

# Homework 4

Dec. 3, 2020

**NOTE: Homework 4 is due next Thursday (Dec. 10, 2020). The questions started with \* are for Exercise only, and you are not required to submit the answers.**

1. The attached data set “data.csv” is a subset of the Ames House data set. The first row of this data set is the name of the variables, where “SalePrice” is the dependent variable (column 1) and “Lot\_Area” is the independent variable (predictor; column 2). There are  $n = 1598$  observations in total (rows 2 - 1599). Suppose we use a linear regression model to approximate the relationship between SalePrice and Lot\_Area:

$$\text{SalePrice} = \beta_0 + \beta_1 \text{Lot\_Area} + \epsilon$$

Suppose that the noise  $\epsilon_i$  i.i.d.  $\sim N(0, \sigma^2)$ . Calculate the MLEs of  $\beta_0$ ,  $\beta_1$ ,  $\sigma^2$ .

2. Let  $\mathbf{X} = (X_1, \dots, X_n)$  be a random sample of size  $n = 15$  from a normal distribution  $N(\mu, 0.25^2)$ , and the observed values are:

2.9, 2.8, 3.0, 2.8, 3.1, 2.7, 2.3, 2.8, 2.4, 2.8, 2.6, 2.6, 3.1, 3.2, 2.9.

Construct a 95% confidence interval for  $\mu$ .