

7) analyze the circuit in

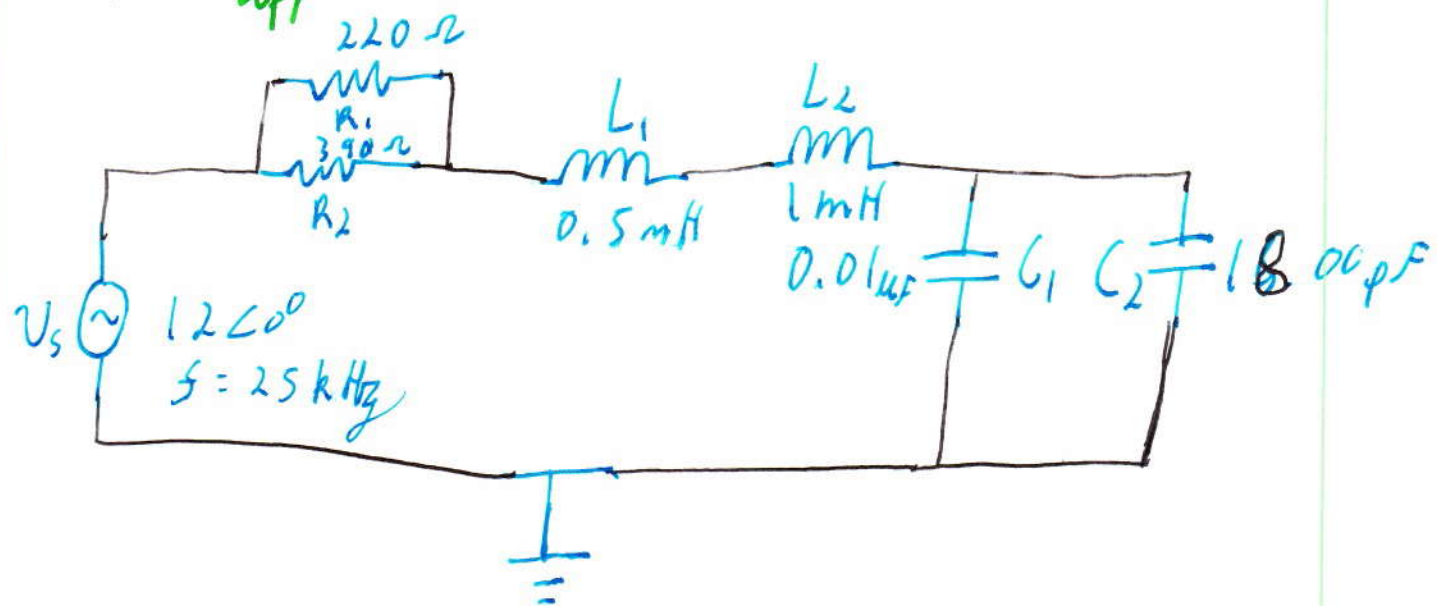
Figure 17-67 for:

a) I_{total}

b) P_{true}

c) P_{reactive}

d) P_{apparent}



$$\frac{R_1 \times R_2}{R_1 + R_2} = R_{1||2} = \frac{220 \times 390}{220 + 390}$$

$$R_{1||2} = 140.655 \Omega$$

$$L_1 + L_2 = 0.5 \text{ mH} + 1 \text{ mH} = 1.5 \text{ mH} = L_{\text{total}}$$

$$X_L = 2\pi L f$$

$$X_L = 2\pi (1.5 \times 10^{-3}) (25 \times 10^3)$$

$$X_L = 235.619 j$$

$$C_1 + C_2 = 0.01 \mu\text{F} + 1800 \text{ pF}$$

$$C_{\text{total}} = 10 \text{ nF} + 1.8 \text{ nF}$$

$$C_{\text{total}} = 11.8 \text{ nF}$$

$$X_C = \frac{-j}{2\pi f C} = \frac{1}{2\pi (25 \times 10^3) (11.8 \times 10^{-9})}$$

$$X_C = -539.51 j$$

$$R_{1112} + X_C + X_L = Z_{total}$$

$$140.655 \Omega + 235.619j - 534.51j$$

$$Z_{total} = 334.863 \angle -65.163^\circ$$

$$\frac{V}{Z} = i_{total}$$

$$\frac{12 \angle 0}{334.863 \angle -65.163^\circ} = \frac{12}{3.583}$$

$$35.836 \times 10^{-3} \angle 65.163^\circ$$

$$i_{total} = 35.836 \angle 65.163^\circ \text{ mA}$$

d)

$$P_{\text{apparent}} = VI$$

$$12 \times 35.836 \angle 65.163^\circ \text{ mA}$$

$$P_{\text{apparent}} = 0.430 \angle 65.163^\circ \text{ VA}$$

$$0.1806 + j0.3902$$

Real

~~Real~~

Real

Reactive

Reactive

$$WP_{\text{real}} = 0.1806 \text{ watts}$$

$$Q_{\text{reactive}} = 0.3902 \text{ Var}$$

11) A certain Series Resonant circuit has a maximum current of 50 mA and V_L of 100 V.

The applied voltage is 10 V.

What is Z ? What are X_L and X_C

known information

Series Resonance circuit $f_H = \frac{1}{2\pi\sqrt{LC}}$

$$I_{\max} = 50 \text{ mA}$$

$$V_L = 100 \text{ V}$$

$$V_S = 10 \text{ V}$$

Objective

Z

X_L

X_C

$$V = iR$$

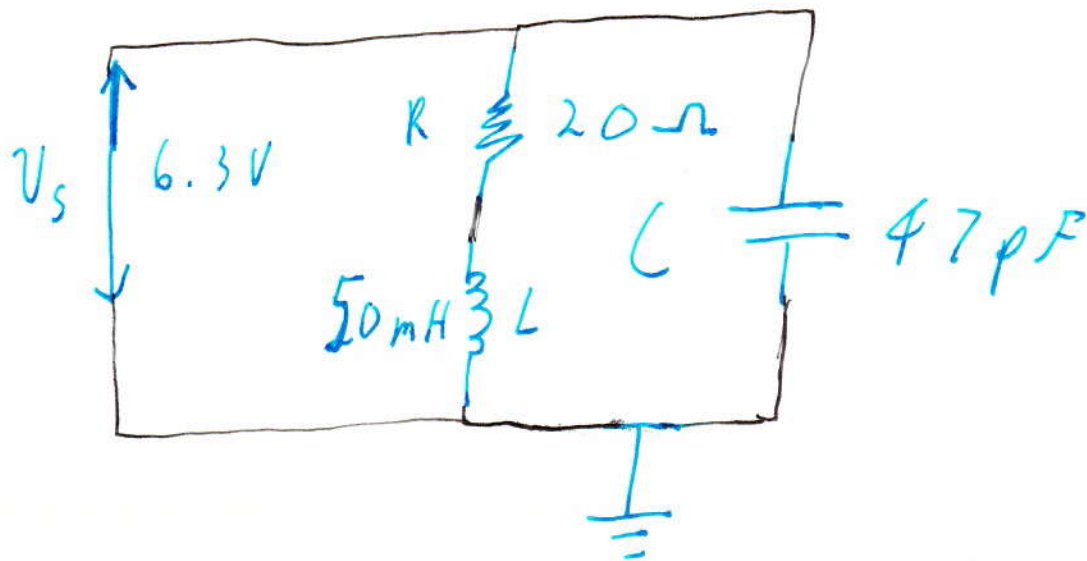
$$\frac{V}{i} = R$$

$$\frac{1\Omega}{5\text{ mA}} =$$

$$\frac{1}{5 \times 10^{-3}} = \boxed{200 = R = Z}$$

$$\boxed{X_L \text{ and } X_C = 0}$$

23) Find Z at resonance and f_r for the tank circuit in Figure 17-71.



$$X_L = 2\pi f L \quad Z_R = R_w (Q^2 + 1)$$

$$X_C = \frac{-j}{2\pi f C}$$

$$f_r = \frac{\sqrt{1 - (R_w^2 C)}}{L}$$

$$Q = \frac{X_L}{R_w}$$

$$2\pi \sqrt{LC}$$

$$f_{\text{resonance}} = \sqrt{\frac{1 - (20^2) \times 47 \times 10^{-12}}{50 \times 10^{-3}}}$$

$$2\pi \sqrt{(50 \times 10^{-3}) \times (47 \times 10^{-12})}$$

$$f_{\text{resonance}} = 1.0382 \times 10^5 \text{ Hz}$$

$$X_L = 2\pi f L \quad X_C = \frac{-j}{2\pi f C}$$

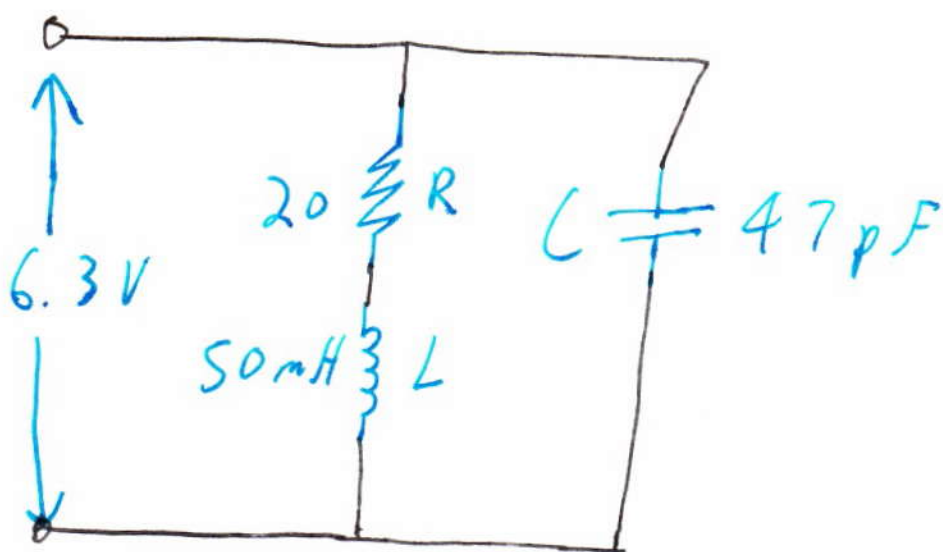
$$Z_H = R_w (Q^2 + 1) \quad Q = \frac{X_L}{R_w}$$

$$Z_r = 20 \left(\frac{50 \times 10^{-3}}{20} \right)^2 + 1$$

$$Z_r = 1.0001 \Omega$$

24) How much current is drawn from the source in Figure 17-71 at Resonance?

What are the inductive current and capacitive current at the Resonant frequency?



Information from 23)

$$f_{\text{resonance}} = 1.0382 \times 10^5 \text{ Hz}$$

$$Z_r = 1.0001 \Omega$$

equations

$$X_L = 2\pi fL$$

$$X_C = 2\pi fC$$

$$I_{\text{branch}} = \frac{Z_{\text{total}}}{Z_{\text{branch}}} I_{\text{source}}$$

$$X_L = 2\pi fL$$

$$X_L = 2\pi (1.0382 \times 10^5) (50 \times 10^{-3})$$

$$X_L = 32.616 \times 10^3$$

$$X_C = \frac{1}{2\pi fC}$$

$$X_C = \frac{1}{2\pi (1.0382 \times 10^5) (47 \times 10^{-12})}$$

$$X_C = 32.617 \times 10^3$$

$$Z_{L \text{ line}} = 20 + 32.616j \times 10^3$$

$$Z_{C \text{ line}} = -32.617 \times 10^3 j$$

$$\frac{Z_L Z_C}{Z_L + Z_C} = \frac{(32.616j \times 10^3 \Omega)(-32.616 \times 10^3 j)}{20 + 0.001j}$$

$$Z_{total} = 5.319 \times 10^7 \angle 0.00286^\circ$$

$$\frac{V}{Z} = i$$

$$\frac{6.3}{5.319 \times 10^7 \angle 0.00286^\circ} = 11.844 \times 10^{-6} \angle -2.864^\circ$$

$$\angle 0.00286^\circ$$

$$i_{total} = 11.844 \mu A$$

phase is negligible

$$\frac{5.319 \times 10^7}{20 + 32 + j16} \quad 11.844 \times 10^{-6} = i_{L \text{ branch}}$$

$$i_{L \text{ branch}} = 1.630 \text{ mA} \angle -89.965^\circ$$

$$\frac{5.319 \times 10^7}{-32 + j16} = i_{C \text{ branch}}$$

$$i_{C \text{ branch}} = 1.5308 \angle 90^\circ \text{ mA}$$

25) Find P_{true} , P_{reactive} and P_{apparent} in the circuit of Figure 17-71 at Resonance.

$$i_{\text{total}} = 11.844 \times 10^{-6} \angle 0.00286^\circ$$

$$V = 6.3 \text{ V}$$

$$P_{\text{apparent}} = V i$$

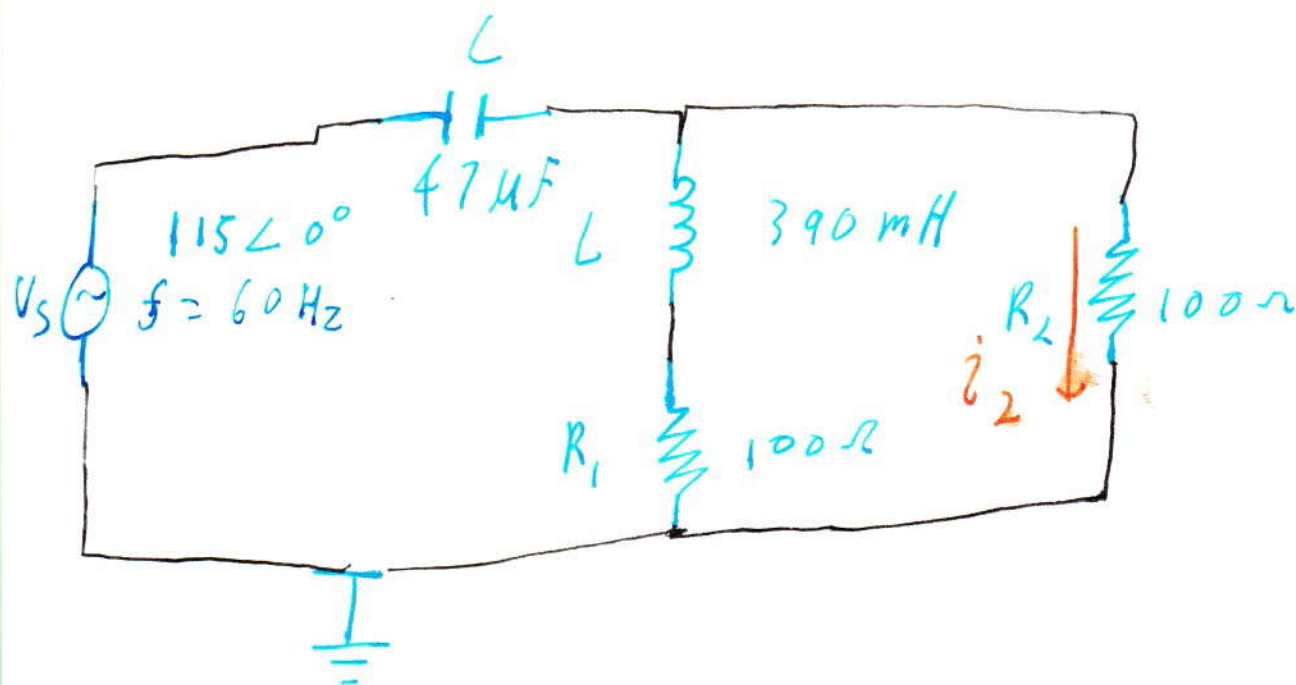
$$P_{\text{apparent}} = 6.3 \times 11.844 \times 10^{-6} \angle 0.00286^\circ$$

$$P_{\text{apparent}} = 0.746 \times 10^{-6} \angle 2.86 \times 10^{-3} \text{ VA}$$

$$P_{\text{real}} = 0.746 \times 10^{-6} \text{ watt}$$

$$P_{\text{reactive}} = 3.7246 \times 10^9 \text{ Var}$$

31) In Figure 17-74, What is the phase angle between i_2 and the source voltage?



$$X_L = 2\pi f L$$

$$X_C = \frac{1}{2\pi f C}$$

$$\frac{Z_{\text{total}}}{Z_{\text{target}}} i_s = i_{\text{target}}$$

$$X_L = 2\pi(60)(390 \times 10^{-3})$$

$$X_L = 147.026j$$

$$X_C = \frac{-j}{2\pi(60)(47 \times 10^{-6})}$$

$$X_C = -56.437j$$

$$Z_{L \text{ line}} = 100 + 147.026j$$

$$Z_{||} = \frac{Z_{L \text{ line}} R_2}{Z_{L \text{ line}} + R_2} = \frac{200 + 147.026j}{200 + 147.026j}$$

$$Z_{||} = 67.541 + 23.861j$$

$$Z_{\text{total}} = Z_{||} + X_C$$

$$Z_{total} = 74.986 \angle -25.748^\circ$$

$$\frac{V}{Z} = i_{total}$$

$$\frac{115}{74.986 \angle -25.748^\circ} = 1.533 \angle 25.748^\circ$$

$$\frac{Z_{total}}{R_2} i_{total} = i_{R_2}$$

$$\frac{74.986 \angle -25.748^\circ}{100} (1.533 \angle 25.748^\circ) =$$

$$i_{R_2} = 1.149 \text{ A}$$

$$\angle i_{R_2} - \angle V_S = 0^\circ$$