

restart

$$\begin{aligned}
 dsys1 &:= \left\{ \begin{aligned} \frac{d}{dx} m(x) &= \frac{kl (Tw - Tlv)}{hlv \delta(x)}, \quad \frac{d}{dx} F(x) = \frac{fR \mu l m(x)}{8 \rho l \delta^2(x)} - \sigma K G(x), \quad \frac{d}{dx} u(x) \\ &= \frac{kl (Tw - Tlv)}{\rho l hlv \delta^2(x)} - \frac{u(x)}{\delta(x)} G(x), \quad \frac{d}{dx} \delta(x) = G(x), \quad \frac{d}{dx} G(x) = K \left((1 + G^2(x))^{\frac{3}{2}} \right), \quad G(0) \\ &= 0.0005, \quad \delta(0) = \left(\frac{(Tv - A)}{(Tw - Tv) \rho v hlv} \right)^{\frac{1}{3}}, \quad u(0) = 0, \quad F(0) = - \frac{1.5 A}{\left(\left(\frac{(Tv - A)}{(Tw - Tv) \rho v hlv} \right)^{\frac{1}{3}} \right)^2}, \\ m(0) &= 0 \end{aligned} \right\} \\
 &\left\{ \begin{aligned} F(0) &= - \frac{1.5 A}{\left(\frac{Tv A}{(Tw - Tv) \rho v hlv} \right)^{2/3}}, \quad G(0) = 0.0005, \quad \delta(0) = \left(\frac{Tv A}{(Tw - Tv) \rho v hlv} \right)^{1/3}, \\ \frac{d}{dx} F(x) &= \frac{1}{8} \frac{fR \mu l m(x)}{\rho l \delta(x)^2} - \sigma K G(x), \quad \frac{d}{dx} G(x) = K (1 + G(x)^2)^{3/2}, \quad \frac{d}{dx} \delta(x) \\ &= G(x), \quad \frac{d}{dx} m(x) = \frac{kl (Tw - Tlv)}{hlv \delta(x)}, \quad \frac{d}{dx} u(x) = \frac{kl (Tw - Tlv)}{\rho l hlv \delta(x)^2} - \frac{u(x) G(x)}{\delta(x)}, \quad m(0) \\ &= 0, \quad u(0) = 0 \end{aligned} \right\}
 \end{aligned} \tag{1}$$

dsol2 := dsolve(dsys1, numeric, method=rkf45, output=procedurelist) :

Warning, The use of global variables in numerical ODE problems is deprecated, and will be removed in a future release. Use the 'parameters' argument instead (see ?dsolve,numeric,parameters)
dsol2(0)

$$\left[\begin{aligned} x=0., \quad F(x) &= - \frac{1.5 A}{\left(\frac{Tv A}{(Tw - 1. Tv) \rho v hlv} \right)^{2/3}}, \quad G(x) = 0.0005, \quad \delta(x) \\ &= \left(\frac{Tv A}{(Tw - 1. Tv) \rho v hlv} \right)^{1/3}, \quad m(x) = 0., \quad u(x) = 0. \end{aligned} \right] \tag{2}$$

K := 0

0

(3)

ρl := 999.7

$$hlv := 2513.6820390512 \cdot 10^3 \quad 999.7 \quad (4)$$

$$2.513682039 \cdot 10^6 \quad (5)$$

$$Tw := 282.98 \quad 282.98 \quad (6)$$

$$kl := 0.61 \quad 0.61 \quad (7)$$

$$\mu l := 0.001 \quad 0.001 \quad (8)$$

$$R := 0 \quad 0 \quad (9)$$

$$f := 0 \quad 0 \quad (10)$$

$$\sigma := 0.06$$

$$Tv := 282.65 \quad 282.65 \quad (11)$$

$$\rho v := 0.03 \quad 0.03 \quad (12)$$

$$A := 1. \cdot 10^{-19} \quad 1.000000000 \cdot 10^{-19} \quad (13)$$

$$Tlv := Tv \left(1 + \frac{\left(\frac{A}{\left(\left(\frac{(Tv - A)}{(Tw - Tv) \rho v hlv} \right)^{\frac{1}{3}}} \right)^3 \right)}{\rho l hlv} \right) \quad 282.65 \quad (14)$$

$$dsol2(0)$$

$$\left[x=0., F(x) = - \frac{1.5 A}{\left(\frac{Tv A}{(Tw - 1. Tv) \rho v hlv} \right)^{2/3}}, G(x) = 0.0005, \delta(x) \right.$$

$$\left. = \left(\frac{Tv A}{(Tw - 1. Tv) \rho v hlv} \right)^{1/3}, m(x) = 0., u(x) = 0. \right] \quad (15)$$

$$dsol2(0.000005)$$

$$\left[x=0.000005, F(x) = -0.0000137791456327161, G(x) = 0.0005000000000000000, \delta(x) \right.$$

$$= 1.06836072442695 \cdot 10^{-7}, m(x) = 0.00000379242610721238, u(x)$$

$$= 0.0355082921738401 \quad (16)$$

for i **from** 0 **to** $100.0 \cdot 10^{-5}$ **by** $100 \cdot 10^{-6}$ **do**
 $dsol2(i);$
end do

$[x=0., F(x) = -0.0000137791456327161, G(x) = 0.0005, \delta(x) = 1.04336072442695 \cdot 10^{-7},$
 $m(x) = 0., u(x) = 0.]$

$[x=0.0001000000000000000, F(x) = -0.0000137791456327161, G(x)$
 $= 0.0005000000000000000, \delta(x) = 1.54336072442695 \cdot 10^{-7}, m(x)$
 $= 0.0000627064530154883, u(x) = 0.406420043088061]$

$[x=0.0002000000000000000, F(x) = -0.0000137791456327161, G(x)$
 $= 0.0005000000000000000, \delta(x) = 2.04336072442695 \cdot 10^{-7}, m(x)$
 $= 0.000107653692275882, u(x) = 0.527004383778885]$

$[x=0.0003000000000000000, F(x) = -0.0000137791456327161, G(x)$
 $= 0.0005000000000000000, \delta(x) = 2.54336072442695 \cdot 10^{-7}, m(x)$
 $= 0.000142711943053275, u(x) = 0.561284006084702]$

$[x=0.0004000000000000000, F(x) = -0.0000137791456327161, G(x)$
 $= 0.0005000000000000000, \delta(x) = 3.04336072442695 \cdot 10^{-7}, m(x)$
 $= 0.000171457452373531, u(x) = 0.563551011764810]$

$[x=0.0005000000000000000, F(x) = -0.0000137791456327161, G(x)$
 $= 0.0005000000000000000, \delta(x) = 3.54336072442695 \cdot 10^{-7}, m(x)$
 $= 0.000195820441790271, u(x) = 0.552806349964308]$

$[x=0.0006000000000000000, F(x) = -0.0000137791456327161, G(x)$
 $= 0.0005000000000000000, \delta(x) = 4.04336072442695 \cdot 10^{-7}, m(x)$
 $= 0.000216962105988431, u(x) = 0.536749580889446]$

$[x=0.0007000000000000000, F(x) = -0.0000137791456327161, G(x)$
 $= 0.0005000000000000000, \delta(x) = 4.54336072442695 \cdot 10^{-7}, m(x)$
 $= 0.000235635686927672, u(x) = 0.518793049215732]$

$[x=0.0008000000000000000, F(x) = -0.0000137791456327161, G(x)$
 $= 0.0005000000000000000, \delta(x) = 5.04336072442695 \cdot 10^{-7}, m(x)$
 $= 0.000252357667121215, u(x) = 0.500526167585693]$

$[x=0.0009000000000000000, F(x) = -0.0000137791456327161, G(x)$
 $= 0.0005000000000000000, \delta(x) = 5.54336072442695 \cdot 10^{-7}, m(x)$
 $= 0.000267497653756295, u(x) = 0.482699866292960]$

$[x=0.0010000000000000000, F(x) = -0.0000137791456327161, G(x)$
 $= 0.0005000000000000000, \delta(x) = 6.04336072442695 \cdot 10^{-7}, m(x)$
 $= 0.000281329252237854, u(x) = 0.465657598307485]$

(17)

$$\delta n := 0.00000509363100481461 \quad 0.00000509363100481461 \quad (18)$$

$$Fn := -0.0000171100741184493 \quad -0.0000171100741184493 \quad (19)$$

$$mn := 0.00000969811837599714 \quad 0.00000969811837599714 \quad (20)$$

$$un := 0.00190453207045465 \quad 0.00190453207045465 \quad (21)$$

$$Ct := \frac{\mu l \cdot kl}{hlv \cdot \rho l \cdot \delta n} \quad 4.765651940 \cdot 10^{-8} \quad (22)$$

$$Kn := \left(\frac{1}{\sigma \cdot \left(\delta n + \frac{Ct \cdot Tv}{hlv \cdot \rho v} \right)} \right) \cdot \left(-Fn - \left(1.5 \cdot \delta n + \frac{Ct \cdot Tv}{hlv \cdot \rho v} \right) \frac{A}{(\delta n)^3} + \frac{1}{2} (mn \cdot un + Ct \cdot (Tw - Tv)) \right) \quad 56.02025566 \quad (23)$$

$$et := \frac{\sigma \cdot Kn + \frac{A}{(\delta n)^3}}{\rho l \cdot hlv} \quad 1.337870451 \cdot 10^{-9} \quad (24)$$

$$et := \frac{\sigma \cdot Kn + \frac{A}{(\delta n)^3}}{\rho v \cdot hlv} \quad 0.00004458230300 \quad (25)$$

$$Tlvn := Tv \left(1 + \frac{\sigma \cdot Kn + \frac{A}{(\delta n)^3}}{\rho v \cdot hlv} \right) \quad 282.6626011 \quad (26)$$

$$TlvnI := Tv \left(1 + \frac{\sigma \cdot Kn + \frac{A}{(\delta n)^3}}{\rho l \cdot hlv} \right) \quad 282.6500003 \quad (27)$$

$$q'' := \frac{kl \left(T_w - T_{lvn1} \right)}{\delta n}$$

39519.90570 (28)

$$h := \frac{q''}{\left(T_w - T_{lvn1} \right)}$$

1.197573989 10⁵ (29)

$$p := 6.35 \cdot 10^{-4}$$

0.0006350000000 (30)

$$Q1 := q'' p$$

25.09514012 (31)

$$\phi0 := 0.5235$$

0.5235 (32)

$$Di := 0.016$$

0.016 (33)

$$Q := \int_{\phi0}^{\pi} 2 \cdot q'' p \cdot Di \cdot d\phi$$

2.102444864 (34)

$$W := 1 \cdot 10^{-4}$$

$\frac{1}{10000}$ (35)

$$H := 1.473 \cdot 10^{-3}$$

0.001473000000 (36)

$$Atcs := W + 2 \cdot H$$

0.003046000000 (37)

$$At := \int_{\phi0}^{\pi} Atcs \cdot d\phi$$

0.007974710223 (38)

$$h := \frac{Q}{At \left(T_w - T_{lvn1} \right)}$$

798.9068763 (39)

$$C1 := 0.48$$

0.48 (40)

$$C2 := 0.25$$

0.25 (41)

$$g := 9.81$$

9.81 (42)

$$Tf := 278$$

278 (43)

$$Tm := \frac{\left(T_w + Tf \right)}{2}$$

280.4900000 (44)

$$\eta := \frac{1}{Tm}$$

$$\mathfrak{v}:=1\,10^{-6} \qquad \qquad \qquad 0.003565189490 \qquad \qquad \qquad (45)$$

$$\qquad \qquad \qquad \frac{1}{1000000} \qquad \qquad \qquad (46)$$

$$\Delta T:=T_w-T_f \qquad \qquad \qquad 4.98 \qquad \qquad \qquad (47)$$

$$l:=0.01905 \qquad \qquad \qquad 0.01905 \qquad \qquad \qquad (48)$$

$$Gr:=\frac{g\,\mathfrak{v}\,\Delta T\,l^3}{\mathfrak{v}^2} \qquad \qquad \qquad 1.204109292\,10^6 \qquad \qquad \qquad (49)$$

$$Pr:=8 \qquad \qquad \qquad 8 \qquad \qquad \qquad (50)$$

$$Nu:=Cl\,(Gr\,Pr)^{C2} \qquad \qquad \qquad 26.74115807 \qquad \qquad \qquad (51)$$

$$hnc:=\frac{Nu\,kl}{l} \qquad \qquad \qquad 856.2785522 \qquad \qquad \qquad (52)$$