

# Inf1B

## Arrays<sup>1</sup>

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adapting earlier version by Perdita Stevens and Ewan Klein

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<sup>1</sup>Thanks to [Sedgewick&Wayne](#) for much of this content

# Arrays

# Many Variables of the Same Type

How do we initialize 10 variables of the same type?

```
double a0, a1, a2, a3, a4, a5, a6, a7, a8, a9;  
a0 = 0.0;  
a1 = 0.0;  
a2 = 0.0;  
a3 = 0.0;  
a4 = 0.0;  
a5 = 0.0;  
a6 = 0.0;  
a7 = 0.0;  
a8 = 0.0;  
a9 = 0.0;  
...  
a4 = 3.0;  
a4 = 8.5;  
...  
double x = a4 + a5;
```

# Many Variables of the Same Type

How do we initialize 10 variables of the same type?

Much more efficient would be something like this:

```
double a = 0.0 X 10;
```

# Many Variables of the Same Type

How do we initialize 10 variables of the same type?

```
// easy alternative  
double[] a = new double[10];  
...  
a[4] = 3.0;  
a[8] = 8.0;  
...  
double x = a[4] + a[8];
```

declares, creates and  
initializes

# Many Variables of the Same Type

How do we initialize 1 million variables of the same type?

```
// just as easy with large arrays
double[] a = new double[1000000];
...
a[123456] = 3.0;
a[987654] = 8.0;
...
double x = a[123456] + a[987654];
```

# Arrays

Arrays: allow us to store and manipulate large quantities of data.  
An **array** is an indexed sequence of values of the same type.

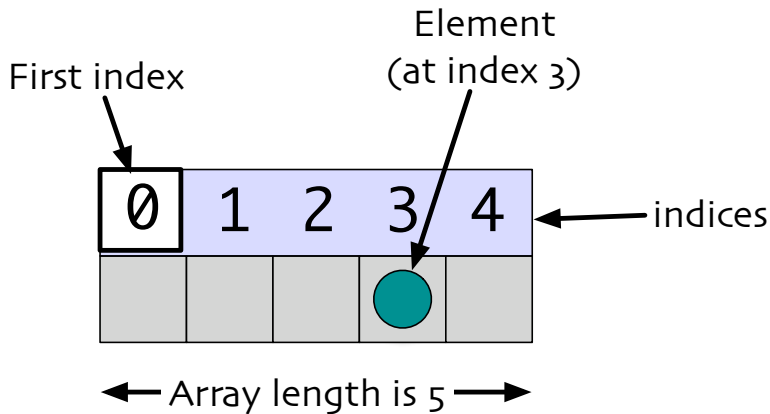
## Examples

- ▶ 52 playing cards in a deck.
- ▶ 17,000 undergraduates in UoE.
- ▶ 1 million characters in a book.
- ▶ 10 million audio samples in an MP3 file.
- ▶ 4 billion nucleotides in a DNA strand.
- ▶ 90 billion Google queries per year.
- ▶ 50 trillion cells in the human body.

<i>index</i>	<i>value</i>
0	Rebecca
1	Isla
2	Brooke
3	Megan
4	Niamh
5	Eilidh
6	Eva
7	Abbie
8	Skye
9	Aimee

(From 100 most popular Scottish girls' names, 2007)

# Arrays





# What happens in memory?

primitives

a0	0
a1	0
a2	0
a3	0
a4	0

array

a	0
	0
	0
	0
	0

# Your first Object!

- ▶ In Java, arrays are considered objects
- ▶ They are a special kind of object

We will get back to that in later lectures ...

# Arrays in Java

Java has special support for arrays:

- ▶ To make an array: declare, create and initialize it.

Declare an array

```
int[] arrayOfInts;
```

Create an array of length 10

```
arrayOfInts = new int[10];
```

# Arrays in Java

Java has special support for arrays:

- ▶ To make an array: declare, create and initialize it.
- ▶ To access element `i` of array named `a`, use `a[i]`.
- ▶ Array indices start at `0`.

```
int n = 10;                // size of array
double[] a;                // declare the array
a = new double[n];         // create the array
for (int i = 0; i < n; i++) {
    a[i] = 0.0;            // initialise each elt
}
```

# Arrays in Java

Java has special support for arrays:

- ▶ To make an array: declare, create and initialize it.
- ▶ To access element `i` of array named `a`, use `a[i]`.
- ▶ Array indices start at `0`.

```
int n = 10;                // size of array
double[] a;                // declare the array
a = new double[n];         // create the array
for (int i = 0; i < n; i++) {
    a[i] = 0.0;            // initialise each elt
}
```

Compact alternative:

- ▶ Declare, create and initialize in one statement.

```
int n = 10;                // size of array
double[] a = new double[n]; // declare, create, init
```

# Default Initialization of Arrays

Each array element is automatically initialized to a default value:

`int`: 0  
`double`: 0.0  
`boolean`: false  
`String`: null

# Types of Array

All elements of a given array must be of the **same type**.

## Array Types

```
int[]  
double[]  
String[]  
char[]  
...
```

Array of Strings:

```
String[] names = new String[5];  
names[0] = "Rebecca";  
names[1] = "Isla";  
names[2] = "Brooke";  
names[3] = "Megan";  
names[4] = "Niamh";
```

# Alternative Initialization Syntax for Arrays

- ▶ Shorthand syntax for initializing arrays.
- ▶ Handy if you only have a few data items.

```
String[] names = {"Rebecca", "Isla", "Brooke", "Megan", "Niamh"};  
int[] mynums = { 0, 7, 9, 1, 4 };  
double[] morenums = { 2.5, -0.1, 33.0 };
```



# The Length of Arrays

Given an array `a`,

- ▶ check the length of the array: `a.length`
- ▶ first element is `a[0]`
- ▶ second element is `a[1]`
- ▶ ...
- ▶ last element is `a[a.length-1]`
- ▶ If an array index is too small or too large, Java throws run-time error: `ArrayIndexOutOfBoundsException`

## Arrays: Another Example

```
public class ArrayEx {  
    public static void main(String[] args) {  
        String[] names = { "Rebecca", "Isla", "Brooke", "Megan", "Niamh" };  
        System.out.println(names.length);  
        System.out.println(names[1]);  
        System.out.println(names[names.length]);  
    }  
}
```

## Arrays: Another Example

```
public class ArrayEx {  
    public static void main(String[] args) {  
        String[] names = { "Rebecca", "Isla", "Brooke", "Megan", "Niamh" };  
        System.out.println(names.length);  
        System.out.println(names[1]);  
        System.out.println(names[names.length]);  
    }  
}
```

### Output

5

## Arrays: Another Example

```
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    public static void main(String[] args) {  
        String[] names = { "Rebecca", "Isla", "Brooke", "Megan", "Niamh" };  
        System.out.println(names.length);  
        System.out.println(names[1]);  
        System.out.println(names[names.length]);  
    }  
}
```

### Output

```
5  
Isla
```

# Arrays: Another Example

```
public class ArrayEx {  
    public static void main(String[] args) {  
        String[] names = { "Rebecca", "Isla", "Brooke", "Megan", "Niamh" };  
        System.out.println(names.length);  
        System.out.println(names[1]);  
        System.out.println(names[names.length]);  
    }  
}
```

## Output

5

Isla

Exception in thread "main" java.lang.ArrayIndexOutOfBoundsException

## Arrays: Another Example

```
public class ArrayEx {  
    public static void main(String[] args) {  
        String[] names = { "Rebecca", "Isla", "Brooke", "Megan", "Niamh" };  
        System.out.println(names.length);  
        System.out.println(names[1]);  
        System.out.println(names[names.length]);  
    }  
}
```

### Output

5

Isla

Exception in thread "main" java.lang.ArrayIndexOutOfBoundsException

To get at last element, use `names[names.length-1]`.

# Vector Dot Product

**Dot Product:** Given two vectors  $x[]$  and  $y[]$  of length  $n$ , their dot product is the sum of the products of their corresponding components.

```
double[] x = { 0.3, 0.6, 0.1 };  
double[] y = { 0.5, 0.1, 0.4 };  
double sum = 0.0;  
for (int i = 0; i < x.length; i++) {  
    sum = sum + x[i] * y[i];  
}
```

## States

i	x[i]	y[i]	x[i]*y[i]	sum
0	0.30	0.50	0.15	0.15
1	0.60	0.10	0.06	0.21
2	0.10	0.40	0.04	0.25

# Array-processing Examples

Create an array with random values



# Array-processing Examples

Create an array with random values

```
double[] a = new double[n];  
for (int i = 0; i < a.length; i++) {  
    a[i] = Math.random();  
}
```

# Array-processing Examples

Create an array with random values

```
double[] a = new double[n];  
for (int i = 0; i < a.length; i++) {  
    a[i] = Math.random();  
}
```

Print the array values, one per line

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double[] a = new double[n];  
for (int i = 0; i < a.length; i++) {  
    a[i] = Math.random();  
}
```

Print the array values, one per line

```
for (int i = 0; i < a.length; i++) {  
    System.out.println(a[i]);  
}
```

# Array-processing Examples

Create an array with random values

```
double[] a = new double[n];  
for (int i = 0; i < a.length; i++) {  
    a[i] = Math.random();  
}
```

Print the array values, one per line

```
for (int i = 0; i < a.length; i++) {  
    System.out.println(a[i]);  
}
```

Find the maximum of the array values

# Array-processing Examples

Create an array with random values

```
double[] a = new double[n];  
for (int i = 0; i < a.length; i++) {  
    a[i] = Math.random();  
}
```

Print the array values, one per line

```
for (int i = 0; i < a.length; i++) {  
    System.out.println(a[i]);  
}
```

Find the maximum of the array values

```
double max = a[0];  
for (int i = 1; i < a.length; i++) {  
    if (a[i] > max) max = a[i];  
}
```

# Array-processing Examples

Copy one array to another.

# Array-processing Examples

Copy one array to another.

```
double[] a = {0.3, 1.2, 1.7, 0.4, 1.5};  
double[] b = new double[a.length];  
for (int i = 0; i < a.length; i++) {  
    b[i] = a[i];  
}
```

# Let's practice that



TOP HAT



# Setting Array Values at Run Time

Print a random card.

```
String[] rank = { "2", "3", "4", "5", "6", "7", "8",  
                  "9", "10", "Jack", "Queen", "King", "Ace" };  
  
String[] suit = { "Clubs", "Diamonds", "Hearts", "Spades" };  
  
int i = (int) (Math.random() * 13); // between 0 and 12  
int j = (int) (Math.random() * 4);  // between 0 and 3  
  
System.out.println(rank[i] + " of " + suit[j]);
```

## Output

7 of Spades

...

Jack of Diamonds

...

# Setting Array Values at Run Time

```
String[] deck = new String[52];
for (int i = 0; i < 13; i++) {
    for (int j = 0; j < 4; j++) {
        deck[4 * i + j] = rank[i] + " of " + suit[j];
    }
}
for (int k = 0; k < deck.length; k++) {
    System.out.println(deck[k]);
}
```

typical array-processing  
code changes values at  
runtime

Q: In what order does the program print the deck?

## Output 1

```
2 of Clubs
2 of Diamonds
2 of Hearts
2 of Spades
3 of Clubs
```

## Output 2

```
2 of Clubs
3 of Clubs
4 of Clubs
5 of Clubs
6 of Clubs
```

## Remark on hard-wired constants

```
1  String[] suit = { "Clubs", "Diamonds", "Hearts",  
2      "Spades" };  
3  String[] rank = { "2", "3", "4", "5", "6", "7",  
4      "8", "9", "10", "Jack", "Queen", "King", "Ace" };  
5  
6  String[] deck = new String[52];  
7  for (int i = 0; i < 13; i++) {  
8      for (int j = 0; j < 4; j++) {  
9          deck[4 * i + j] = rank[i] + " of " + suit[j];  
10     }  
11 }  
12  
13 for (int k = 0; k < 52; k++) {  
14     System.out.println(deck[k]);  
15 }
```

Avoid hard-wired constants to increase readability and maintainability.

## Remark on hard-wired constants

```
1  final String[] SUIT = { "Clubs", "Diamonds", "Hearts",
2      "Spades" };
3  final String[] RANK = { "2", "3", "4", "5", "6", "7",
4      "8", "9", "10", "Jack", "Queen", "King", "Ace" };
5
6  final int CARDS = SUIT.length * RANK.length;
7
8  String[] deck = new String[CARDS];
9  for (int i = 0; i < 13; i++) {
10     for (int j = 0; j < 4; j++) {
11         deck[4 * i + j] = RANK[i] + " of " + SUIT[j];
12     }
13 }
14
15 for (int k = 0; k < CARDS; k++) {
16     System.out.println(deck[k]);
17 }
```

Use a local constant value instead!

The `final` keyword allows only a single initialisation of that variable. Further attempts to change it are caught by the compiler.

## Remark on hard-wired constants

```
1  final String[] SUIT = { "Clubs", "Diamonds", "Hearts",  
2      "Spades" };  
3  final String[] RANK = { "2", "3", "4", "5", "6", "7",  
4      "8", "9", "10", "Jack", "Queen", "King", "Ace" };  
5  
6  final int SUITS = SUIT.length;  
7  final int RANKS = RANK.length;  
8  final int CARDS = SUITS * RANKS;  
9  
10 String[] deck = new String[CARDS];  
11 for (int i = 0; i < RANKS; i++) {  
12     for (int j = 0; j < SUITS; j++) {  
13         deck[SUITS * i + j] = RANK[i] + " of " + SUIT[j];  
14     }  
15 }  
16  
17 for (int k = 0; k < CARDS; k++) {  
18     System.out.println(deck[k]);  
19 }
```

Constants also improve readability and get rid of "magic" numbers.

## Remark on hard-wired constants

There are better ways to deal with this situation such as using *global* constants, functions or even [enums](#). But more about that later ...

# Shuffling

Given an array, rearrange its elements in random order.

Shuffling algorithm:

1. In iteration `i`, pick random card from `deck[i]` through `deck[CARDS-1]`, with each card equally likely.
2. Exchange it with `deck[i]`.

# Shuffling

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**Shuffling algorithm:**

1. In iteration `i`, pick random card from `deck[i]` through `deck[CARDS-1]`, with each card equally likely.
2. Exchange it with `deck[i]`.

```
1  for (int i = 0; i < CARDS; i++) {  
2      int randCard = i + (int) (Math.random() * (CARDS - i));  
3      String temp = deck[randCard];  
4      deck[randCard] = deck[i];  
5      deck[i] = temp;  
6  }
```



# Shuffling a Deck of Cards: Putting Everything Together

```
1  public class Deck {
2      public static void main(String[] args) {
3          final String[] SUIT = { "Clubs", "Diamonds", "Hearts", "Spades" };
4          final String[] RANK = { "2", "3", "4", "5", "6", "7",
5              "8", "9", "10", "Jack", "Queen", "King", "Ace" };
6          final int SUITS = SUIT.length;
7          final int RANKS = RANK.length;
8          final int CARDS = SUITS * RANKS;
9
10         String[] deck = new String[CARDS];
11         for (int i = 0; i < CARDS; i++) {
12             for (int j = 0; j < SUITS; j++) {
13                 deck[SUITS * i + j] = RANK[i] + " of " + SUIT[j];
14             }
15         }
16         for (int i = 0; i < CARDS; i++) {
17             int randCard = i + (int) (Math.random() * (CARDS - i));
18             String temp = deck[randCard];
19             deck[randCard] = deck[i];
20             deck[i] = temp;
21         }
22         for (int k = 0; k < CARDS; k++) {
23             System.out.println(deck[k]);
24         }
25     }
26 }
```

# Shuffling a Deck of Cards

## Output

```
% java Deck
Jack of Clubs
4 of Spades
5 of Clubs
10 of Diamonds
2 of Hearts
Queen of Clubs
8 of Hearts
5 of Hearts
3 of Clubs
7 of Hearts
10 of Hearts
6 of Hearts
Jack of Spades
...
3 of Hearts
```

## Output

```
% java Deck
4 of Spades
2 of Diamonds
5 of Hearts
7 of Diamonds
3 of Hearts
10 of Hearts
2 of Clubs
King of Diamonds
Queen of Diamonds
10 of Clubs
3 of Spades
7 of Hearts
8 of Clubs
...
3 of Clubs
```

# Two-Dimensional Arrays

Examples of two-dimensional arrays:

- ▶ Table of data for each experiment and outcome.
- ▶ Table of grades for each student and assignment.
- ▶ Table of grayscale values for each pixel in a 2D image.

Mathematical abstraction: matrix

Java abstraction: 2D Array

# Two-Dimensional Arrays in Java

**Array access:** Use `a[i][j]` to access element in row `i` and column `j`. **Zero-based indexing:** Row and column indices start at 0.

```
int m = 10;
int n = 3;
double[][] a = new double[m][n];
for (int i = 0; i < m; i++) {
    for (int j = 0; j < n; j++) {
        a[i][j] = 0.0;
    }
}
```

Initialize a 10-by-3 array of doubles

`a[i][ ]`

-----
a[0][0]   a[0][1]   a[0][2]
-----
a[1][0]   a[1][1]   a[1][2]
-----
a[2][0]   a[2][1]   a[2][2]
-----
a[3][0]   a[3][1]   a[3][2]
-----
a[4][0]   a[4][1]   a[4][2]
-----
a[5][0]   a[5][1]   a[5][2]
-----
a[6][0]   a[6][1]   a[6][2]
-----
a[7][0]   a[7][1]   a[7][2]
-----
a[8][0]   a[8][1]   a[8][2]
-----
a[9][0]   a[9][1]   a[9][2]
-----

`a[5]` →

A 10-by-3 array

## Setting 2D Array Values at Compile Time

Initialize 2D array of doubles by listing values. Each element of the array `p` is itself an array of type `double[]`.

```
double[][] p = {  
    { .02, .92, .02, .02, .02 },  
    { .02, .02, .32, .32, .32 },  
    { .02, .02, .02, .92, .02 },  
    { .92, .02, .02, .02, .02 },  
    { .47, .02, .47, .02, .02 },  
};
```

```
0.02 0.92 0.02 0.02 0.02  
0.02 0.02 0.32 0.32 0.32  
0.02 0.02 0.02 0.92 0.02  
0.92 0.02 0.02 0.02 0.02  
0.47 0.02 0.47 0.02 0.02
```

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    { .02, .02, .02, .92, .02 },  
    { .92, .02, .02, .02, .02 },  
    { .47, .02, .47, .02, .02 },  
};
```

`p[1][3]`

```
0.02 0.92 0.02 0.02 0.02  
0.02 0.02 0.32 0.32 0.32  
0.02 0.02 0.02 0.92 0.02  
0.92 0.02 0.02 0.02 0.02  
0.47 0.02 0.47 0.02 0.02
```

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    { .02, .92, .02, .02, .02 },  
    { .02, .02, .32, .32, .32 },  
    { .02, .02, .02, .92, .02 },  
    { .92, .02, .02, .02, .02 },  
    { .47, .02, .47, .02, .02 },  
};
```

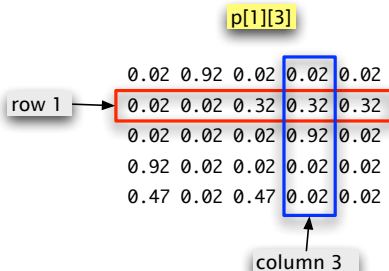
`p[1][3]`

	0.02	0.92	0.02	0.02	0.02
row 1 →	0.02	0.02	0.32	0.32	0.32
	0.02	0.02	0.02	0.92	0.02
	0.92	0.02	0.02	0.02	0.02
	0.47	0.02	0.47	0.02	0.02

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double[][] p = {  
    { .02, .92, .02, .02, .02 },  
    { .02, .02, .32, .32, .32 },  
    { .02, .02, .02, .92, .02 },  
    { .92, .02, .02, .02, .02 },  
    { .47, .02, .47, .02, .02 },  
};
```

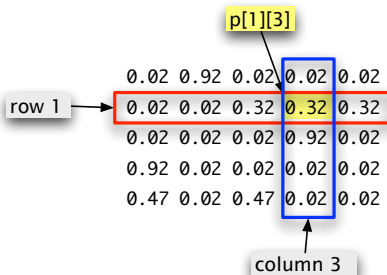




## Setting 2D Array Values at Compile Time

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double[][] p = {  
    { .02, .92, .02, .02, .02 },  
    { .02, .02, .32, .32, .32 },  
    { .02, .02, .02, .92, .02 },  
    { .92, .02, .02, .02, .02 },  
    { .47, .02, .47, .02, .02 },  
};
```



# Matrix Addition

Matrix Addition: given two  $n$ -by- $n$  matrices  $a$  and  $b$ , define  $c$  to be the  $n$ -by- $n$  matrix where  $c[i][j]$  is the sum  $a[i][j] + b[i][j]$ .

```
double[][] c = new double[n][n];
for (int i = 0; i < n; i++) {
    for (int j = 0; j < n; j++) {
        c[i][j] = a[i][j] + b[i][j];
    }
}
```

$a[i][j]$

.70	.20	.10
.30	.60	<b>.10</b>
.50	.10	.40

$b[i][j]$

.80	.30	.50
.10	.40	<b>.10</b>
.10	.30	.40

$c[i][j]$

1.5	.50	.60
.40	1.0	<b>.20</b>
.60	.40	.80

# Matrix Multiplication

Matrix Multiplication: given two  $n$ -by- $n$  matrices **a** and **b**, define **c** to be the  $n$ -by- $n$  matrix where **c**[**i**][**j**] is the dot product of the  $i^{th}$  row of **a**[] [] and the  $j^{th}$  column of **b**[] [].

```
double[] [] c = new double[n][n];
for (int i = 0; i < n; i++) {
    for (int j = 0; j < n; j++) {
        for (int k = 0; k < n; k++) {
            c[i][j] += a[i][k] * b[k][j];
        }
    }
}
```

a[] []

.70	.20	.10
.30	.60	.10
.50	.10	.40

← row 1

b[] []

column 2

.80	.30	.50
.10	.40	.10
.10	.30	.40

c[] []

.59	.32	.41
.31	.36	.25
.45	.31	.42

c[1][2] =

$$.30 \times .50 + .60 \times .10 + .10 \times .40 = .25$$

## Enhanced for loop, 1

Ordinary for loops are easy to get wrong! Often there's a better way:

```
int[] numbers = {2, 5, 6, 1, 0, 5};
```

### Ordinary for loop

```
for (int i = 0; i < numbers.length; i++) {  
    System.out.println(numbers[i]);  
}
```

### Enhanced for loop

```
for (int num : numbers)  
    System.out.println(num);  
}
```

## Enhanced for loop, 2

- ▶ Also called *for-each* loop, with `:` pronounced “in”.
- ▶ On each iteration, an element of the iterable gets assigned to the loop variable.
- ▶ Loop gets executed once for each element in the iterable.
- ▶ Easier and more concise: no need to initialise loop counter, increment, set termination condition...
- ▶ ... but less flexible; no access to the loop counter.
- ▶ Use them whenever you don't need access to the loop counter.
- ▶ Typical use: when you need access to all the elements of an array, but you don't care about their indexes.

General form:

```
for ( variable declaration : iterable ){  
    ...  
}
```

NB the variable must have same type as elements in *iterable*.

# Enhanced for loop, 3

## Another Example: Right

```
String[] words = {"hello", "world", "yes", "we", "can"};
for (String w : words) {
    System.out.println(w);
}
```

## Another Example: Wrong

```
String[] words = {"hello", "world", "yes", "we", "can" };
for (int w : words) {
    System.out.println(w);
}
```

# Summary

## Arrays:

- ▶ Method of storing large amounts of data.
- ▶ Almost as easy to use as primitive types.
- ▶ We can directly access an element given its index.

## Local Constants:

- ▶ specify constants using the `final` keyword to improve maintainability and readability

## Enhanced for loop:

- ▶ Good alternative to ordinary for loop where you just want to iterate over an array, and don't care about the indexes.

# Reading

## Java Tutorial

pp51-57

i.e. now it's time to read carefully the section on Arrays within Chapter 3, *Language Basics*, that I suggested skimming over before.