

Initialization

$$\mathbf{G} = \mathbf{D}^\top \mathbf{D} \quad (1)$$

$$\mathbf{a}^{(0)} = 0 \quad (2)$$

$$e^{(0)} = x^{(0)} \quad (3)$$

$$w^{(0)} = \|\mathbf{e}^{(0)}\|^2 \quad (4)$$

$$\mathbf{r}^{(0)} = \mathbf{D}^\top \mathbf{e}^{(0)} \quad (5)$$

$$\mathbf{h}_k^{(0)} = \|\mathbf{D}_k - \mathbf{e}^{(0)}\|^2 = g_{kk} - 2r_k + w^{(0)} \quad (6)$$

$$t = 0 \quad (7)$$

Loop

$$j^* = \arg \min_j \left\{ \|\mathbf{h}_j^{(t)}\| \right\} \quad (8)$$

$$w^{(t+1)} = \mathbf{h}_{j^*}^{(t)} \quad (9)$$

$$\mathbf{r}^{(t+1)} = \mathbf{r}^{(t)} - \mathbf{g}_{j^*} \quad (10)$$

$$h_k^{(t+1)} = \|\mathbf{e}^{(t)} - \mathbf{d}_k - \mathbf{d}_{j^*}\| \quad (11)$$

$$= \|(\mathbf{e}^{(t)} - \mathbf{d}_k) - \mathbf{d}_{j^*}\| \quad (12)$$

$$= [(\mathbf{e}^{(t)} - \mathbf{d}_k) - \mathbf{d}_{j^*}]^\top [(\mathbf{e}^{(t)} - \mathbf{d}_k) - \mathbf{d}_{j^*}] \quad (13)$$

$$= h_k^{(t)} - 2\mathbf{d}_{j^*}^\top (\mathbf{e}^{(t)} - \mathbf{d}_k) + \mathbf{d}_{j^*}^\top \mathbf{d}_{j^*} \quad (14)$$

$$= h_k^{(t)} - 2r_{j^*}^{(t)} + 2g_{kj^*} + g_{j^*j^*} \quad (15)$$

$$(16)$$