



$$-5 + 470i_1 + 2000(i_1 - i_2) + 510i_1 = 0$$

$$+15 + 1000i_2 + 2000(i_2 - i_1) + 620i_2 = 0$$

$$\text{eq}_1 \quad -5 + 470i_1 + 2000i_1 - 2000i_2 + 510i_1 = 0$$

$$-5 + 2980i_1 - 2000i_2 = 0$$

$$2980i_1 - 2000i_2 = 5$$

$$\text{eq}_2 \quad 1000i_2 + 2000i_2 - 2000i_1 + 620i_2 = -15$$

$$-2000i_1 + 3620i_2 = -15$$

Simplified equations

$$\begin{aligned} 2980 i_1 - 2000 i_2 &= 5 \\ -2000 i_1 + 3600 i_2 &= -15 \end{aligned}$$

Δ matrix

$$\begin{bmatrix} 2980 & -2000 \\ -2000 & +3600 \end{bmatrix}$$

$$2980 \times 3600 - (-2000 \times -2000)$$

$$(10.728 \times 10^6) - (4 \times 10^6)$$

$$\Delta = 6.278 \times 10^6$$

i_1 matrix

$$\begin{bmatrix} 5 & -2000 \\ -15 & 3600 \end{bmatrix}$$

$$(5 \times 3600) - (-2000 \times -15)$$

$$(1.8 \times 10^4) - (3.0 \times 10^4)$$

$$-1.2 \times 10^4$$

$$\Delta i_1 = -12000$$

i_2 matrix

$$\begin{bmatrix} 2980 & 5 \\ -2000 & -15 \end{bmatrix}$$

$$(-15 \times 2980) - (5 \times 2000)$$

$$(-44.7 \times 10^3) - (-10^4) = \Delta i_2 - 34700$$

Δ results

$$\Delta = 6.278 \times 10^6$$

$$\Delta i_1 = -12000$$

$$\Delta i_2 = -34700$$

$$i_1 = \frac{-1.2 \times 10^4}{6.278 \times 10^6} = \frac{1.2}{6.278 \times 10^2}$$

$$i_1 = -1.911 \text{ mA}$$

$$i_2 = \frac{-3.47 \times 10^4}{6.278 \times 10^6} = \frac{3.47}{6.278 \times 10^2}$$

$$i_2 = -5.527 \text{ mA}$$

$$i_{R_2} = i_1 - i_2$$

$$i_{R_2} = -1.911 \text{ mA} + 5.527 \text{ mA}$$

$$i_{R_2} = 3.616 \text{ mA}$$

Voltage calculations

$$V = i R$$

$$V_{R_1} = i_1 R_1$$

$$V_{R_1} = (-1.911 \times 10^{-3})(470)$$

$$V_{R_1} = -0.898 \text{ V}$$

$$V_{R_2} = 3.616 \times 10^{-3} \times 2 \times 10^3$$

$$V_{R_2} = 7.232 \text{ V}$$

$$V_{R_3} = -5.527 \times 10^{-3} \times 620$$

$$V_{R_3} = -3.426 \text{ V}$$

Currents

$$i_1 = -1.911 \text{ mA}$$

$$i_2 = -5.527 \text{ mA}$$

$$i_{R_2} = 3.616 \text{ mA}$$

$$V_{R4} = -5.527 \times \cancel{10^{-3}} \times \cancel{10^3}$$

$$V_{R4} = -5.527 \text{ V}$$

$$V_{R5} = -1.911 \times 10^{-3} \times 510$$

$$V_{R5} = -0.974 \text{ V}$$