2x(n)$.

Unit-III

3. a) Define DFT for a sequence $x(n)$.
- b) Define circular convolution. What is the difference between circular and linear convolutions.

[3]

- c) State and prove the following property of DFT.
 - i) Periodicity
 - ii) Linearity
- d) A finite duration sequence of length L is given as

$$x(n) = \begin{cases} 1 & 0 \leq n \leq L-1 \\ 0 & \text{otherwise} \end{cases}$$

Determine the N-point DFT of this sequence for $N \geq L$

OR

Compute the DFT of the four point sequence $x(n) = (0 \ 1 \ 2 \ 3)$

Unit-IV

4. a) Why is FFT called so?
- b) State the computational requirements of FFT.
- c) Explain the difference between decimation in time and decimation in frequency FFT algorithm.
- d) Draw the flow graph of an eight point decimation in time FFT algorithm.

OR

Given $x(n) = \{1, 2, 3, 4, 4, 3, 2, 1\}$ find $X(k)$ using decimation in time FFT algorithm.

Unit-V

5. a) Define FIR filter and IIR filter.
- b) Compare FIR filter with IIR filters.
- c) What is bilinear transformation method of designing IIR filter? Explain.