MP 5 Quadtrees

Extra credit: Friday, March 18 at 11:59 PM

Due: Friday, April 1 at 11:59 PM

Goals and Overview

In this MP, you will gain experience in implementing unfamiliar data structures, and in writing simple recursive functions.



A Solo MP

- You are not allowed to work with a partner on this MP. You must do this MP SOLO (alone).
- This is a long MP. It will probably take you a long time to understand the concept presented in the writeup and figure out exactly what we're asking you to do. It will almost definitely take you a long time to debug your program, even after you get it to compile. Please start early, for your own sake.

Checking Out the Code

To check out the provided code for MP5 from the class repository, just run

svn up

from your cs225 directory.

For the list of functions used in this MP, check out the <u>Doxygen for MP5</u>.

Background Information: Quadtrees

Let us create a tree in the following manner. First, let us require that each node of our tree correspond to some particular region of the plane. Second, we require that the regions corresponding to the children of a node n form a partition of the region corresponding to n (i.e. no two children's regions have overlapping interiors, although overlapping boundaries are allowed), and all the children's regions put together cover the region corresponding to n exactly). Notice that given this property, for a tree T, the regions corresponding to the leaves of T form a partition of the region corresponding to the root of T (you can prove this using induction).

Now, let us construct a special tree T of the above type, as follows. First, every node of Tcorresponds to a square on the plane. Second, given n is a node of T (with corresponding square region s on the plane), n may have either zero or four children; if n has four children, then the regions corresponding to these four children are the four squares obtained by splitting s vertically and horizontally. We refer to these "subsquares" of s by their cardinal directions - NW (north west), NE (north east), SW (south west), and SE (south east). A tree built in this way, by selecting a single square region to corresponding to the root of T and then creating descendants according to the procedure above, is called a quadtree. See Figure 1.

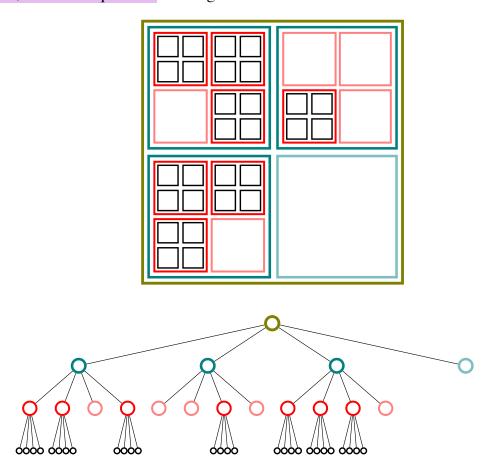


Figure 1. Quadtree, with pointers ordered NW, NE, SW, SE.

Notice that the node at the green level of the tree corresponds to the cell of a 1x1 grid over the root square; the nodes at the teal level of the tree correspond to cells of a 2x2 grid over the root square; the nodes at the red level of the tree correspond to cells of a 4x4 grid over the root square; the nodes at the black level of the tree correspond to cells of an 8x8 grid over the root square; and so on.

In Figure 1, the 34 leaves of the tree correspond to the 34 unequal squares into which the root square is split by the diagram.

Background Information: The Quadtree class

A bitmap image is composed of many identically-sized square pixels arranged in a grid. If the number of pixels is 2^k by 2^k for some k, then one can build a quadtree with its root corresponding to the entire image, and with each leaf corresponding to a pixel. This provides us with an interesting way to store an image: put an RGBApixel into each leaf of an appropriate quadtree.

For this MP, you will write a Quadtree class. In order to facilitate testing of your MPs, we have already partially implemented this class for you. In particular, we have declared a class QuadtreeNode, which represents a single node of a quadtree. The static data stored in a QuadtreeNode object are one RGBApixel (the "element"), and four QuadtreeNode* variables:

nwChild, neChild, swChild, and seChild. These pointers provide links from each node object to child node objects. As this scheme suggests, every QuadtreeNode of a Quadtree object is allocated in dynamic memory, and must be managed properly to avoid memory leaks. Additionally, we have specified in the given file quadtree.h that each Quadtree object should contain a pointer to a QuadtreeNode, named root; this pointer will point to the root node of the Quadtree.

We have also provided a couple of member functions for you, printTree() and operator==(). These functions do just what you might expect; the former prints out the contents of the leaves of the quadtree, using a preorder traversal, while the latter compares two Quadtree objects to see if they are "equivalent". Unfortunately, you will probably not find these functions too useful in implementing the remainder of the MP. However, you may find them useful for debugging.

You may implement the Quadtree class however you wish, with the following restrictions: you must not remove or alter the given functions, and you must use the already-declared member variables in the intended manner. That is, root should always point to the root of the quadtree, and within each QuadtreeNode object, the pointers nwChild, neChild, swChild, and seChild should point to the appropriate child nodes. In short, you may do whatever you like, as long as you do not break printTree() or operator==(); these functions are vital for grading.

Implementation Advice

Here are some suggestions to guide your implementation. These are just suggestions; you are not obligated to adhere to them.

- Your Quadtree objects will probably need some way of remembering the resolution of their underlying bitmaps.
- Remember the technique shown in class and lab for implementing recursive tree functions. In particular, you will often want to have a public version of some method, which conforms to the interface specifications above, along with a private version of the same method, which takes in additional arguments (such as a pointer to a QuadtreeNode, for example).
- You may find it useful to create private helper methods. In general, whenever you find that you are performing the same task in multiple places, you should consider encapsulating that task into a helper method. This can save a bit of time in the coding process, and a lot of time in the debugging process.
- You may want to ensure that, at all times, the element field of each interior (i.e. non-leaf) node of your quadtree stores the average of its children's element fields. (See the description for prune.) It is much easier to calculate all of this information once, when the tree is first constructed, than to calculate it "on demand" whenever it is needed.

In addition, be mindful of the following:

- You will be responsible for testing your code before handing it in. Using our main.cpp and test images to check your program, while not required, is strongly recommended. You are also strongly encouraged to perform further tests; in particular, you are encouraged to modify the given main.cpp file as you please, or to create a new main.cpp file, to further test your program.
- The Quadtree class implementation uses dynamic memory allocation; be sure to avoid

- memory leaks in your program. Memory leaks will adversely affect your grade.
- With the exception of printTree(), your functions should print nothing to the screen when they run correctly. You are welcome to use a debugger, or another method, to track and examine the execution of your functions during the development process. Just be sure that if your final submission functions execute without errors, they print nothing; this is to ensure your program will match the solution output during grading.

Implementation Requirements

These are strict requirements that apply to **both** parts of the MP. Failure to follow these requirements may result in a failing grade on the MP.

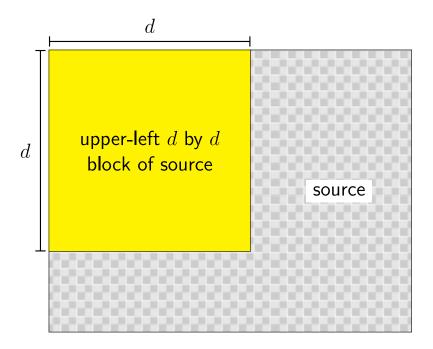
- Your functions may be graded for their big-Oh efficiency.
- You are required to comment the MP as per the commenting standard described by the <u>Coding Style Policy</u>.
- You must name all files, public functions, public member variables (if any exist), and executables **exactly** as we specify in this document.
- Your code must produce the **exact** output that we specify: nothing more, nothing less. Output includes standard and error output and files (such as images).
- Your code must compile on the EWS machines using **clang++**. Being able to compile on a different machine is **not** sufficient.
- Your code must be submitted correctly by the **due date and time**. Late work is not accepted.
- Your code must not have any memory errors or leaks for full credit. ASAN tests will be performed separately from the functionality tests.
- Your public function signatures must match ours **exactly** for full credit. If using different signatures prevents compilation, you will receive a zero. Tests for **const**-correctness may be performed separately from the other tests (if applicable).

MP 5.1: Quadtree Basics

For the first part of MP 5, you will implement the constructors, the Big Three, buildTree, getPixel, and decompress functions of the Quadtree class.

The buildTree Function

This function takes two arguments, a PNG object source, and an integer d, in that order. It returns nothing. It should delete the current contents of the Quadtree object, then turn it into a Quadtree object representing the upper-left d by d block of source. You may assume that d is a power of two, and that the width and height of source are each at least d.



See the Doxygen for the <u>buildTree</u> function.

Quadtree Constructors

You will write two constructors for the Quadtree class:

- The first takes no arguments, and produces an empty Quadtree object, i.e., one which has no associated QuadtreeNode objects, and in which root is NULL.
- The second takes two arguments: a PNG object source, and an integer d, in that order. Its purpose is to build a Quadtree representing the upper-left d by d block of the source image. This effectively crops the source image into a $d \times d$ square.

You may assume that d is a power of two, and that the width and height of source are each at least d. Perhaps, to implement this, you could leverage the functionality of another function you have written in 5.1...

See the Doxygen for the <u>no argument constructor</u> and the <u>two argument constructor</u>.

The Big Three

You will also write the Big Three (copy constructor, destructor, assignment operator) for the Ouadtree class.

See the Doxygen for the <u>copy constructor</u>, <u>destructor</u>, and <u>operator=</u>.

The getPixel Function

This function takes two arguments, x and y, in that order, both nonnegative integers. It returns the RGBApixel corresponding to the pixel at coordinates (x, y) in the image which the Quadtree represents. Note that the Quadtree may not contain a node specifically corresponding to this pixel

(due, for instance, to pruning — see below). In this case, getPixel will retrieve the pixel (i.e. the color) of the square region within which the smaller query grid cell would lie. (That is, it will return the element of the nonexistent leaf's deepest surviving ancestor.) If the supplied coordinates fall outside of the bounds of the underlying bitmap, or if the current Quadtree is empty (i.e., it was created by the default constructor) then the returned RGBApixel should be the one which is created by the default RGBApixel constructor.

See the Doxygen for the **getPixel** function.

The decompress Function

This function takes no arguments, and returns a PNG object. The return value should be the underlying PNG object represented by the Quadtree. If the current Quadtree is empty (i.e., it was created by the default constructor) then the returned PNG should be the one which is created by the default PNG constructor.

This function effectively "decompresses" the quadtree. A Quadtree object, in memory, may take up less space than the underlying bitmap image, but we cannot simply look at the Quadtree and tell what image it represents. By converting the Quadtree back into a PNG image, we lose the compression, but gain the ability to view the image directly.

See the Doxygen for the <u>decompress</u> function.

Extra Credit Submission

For extra credit, you can submit the code you have implemented and tested for part one of MP 5. You must submit your work before the extra credit deadline as listed at the top of this page.



A Warning

Although we will only be testing the functions listed above, your code must be able to compile. That is, you need to <u>stub out</u> or implement the functions listed in MP 5.2.

MP 5.2: Quadtree Manipulations

For the second part of MP 5, you will implement four more functions in the Quadtree class: clockwiseRotate, prune, pruneSize, and idealPrune.

The clockwiseRotate() Function

Please see the Doxygen for <u>clockwiseRotate</u>.

This function takes no arguments, and returns nothing. clockwiseRotate rotates the Quadtree object's underlying image clockwise by 90 degrees. (Note that this should be done using pointer manipulation, not by attempting to swap the element fields of QuadtreeNodes. Trust us; it's easier this way.)

The prune Function

See the Doxygen for prune.

This function takes a single argument, an integer tolerance. It returns nothing.

If the color values of the leaves of a subquadtree don't vary by much, we might as well represent the entire subtree by, say, the average color value of those leaves. We may use this information to effectively "compress" the image, by strategically trimming the Quadtree.

Consider a node n and the subtree, T_n rooted at n, and let a denote the component-wise average color value of all the leaves of T_n . Component-wise average means that every internal node in the tree calculates its value by averaging its immediate children. This implies that the average must be calculated in a "bottom-up" manner. (Due to rounding errors, using the component-wise average is not equivalent to using the true average of all leaves in a subtree.) If a node n is pruned, the children of n and the subtrees for which they are the roots are removed from the Quadtree. Node n is pruned if the color value of no leaf in T_n , differs from a by more than tolerance. (Note: for all average calculations, just truncate the value to integer.)

We define the "difference" between two colors (r_1, g_1, b_1) and (r_2, g_2, b_2) to be:

$$(r_2 - r_1)^2 + (g_2 - g_1)^2 + (b_2 - b_1)^2$$

To be more complete, if the tolerance condition is met at a node n, then the block of the underlying image which n represents contains only pixels which are "nearly" the same color. For each such node n, we remove from the Quadtree all four children of n, and their respective subtrees (an operation we call a pruning). This means that all of the leaves that were deleted, corresponding to pixels whose colors were similar, are now replaced by a single leaf with color equal to the average color a over that square region.

The prune function, given a tolerance value, prunes the Quadtree as extensively as possible. (Note, however, that we do not want the prune function to do an "iterative" prune. It is conceivable that by pruning some mid-level node n, an ancestor p of n then becomes prunable, due to the fact that the prune changed the leaves descended from p. Your prune function should evaluate the prunability of each node based on the presence of all nodes, and then delete the subtrees based at nodes deemed prunable.)

You should start pruning from the root of the Quadtree.

The pruneSize Function

See the Doxygen for pruneSize.

This function takes a single argument, an integer tolerance. It returns an integer. This function is similar to prune; however, it does not actually prune the Quadtree; rather, it returns a count of the total number of leaves the Quadtree would have if it were pruned as in the prune function.

The idealPrune Function

See the Doxygen for idealPrune.

This function takes a single argument, a positive integer numLeaves. It returns an integer. This function should calculate and return the minimum tolerance necessary to guarantee that upon pruning the tree as above, no more than numLeaves leaves remain in the Quadtree. Essentially, this function is an inverse of pruneSize; for any Quadtree object theTree, and for any positive integer tolerance, the following inequality should hold:

theTree.pruneSize(theTree.idealPrune(numLeaves)) <= numLeaves</pre>

Once you understand what this function is supposed to do, you will probably notice that there is an "obvious" implementation. This is probably not the implementation you want to use! There is a fast way to implement this function, and a slow way; you will need to find the fast way. (If you doubt that it makes a significant difference, the tests in the given main.cpp should convince you.)



The "obvious" implementation involves a sort of linear search over all possible tolerances. What if you tried a binary search instead?

Testing Your Code

We have provided you with a sample main.cpp file, and corresponding test images. However, to grade your program, we will use different main.cpp files that implement different tests. Consequently, you will not submit main.cpp. You are strongly encouraged to write your own main.cpp file to more thoroughly test your program.

You can compile your code with the following command:

make

You can run it with the following command:

./mp5

As usual, an ASAN version is also produced:

./mp5-asan

The output it produces can be compared with the expected (soln_mp5.out) and the images created can be compared with the solution images using a diff utility (e.g., diff and compare).

As usual, passing these tests does not ensure correctness. You should augment these tests with your own.

Handing In Your Code

To facilitate anonymous grading, do not include any personally-identifiable information (like your name, your UIN, or your NetID) in any of your source files. Instead, before you hand in this assignment, create a file called partners.txt that contains only the NetIDs of people in your collaboration group (if it exists), one per line. If you worked alone, include only your own NetID in this file. We will be automatically processing this information, so do not include anything else in the file. (If we must manually correct your submission, you may lose points.) As always, if you're working in a group, each group member must hand in the assignment. (Failure to cite collaborators violates our academic integrity policy; we will be aggressively pursuing such violators.)

To commit your changes to the repository type:

svn ci -m "mp5 submission"

Grading Information

The following files are used to grade MP5:

- quadtree.cpp
- quadtree.h
- partners.txt

All other files (including your main.cpp) will not be used for grading.

Further Study

One can think of many ways to define distances between colors. We defined the distance between two colors simply by the distance between the colors' corresponding points in the 3-dimensional space of the colors' RGB representations. However, this distance doesn't represent the human perception of the difference between colors especially well. A search on "CIE color" provides a starting point to learn more about color schemes that endeavor to better model actual human color perception. Using a better concept of intercolor distance could yield images that, when compressed with the pruning function in this MP, look more natural; or from another perspective, images that can be compressed more yet still look as natural.

Quadtrees have uses reaching far beyond storing of images. One can store a set of points within a quadtree, and then manipulate the structure in various ways. The k-d tree is a binary variant of the quadtree in which nodes correspond to rectangles (and child and parent regions again follow a certain set of rules). Quadtrees can be generalized to three-dimensional space, where they are called octrees.

Good luck!