18.11 Depth first search using time stamps

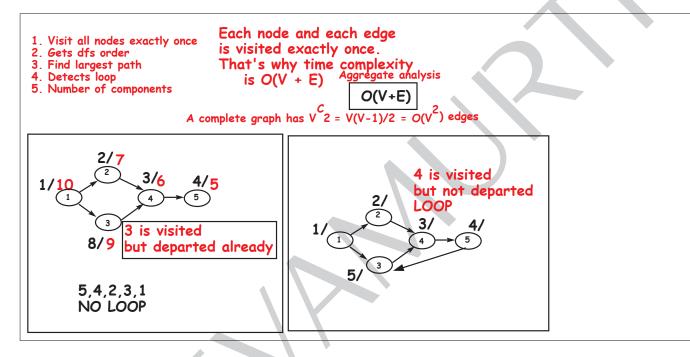


Figure 18.32: Depth first search on a directed graph using time stamps

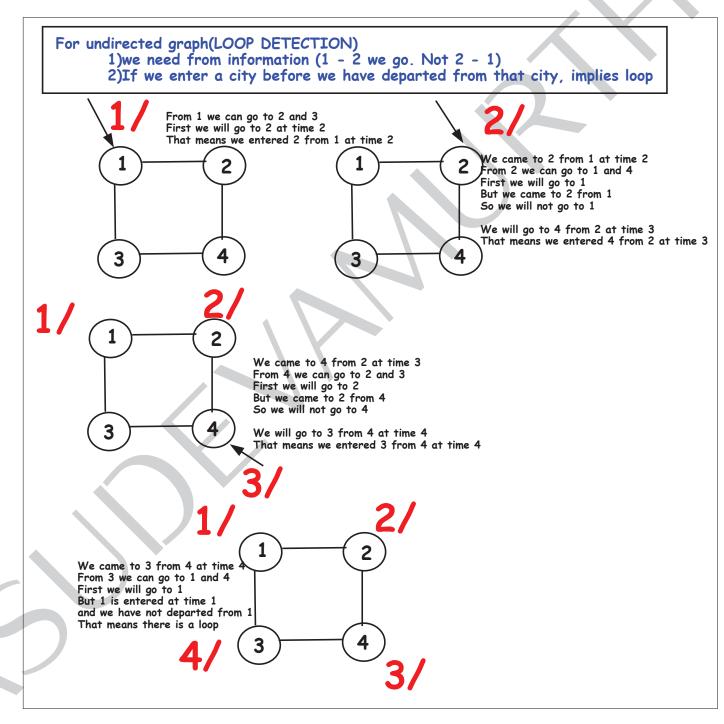


Figure 18.33: Depth first search on an undirected graph using time stamps and from

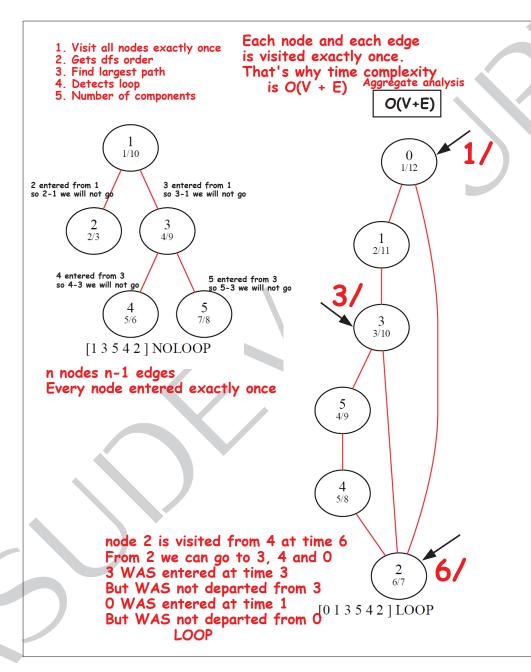
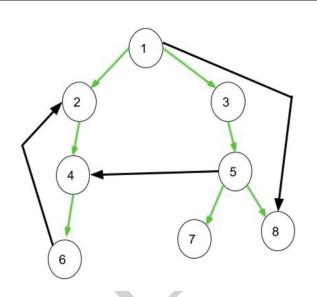


Figure 18.34: Depth first search on an undirected graph



Tree Edge: All the Green edges are tree edges.

Forward Edge: It is an edge $(u,\,v)$ such that v is descendant but not part of the DFS tree. Edge from 1 to 8 is a forward edge.

Back edge: It is an edge (u, v) such that v is ancestor of edge u but not part of DFS tree.
Edge from 6 to 2 is a back edge.
Presence of back edge indicates a cycle in directed graph.

Cross Edge: It is a edge which connects two node such that they do not have any ancestor and a descendant relationship between them. Edge from node 5 to 4 is cross edge.

Tree edge:

arrival[u] < arrival[v]
departure[u] > departure[v]

Back edge:

arrival[u] > arrival[v]
departure[u] < departure[v]</pre>

Forward edge:

arrival[u] < arrival[v]
departure[u] > departure[v]

Cross edge:

arrival[u] > arrival[v]
departure[u] > departure[v]

Figure 18.35: classification of edges in a directed graph

18.11.1 Depth first search on a undirected graph with no loop

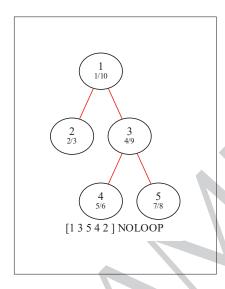


Figure 18.36: undirected graph with no loop

```
## Jagadeesh Vasudevamurthy ####
## dot -Tpdf C:\scratch\outputs\dot\1dfs.dot -o C:\scratch\outputs\dot\1dfs.dot.pdf
digraph g {
    label = "[1 3 5 4 2 ] NOLOOP"
    1[label = <1<BR /><FONT POINT-SIZE="10">1/10</FONT>>]
    2[label = <2<BR /><FONT POINT-SIZE="10">2/3</FONT>>]
    3[label = <3<BR /><FONT POINT-SIZE="10">4/9</FONT>>]
    4[label = <4<BR /><FONT POINT-SIZE="10">5/6</FONT>>]
    5[label = <5<BR /><FONT POINT-SIZE="10">7/8</FONT>>]
edge [dir=none, color=red]
    1 -> 2
    1 -> 3
    3 -> 4
    3 -> 5
}
```

18.11.2 Depth first search on a undirected graph with loop

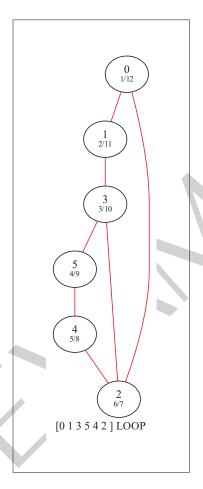


Figure 18.37: undirected graph with loop

```
## Jagadeesh Vasudevamurthy ####
## dot -Tpdf C:\scratch\outputs\dot\udf1dfs.dot -o C:\scratch\outputs\dot\udf1dfs.dot.
digraph g {
   label = "[0 1 3 5 4 2 ] LOOP"
  0[label = <0<BR /><FONT POINT-SIZE="10">1/12</FONT>>]
   1[label = <1<BR /><FONT POINT-SIZE="10">2/11</FONT>>]
   3[label = <3<BR /><FONT POINT-SIZE="10">3/10</FONT>>]
   5[label = <5<BR /><FONT POINT-SIZE="10">4/9</FONT>>]
  4[label = <4<BR /><FONT POINT-SIZE="10">5/8</FONT>>]
   2[label = <2<BR /><FONT POINT-SIZE="10">6/7</FONT>>]
edge [dir=none, color=red]
  0 -> 1
  0 -> 2
   1 -> 3
  3 -> 5
  3 -> 2
  5 -> 4
   4 -> 2
}
```

18.11.3 Depth first search on a directed graph with no loop

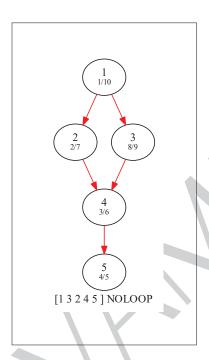


Figure 18.38: directed graph with no loop

```
## Jagadeesh Vasudevamurthy ####
## dot -Tpdf C:\scratch\outputs\dot\2dfs.dot -o C:\scratch\outputs\dot\2dfs.dot.pdf
digraph g {
   label = "[1 3 2 4 5 ] NOLOOP"
   1[label = <1<BR /><FONT POINT-SIZE="10">1/10</FONT>>]
   2[label = <2<BR /><FONT POINT-SIZE="10">2/7</FONT>>]
   3[label = <3<BR /><FONT POINT-SIZE="10">8/9</FONT>>]
   4[label = <4<BR /><FONT POINT-SIZE="10">3/6</FONT>>]
   5[label = <5<BR /><FONT POINT-SIZE="10">4/5</FONT>>]
edge [color=red]
   1 -> 2
   1 -> 3
   2 -> 4
   3 -> 4
   4 -> 5
}
```

18.11.4 Depth first search on a directed graph with loop

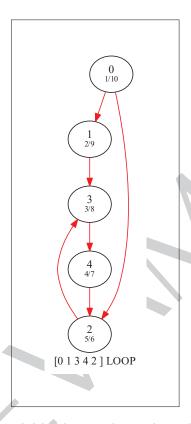


Figure 18.39: directed graph with loop

```
## Jagadeesh Vasudevamurthy ####
## dot -Tpdf C:\scratch\outputs\dot\3dfs.dot -o C:\scratch\outputs\dot\3dfs.dot.pdf
digraph g {
  label = "[0 1 3 4 2 ] LOOP"
  0[label = <0<BR /><FONT POINT-SIZE="10">1/10</FONT>>]
   1[label = <1<BR /><FONT POINT-SIZE="10">2/9</FONT>>]
   2[label = <2<BR /><FONT POINT-SIZE="10">5/6</FONT>>]
  3[label = <3<BR /><FONT POINT-SIZE="10">3/8</FONT>>]
  4[label = <4<BR /><FONT POINT-SIZE="10">4/7</FONT>>]
edge [color=red]
  0 -> 1
  0 -> 2
  1 -> 3
  2 -> 3
  3 -> 4
  4 -> 2
}
```

18.11.5 Depth first search on a directed graph with no loop

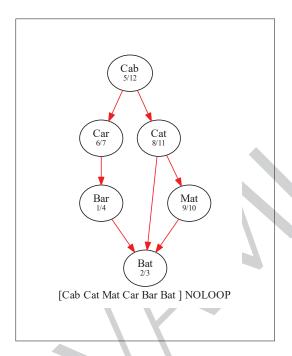


Figure 18.40: directed graph with no loop

```
## Jagadeesh Vasudevamurthy ####
## dot -Tpdf C:\scratch\outputs\dot\catdfs.dot -o C:\scratch\outputs\dot\catdfs.dot.pd
digraph g {
   label = "[Cab Cat Mat Car Bar Bat ] NOLOOP"
   Bar[label = <Bar<BR /><FONT POINT-SIZE="10">1/4</FONT>>]
   Bat[label = <Bat<BR /><FONT POINT-SIZE="10">2/3</FONT>>]
   Cab[label = <Cab<BR /><FONT POINT-SIZE="10">5/12</FONT>>]
   Car[label = <Car<BR /><FONT POINT-SIZE="10">6/7</FONT>>]
   Mat[label = <Mat<BR /><FONT POINT-SIZE="10">9/10</FONT>>]
   Cat[label = <Cat<BR /><FONT POINT-SIZE="10">8/11</FONT>>]
edge [color=red]
   Bar -> Bat
   Cab -> Car
   Cab -> Cat
   Car -> Bar
   Mat -> Bat
   Cat -> Bat
   Cat -> Mat
}
```

18.11.6 Depth first search on a directed graph with no loop

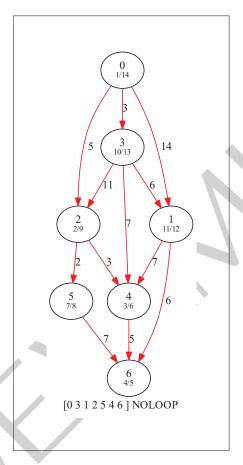


Figure 18.41: directed graph with no loop

```
## Jagadeesh Vasudevamurthy ####
## dot -Tpdf C:\scratch\outputs\dot\7dfs.dot -o C:\scratch\outputs\dot\7dfs.dot.pdf
digraph g {
   label = "[0 3 1 2 5 4 6 ] NOLOOP"
   0[label = <0<BR /><FONT POINT-SIZE="10">1/14</FONT>>]
   2[label = <2<BR /><FONT POINT-SIZE="10">2/9</FONT>>]
   3[label = <3<BR /><FONT POINT-SIZE="10">10/13</FONT>>]
   1[label = <1<BR /><FONT POINT-SIZE="10">11/12</FONT>>]
   6[label = <6<BR /><FONT POINT-SIZE="10">4/5</FONT>>]
   4[label = <4<BR /><FONT POINT-SIZE="10">3/6</FONT>>]
   5[label = <5<BR /><FONT POINT-SIZE="10">7/8</FONT>>]
edge [color=red]
   0 \rightarrow 2 [label = 5]
   0 \rightarrow 3 [label = 3]
   0 \to 1 [label = 14]
   2 \rightarrow 4 [label = 3]
   2 \rightarrow 5 [label = 2]
   3 \rightarrow 2 [label = 11]
   3 \rightarrow 1 [label = 6]
   3 \rightarrow 4 [label = 7]
   1 -> 6 [label = 6]
   1 -> 4 [label = 7]
   4 \rightarrow 6 [label = 5]
   5 -> 6 [label = 7]
}
```

18.11.7 Implementing depth first search

Implementing Depth First Search

```
class GraphDFSUsingTimeStamp{
 private Graph g;
                            GraphDFSUsingTimeStamp.java
 private int [] work ;
 private boolean [] cycle;
 private ArrayList<Integer> topologicalOrderArray;
 private String f;
 GraphDFSUsingTimeStamp(Graph g, int [] work, boolean [] cycle, rrayList<Integer> topologicalOrderArray,String f) {
   this.g = g;
   this.work = work ;
   this.cycle = cycle ;
   this topologicalOrderArray = topologicalOrderArray;
   this.f = f
   //You MUST WRITE 2 routines
   dfs()
   writeDFSDot();
}
```

```
public void dfsUsingTimeStamp(int [] work, boolean [] cycle, rrayList<Integer> topologicalOrderArray, String f) {
    GraphDFSUsingTimeStamp g = new GraphDFSUsingTimeStamp(this, work, cycle,topologicalOrderArray,f);
}

Graph.java
```

```
private void dfsUsingTimeStamp(String name, GraphType.Type graphType, boolean expectedHasloop) {
    GraphIO io = new GraphIO();
    Graph g = new Graph(graphType,io);
    String f = name + ".txt";
    GraphTest.java

    a.buildGraph(f);
    Make sure toplogical order is correct

int [] work = {0};
    boolean [] cycle = {false};
    ArrayListInteger> toplogicalOrderArray = new ArrayListInteger>();
    f = name + "dfs.dot";
    g.dfsUsingTimeStamp(work.cycle,topologicalOrderArray,f);
    boolean x = q.assertDFS(cycle[0], topologicalOrderArray);
}

private void testDfsUsingTimeStamp() {
    dfsUsingTimeStamp("1", GraphType.Type.UNDIRECTED,false);
    dfsUsingTimeStamp("4f1", GraphType.Type.UNDIRECTED,false);
    dfsUsingTimeStamp("2", GraphType.Type.UNDIRECTED,false);
    dfsUsingTimeStamp("3", GraphType.Type.DIRECTED,false);
    dfsUsingTimeStamp("3", GraphType.Type.DIRECTED,false);
    dfsUsingTimeStamp("cat", GraphType.Type.DIRECTED,false);
    dfsUsingTimeStamp("cat", GraphType.Type.DIRECTED,false);
    dfsUsingTimeStamp("7", GraphType.Type.DIRECTED,false);
    dfsUsingTimeStamp("7", GraphType.Type.WEIGHTED_DIRECTED,true); //loop

dfsUsingTimeStamp("mediumEWD", GraphType.Type.WEIGHTED_DIRECTED,true); //loop
```

Figure 18.42: Implementing depth first search