W11. Advertising

December 16, 2018

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12/16/2018

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Data: "fruitazia.csv" file
market test for juice with 6 experimental conditions (2 advertising levels Œ 3 price levels), with
5 supermarkets per condition.

In [55]: data<-read.csv(file="fruitazia.csv")
    attach(data)
    AdSpend <- as.factor(data$AdSpend)
    Price <- as.factor(data$Price)
    data

The following objects are masked from data (pos = 3):
    AdSpend, AdSpend2, Price, Price4.9, Price5.9, Sales

The following objects are masked from data (pos = 4):
    AdSpend, AdSpend2, Price, Price4.9, Price5.9, Sales

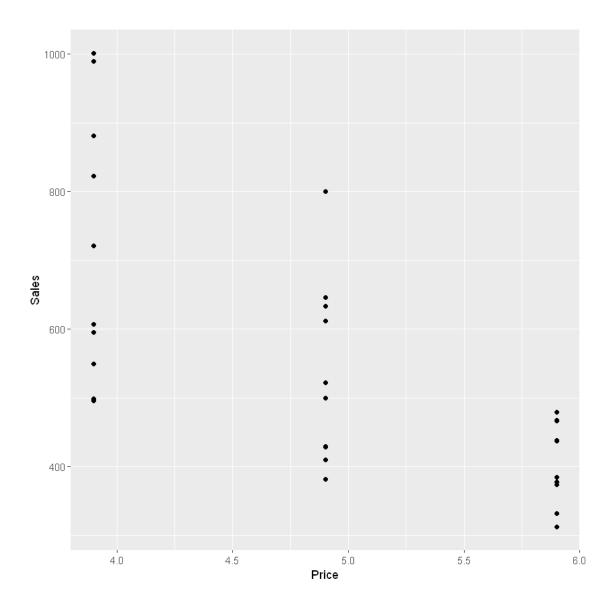
The following objects are masked from data (pos = 5):
```

AdSpend, AdSpend2, Price, Price4.9, Price5.9, Sales

Sales	Price	AdSpend	AdSpend2	Price4.9	Price5.9
499	3.9	1	0	0	0
595	3.9	1	0	0	0
496	3.9	1	0	0	0
607	3.9	1	0	0	0
550	3.9	1	0	0	0
989	3.9	2	1	0	0
721	3.9	2	1	0	0
823	3.9	2	1	0	0
1001	3.9	2	1	0	0
881	3.9	2	1	0	0
382	4.9	1	0	1	0
429	4.9	1	0	1	0
410	4.9	1	0	1	0
500	4.9	1	0	1	0
430	4.9	1	0	1	0
522	4.9	2	1	1	0
800	4.9	2	1	1	0
612	4.9	2	1	1	0
633	4.9	2	1	1	0
646	4.9	2	1	1	0
374	5.9	1	0	0	1
437	5.9	1	0	0	1
385	5.9	1	0	0	1
313	5.9	1	0	0	1
378	5.9	1	0	0	1
332	5.9	2	1	0	1
479	5.9	2	1	0	1
468	5.9	2	1	0	1
467	5.9	2	1	0	1
438	5.9	2	1	0	1

In [50]: aggregate(Sales~Price+AdSpend,data=data,FUN=mean)

Price	AdSpend	Sales
3.9	1	549.4
4.9	1	430.2
5.9	1	377.4
3.9	2	883.0
4.9	2	642.6
5.9	2	436.8



0.1.1 Regression Model: impact of advertising and price on sales

$$Sales = \beta_0 + \beta_1 * Adv_{2m} + \beta_2 * Price_{4.9} + \beta_3 * Price_{5.9} + e$$

In [64]: summary(lm(Sales~ + AdSpend2+Price4.9+Price5.9))

Call:

lm(formula = Sales ~ +AdSpend2 + Price4.9 + Price5.9)

Residuals:

Min 1Q Median 3Q Max -176.00 -50.38 -7.40 64.35 183.90

```
Coefficients:
```

```
Estimate Std. Error t value Pr(>|t|)

(Intercept) 615.30 34.39 17.893 3.89e-16 ***

AdSpend2 201.80 34.39 5.868 3.46e-06 ***

Price4.9 -179.80 42.12 -4.269 0.000231 ***

Price5.9 -309.10 42.12 -7.339 8.56e-08 ***

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Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Residual standard error: 94.17 on 26 degrees of freedom Multiple R-squared: 0.7735, Adjusted R-squared: 0.7474 F-statistic: 29.59 on 3 and 26 DF, p-value: 1.537e-08

Significant relationship between two covariates (price and advertising) and sales volumn. 77% of the variability of sales is explained by variability of price and advertising.

0.1.2 Regression Model with interaction terms: impact of increased advertising on sales at different price levels

$$Sales = \beta_0 + \beta_1 * Adv_{2m} + \beta_2 * Price_{4.9} + \beta_3 * Price_{5.9} + \beta_4 * Price_{4.9} * Adv_{2m} + \beta_5 * Price_{5.9} * Adv_{2m} + e$$

In [67]: summary(lm(Sales~AdSpend2+Price4.9+Price5.9+Price4.9*AdSpend2+Price5.9*AdSpend2))

Call:

```
lm(formula = Sales ~ AdSpend2 + Price4.9 + Price5.9 + Price4.9 *
AdSpend2 + Price5.9 * AdSpend2)
```

Residuals:

Min	1Q	Median	3Q	Max
-162.00	-43.80	0.20	39.45	157.40

Coefficients:

	${\tt Estimate \ Std.}$	Error	t value	Pr(> t)	
(Intercept)	549.40	33.69	16.309	1.73e-14	***
AdSpend2	333.60	47.64	7.002	3.06e-07	***
Price4.9	-119.20	47.64	-2.502	0.019565	*
Price5.9	-172.00	47.64	-3.610	0.001401	**
AdSpend2:Price4.9	-121.20	67.37	-1.799	0.084625	
AdSpend2:Price5.9	-274.20	67.37	-4.070	0.000442	***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 75.33 on 24 degrees of freedom Multiple R-squared: 0.8662, Adjusted R-squared: 0.8384

F-statistic: 31.08 on 5 and 24 DF, $\,$ p-value: 9.777e-10 $\,$

Effect of increased ad spend at \$3.9: +333.6

Effect of increased ad spend at \$4.9: +333.6 - 121.2 Effect of increased ad spend at \$4.9: +333.6 - 274.2

Advertising works much better at low price for this product.