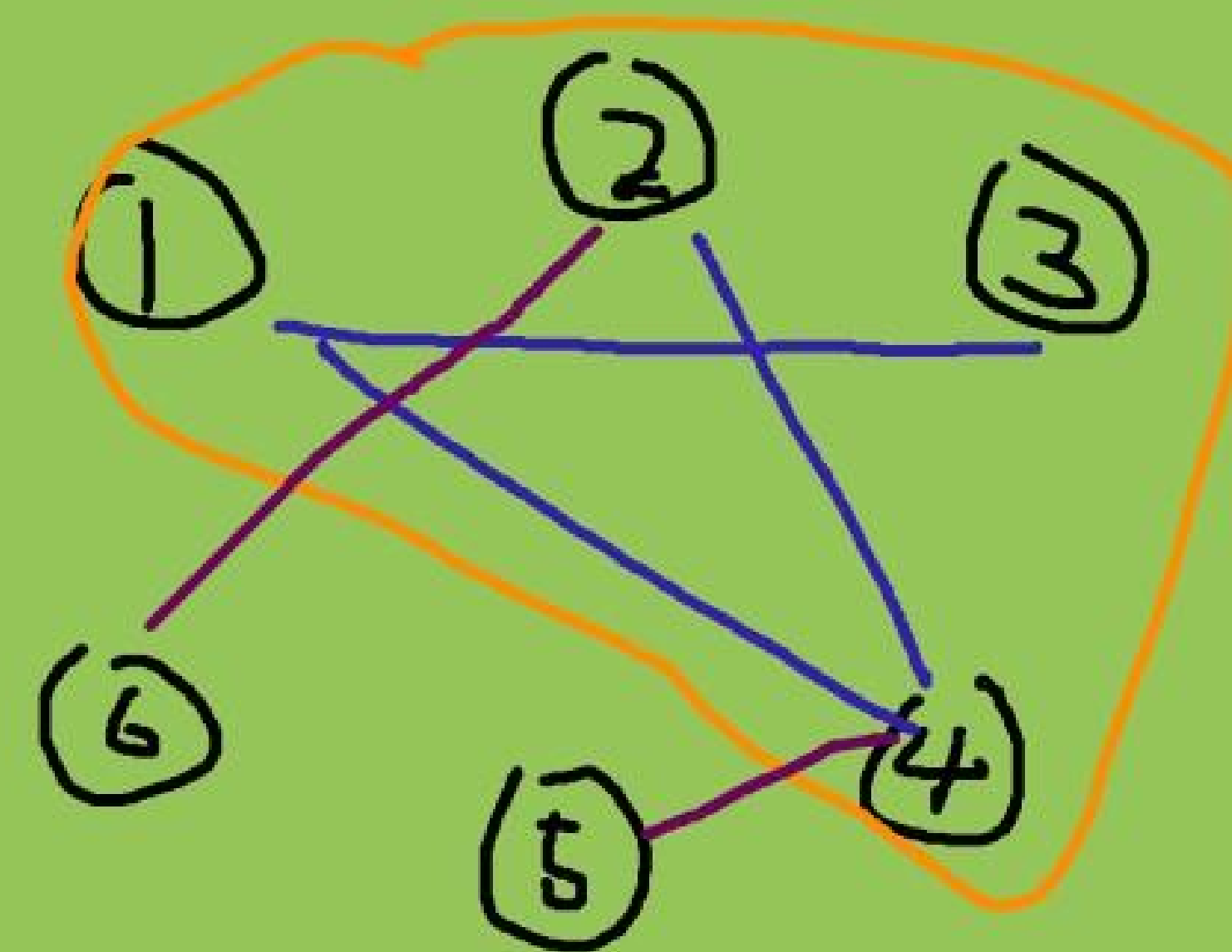
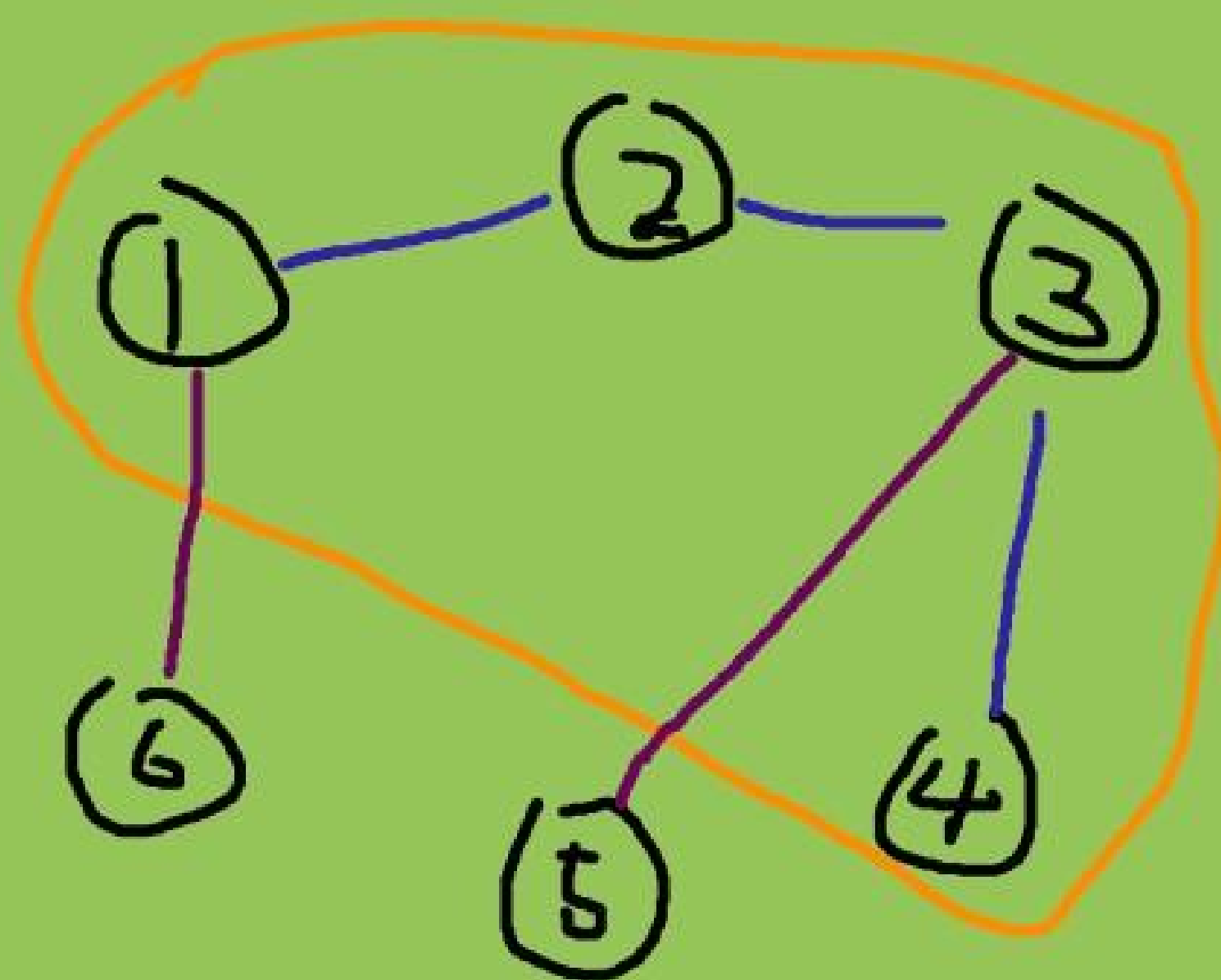
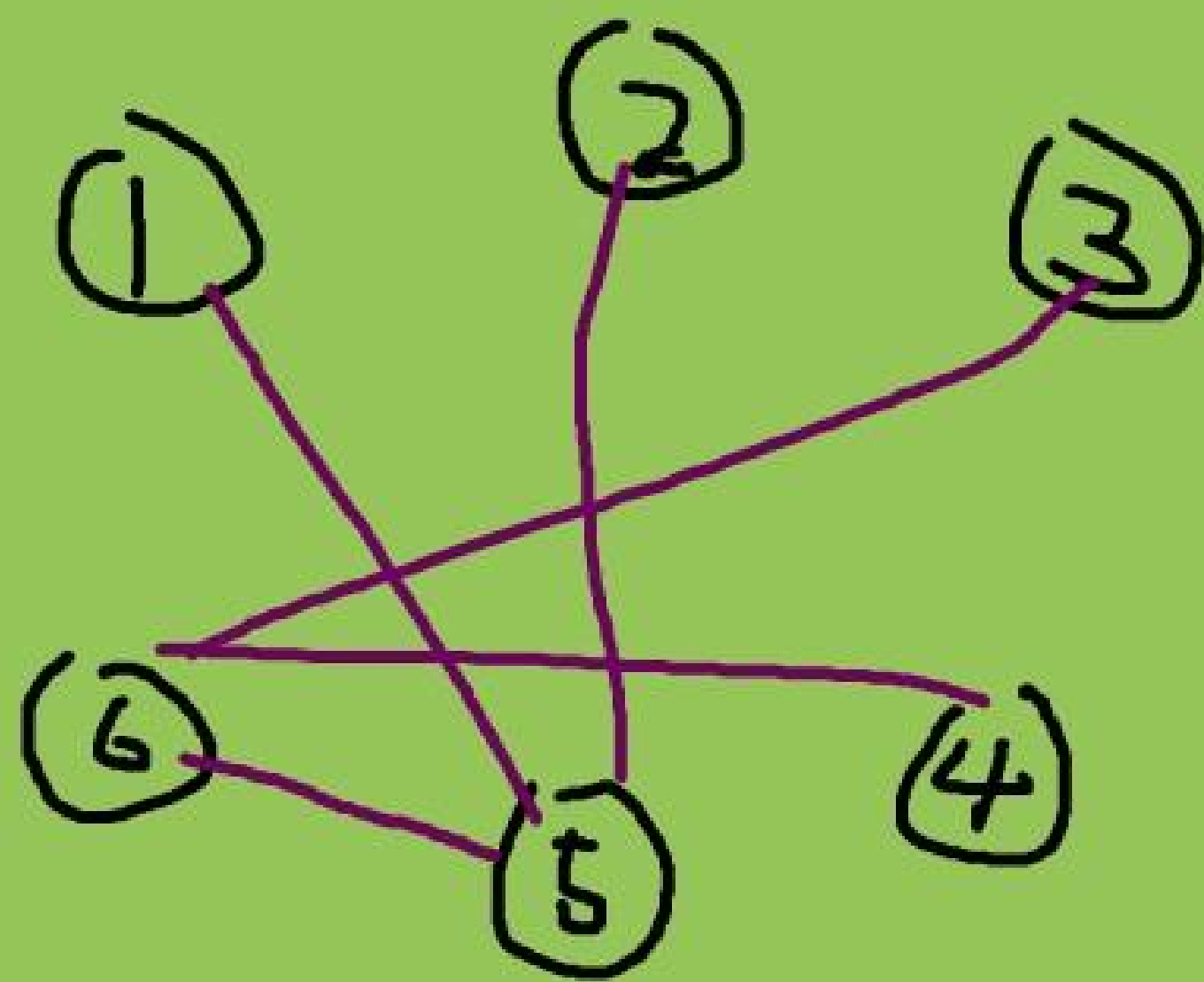
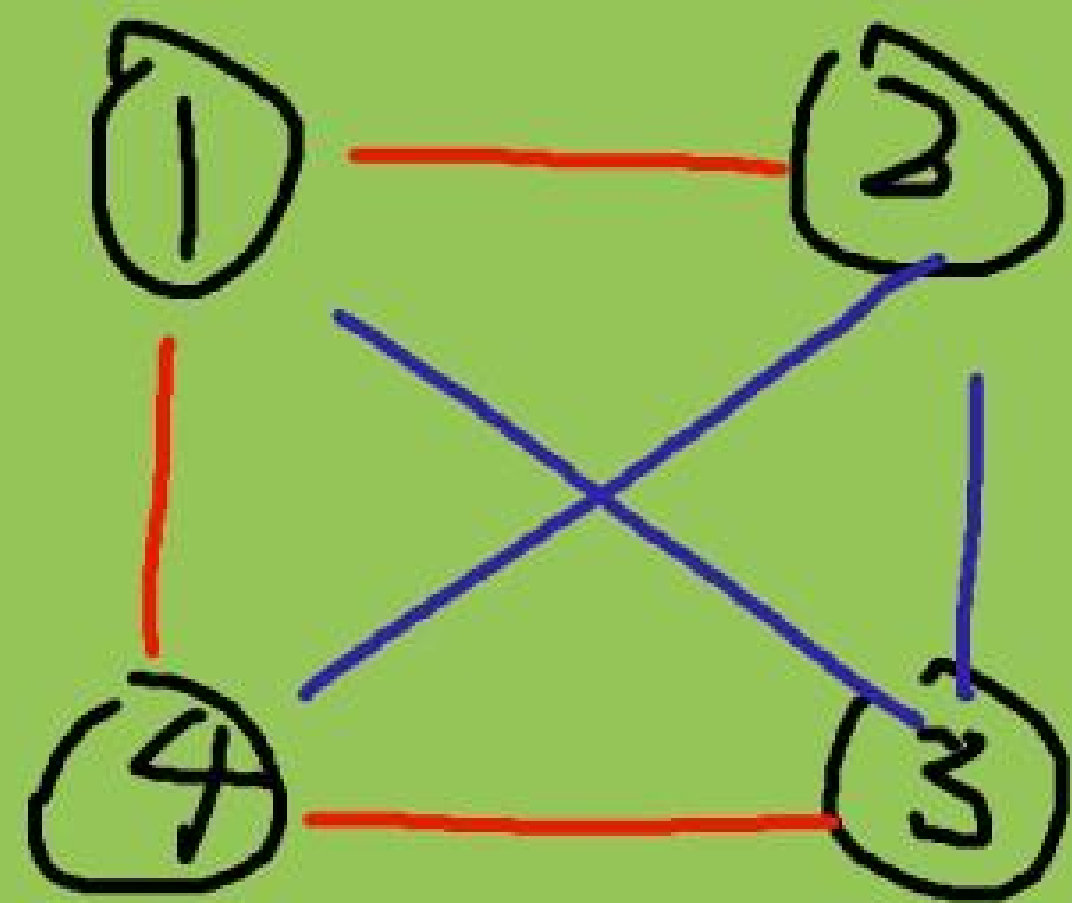
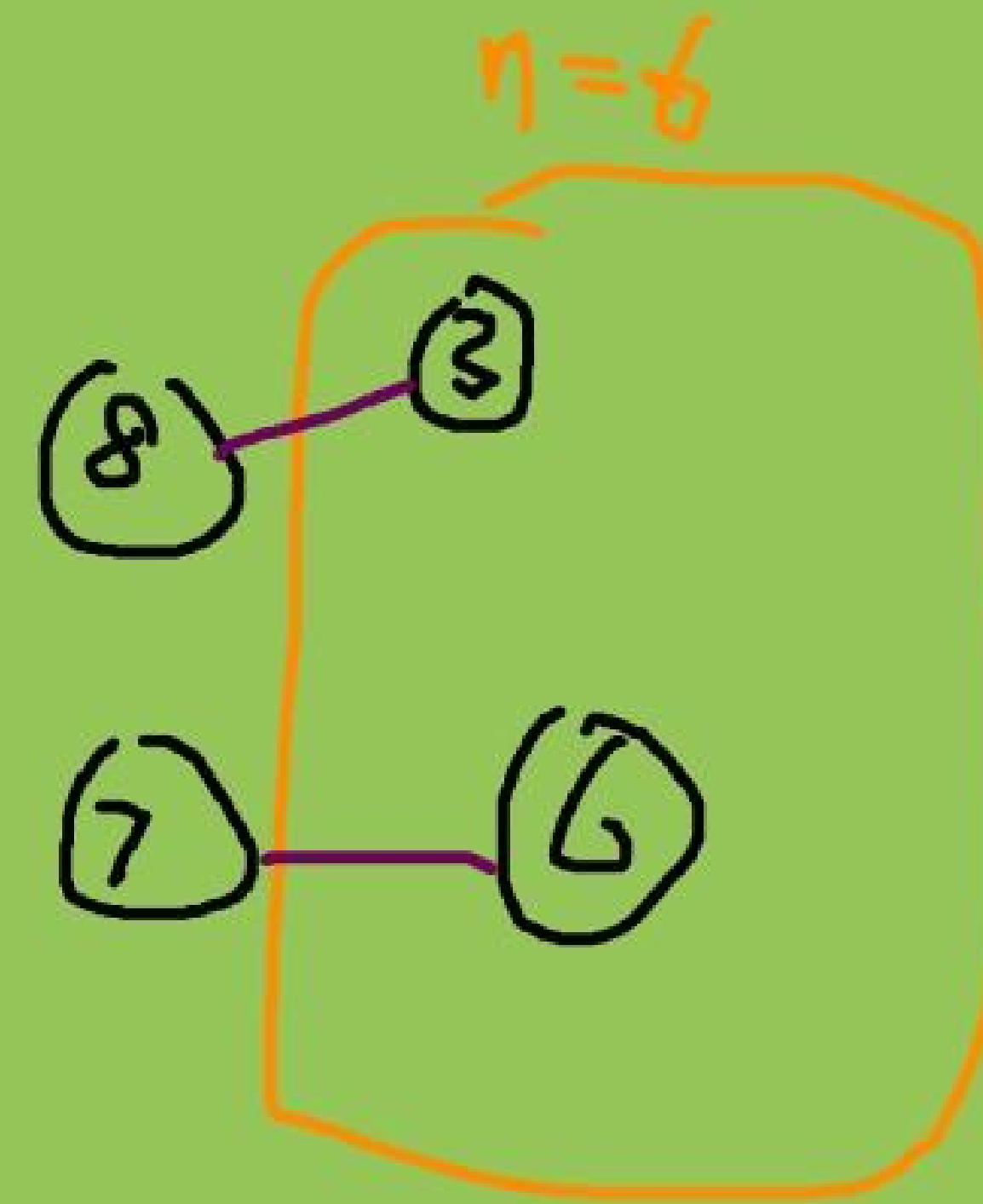
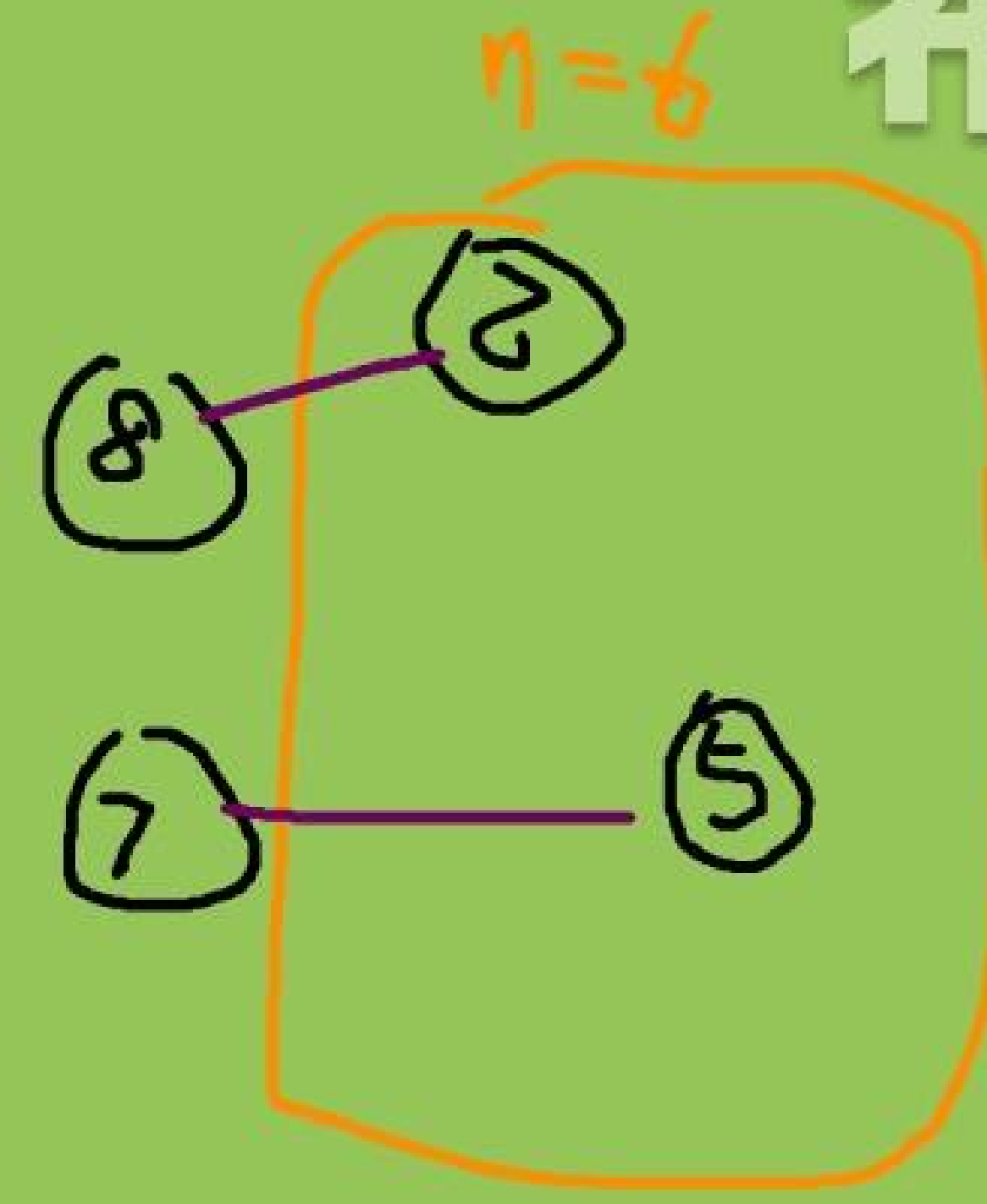
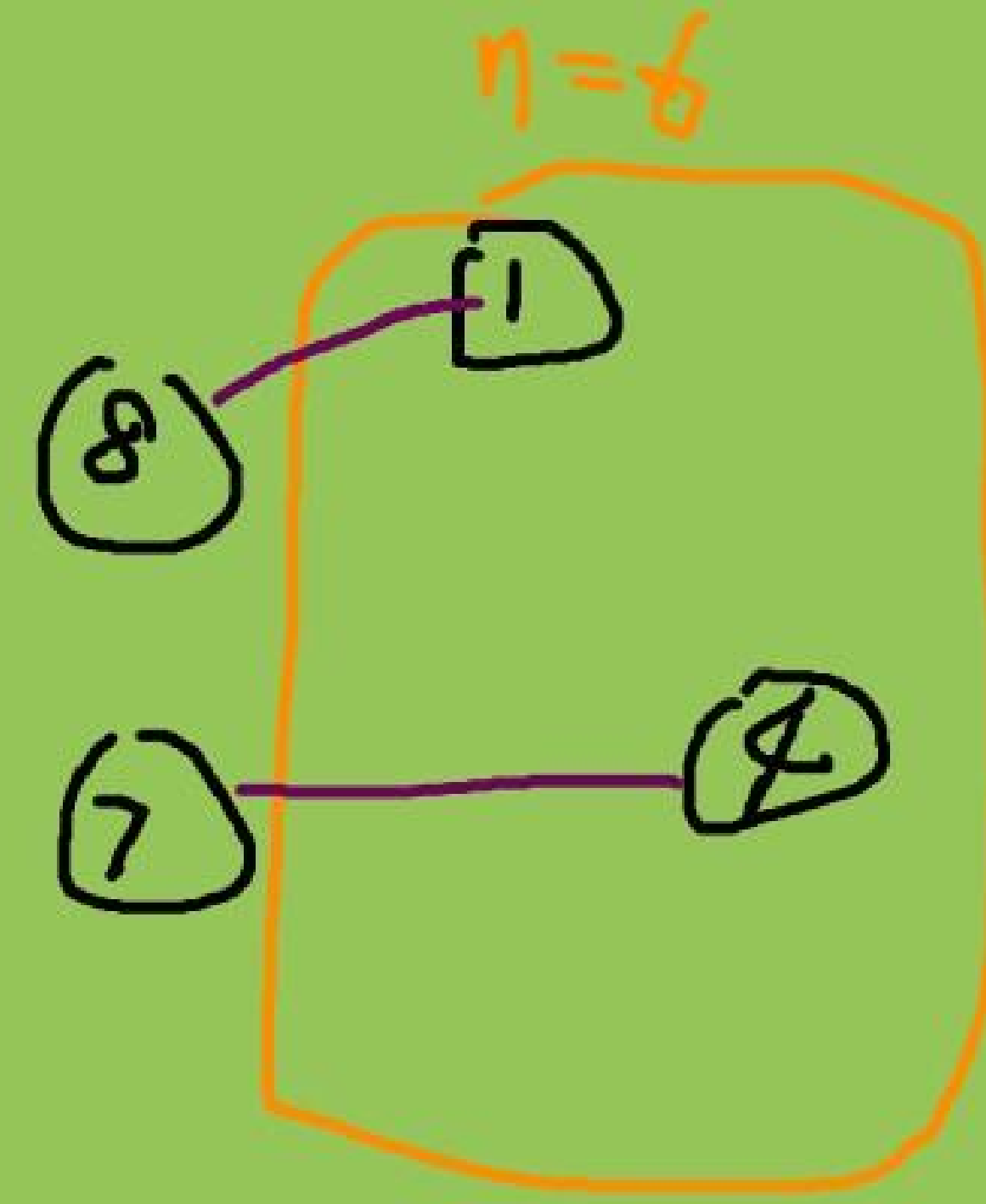
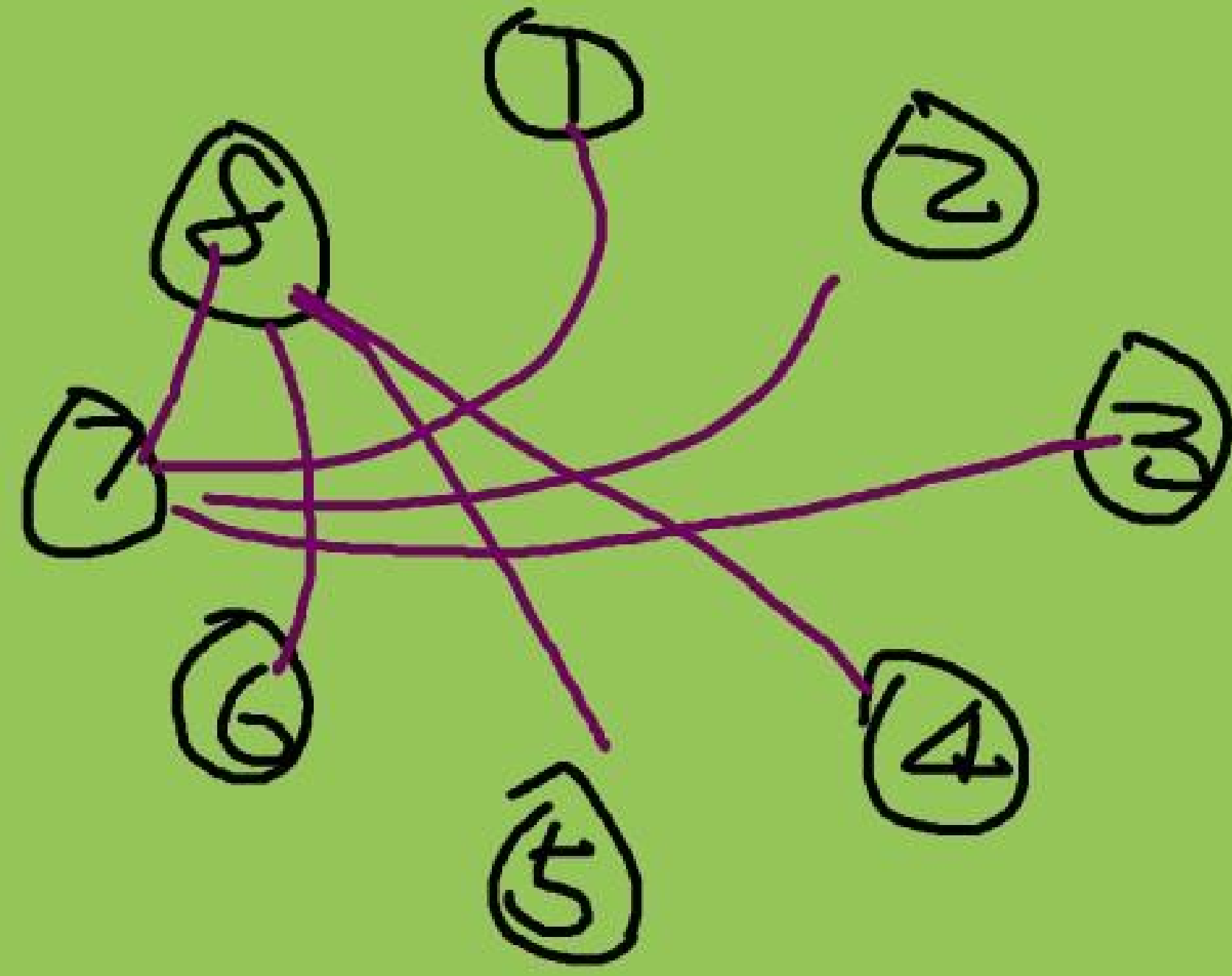


$$n=4$$

$$h=6$$

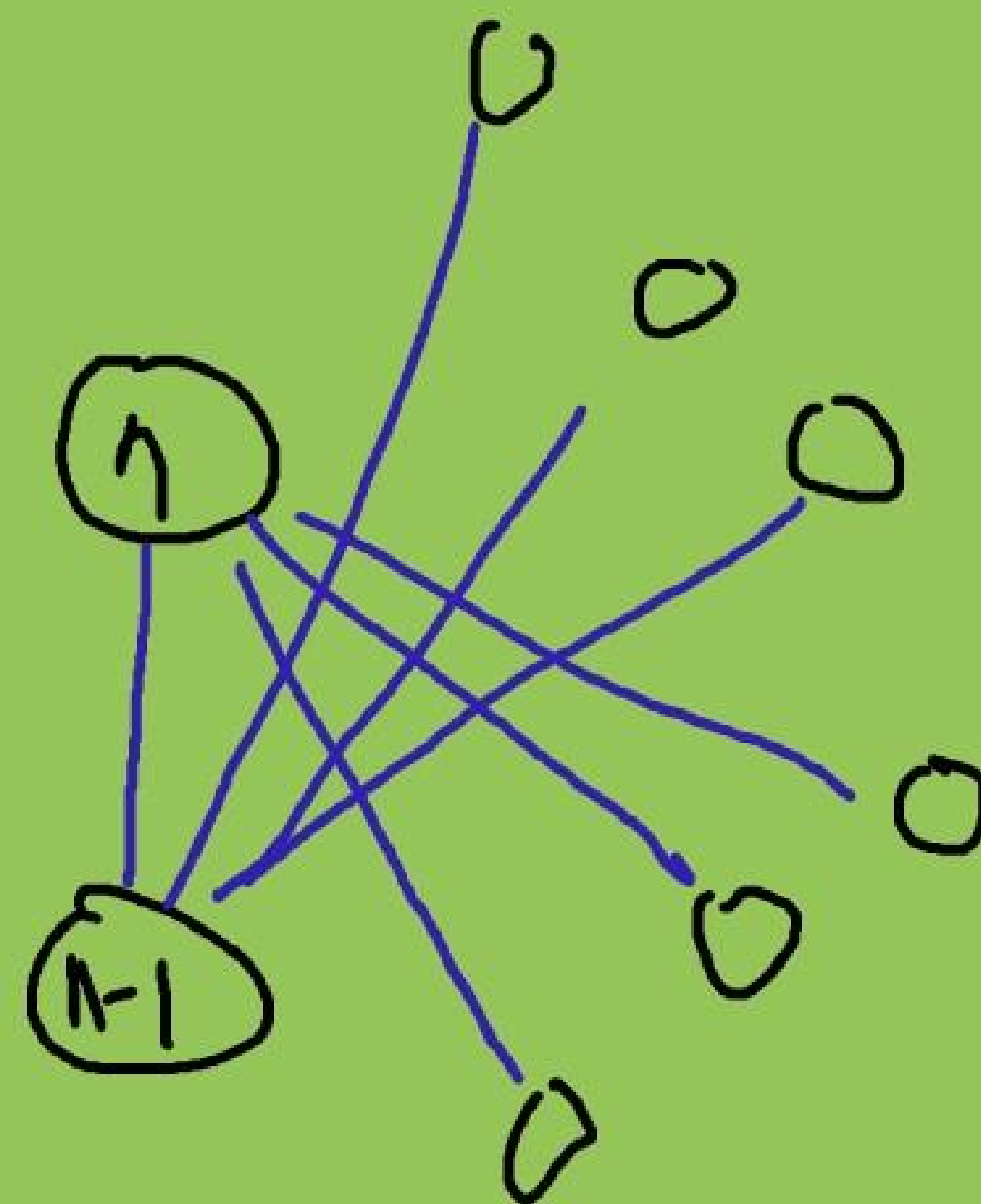
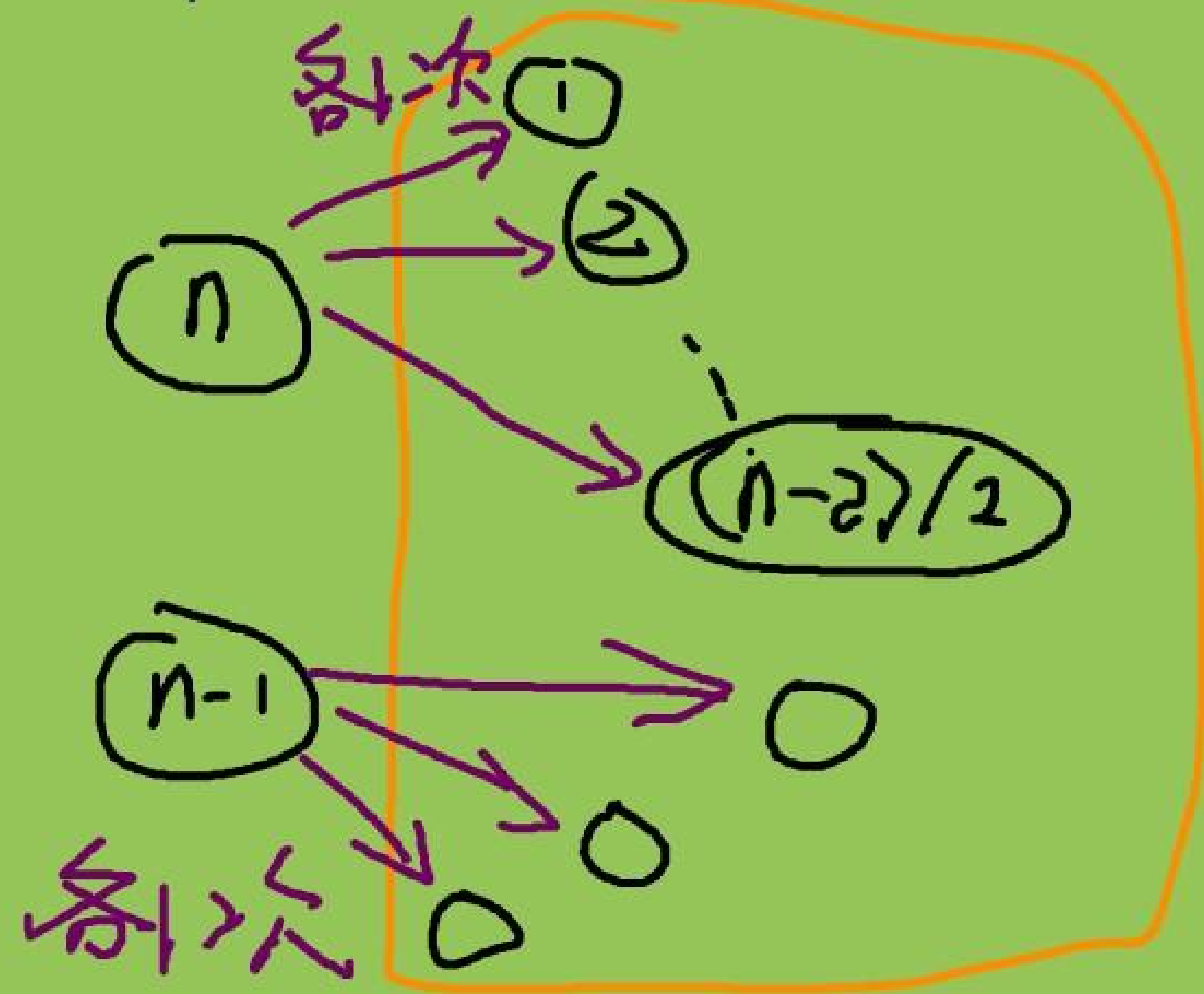


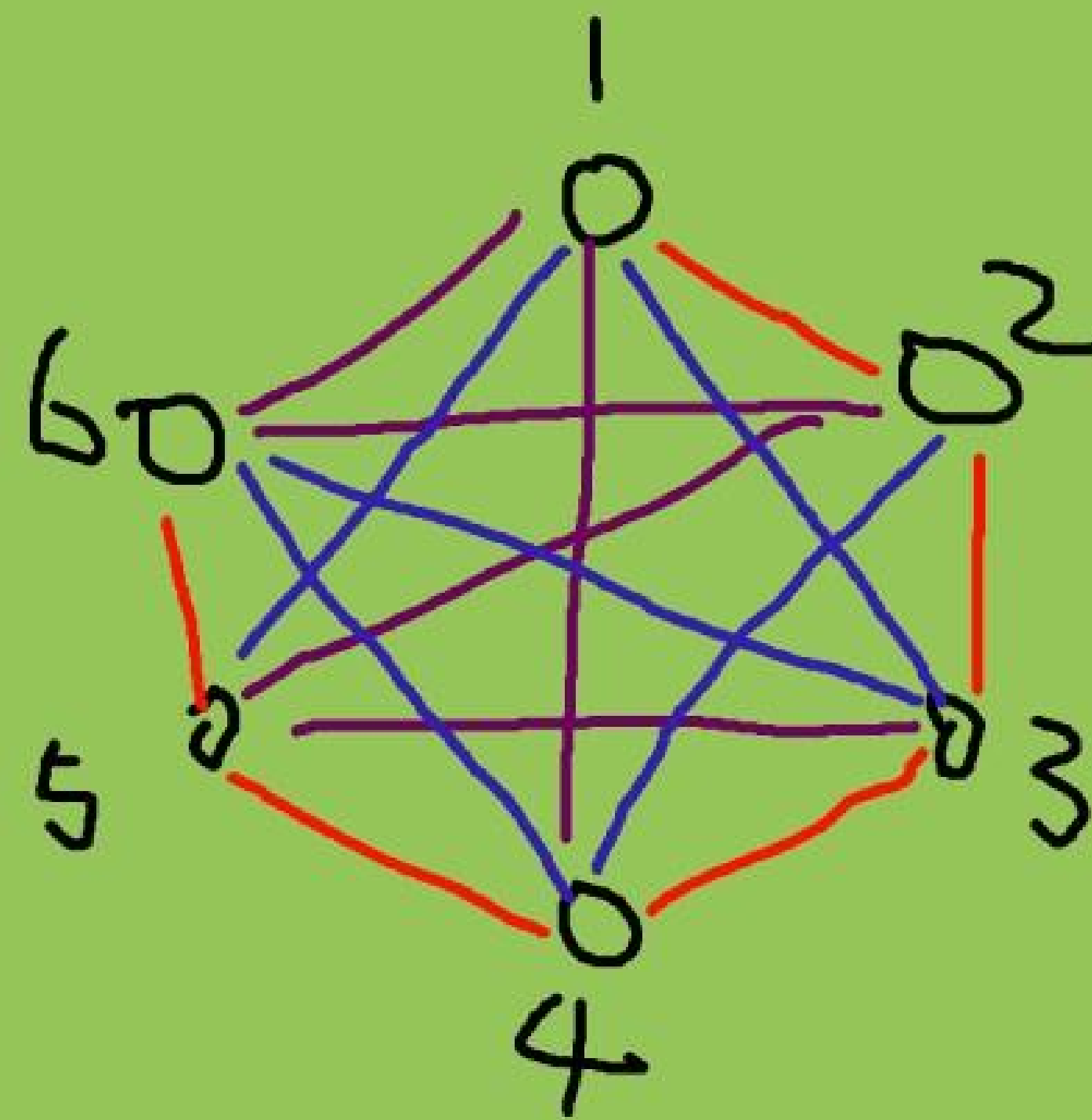
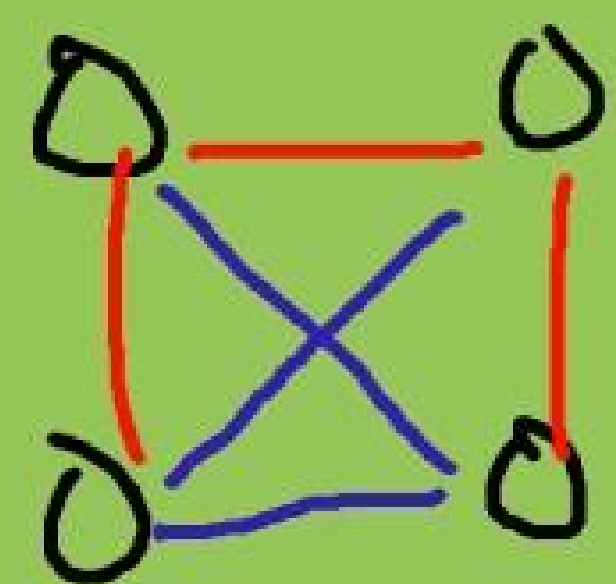


$n \longrightarrow n-2$

原有  $(n-2)/2$

$(n)$   $(n-1)$  当叶



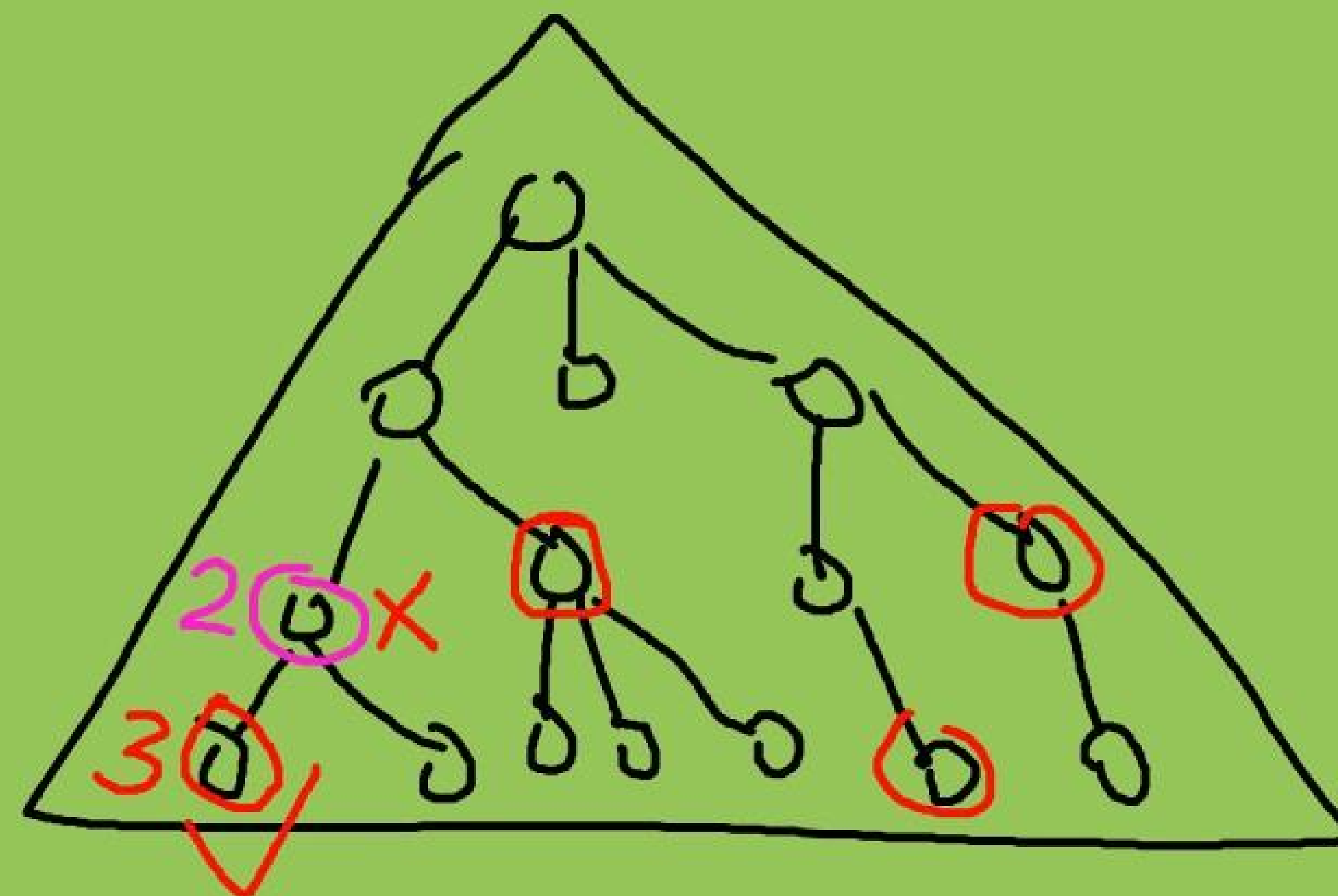
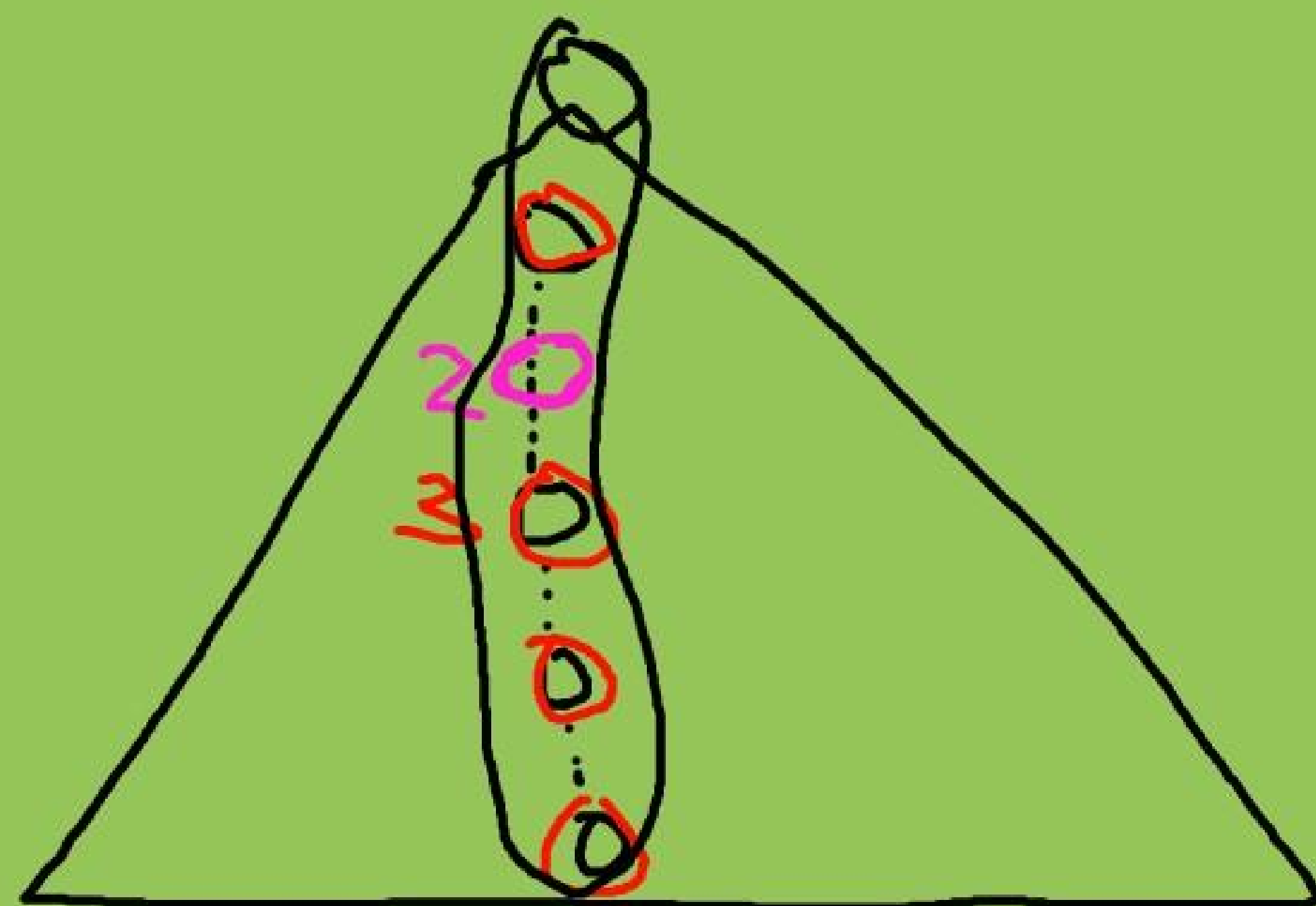


1-2-3-4-5-6

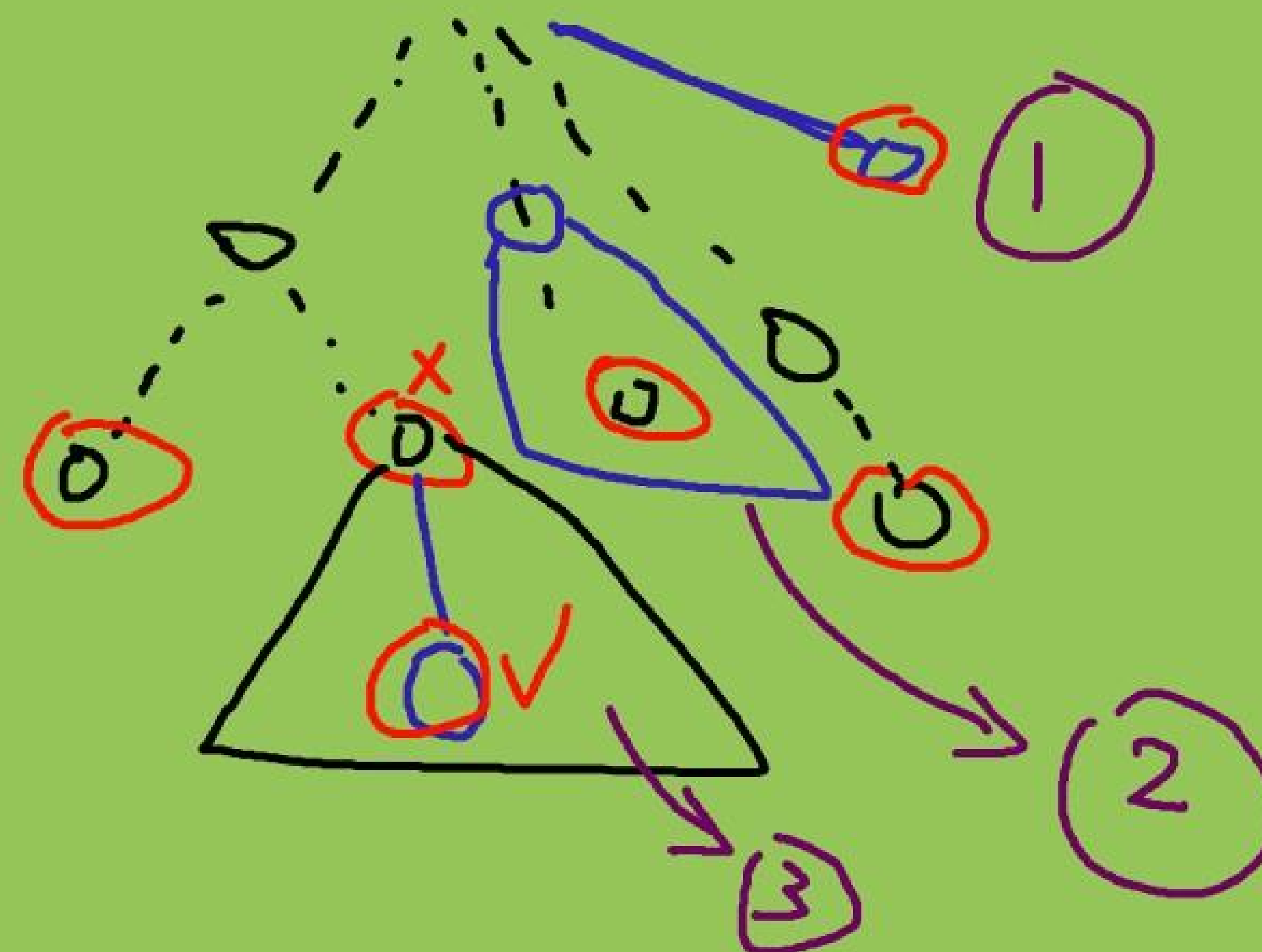
5-1-3-6-4-2

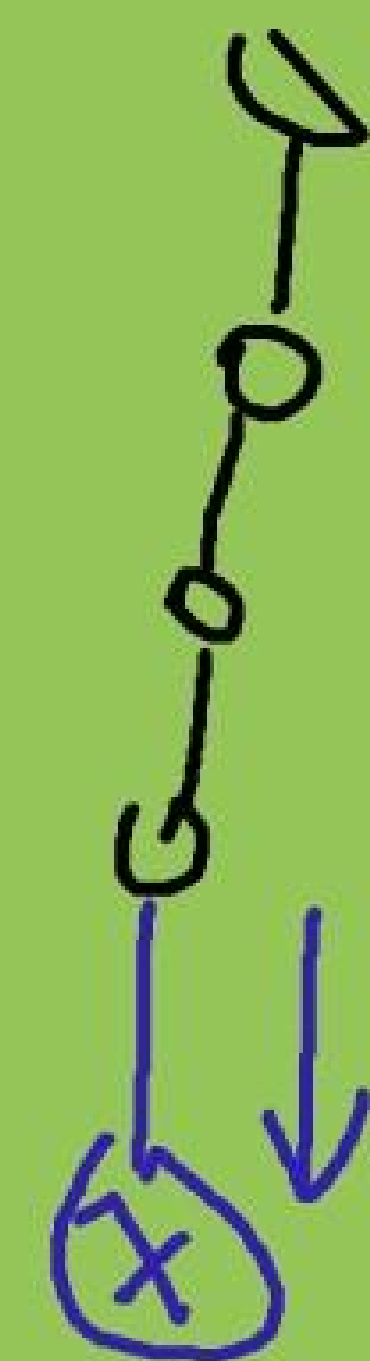
3-5-2-6-1-4





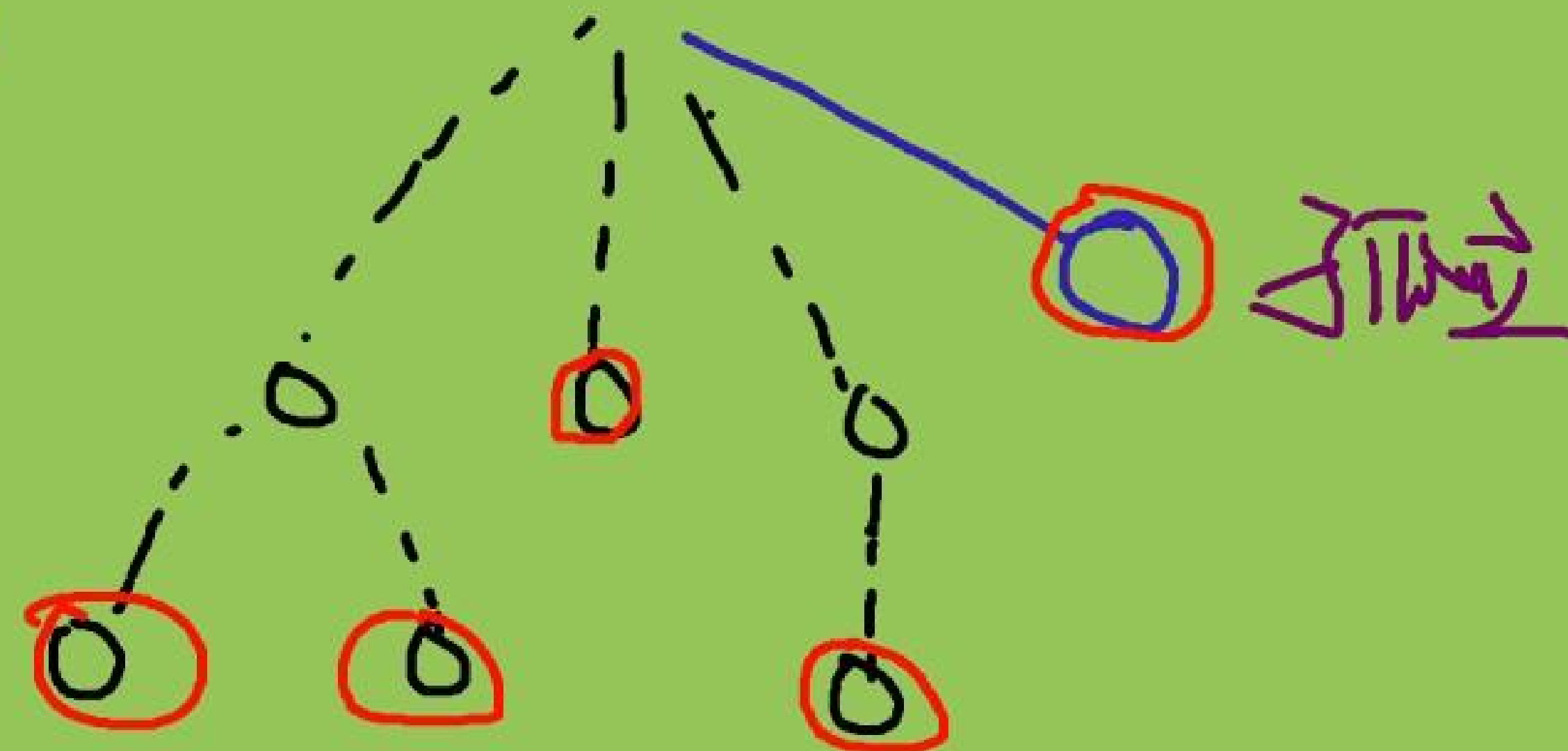
DFS





返回:还原

T2: (1)



已选: 无祖先  
Set

(2)

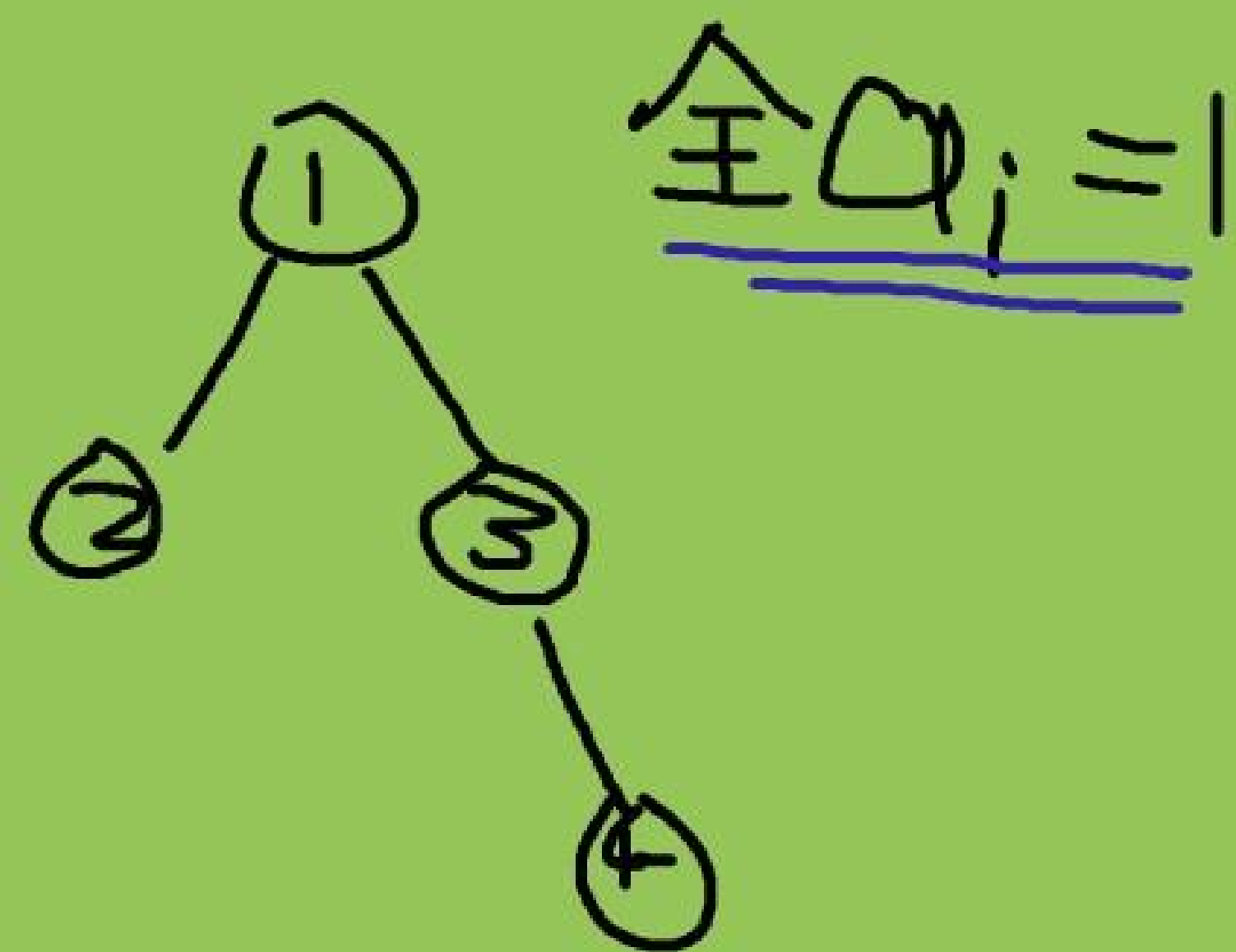


查  $dfn[x]$  后继

(3)



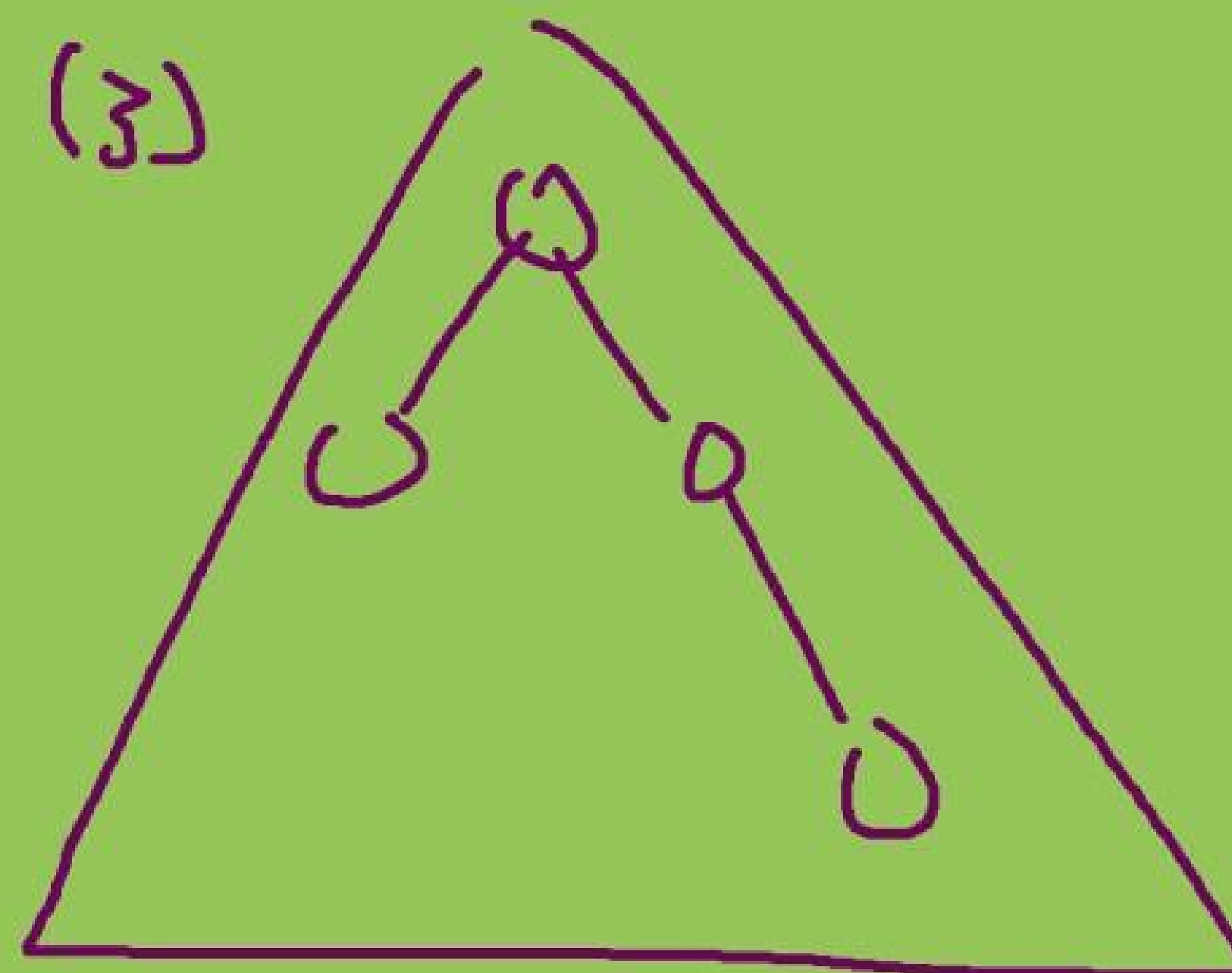
查  $dfn[x]$  前驱



(2)



(3)



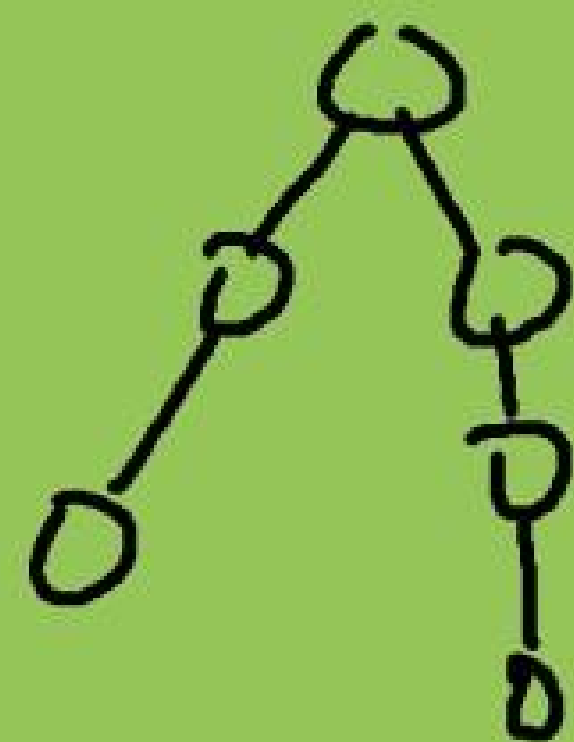
(4)





$$n=6$$

$$a_i=1$$



$$x=1.2.3.6$$

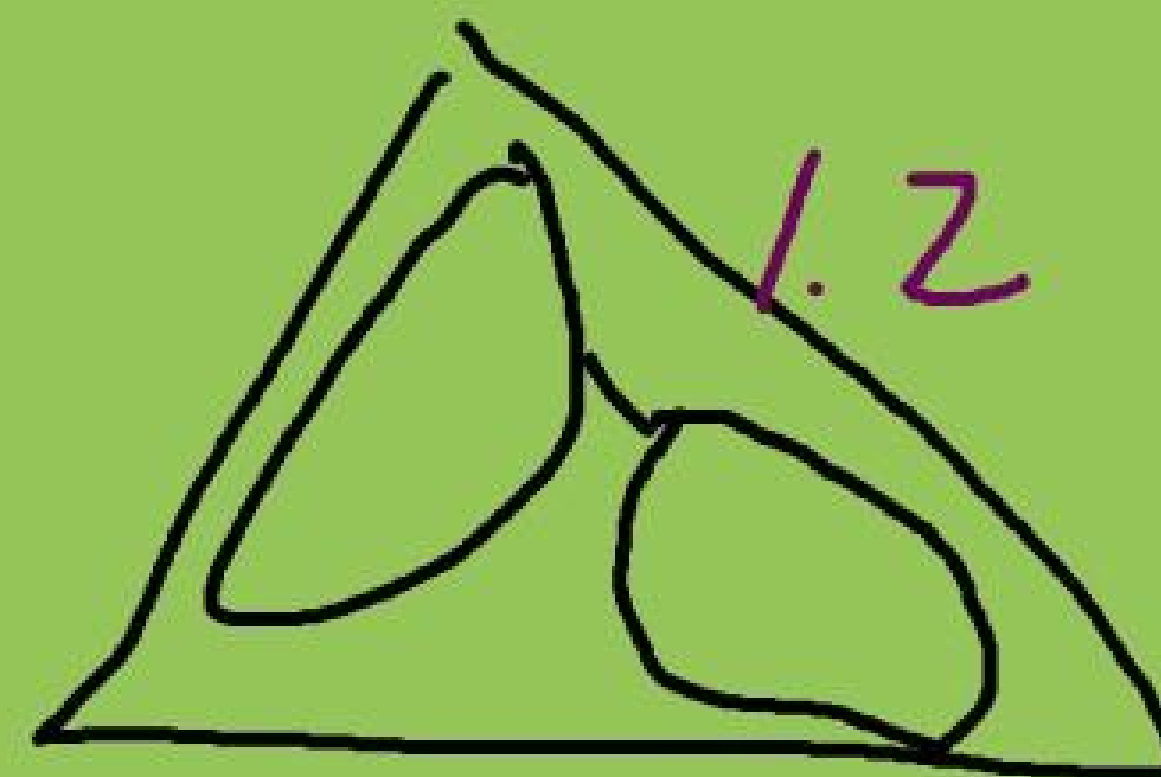
$$x_i=1$$

$$x_i/x_{i+1}$$

(1)



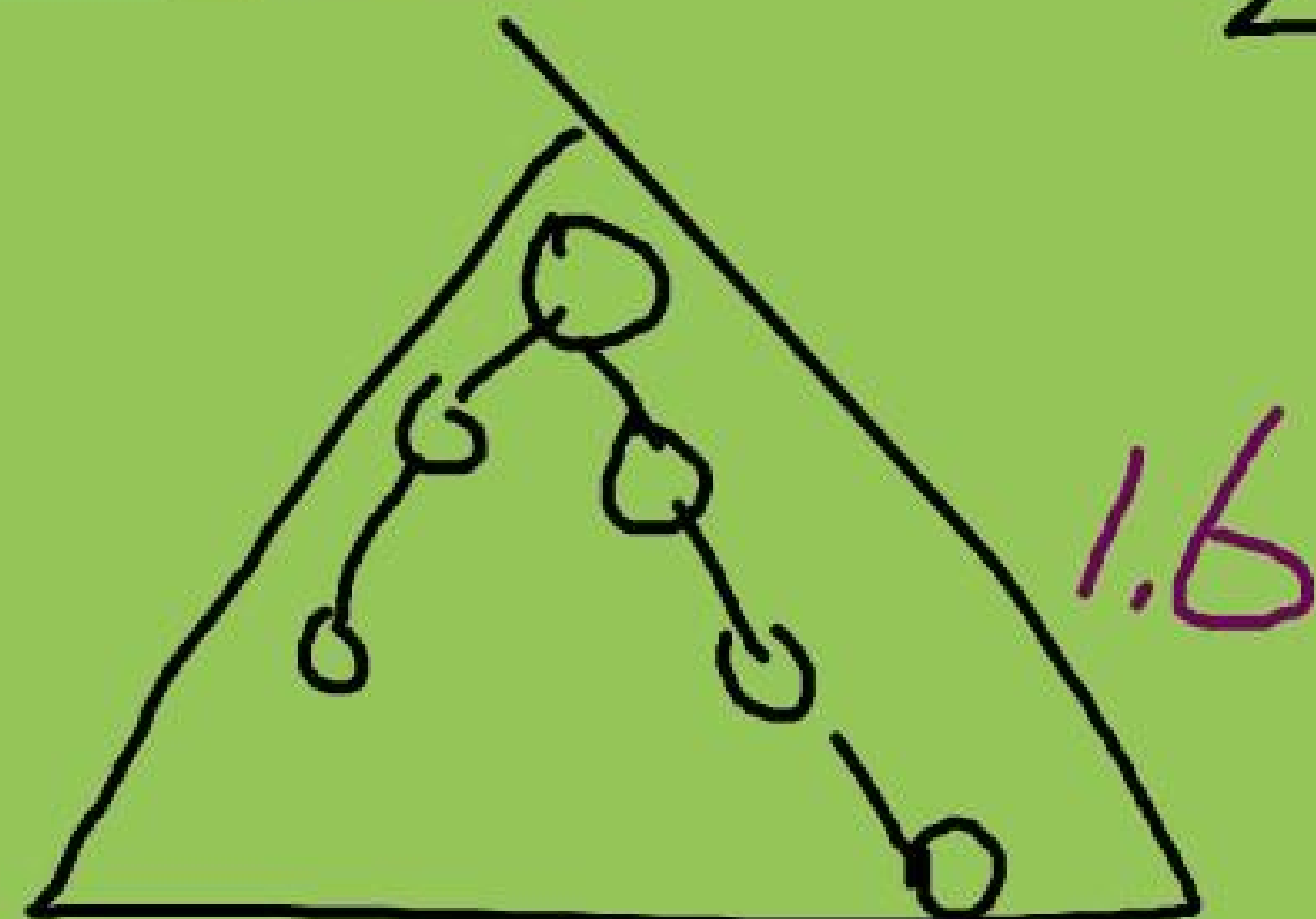
(2)



(3)

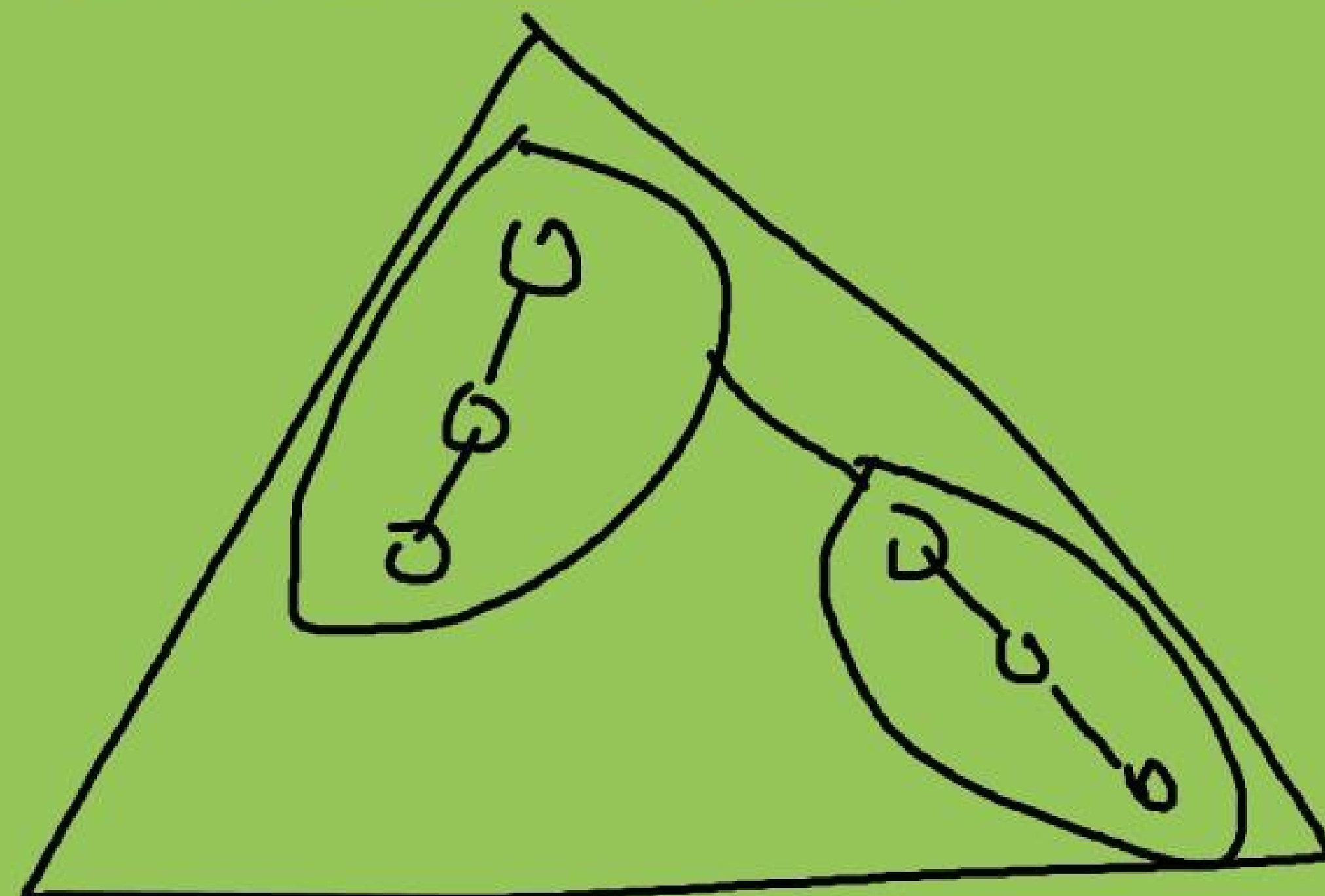


(4)



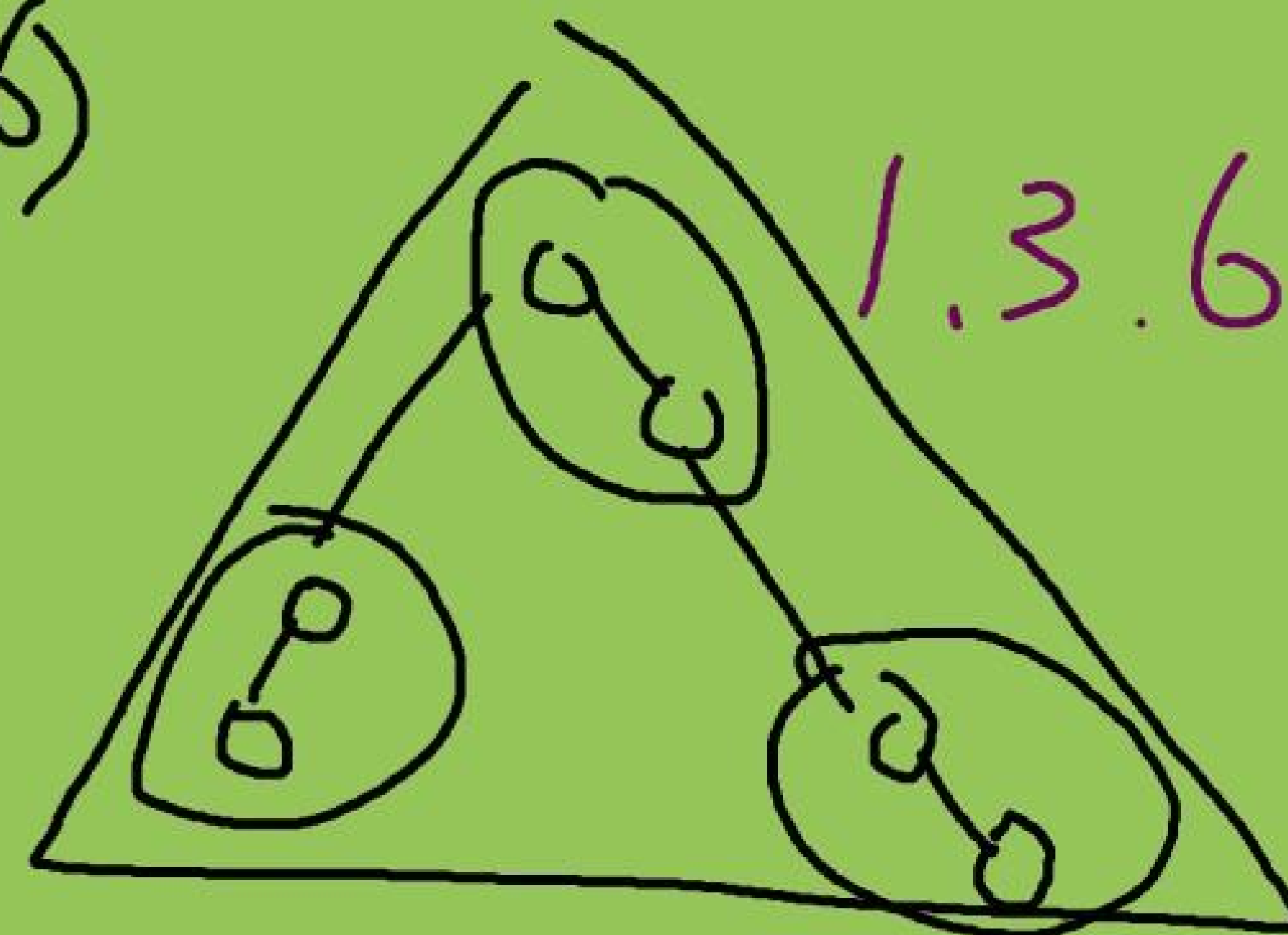
(5)

$$1.2.6$$

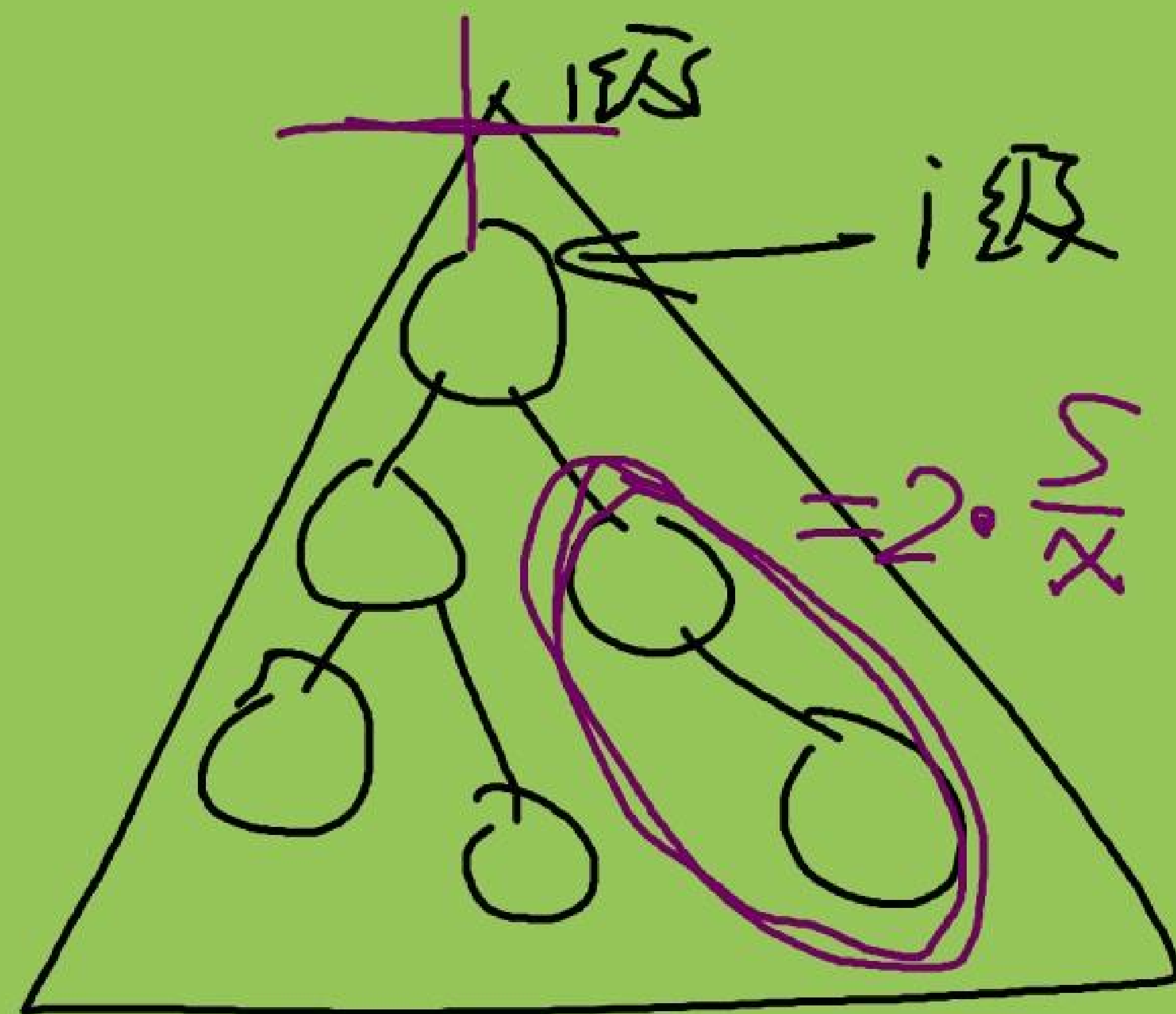


(6)

$$1.3.6$$







$x$  个

$x | S$

遍历

$$S = \sum a_i$$

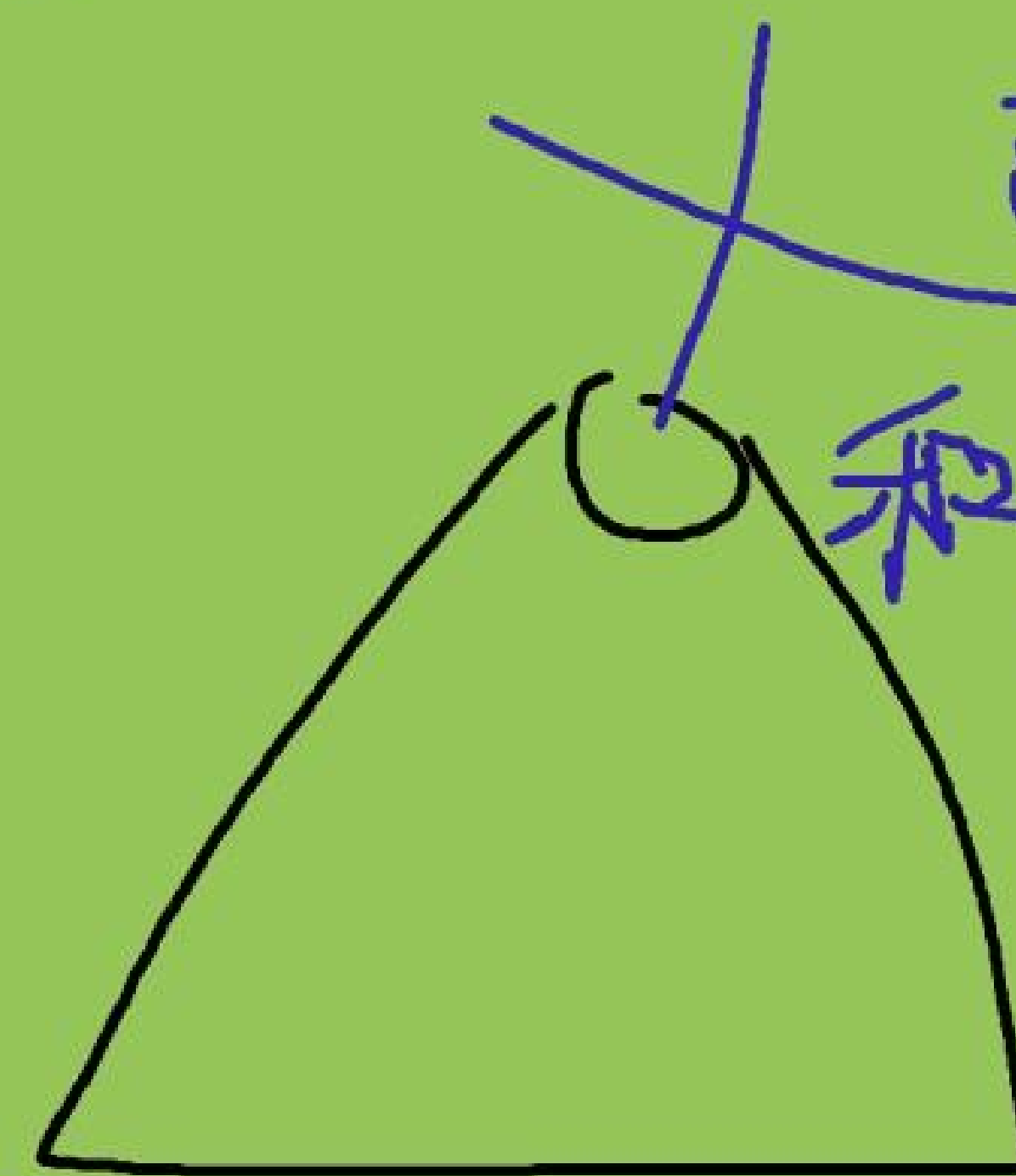
每个  $i$  级  $\sum a_i = S/x$

子树和  $S_i = \sum a_i$

看  $S_i$  是  $S/x$  的倍数

是否有  $x$  个

$\begin{cases} < x & \text{不行} \\ = x & \text{可能} \\ > x & \text{不可能} \end{cases}$



可断的为  $x$  条

和是

$S/x$  的倍

$x = 1, 2, \dots, n$   
 是否可行

若  $s_i$  是  $S/x$  的倍  $\rightarrow$

$$f[x]++$$

~~并查集~~  $\left| \frac{\gcd(s_i, S)}{S/x} \right|$

先: 救  $s_i$   $\boxed{x_0 = \frac{S}{\gcd}}$   $f[x_0]++$

$$x \mid \frac{S}{\gcd(s_i, S)}$$

再: 救  $x$  倍  $f[x] += f[\frac{S}{x}]$

$$O(n \log n)$$

$$f[x] == x \Rightarrow$$

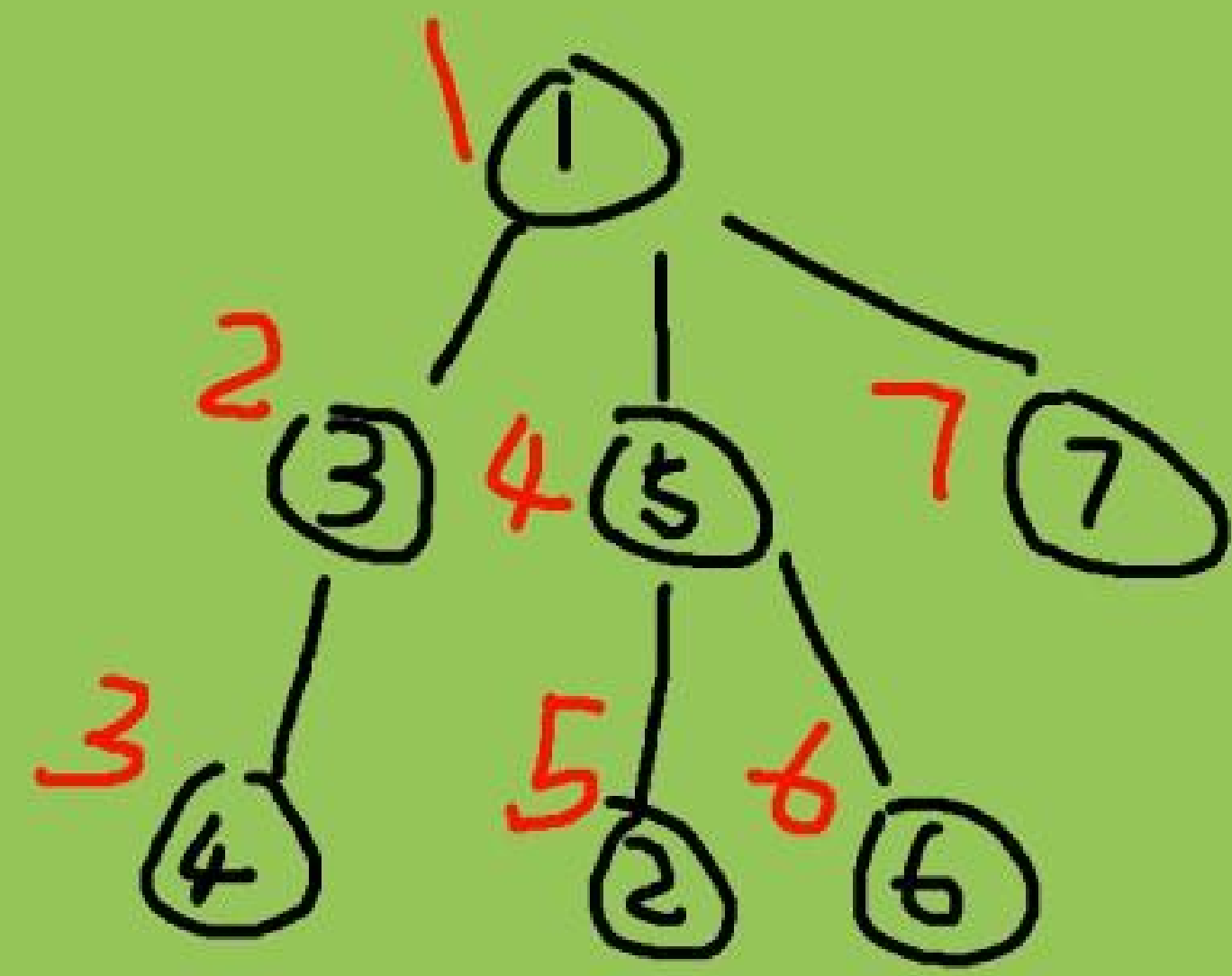
某级  $x$  块可行

$g[x]$ : 以  $x$  结尾

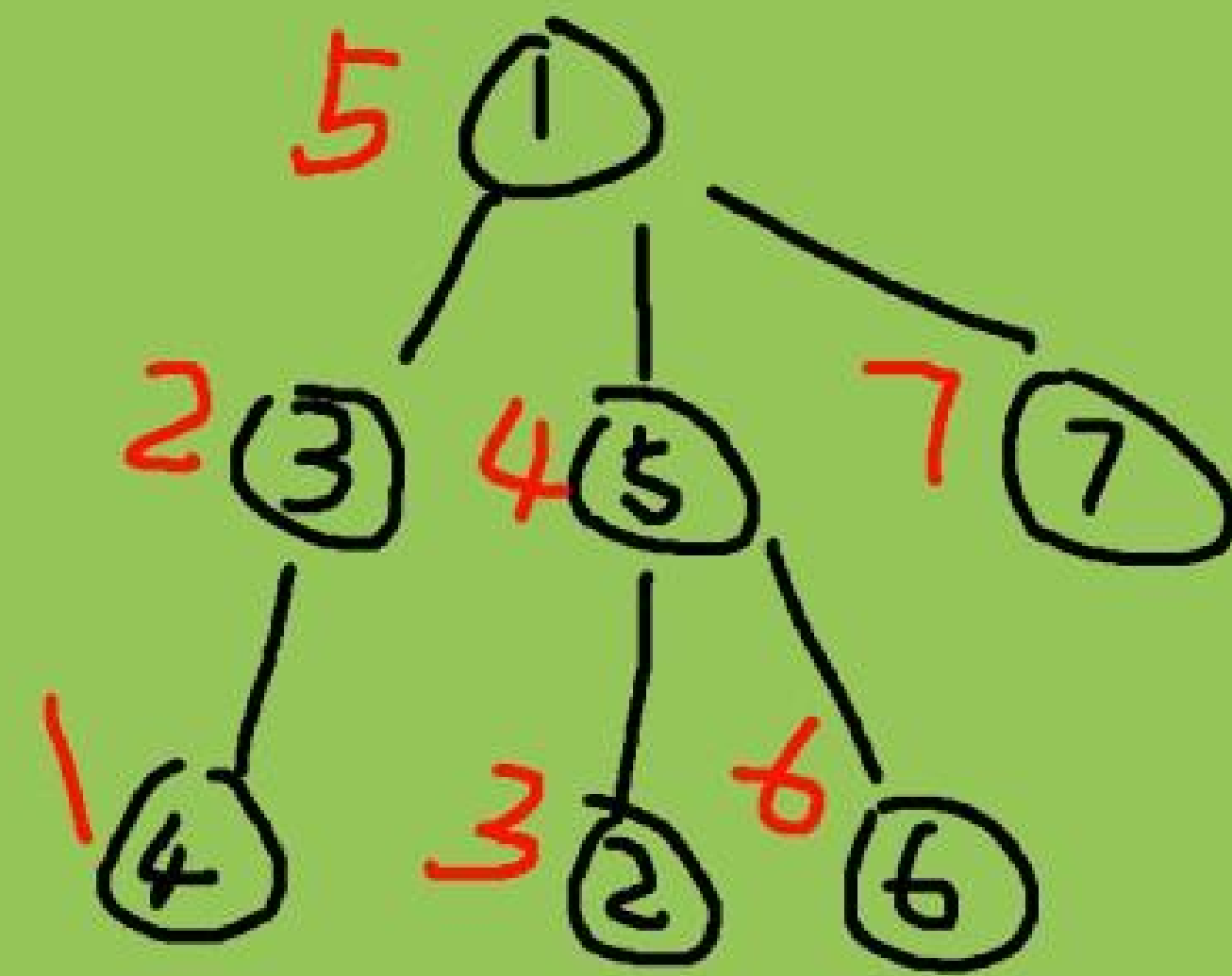
$$g[x] = \sum g[\text{约}]$$

$$O(n \log n)$$

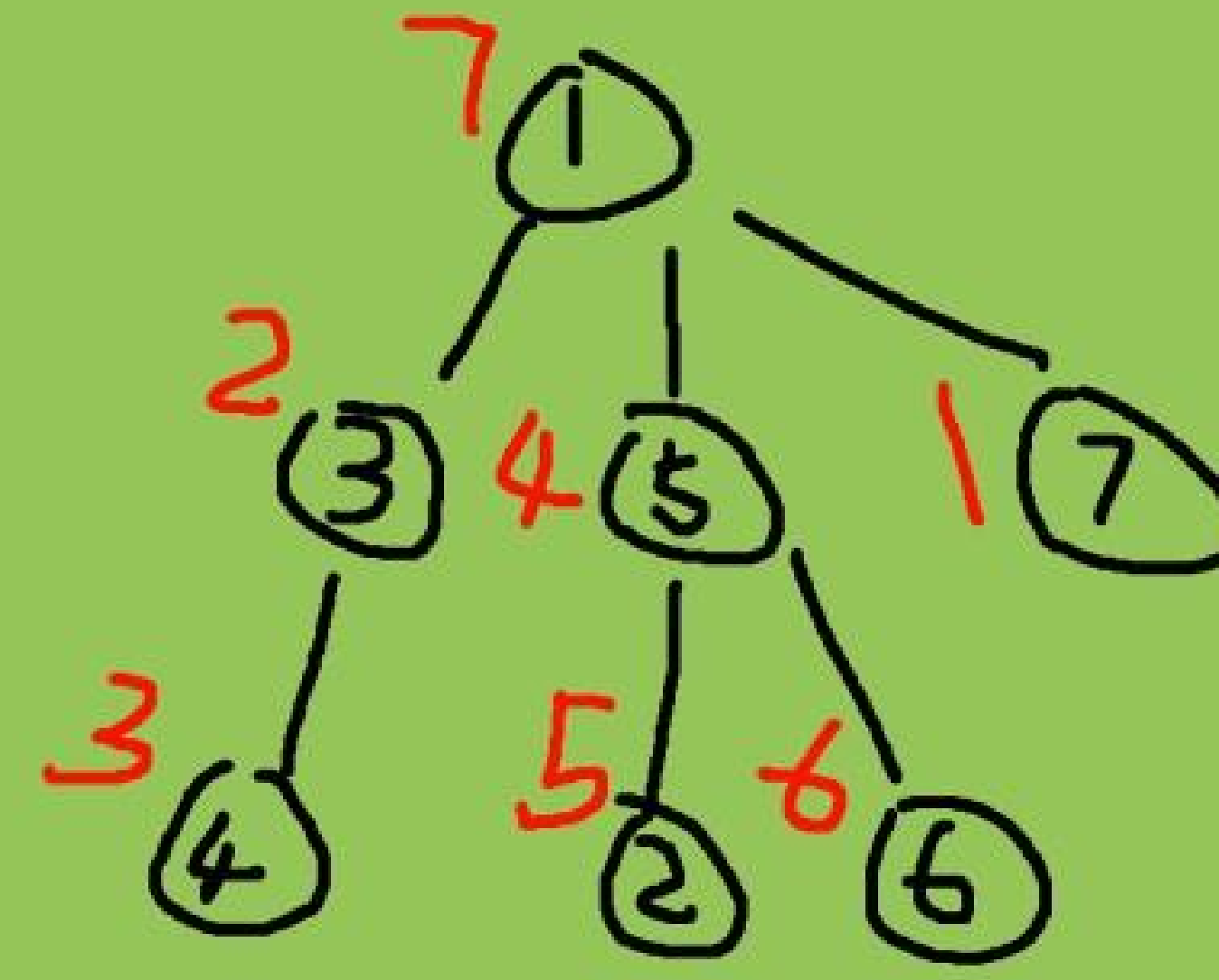




初DFS



给你



给你。

No

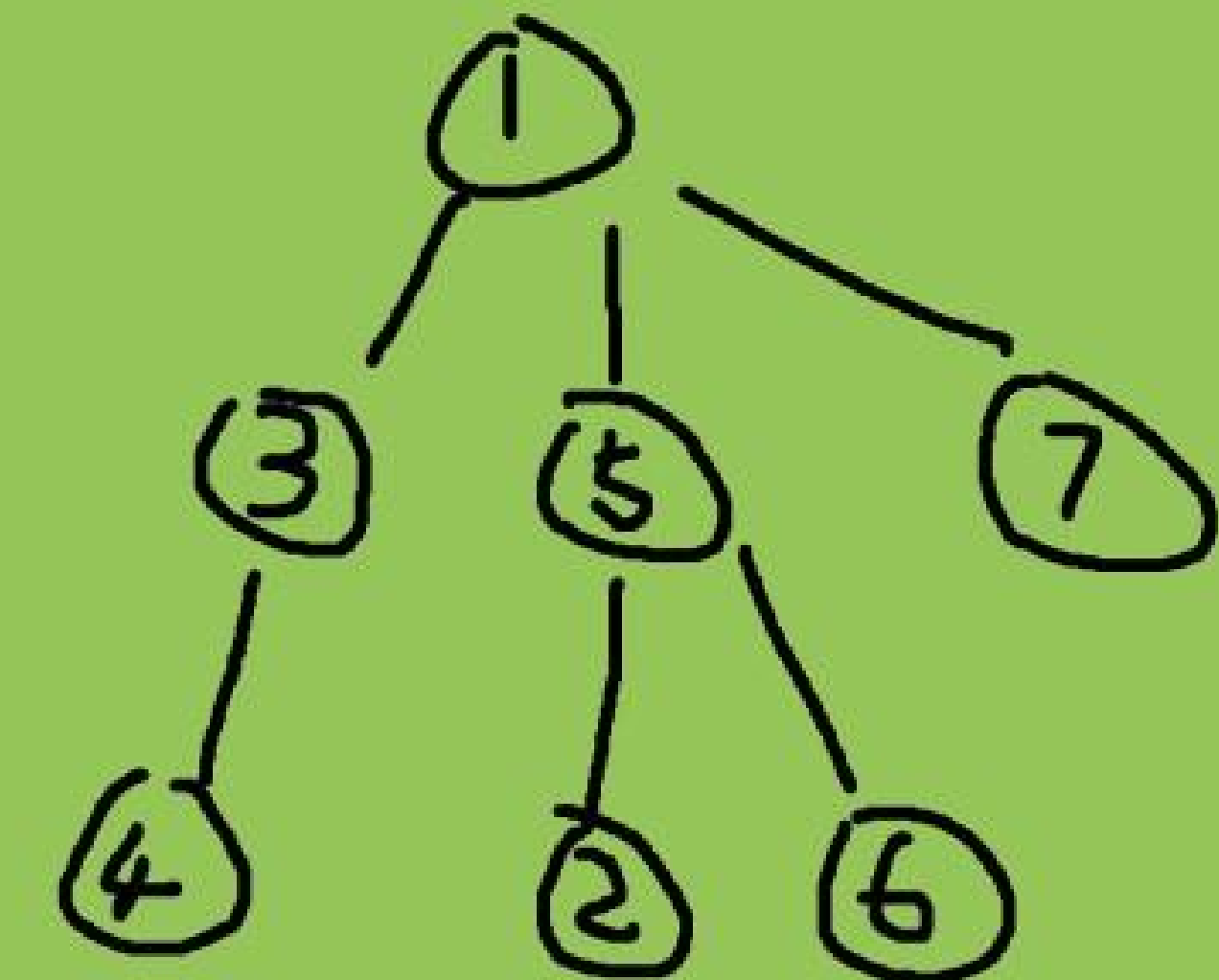
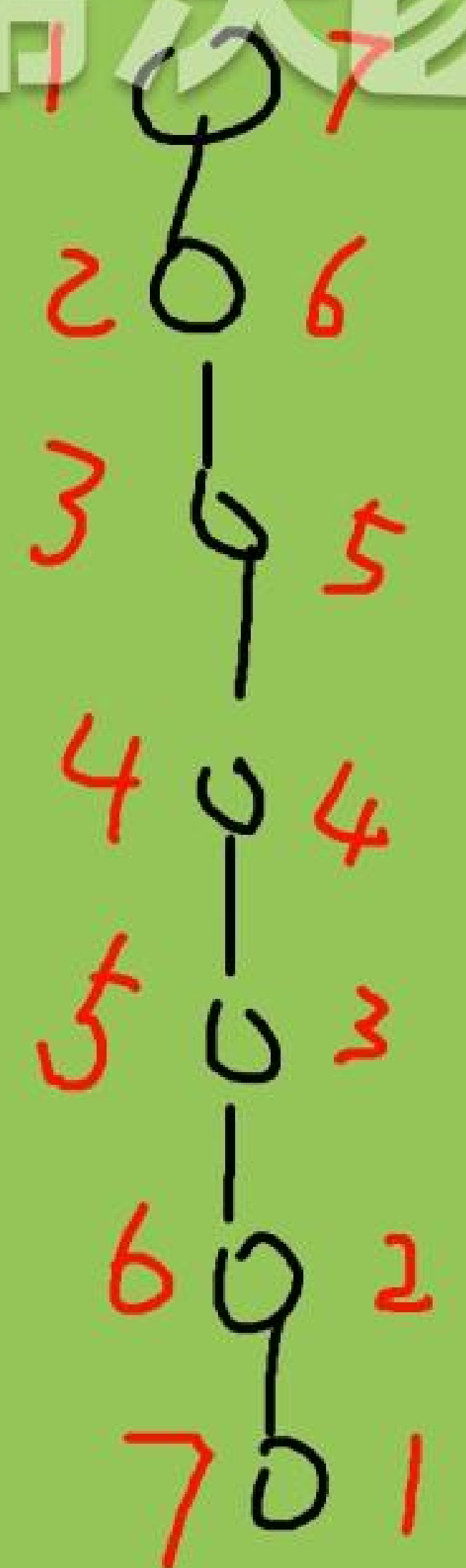
output

$O(n^2)$

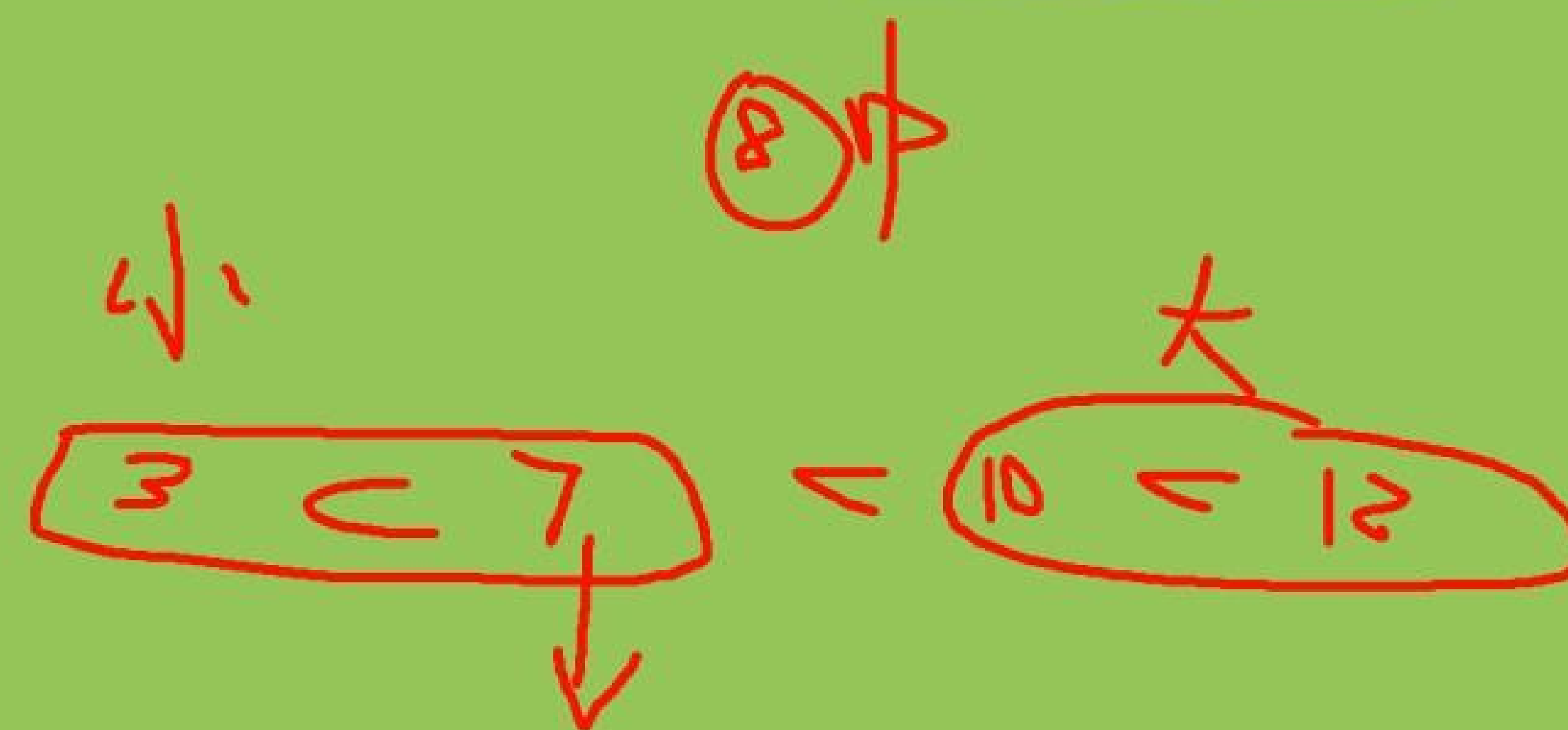
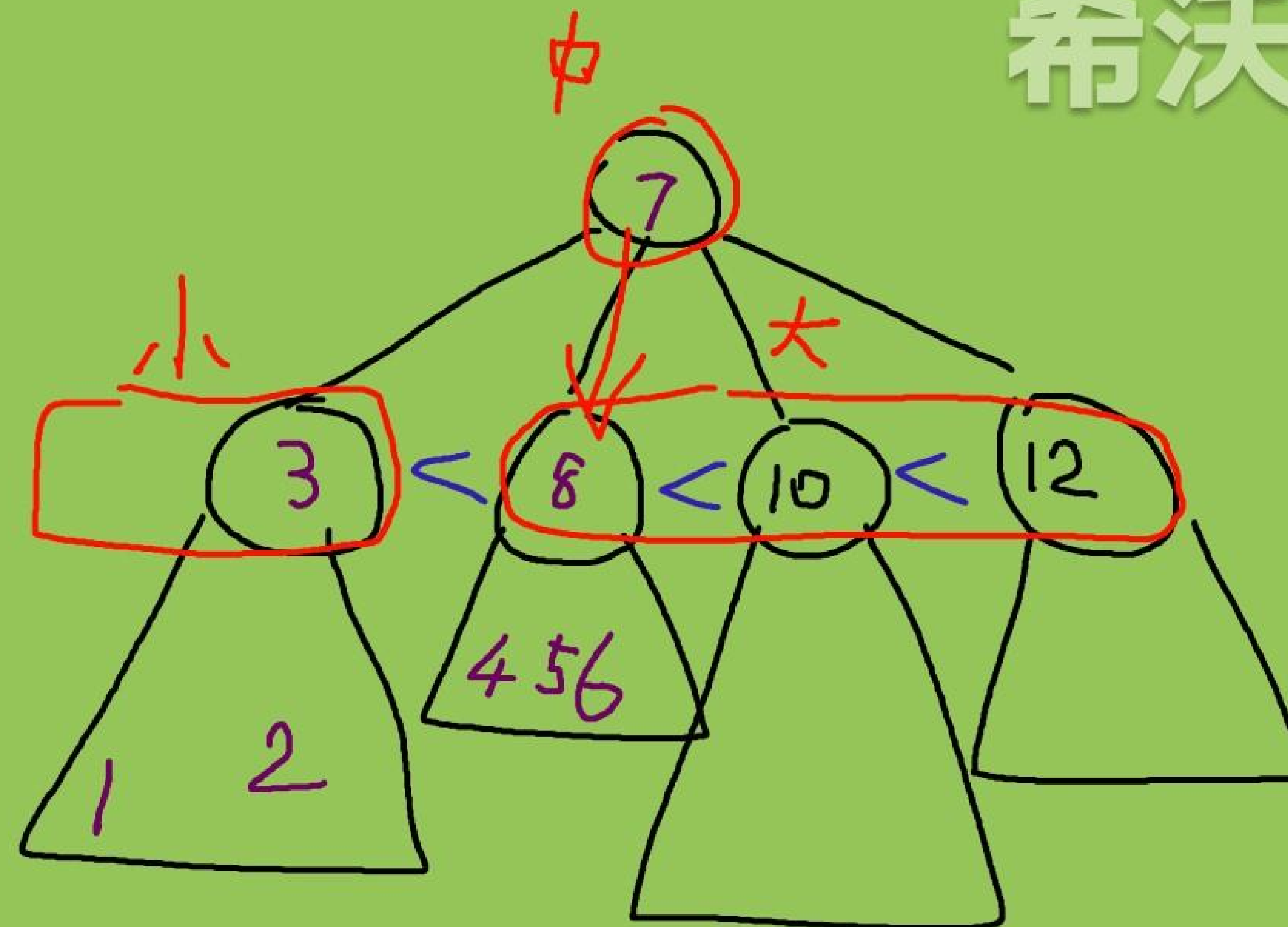
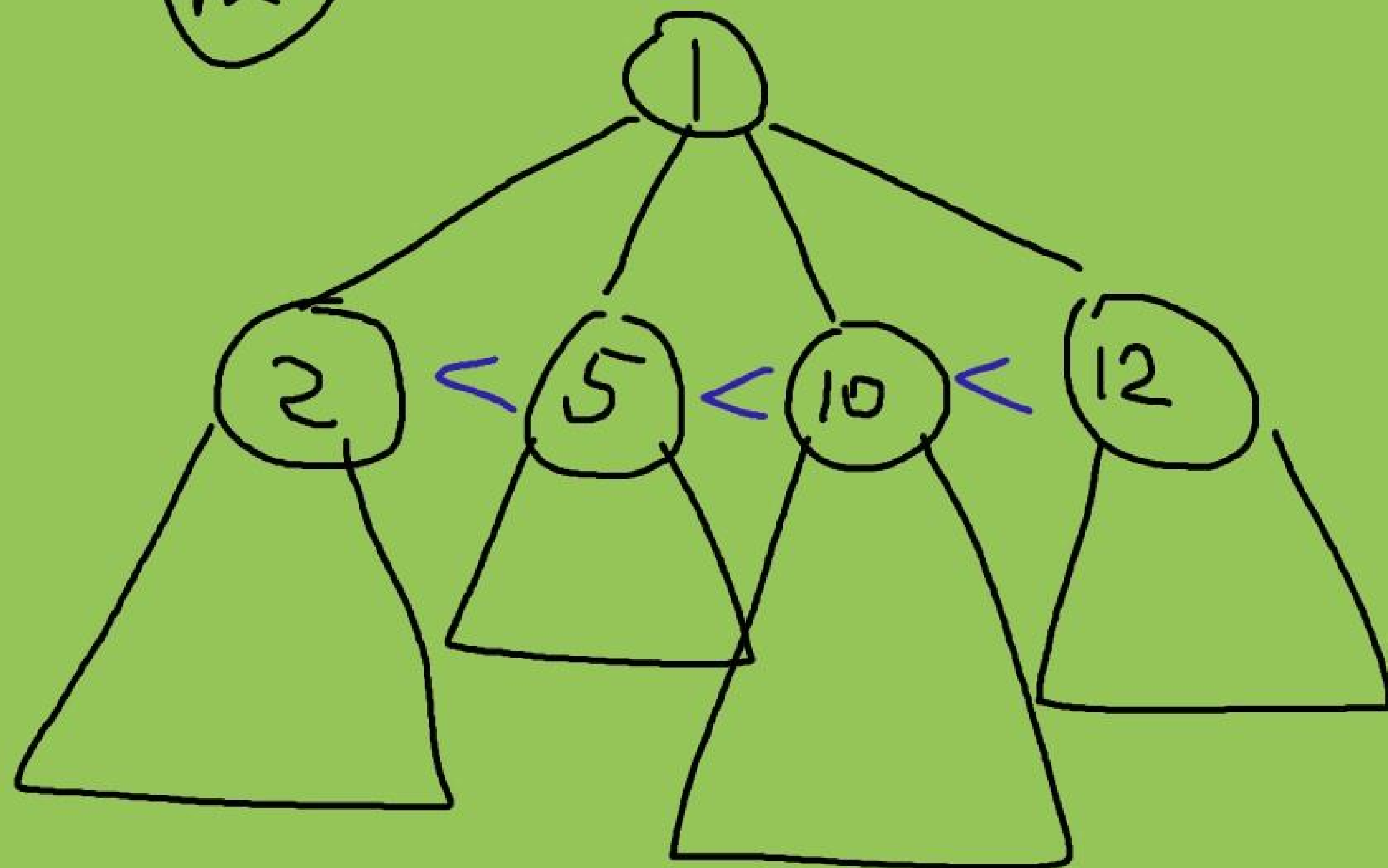
Yes

6

原 a . . . . .

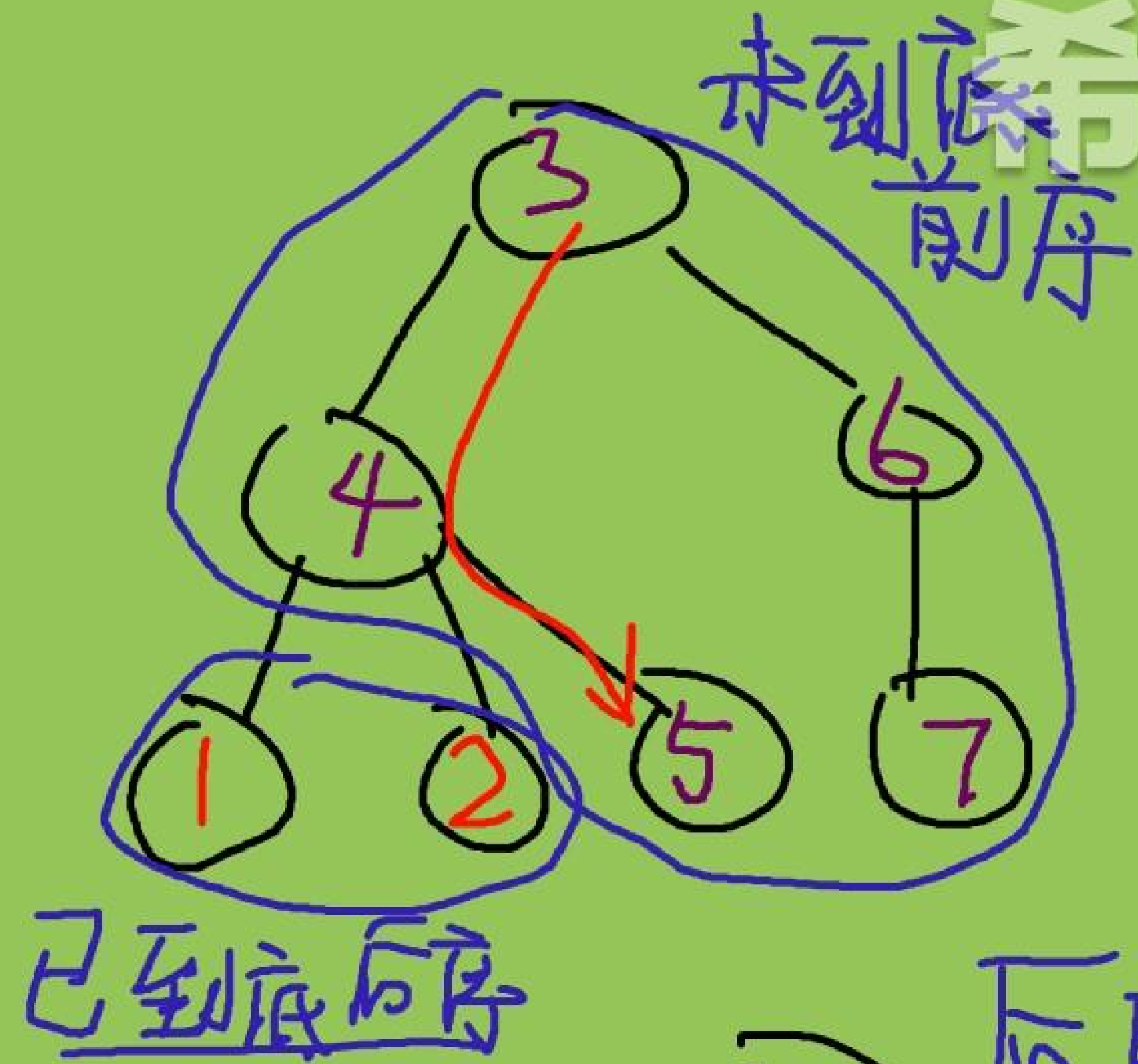
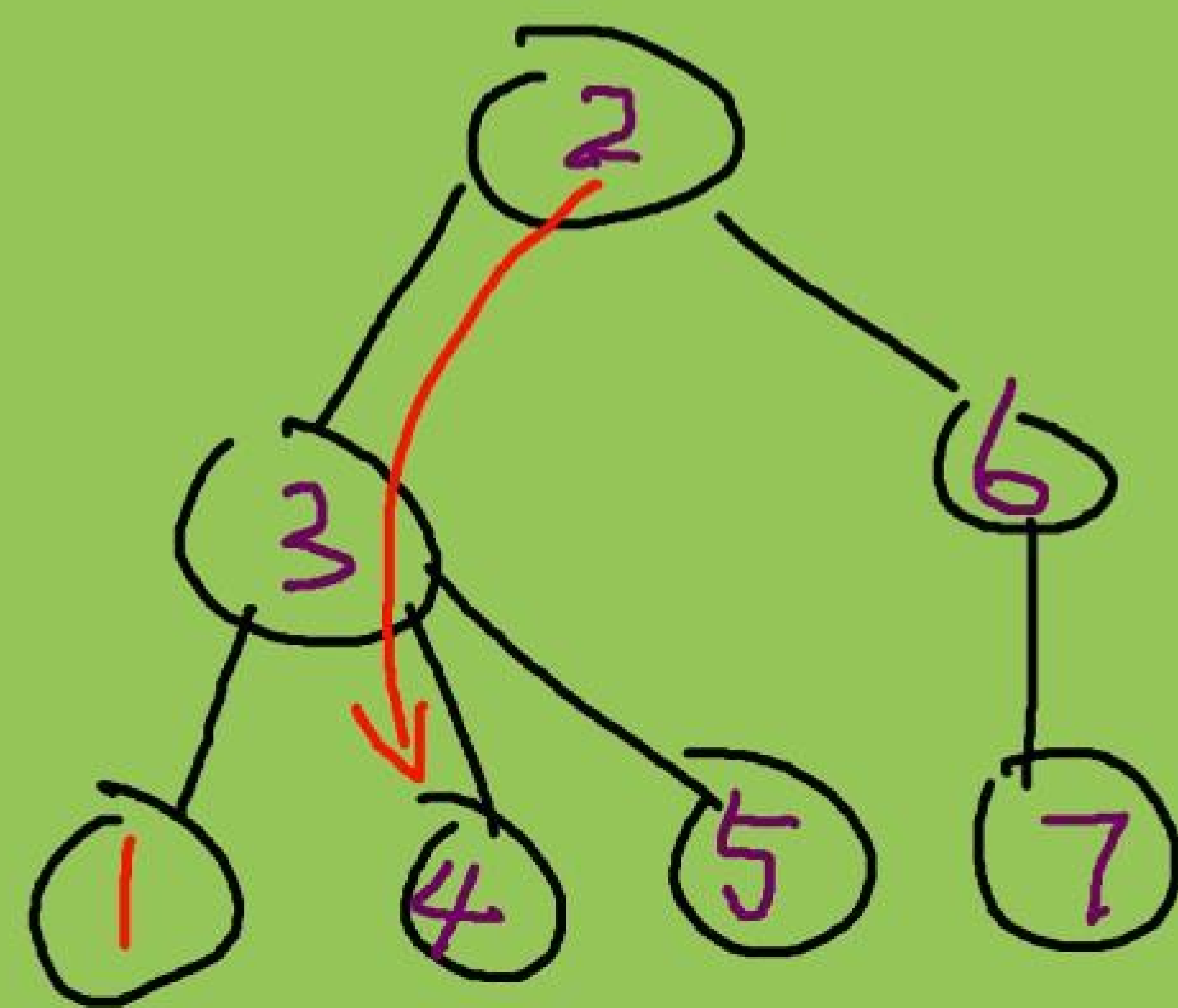
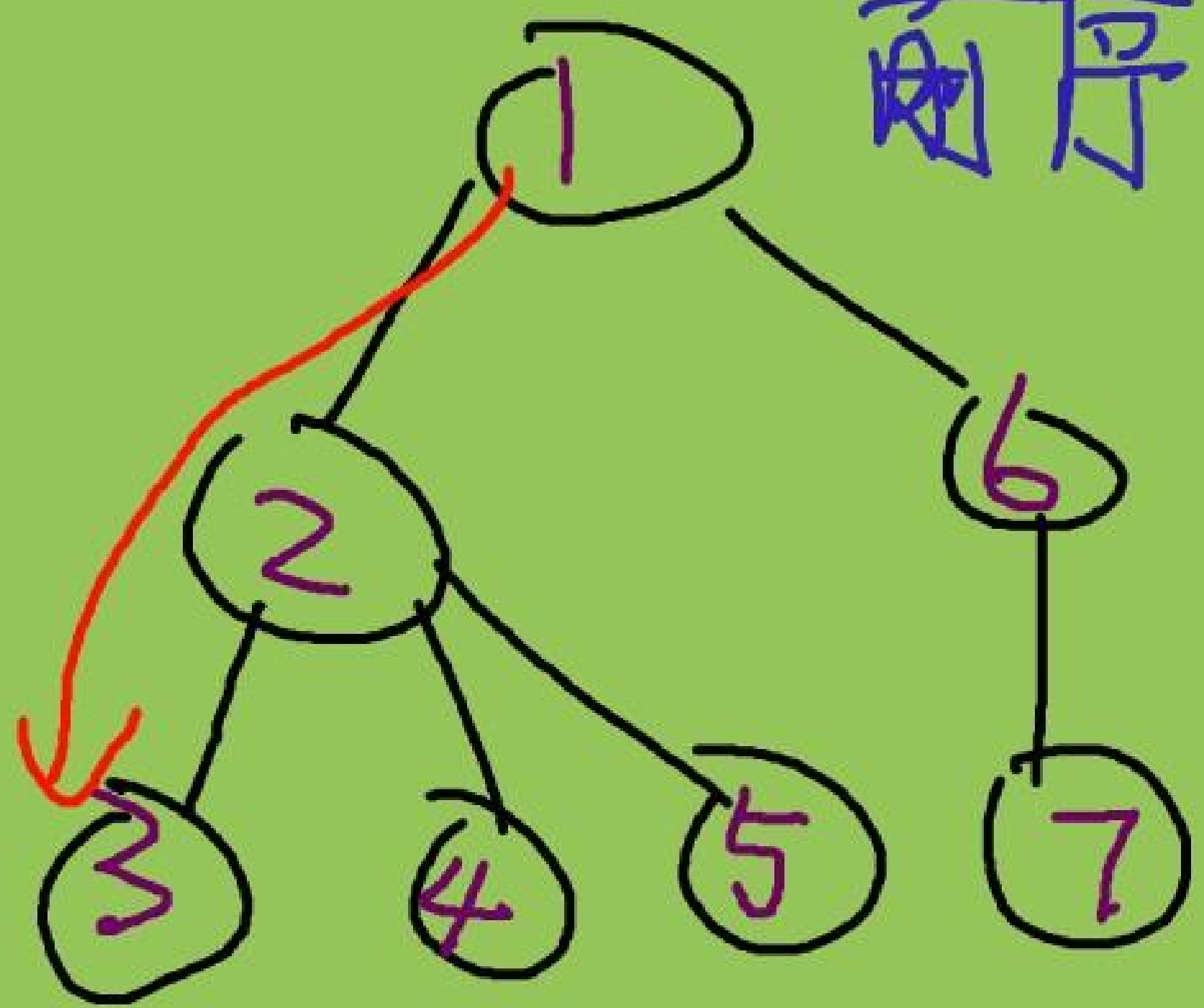


叔

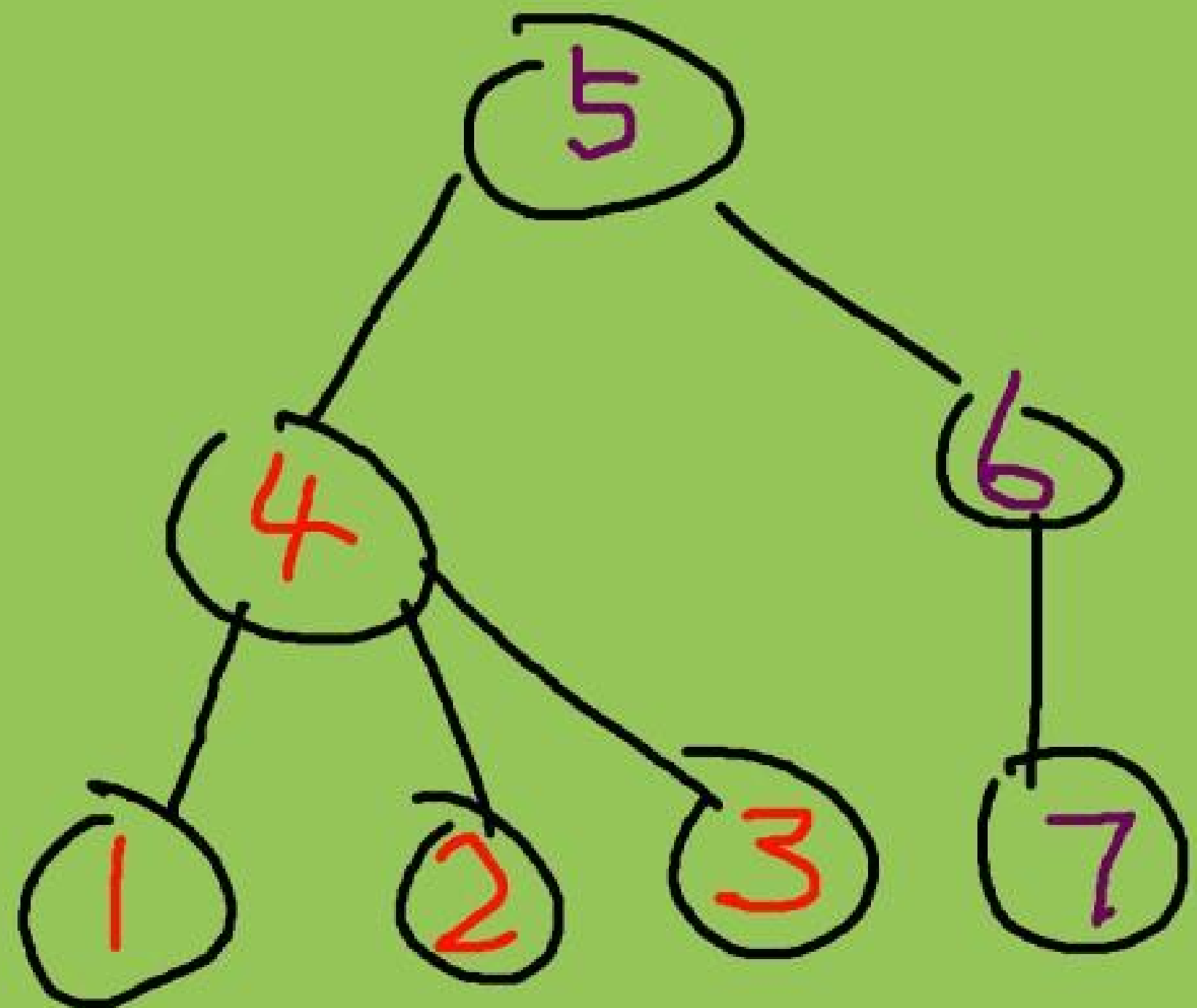
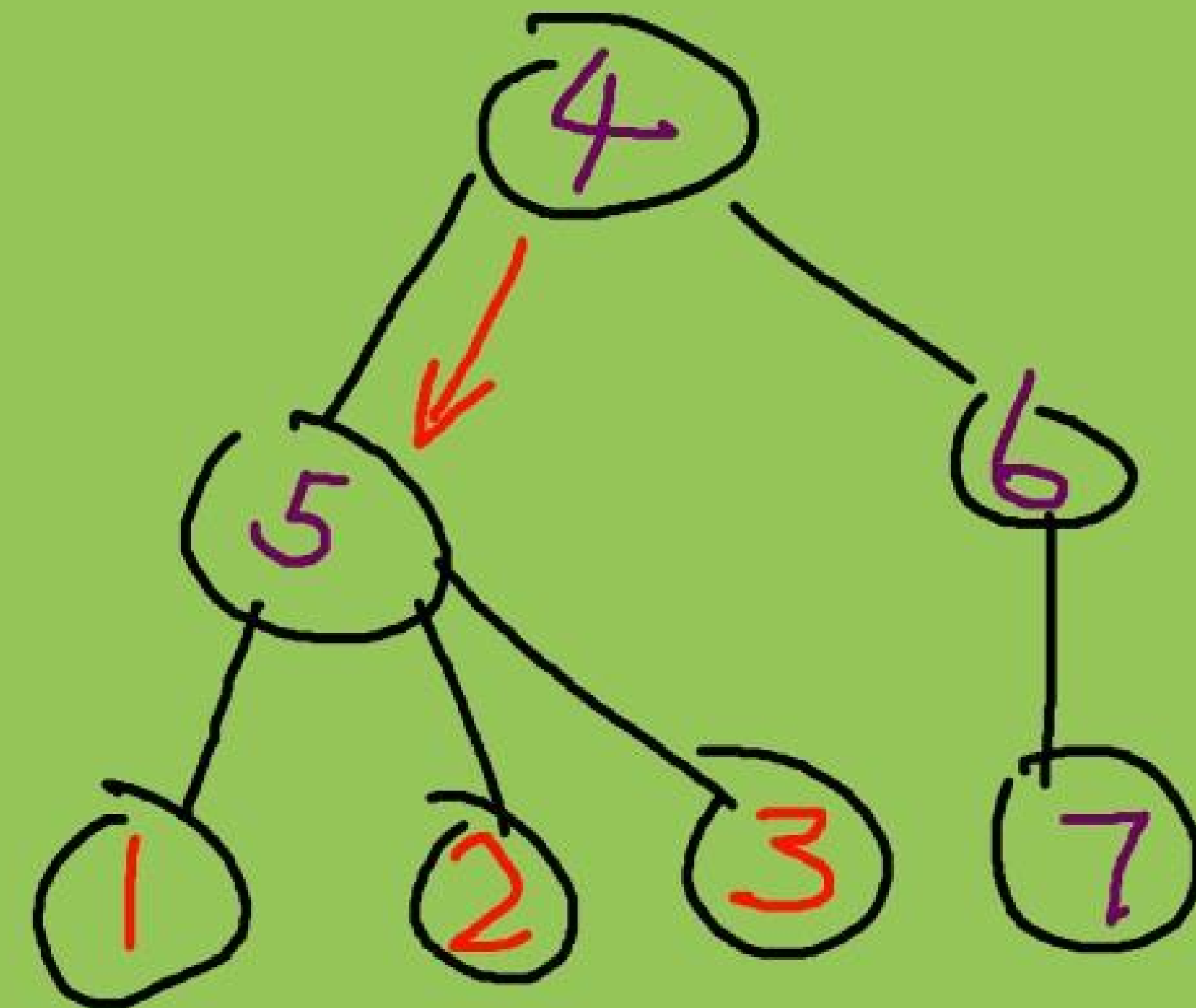




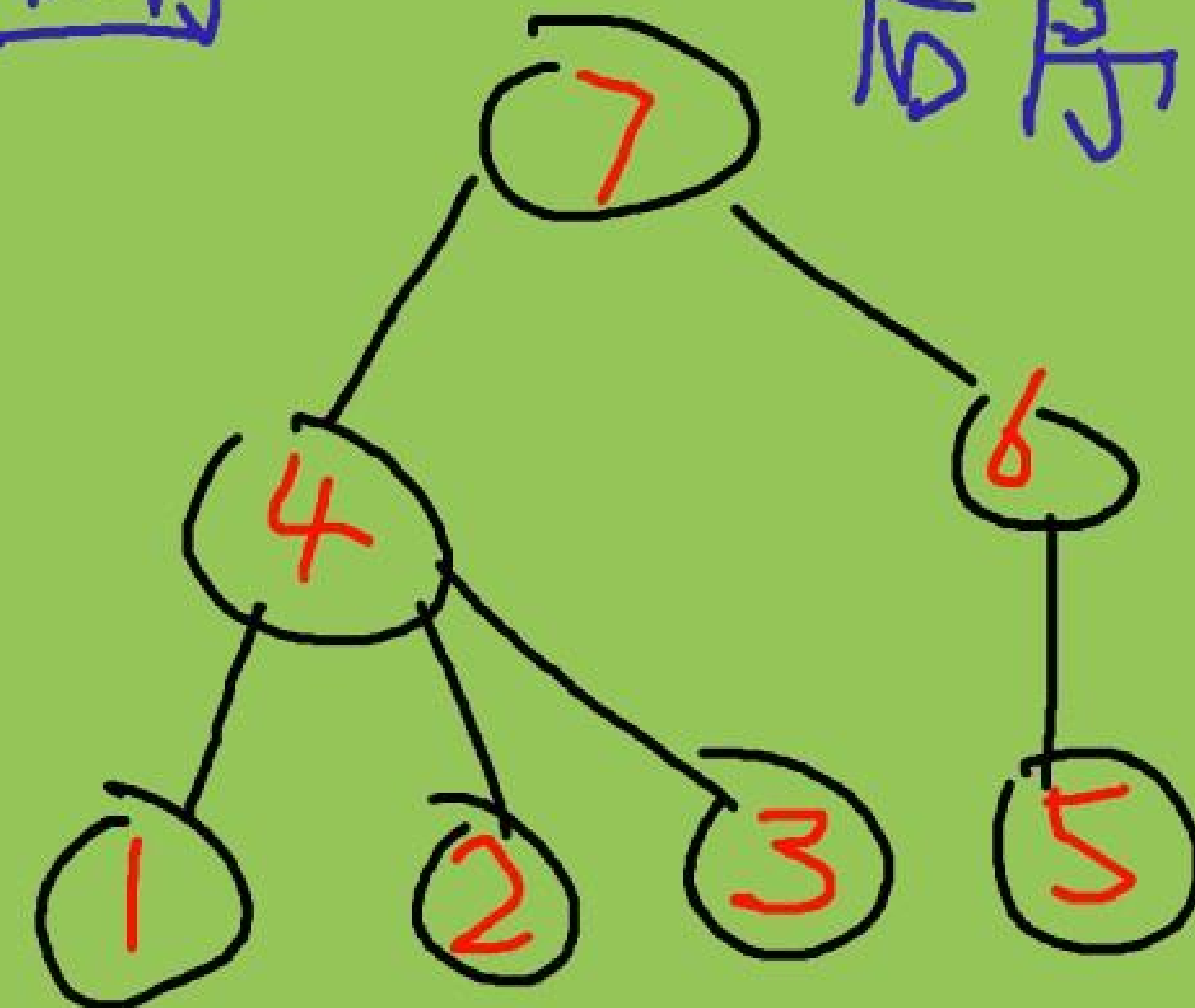
前序



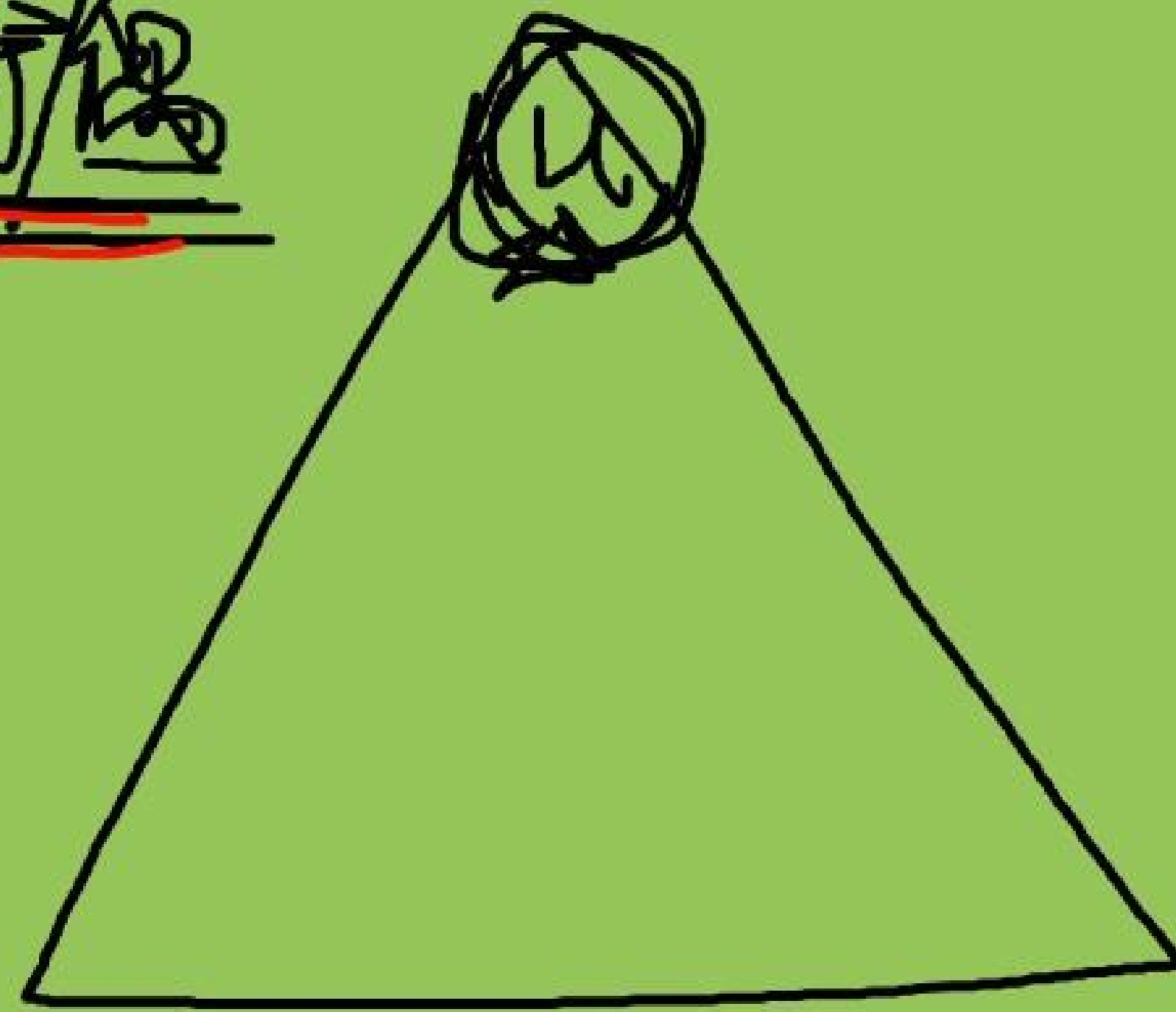
后序



|||



已奇偶



u子树

$f_0[u]$

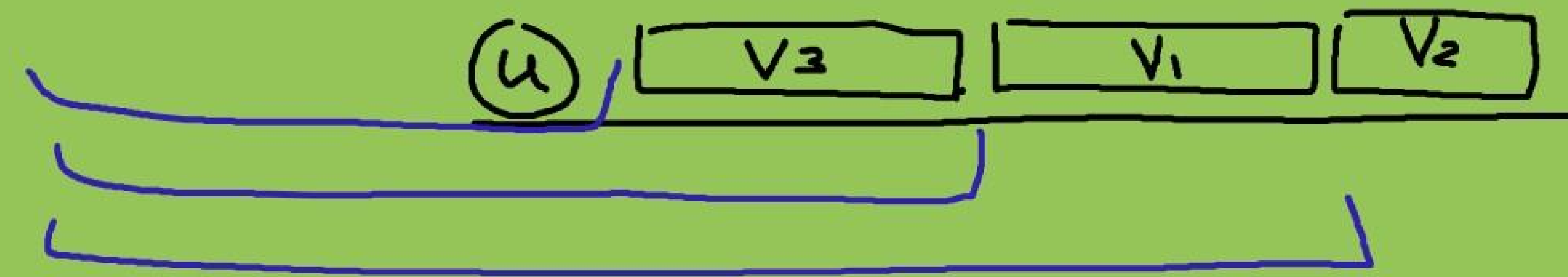
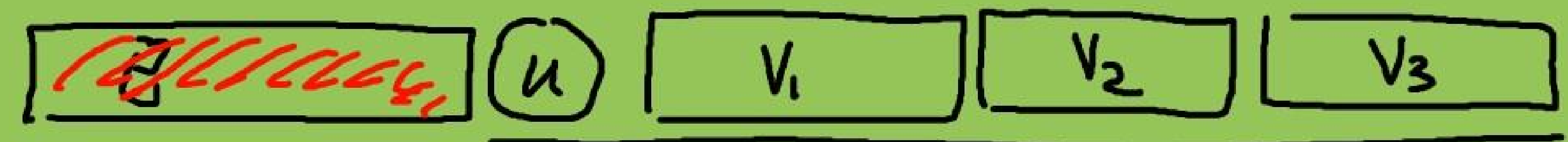
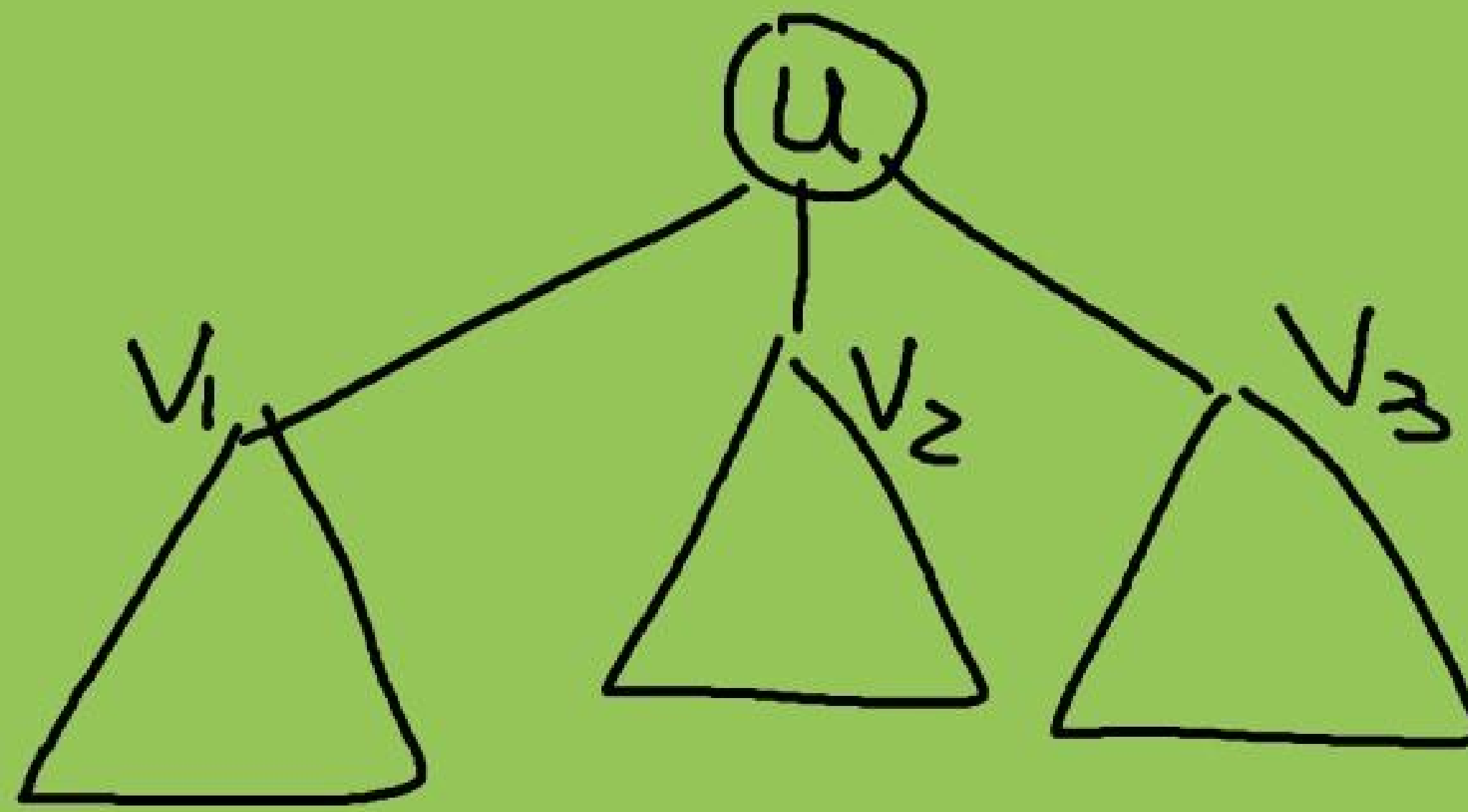
已偶  
u是奇

$f_1[u]$

已奇 u是偶

问题: 儿子顺序

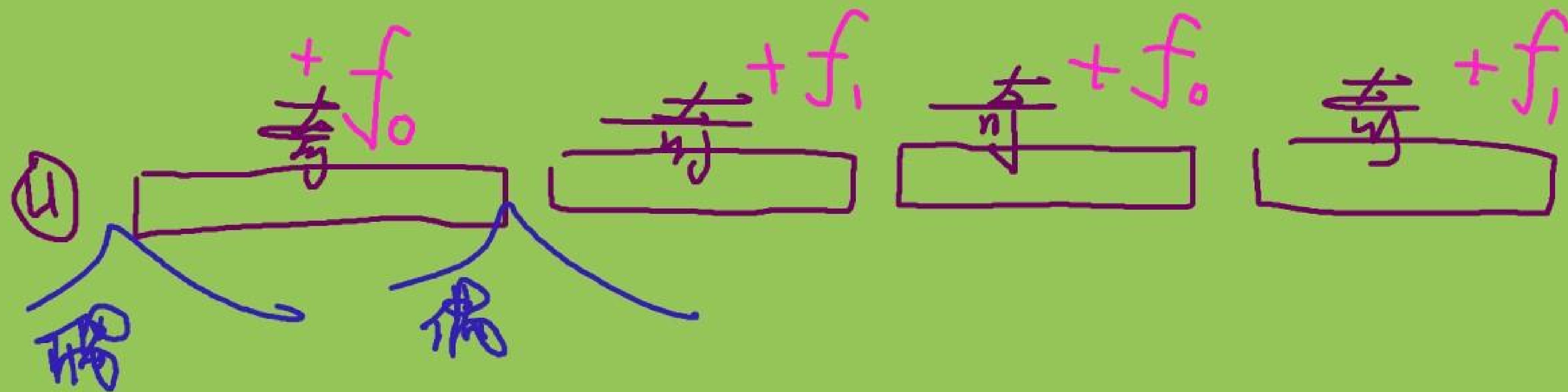
$S[V_i]$  有





(1) 儿子的  $S[v_i]$  全偶 顺序无关

(2) 有奇



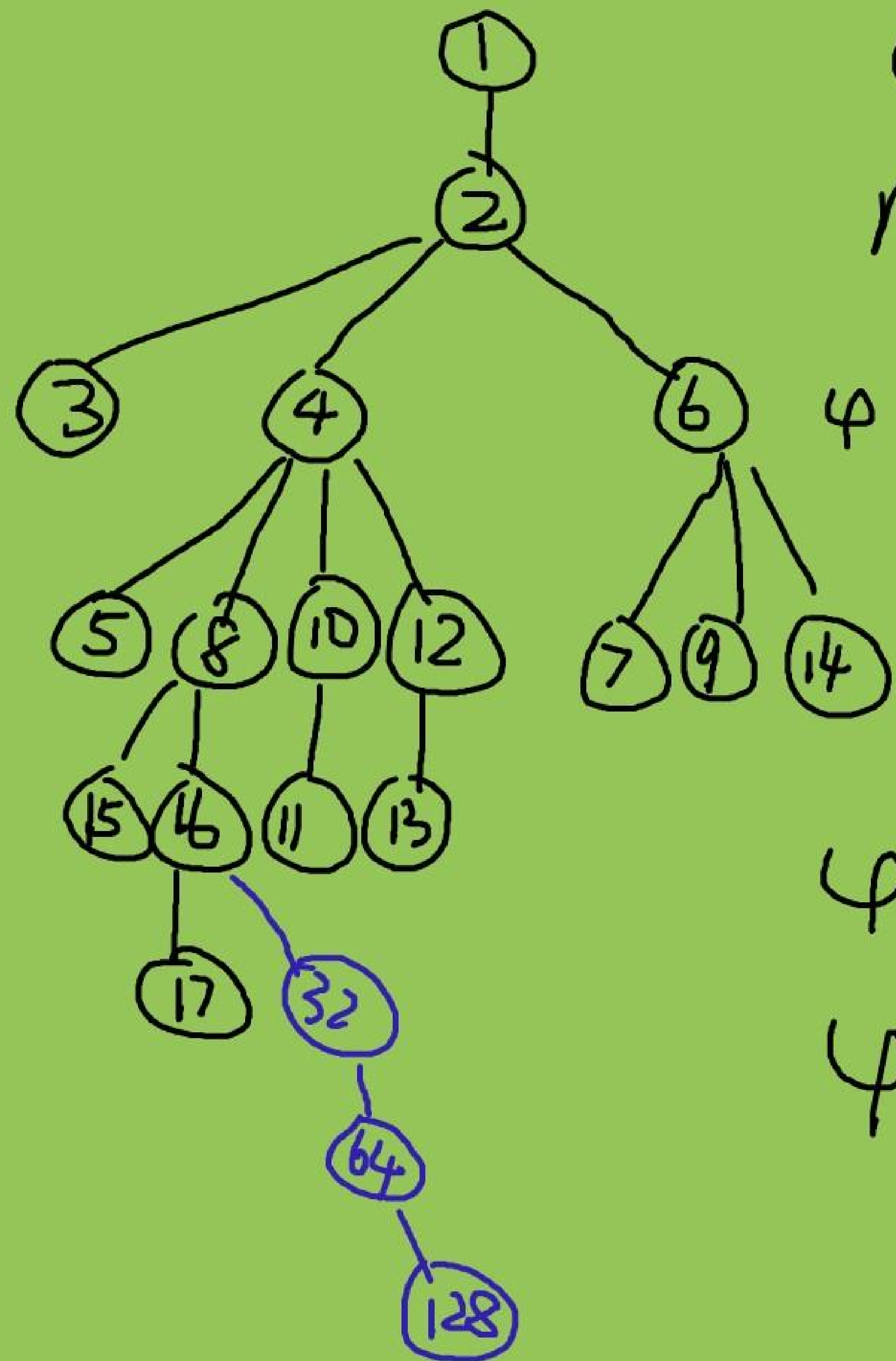
偶儿子  $f_0$   $f_1$  选  $\min(f_0, f_1)$

奇儿子  $f_0$  和  $f_1$  各选多少个 ✓

先全  $f_0$  再调  $+ = (f_1 - f_0)$   
 $\rightarrow$  最小的  $k$  个

全  $f_1$   
 全  $\min$

$O(n \log n)$   
 sort ✓  
 nth\_element ✓  
 $O(n)$



$$p_1 = 2$$

$$n = p_1^{q_1} p_2^{q_2} \dots p_k^{q_k}$$

$$\varphi = (p_1^{q_1-1} p_1^{q_1-1} \dots p_k^{q_k-1}) \dots$$

$$\varphi(1) = 1$$

$$\varphi(n) \in [1, n-1]$$

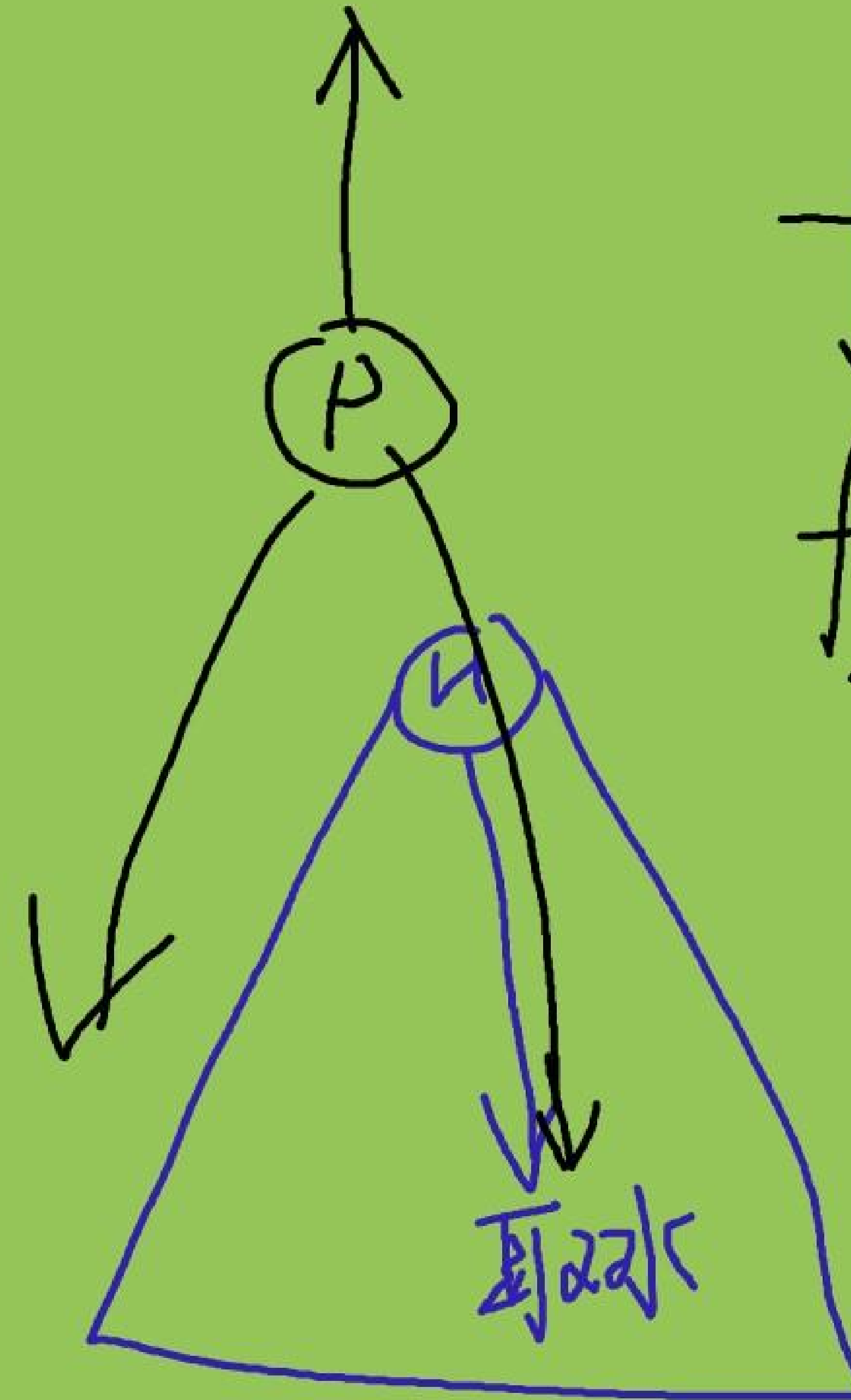
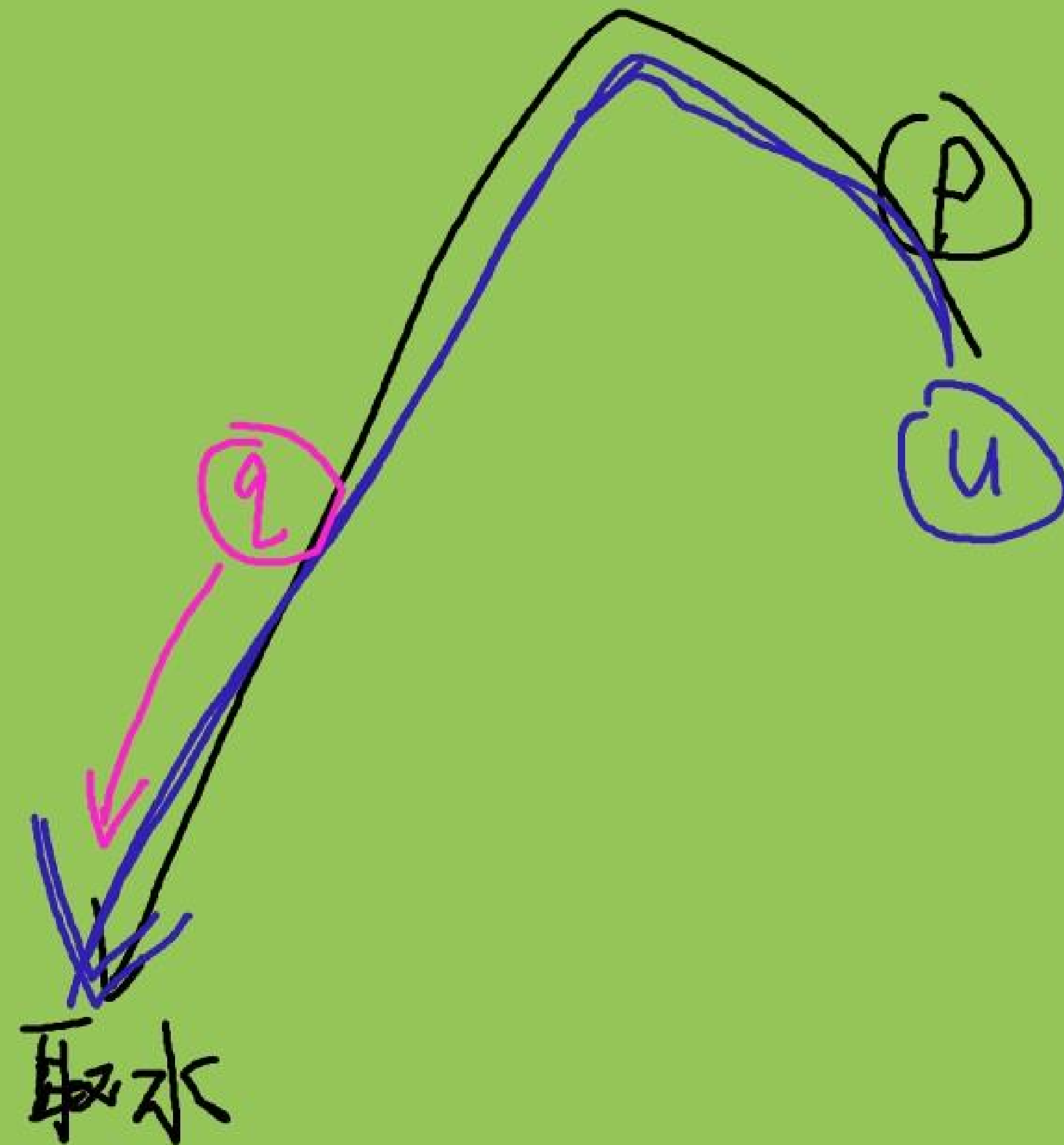
$$2, 4, 6 : + C_0 \times 3$$

$$1, 3, 5, 7, 9 : + C_1 \times 6$$

$$\varphi(\text{奇}) = \text{偶}$$

$$\varphi(\text{偶}) \leq \frac{n}{2}$$



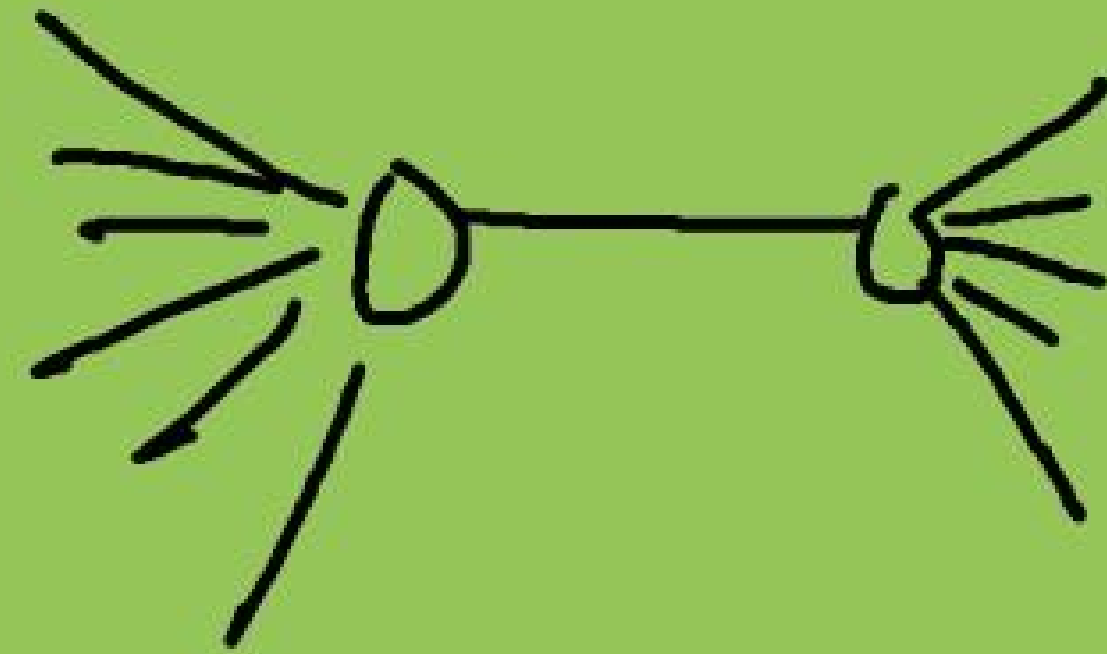


$f_1[u][d]$   $d \geq 1$  外圈  
 $f_2[u][d]$   $d \geq 0$  内圈

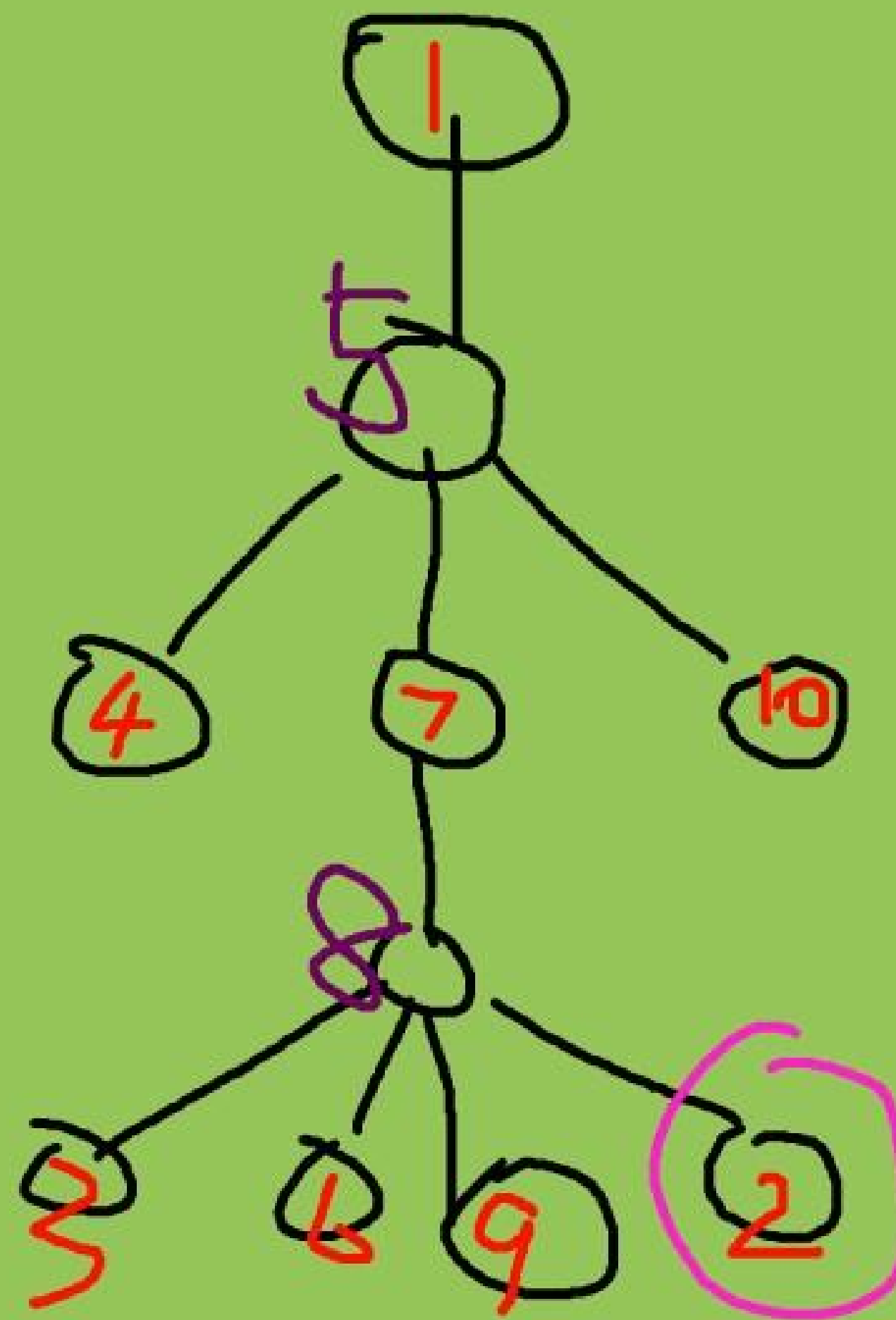
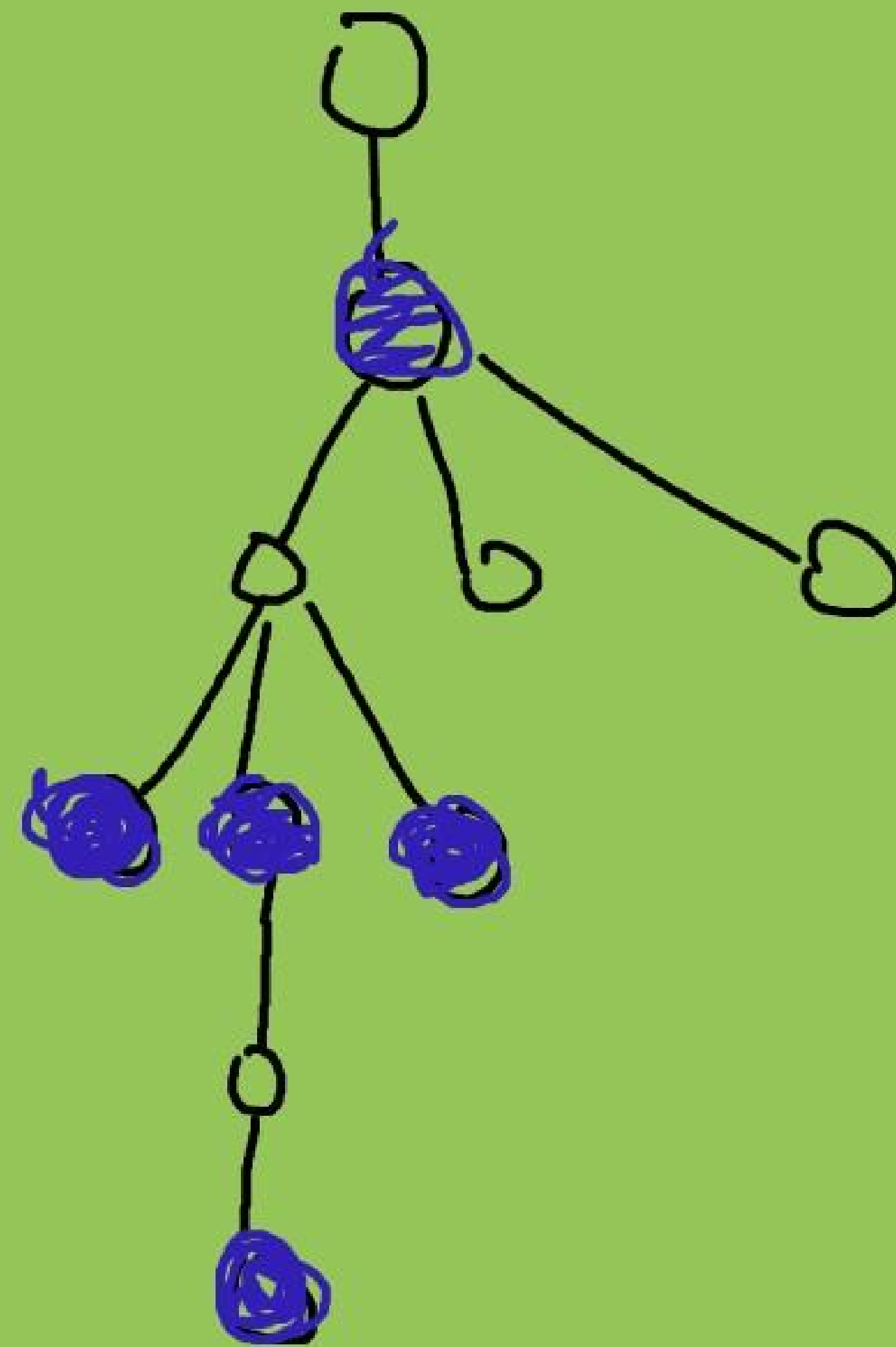


度=3

$O(n)$  对



$O(n^2)$  对



1~10

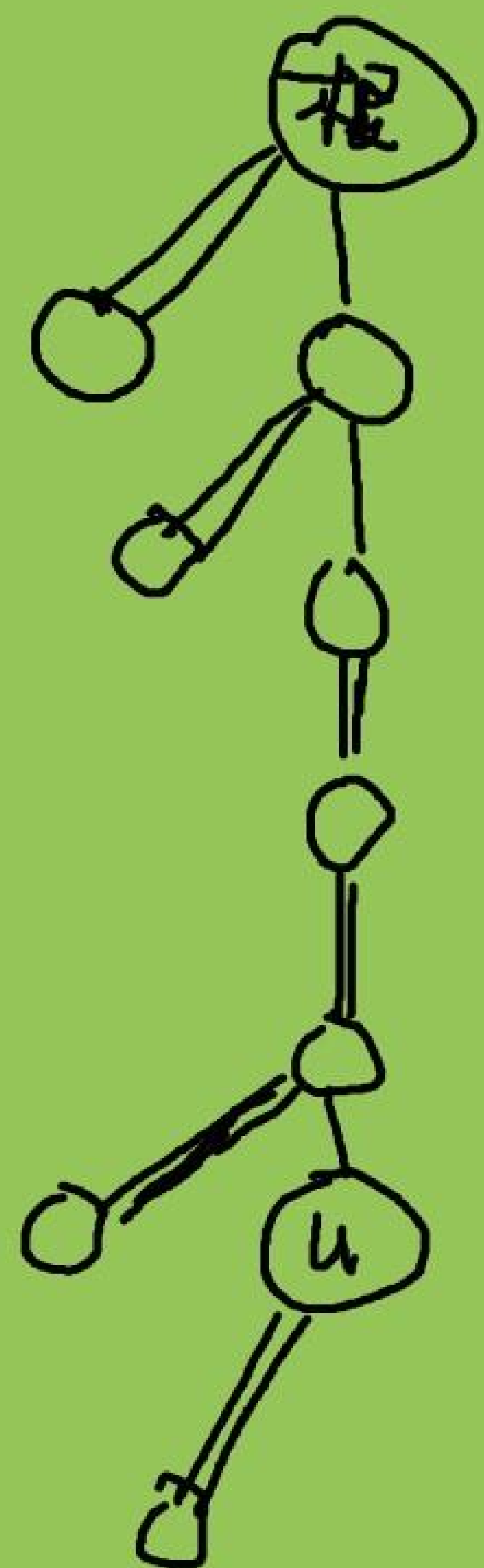
红(奇层) 8个  
紫偶层 2个

$3k+1$   
 $3k$

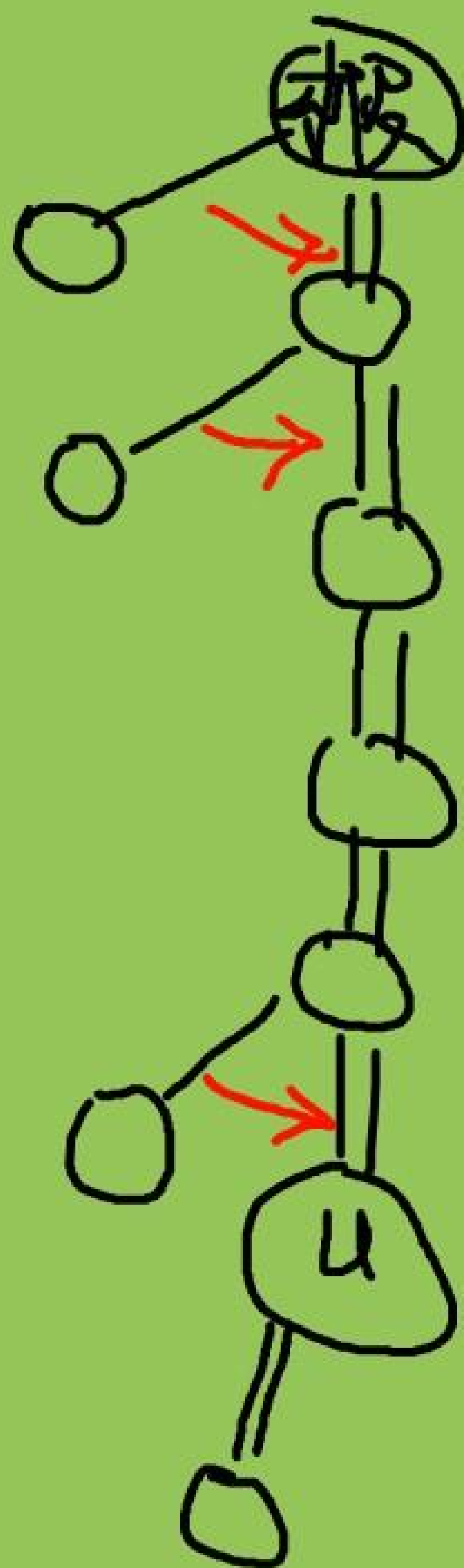
$3k+2$   
 $3k$

$3k+2$   
 $3k+1$   
 $3k$   
 $> \frac{2}{3}n$   
 $< \frac{1}{3}n$



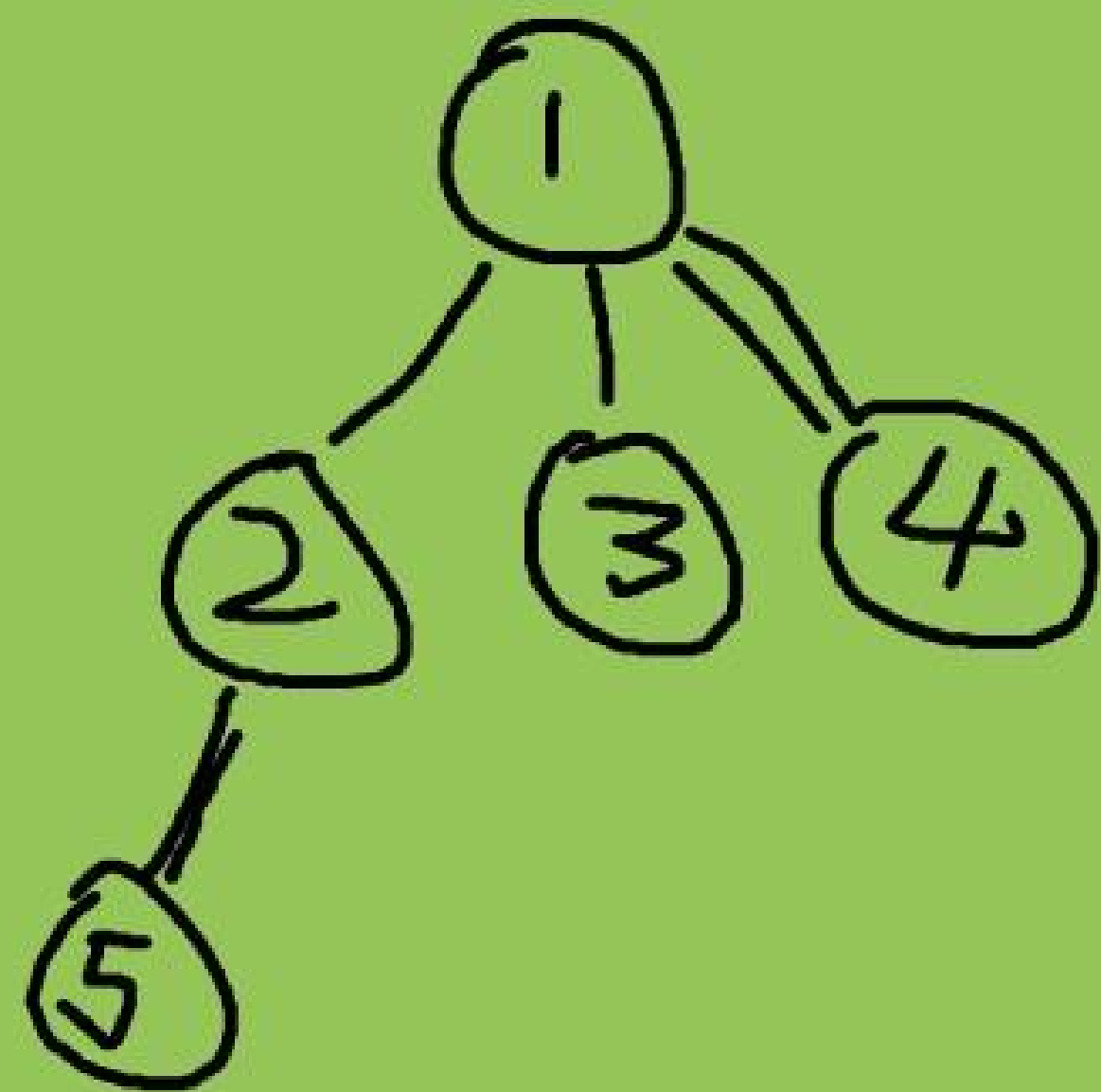


$\text{Access}(u)$



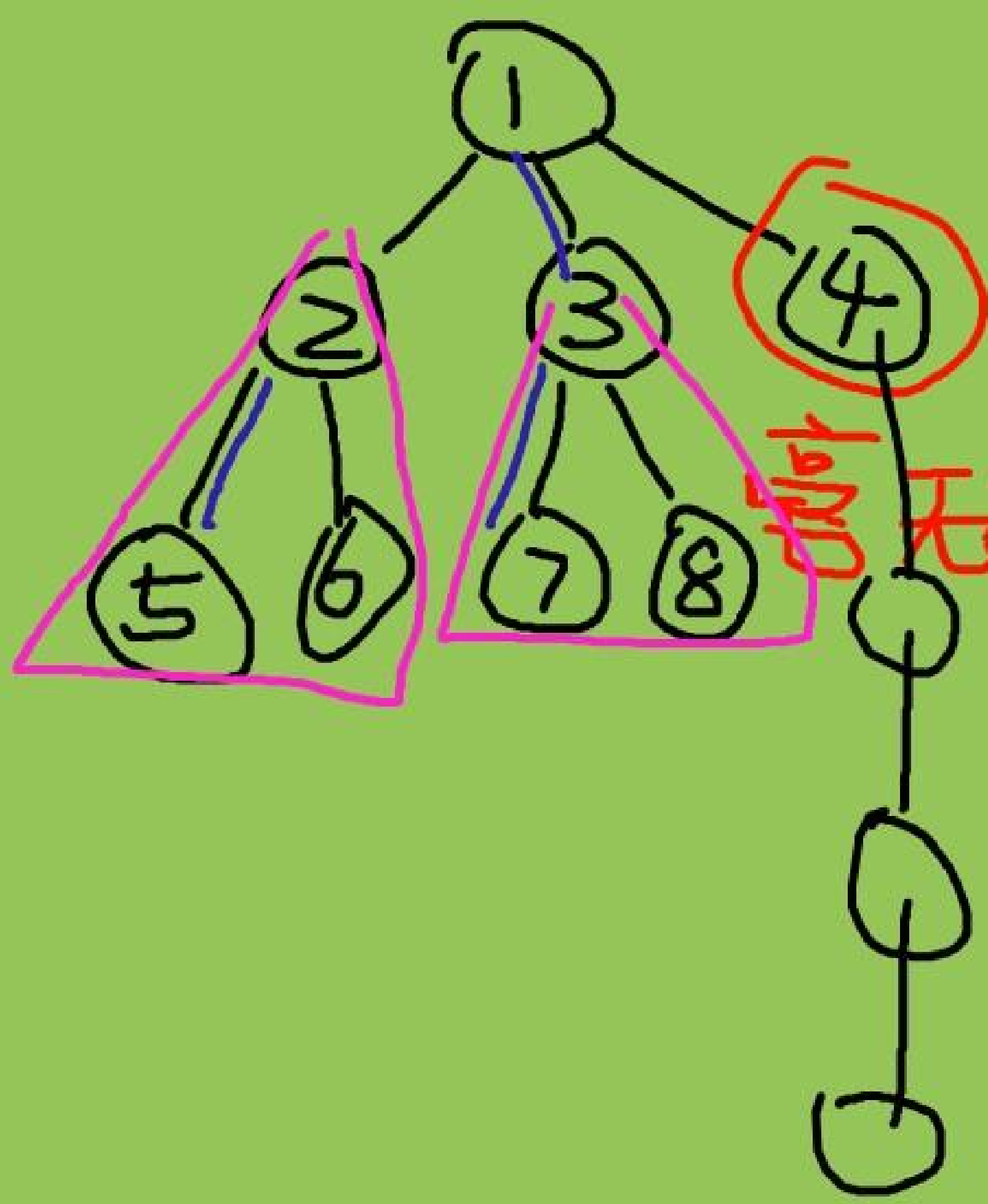
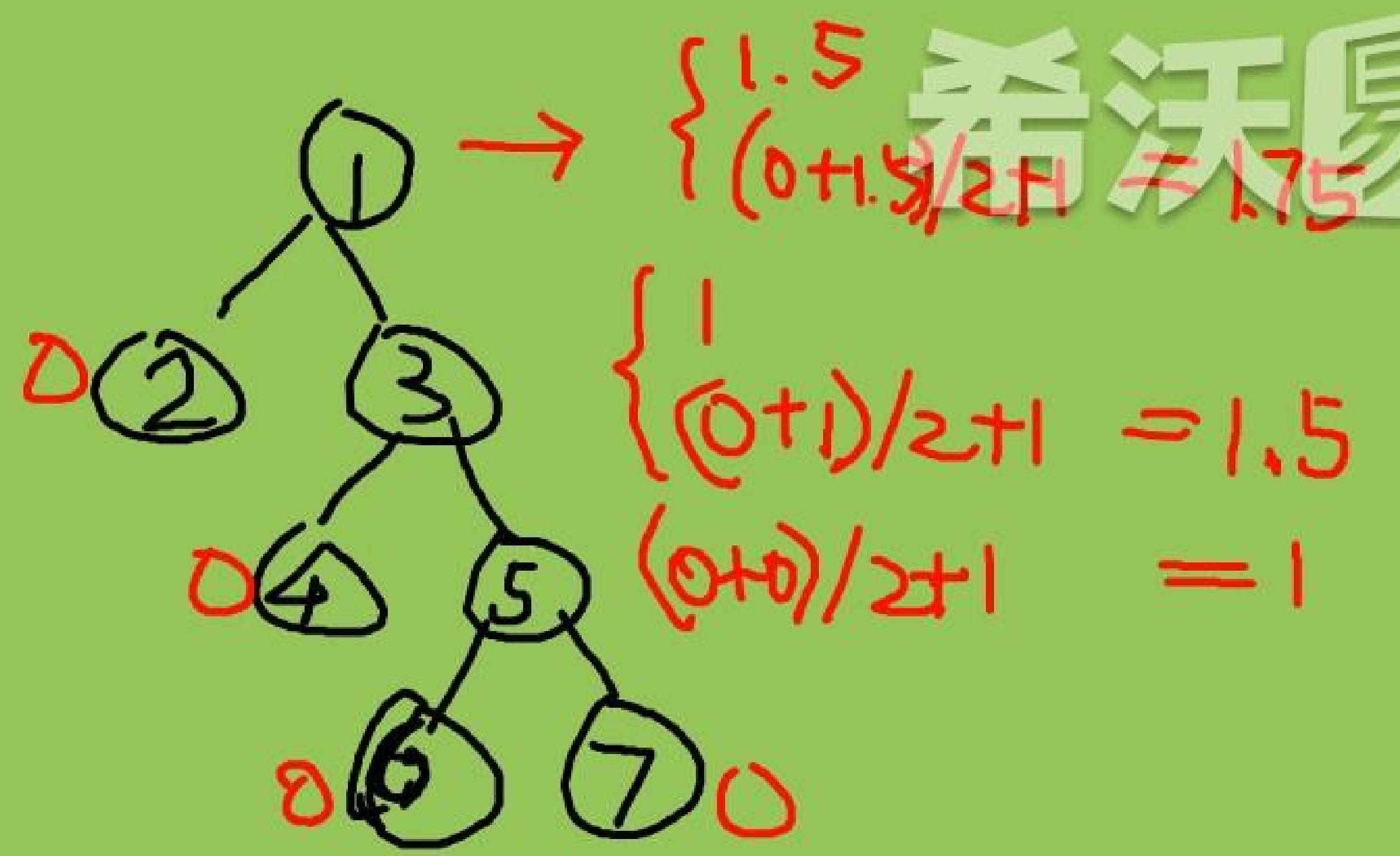
3次切树





$m=1$   
 $m=2$   
 3  
 4  
 ...  
 $\infty$

2次  
 +1次  
 +1次  
 +1次  
 ...  
 平均 1次



$m=1$   
 $m=2$   
 $m=3$   
 4  
 5  
 6

2次  
 +2  
 +2  
 +2  
 +2  
 +2  
 +2



平均 2次

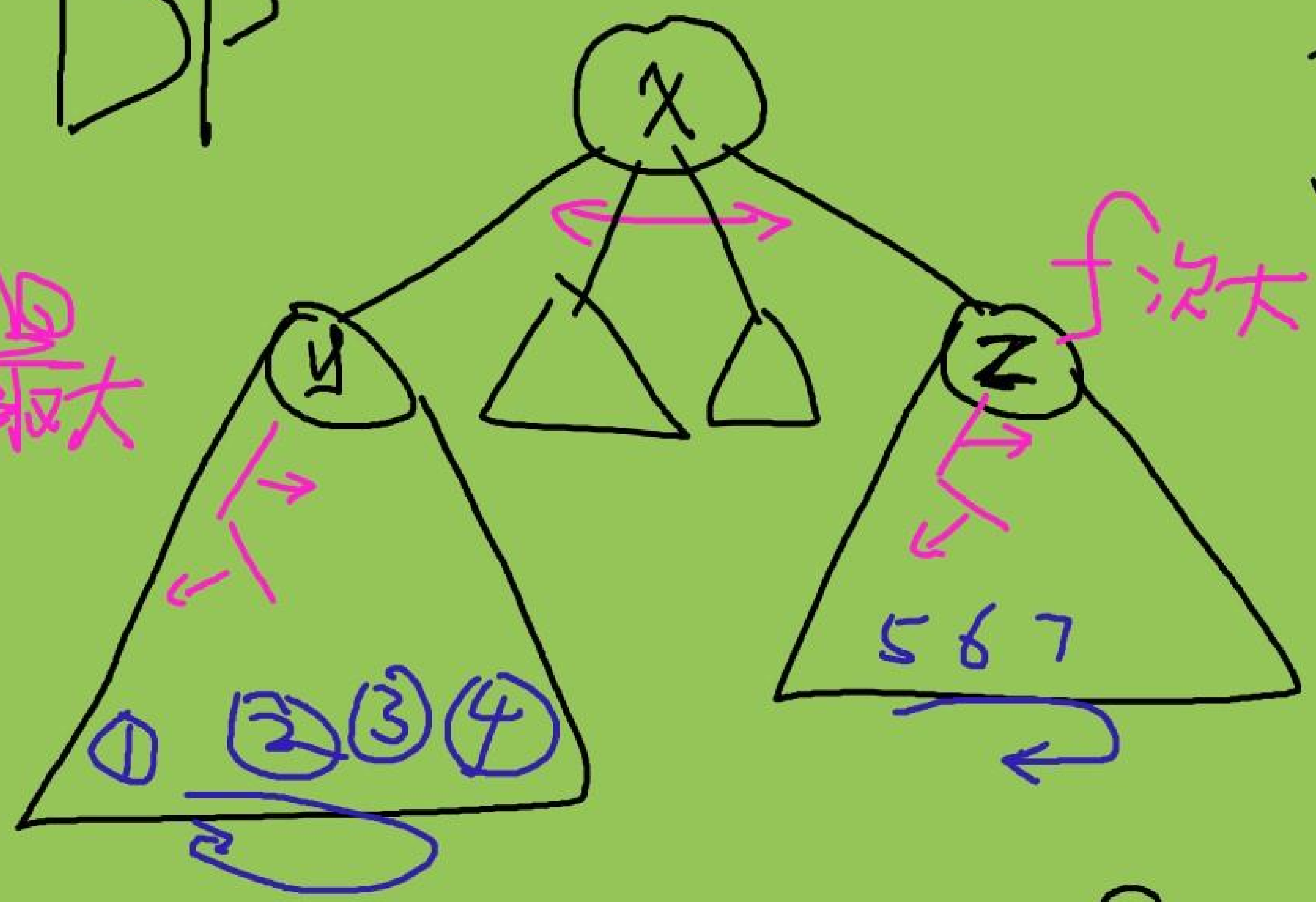


DP

$f[x]$ :  $x$ 为根时最优解

$f_{\text{最大}}$

$f_{\text{次大}}$

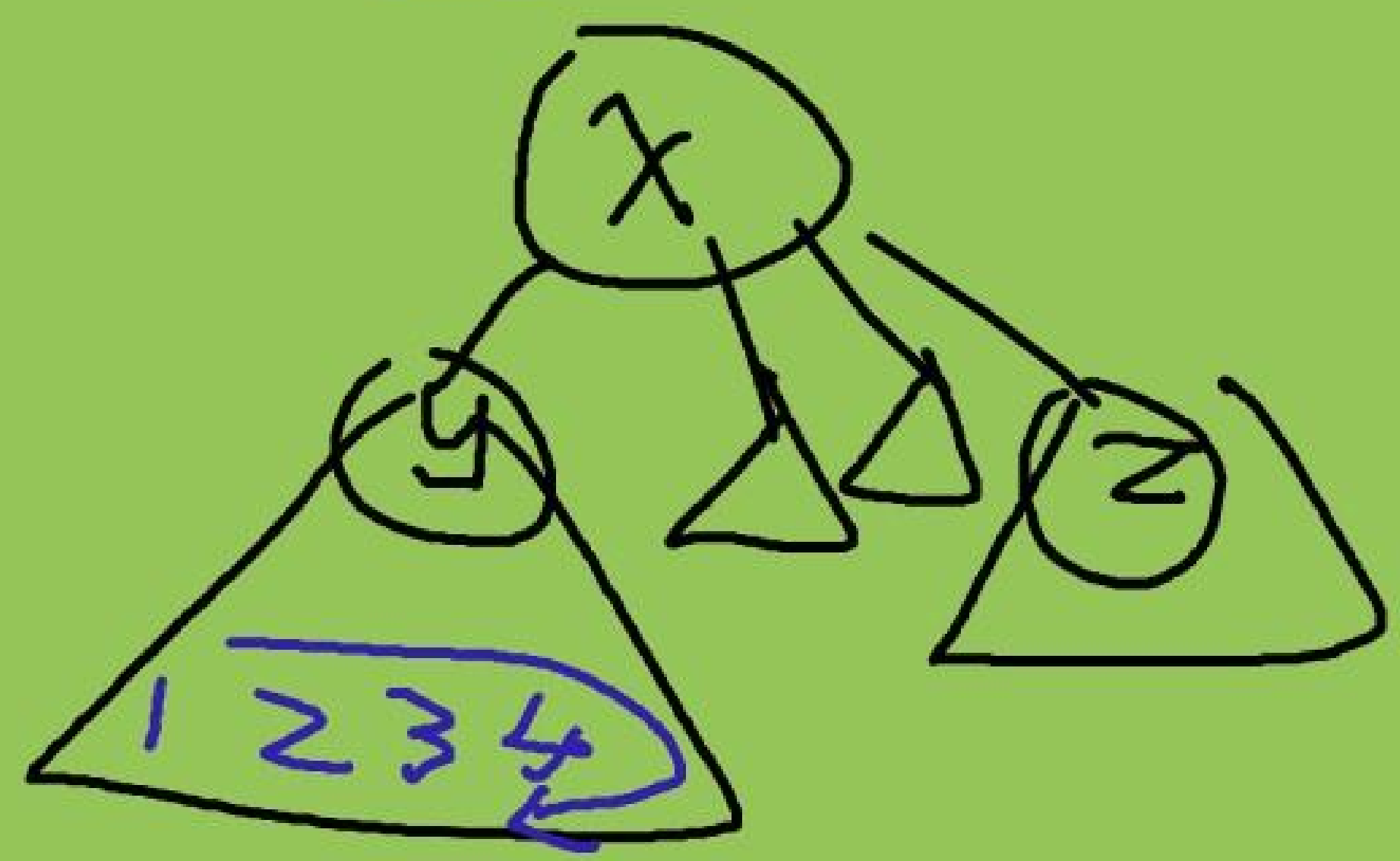


$y$ 最优: 1 2 3 4 ...

$z$ 最优: 5 6 7 ...

$x$ 可: 1 5 2 6 3 7 4 5 1 6 2 7 3 5

$$f[x] = \max \left\{ \frac{f[y] + f[z]}{2} + 1, f[y] \right\}$$



整. 0101011101 - - - 101

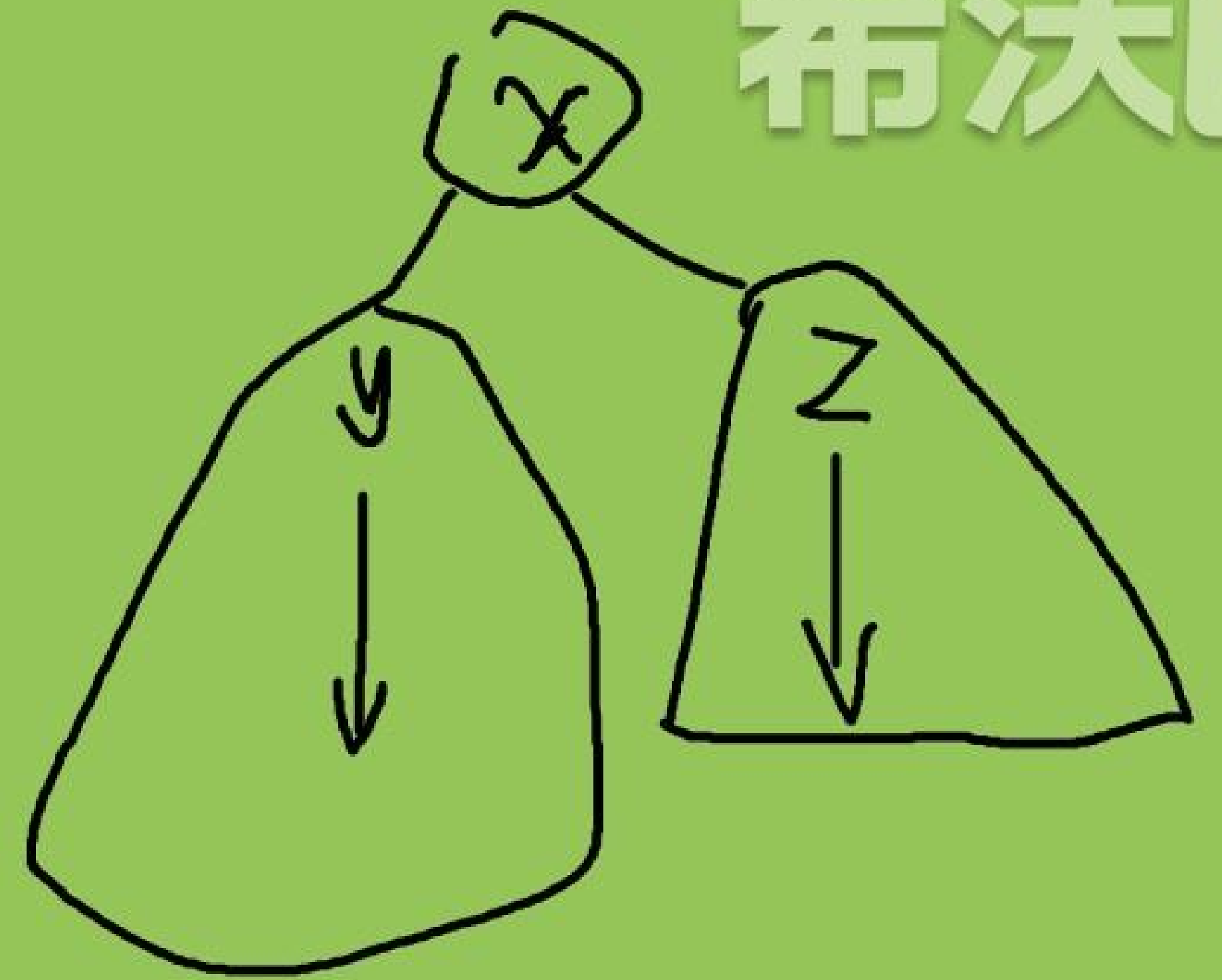
$len \leq h$

$f[y]$     $f[z]$

vector

比大小

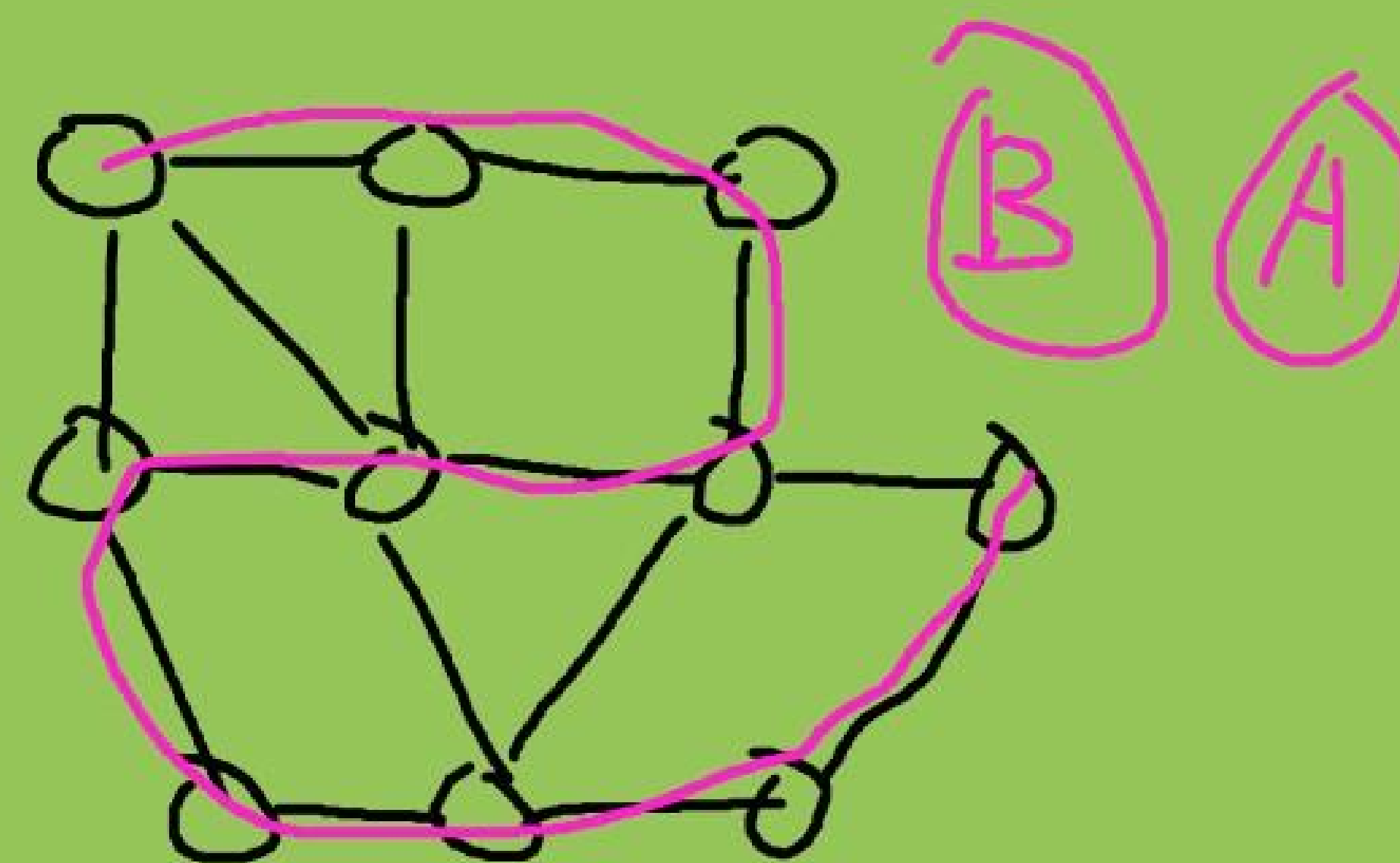
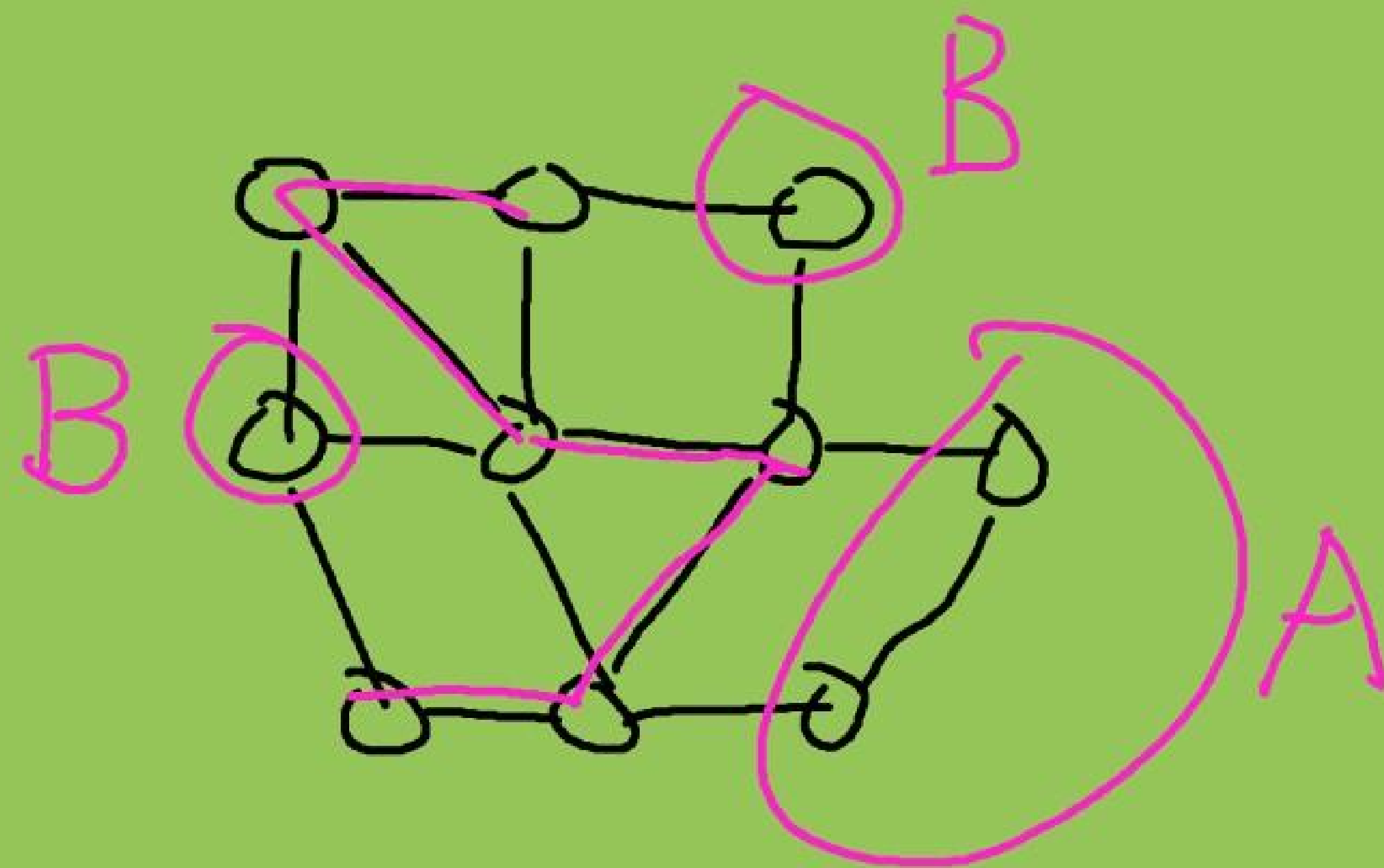
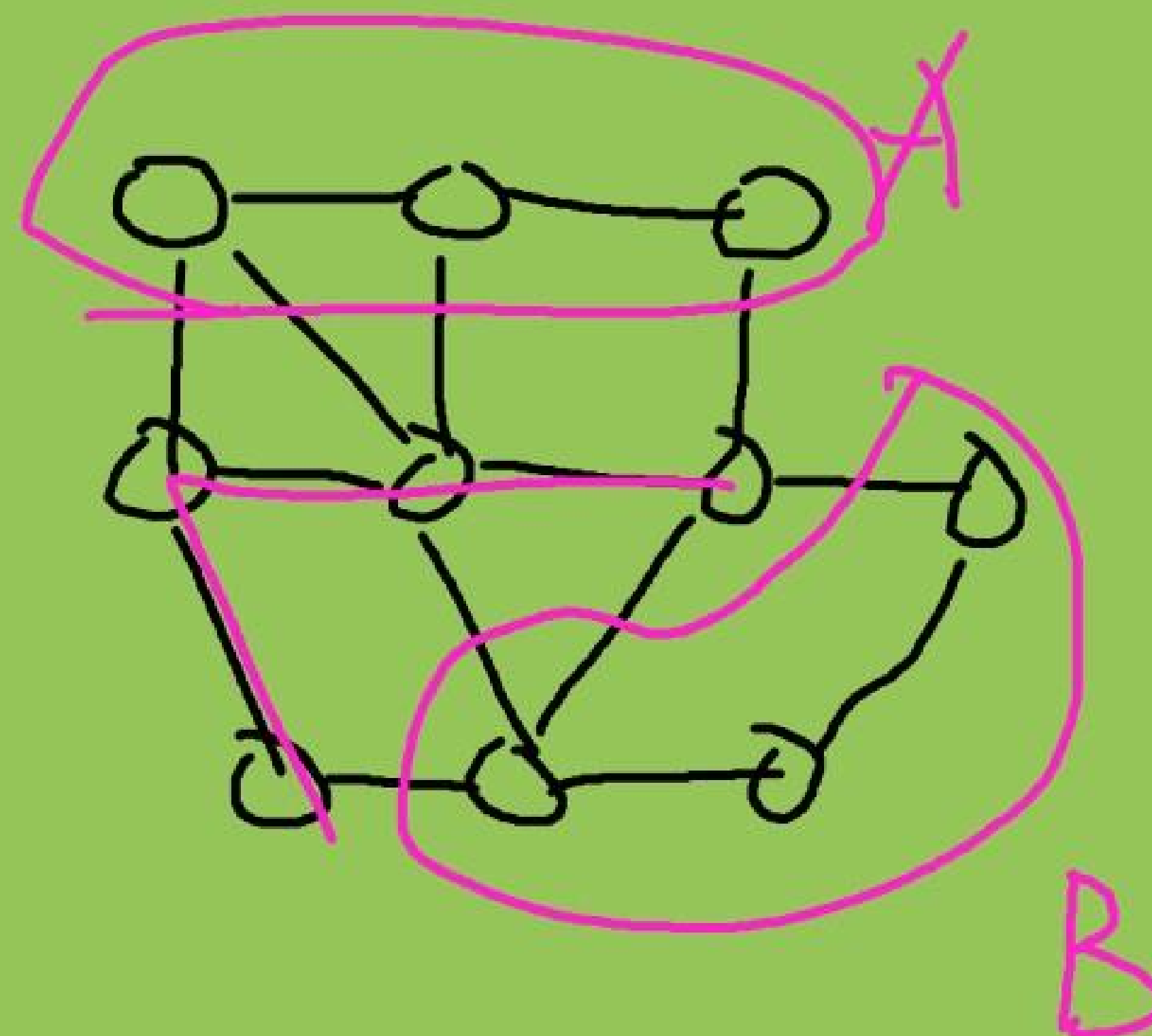
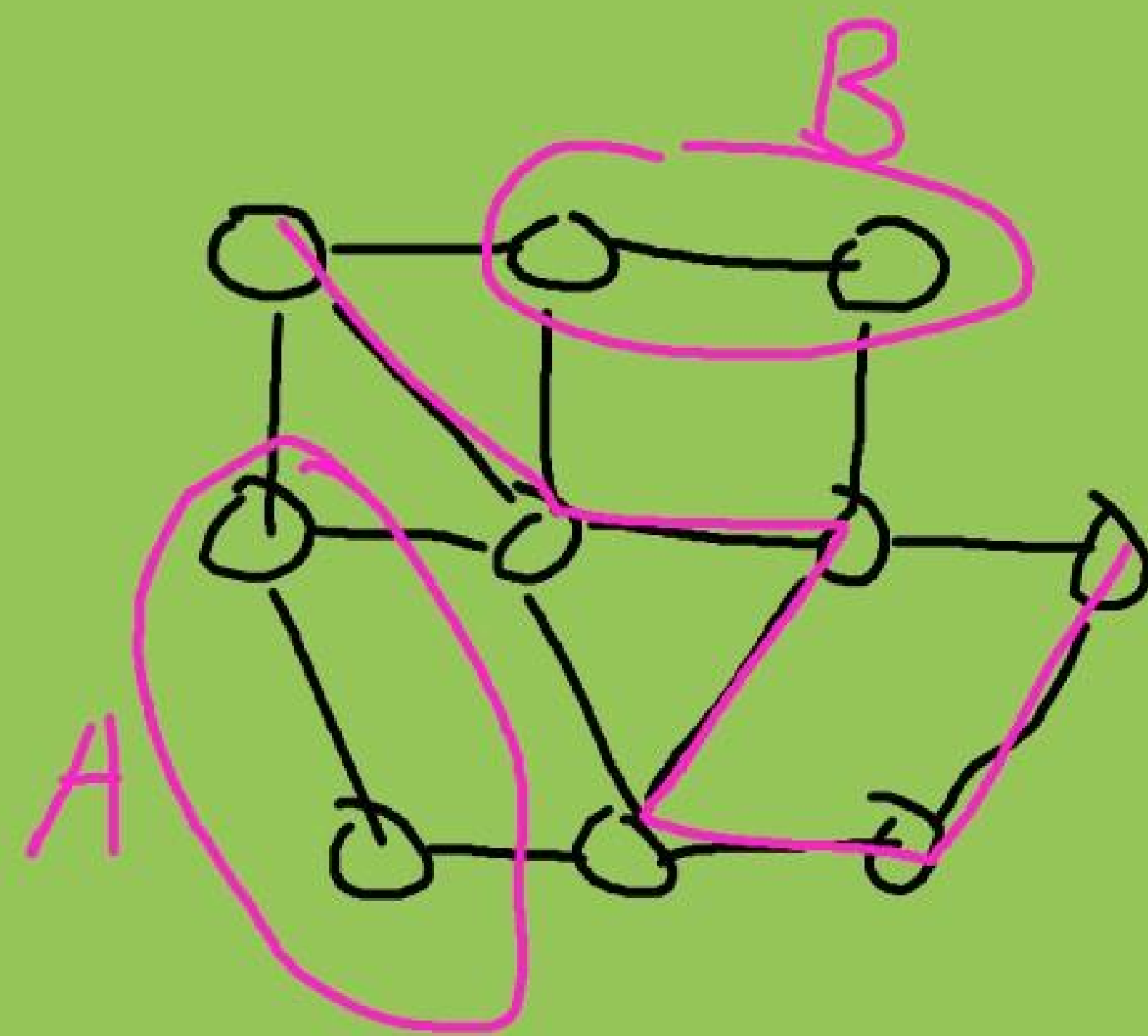
暴力



$tmp = f[y] + f[z]$    加   暴力

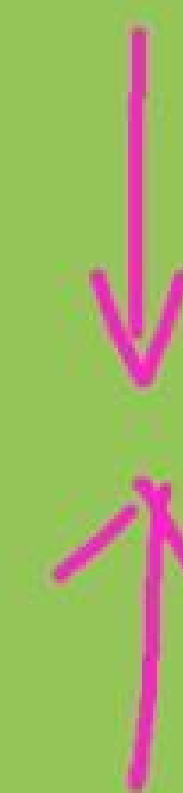
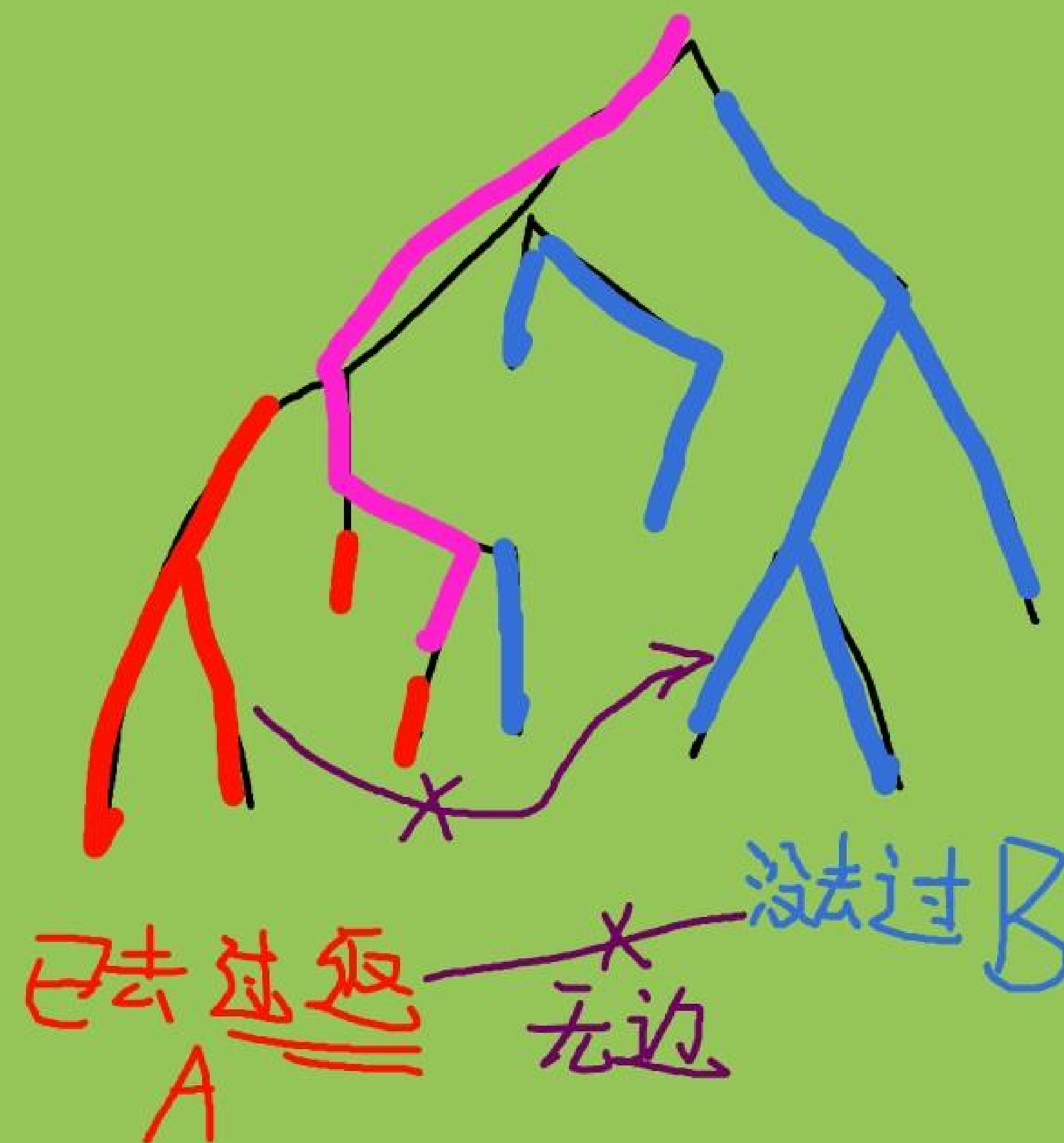
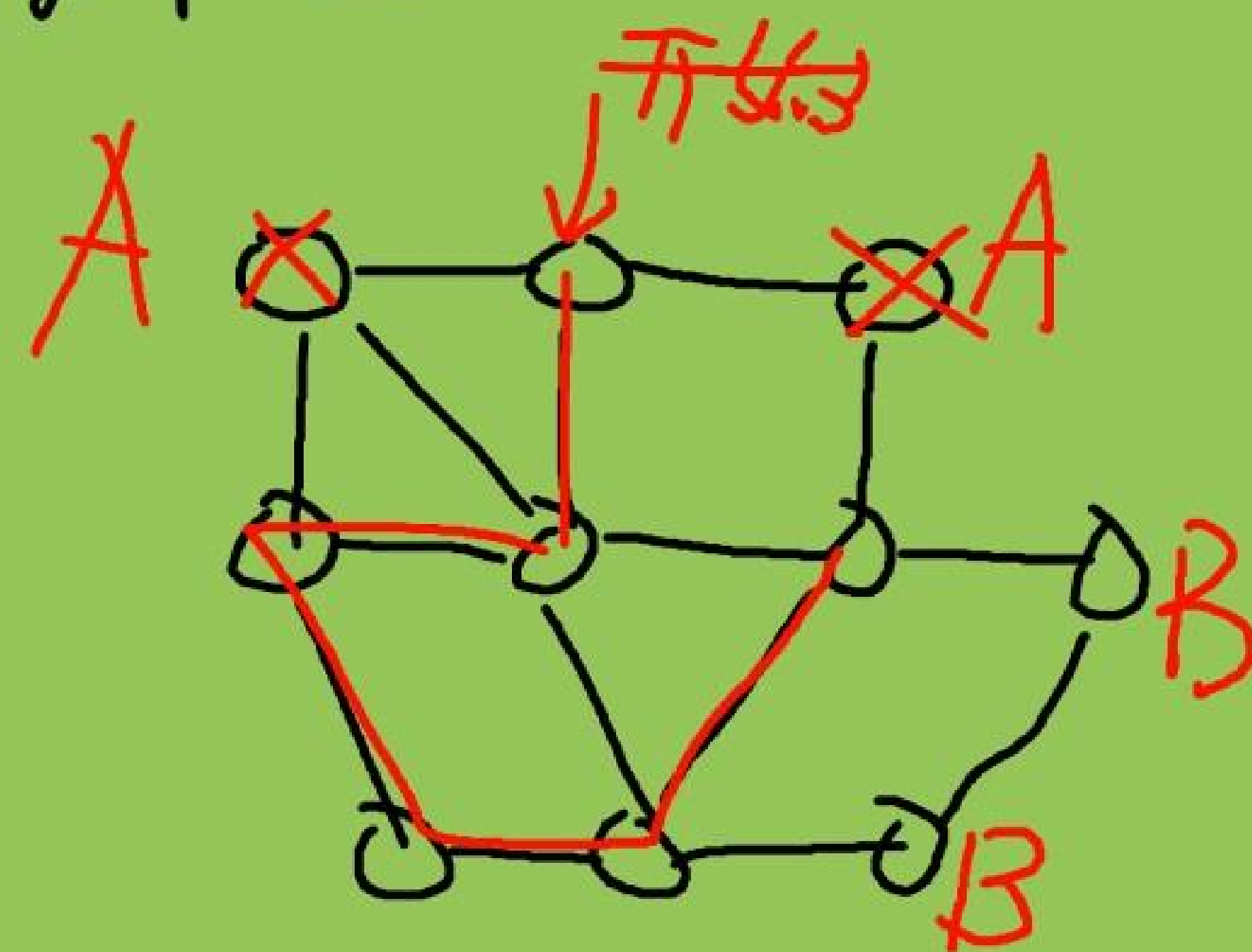
$f[x] = tmp / 2 + 1$    push-back    $O(1)$

$O(n \log n)$





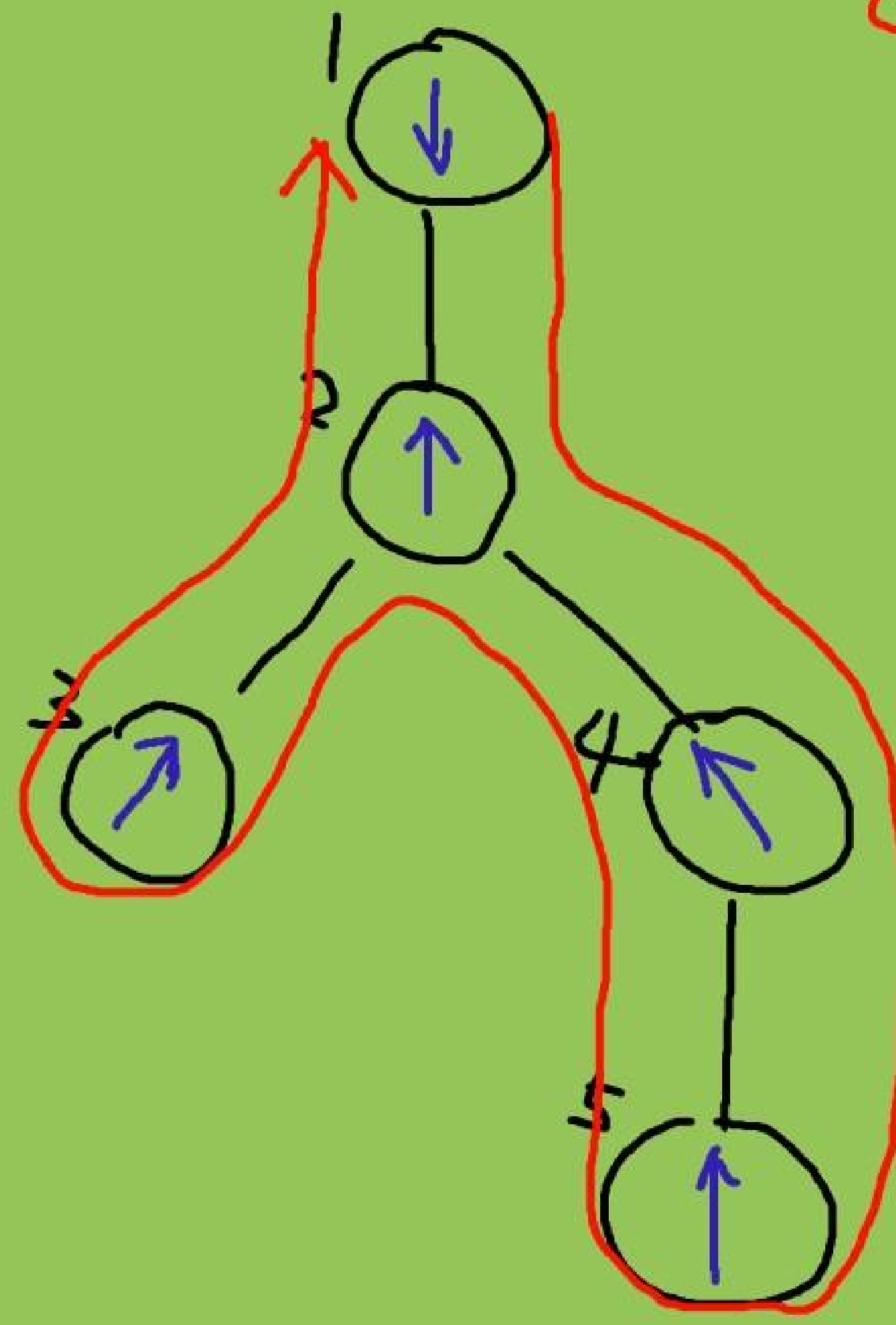
DFS



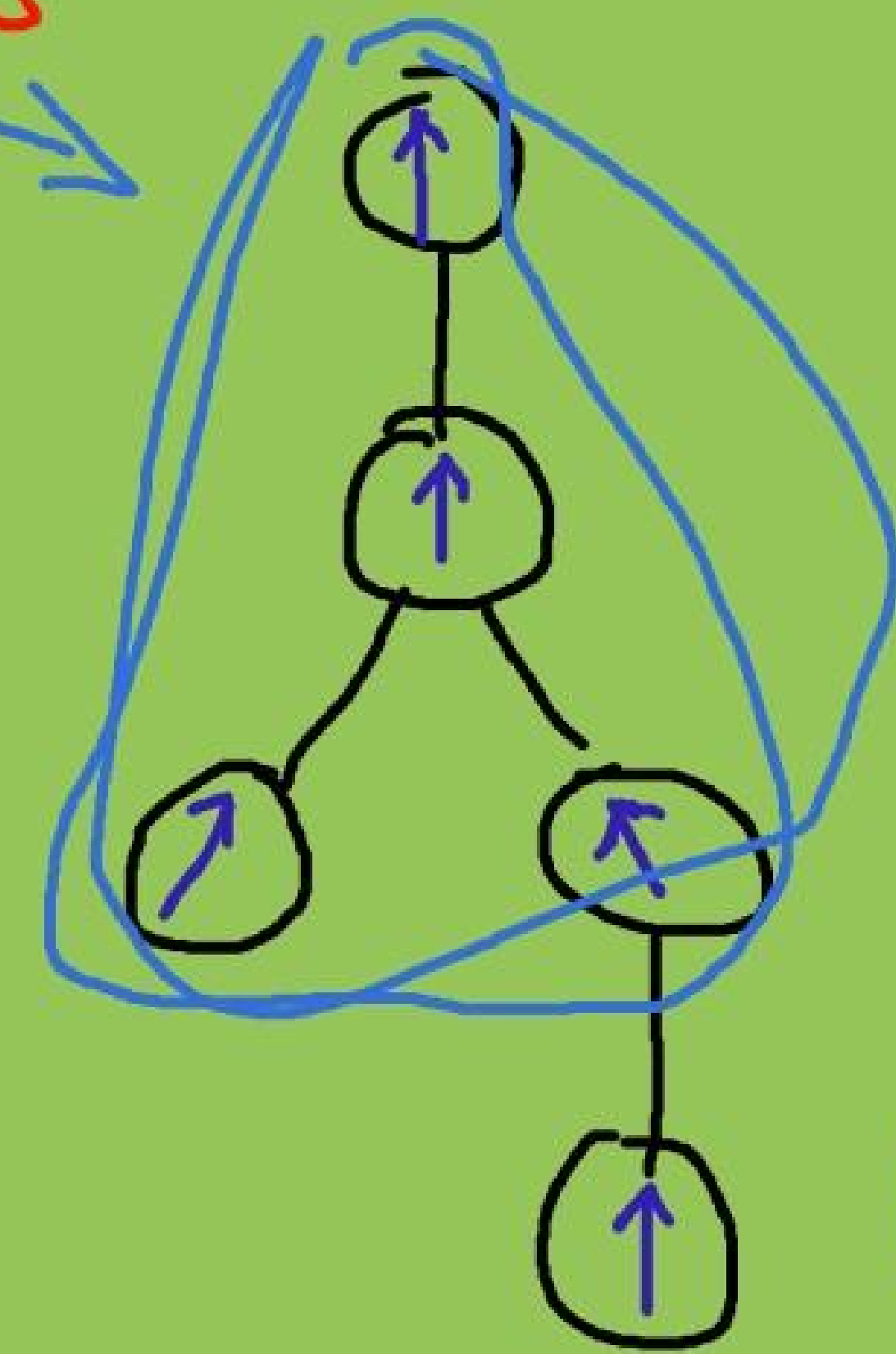
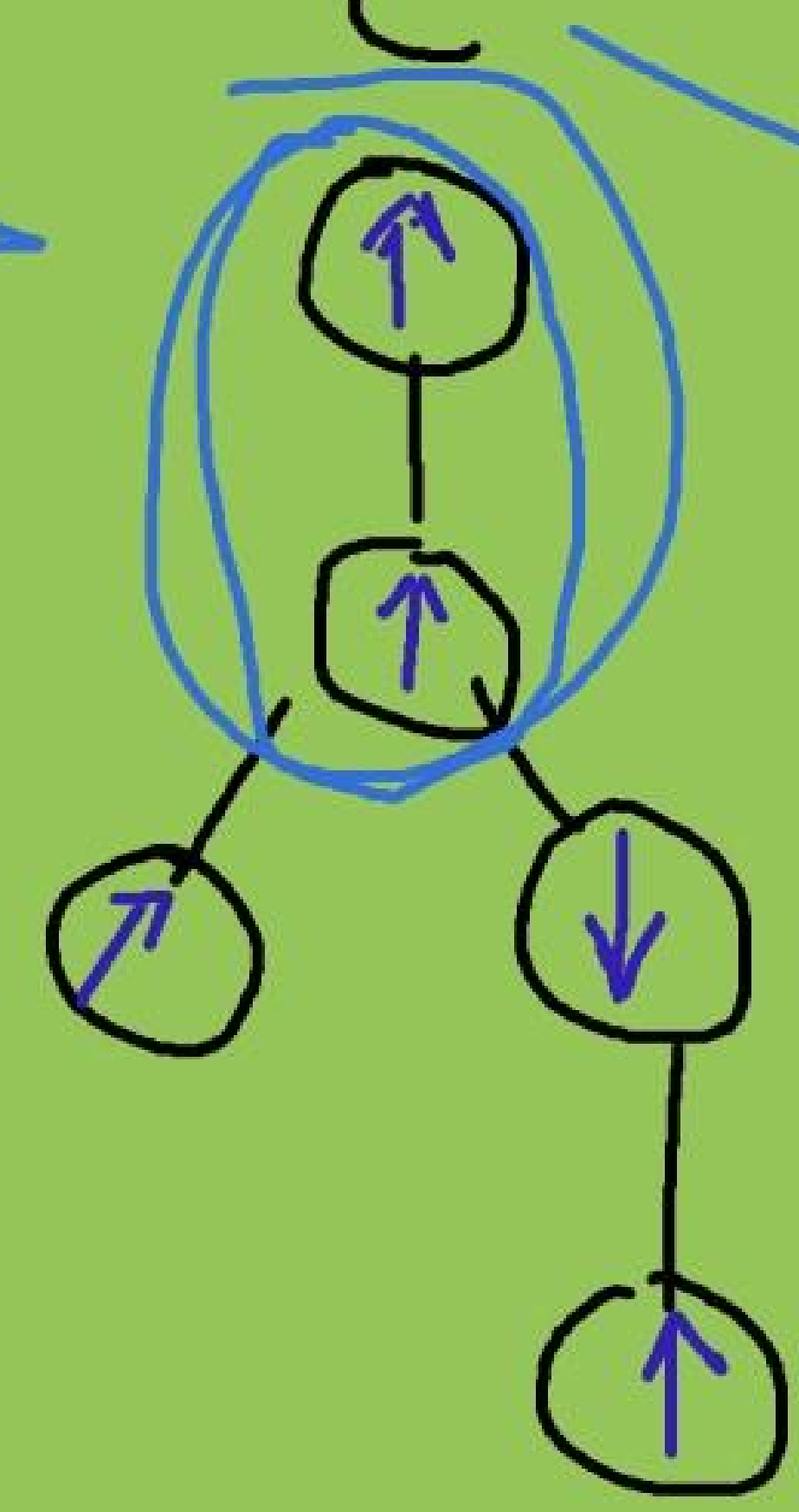
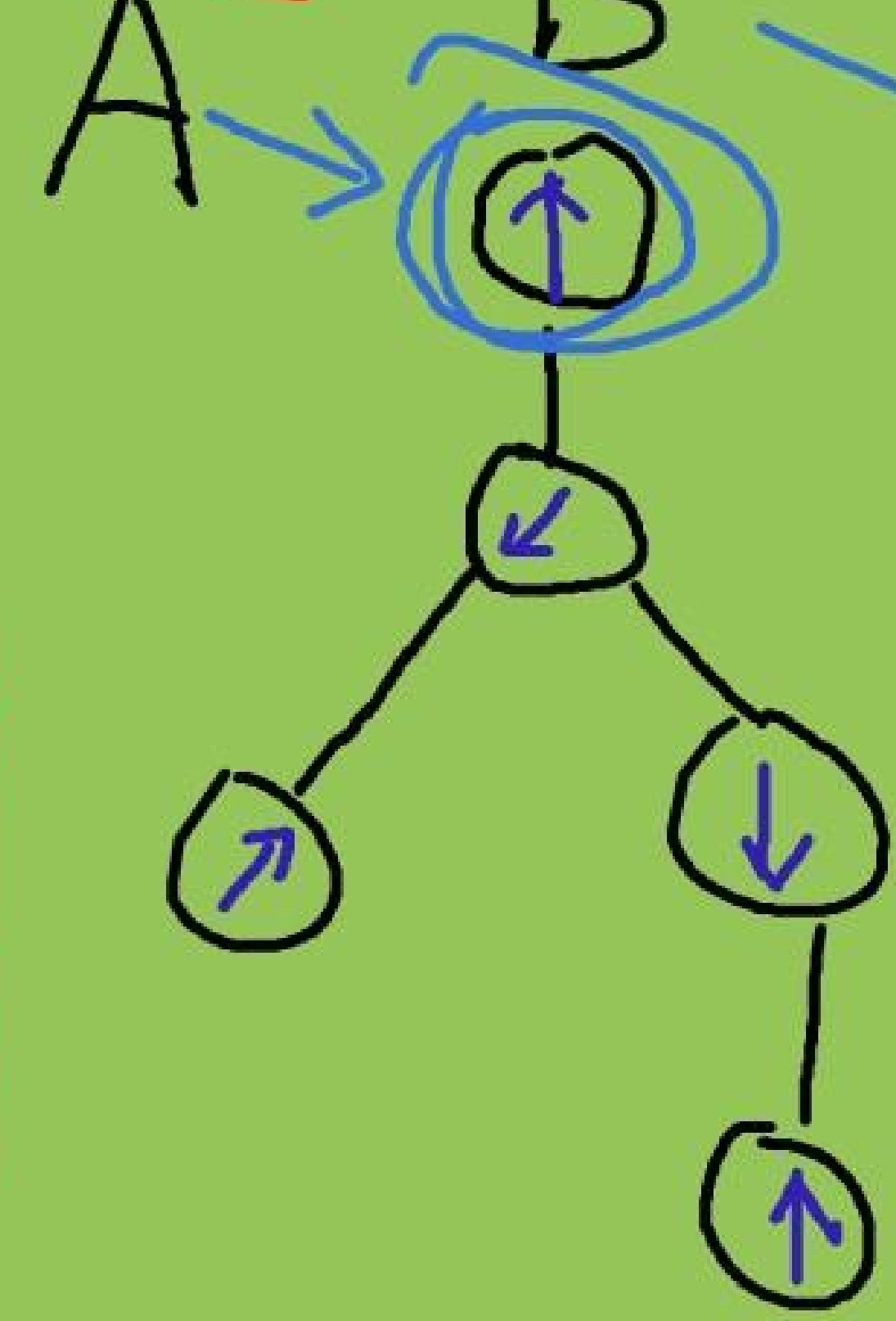
B - 1个

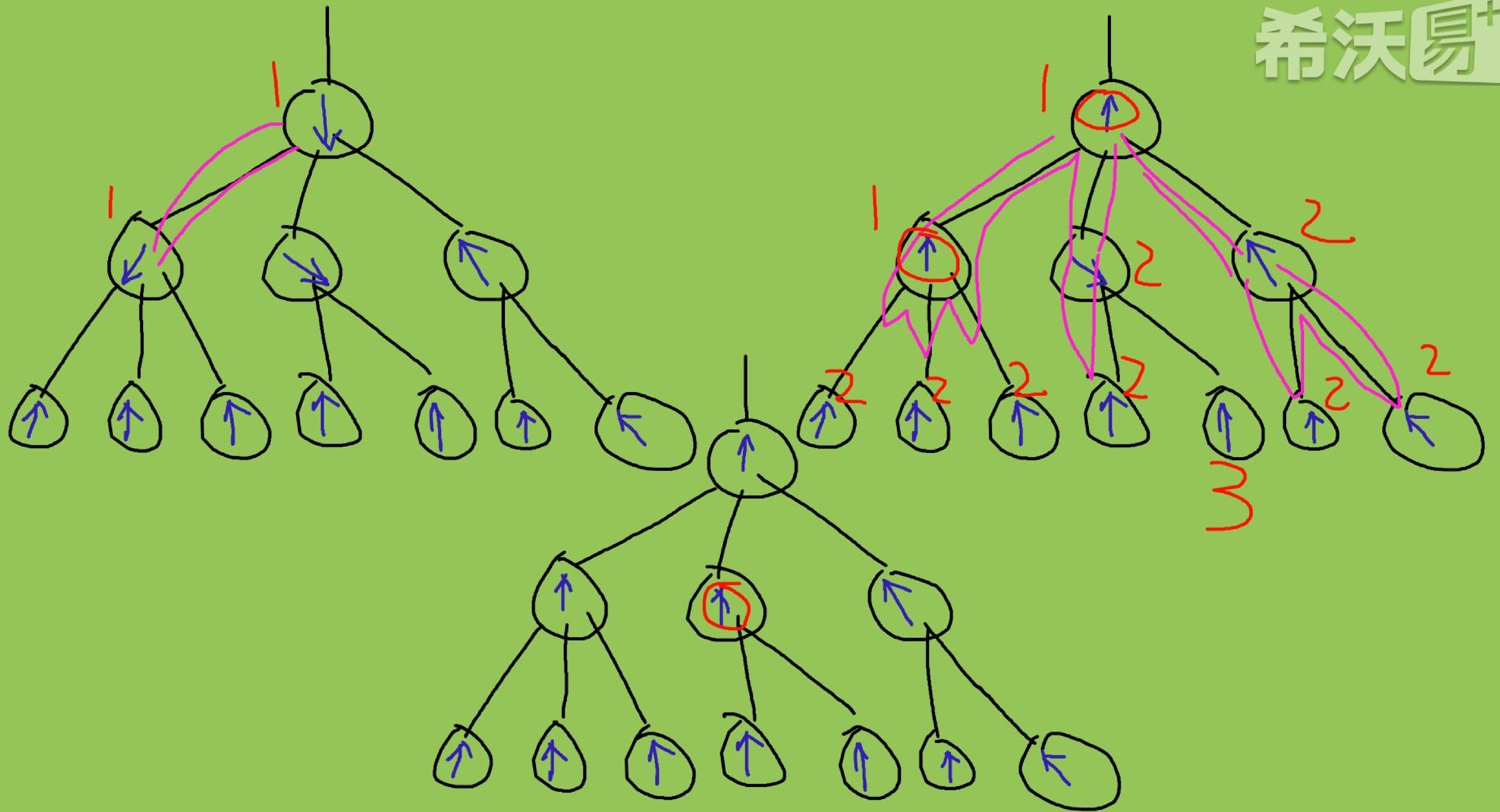
A + 1个



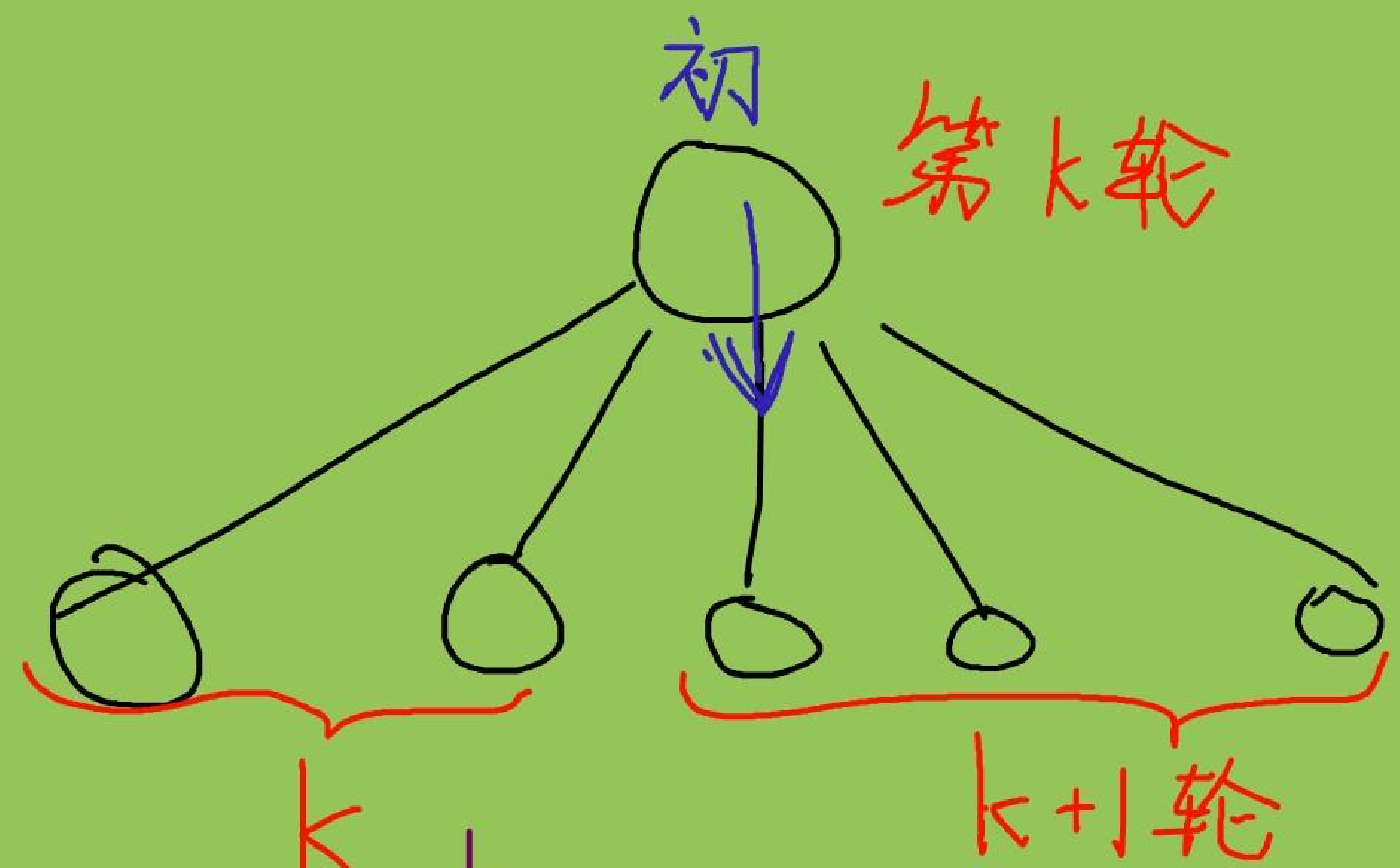


0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	
1	2	1	2	4	2	3	2	1	2	4	5	4	2	3	2	1
A		B		C				D				E				









$Q_i$  : 第i轮  
 $C_k$  : 第k轮几步  
 $C_k$  步  $Q_i \leq k$   
间k  $\rightarrow$  第k轮  
第k步

