

# **Master Thesis**

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## **Deep Learning of Cardiac Related Condition using a Non-Contact Multi-Sensor System**

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Date: 8. Januar 2018



# Acknowledgments

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# **Abstract**

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# Symbols

## 1 Abbreviations

AV	Atrioventricular
ANN	Artificial Neural Network
CNN	Convolutional Neural Network
DWT	Discrete Wavelet Transform
ECG	Electrocardiogram
FFT	Fast Fourier Transfrom
HRC	Heart Rate Variability
LBBB	Left Bundle Branch Block
PVC	Premature Ventricular Contraction
RBBB	Right Bundle Branch Block
RMSE	Root Mean Square Error
RT	Repolarization Time
SA	Sinoatrial
WT	Wavelet Transform



# 1 Introduction

According to one of the reports of US, around one billion people travel on airlines each year [ML08],[F<sup>+</sup>03]. It has also been predicted that the number will be double in the coming two decades. During a flight, emergencies occur at a rate of 20 to 100 million per million passengers. Out of which 0.1 to 1 million people died [LWDHr00]. Many of the cases are not even on the record as there is no proper reporting system. The most common in-flight complaints are related to respiration, cardiac, traumatic and gastrointestinal. Out of these, cardiac and respiration related complaints are more serious. During inflight, a doctor is present only 30 to 60 percent [ML08],[Dow00]. These number may have changed as the article was published in 2008.

## 1.1 Motivation

Environmental changes such as when moving from sea level to high altitude, the level of oxygen gradually decreases as the air thins out, including the reduction of atmospheric pressure, temperature, and humidity. As a result, the heart rate increases as it tries to deliver more oxygen to the muscles, which can lead to fainting or even heart attacks among some passenger.

It is important to realize the onboard medical resources are limited. Therefore, a technology advancement is required, which can reduce the workload of doctors during a flight. Healthcare is one of the hottest research areas in the current era. Monitoring of vital signs, parameter like respiration, ECG, EEG, temperature, and heart rate, getting more and more important in every field of life.

A variety of technologies are already in used to measure the vital signs [LU17]. They include traditional stethoscopes, electrodes for measuring ECG, and different types of gauges, but they have their drawbacks in terms of comfort and convenience. For example, to measure the ECG, the electrodes are required to be directly attached to the skin of the patient, which is very inconvenient and limits the patient's movement. Strain gauges use the belts to measure the blood pressure and respiration which again limits the daily activities. Even though these technologies are reliable and provide better results, but they are inadequate for long-term everyday activities.

Contact-less sensors are the next big thing in the healthcare. They are designed in such a way that they can disappear in the daily surroundings without any disruption. Different techniques have been used to integrate contact-less sensors into clothes, chairs, smartwatches, smartphones, shoes, and beds to measure different vital signs.

As mentioned earlier, most of the work done in the healthcare technologies have used the

sensors which are required to be placed on the body, therefore, trends need to be shifted towards contact-less sensors as they are much more convenient to use. Moreover, not much work has been carried out to use the deep learning technologies along with a contact-less sensor to identify the cardiac arrhythmias in a real-time environment.

The distributed computing, streaming analytics and machine learning has become more powerful and cheaper than ever enabling the analysis of many different kinds of data much faster [McD17]. Some examples of machine learning and big data working together for the analysis are:

- Health care
- Transportation
- Automobile
- Manufacturing
- Retail

The combination of streaming data, big data analysis, and machine learning can benefit health care as well in identifying chronic diseases such as cardiac disease. Vital signs of the patient can be analyzed in real-time while keeping the false alarm as low as possible.

## **1.2 Aim**

The aim of this thesis is to build a system that provides a healthcare solution which would be able to track the pilot's vital signs such as heart rate, temperature, and ECG. Moreover, it can detect the cardiac arrhythmias in real-time.

Multiple contact-less sensors are used in the development of the system to measure the various vital signs of pilots. These sensors include:

1. Capacitive ECG sensor
2. Photoplethysmogram sensor
3. Magnetic impedance sensor
4. Ballistocardiogram sensor
5. Thermal camera

These sensors will be installed in the pilot seat so they can continuously track the health status of the pilot during a course of the flight. The early identification of the disease can help to provide quick treatment to the pilot, as well as can stop from reaching any dangerous situation.

An arrhythmia can be harmless or a life threatening, therefore, for pilot's, a thorough medical evaluation is necessary to assess the severity of an arrhythmia for the safety of both pilot and the passengers.

A deep learning model has been trained using a convolutional neural network to detect the cardiac arrhythmias. Various cardiac arrhythmias dataset have taken from already existed dataset to train the model. The advantage of using CNN is that unlike other machine learning algorithms, it does not require a feature extraction phase.

Multiple platforms have been used along with tablets to visualize the results and vital signs of the passengers. A cloud has been set up to store all the sensors data and vital signs so, the data can be accessed from anywhere in the world. The sensor's data later can also be used for a different purpose such as for the re-training of the deep learning model.

## 1.3 Objective

The objective of this thesis are:

- Programming of a software visualization (cECG, MI, BKG, and PPG) for a PC along with the tablet notification and visualization.
- Construction of the data bank on the cloud.
- Deep learning of the cardiac conditions.
- Evaluation of the algorithm with real-time data from the sensors.



## 2 Background

### 2.1 Anatomy of Heart

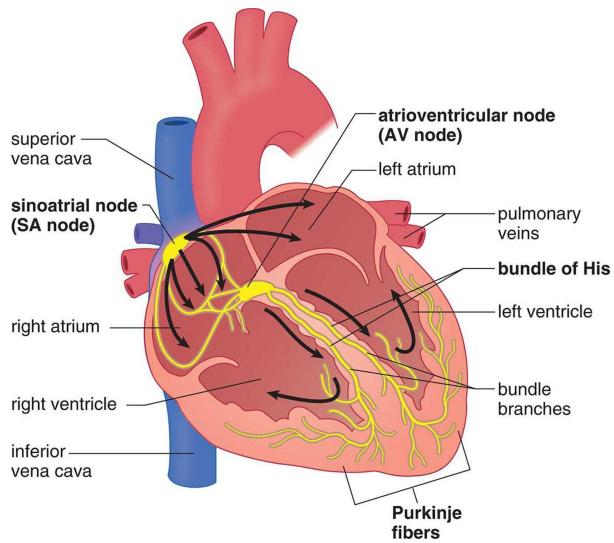
The function of the heart is to pump the blood inside the body, which is stimulated by an electrical stimulus [Wil05] [Sch17]. The heart pumps blood to the different parts of the body such as organs, muscles, and tissues.

The heart shown in Figure 2.1 is made up of 4 chambers, left and right atria, and left and right ventricles. The right atrium receives de-oxygenated blood from the whole body and pumps it into the right ventricle which then pumps the blood to the lungs for increasing oxygenation. The left atrium receives oxygenated blood from the lungs and pumps it into the left ventricle which then pumps the oxygenated blood to the whole body. The aorta carries oxygenated blood to the different part of the body and the pulmonary arteries carry the de-oxygenated blood back to the lungs for improving oxygenation. The blood flows to different organs via arteries and returns back to the heart via veins.

The main components of the cardiac conduction system are:

1. Sinoatrial (SA) node
2. The Atrioventricular (AV) node
3. Atrioventricular (AV) bundle or bundle of His
4. Right and left bundle branches
5. Purkinje fibers

The SA node, also known as sinus node, is a natural pacemaker of the heart which is located in the right atrium. It produces an electrical stimulus at the rate of 60 to 100 signals per minute (under normal condition), which travels through the heart to make it pump the blood to the body. It initiates all heartbeats and determines the heart rate. The electrical impulse from the SA node spreads throughout the atrium which results in the contraction of the atrium. The AV node which is located on the other side of the right atrium, near the AV valve, serve as a gateway to the ventricles. It also delays the passage of electrical impulse to the ventricles. This is to ensure that all the blood is ejected from the atria to the ventricles before the ventricles contract. The AV node then passes the signal to the atrioventricular (AV) bundle or bundle of His. The bundle is divided into two parts, right and left bundle branches to stimulate the right and left ventricles. The signal then travels down to the Purkinje fibers, where the signal spreads upwards throughout the ventricular myocardium. Each contraction of the ventricles represents one single heartbeat.



**Figure. 2.1:** The electrical activity of heart [Sch17].

Each heartbeat is composed of two phases, known as systole and diastole. During **systole**, the heart muscles contract and the blood is pumped from ventricles to the different parts of the body. During **diastole**, the hearts muscles relax and the blood from atria flows into the ventricles. The pressure generated during systole from the ventricular contraction is high, whereas, during diastole, due to the muscle relaxation this pressure reduces.

The electrical activity of the heart can be detected in the form of electrocardiogram by placing electrodes on the body surface. It is a powerful tool for diagnosing the status of patient's heart.

## 2.2 The Electrocardiogram

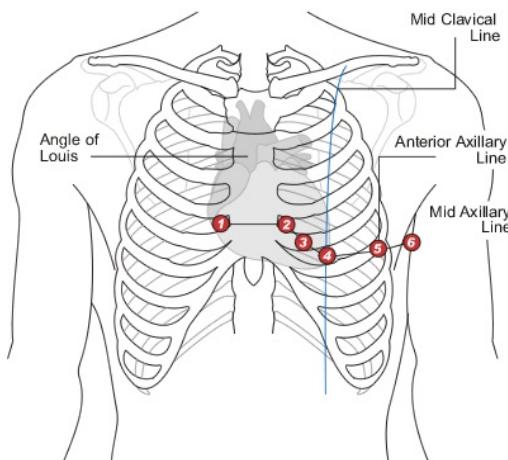
Electrocardiogram (ECG) is an essential tool for diagnosing the electrical activity of the heart [Wil05]. It is a simple and non-invasive procedure to measure the activity of the heart. Most of the tools available today to measure the ECG are based on the electrodes which are required to be attached to the body. The electrodes sense the electrical potentials of the body and transmit them to the ECG monitor. These voltages are then transformed into appropriate waveforms which represent the heart's polarization and depolarization cycle. Different components of the wave represent the activity of different parts of the heart.

In conventional 12-lead ECG, only 10 electrodes or leads are attached to the patient's body and the electrical activity of the heart can be viewed from 12 different perspectives [cab17]. These 12 views of the heart are captured by placing the electrodes on chest, wrists, and ankles. The main purpose of ECG is to identify any cardiac arrhythmia, ischemia, problems

with heart rate or any other irregularities.

These 10 electrodes are divided into 2 groups.

1. 6 chest electrodes
2. 4 limb electrodes



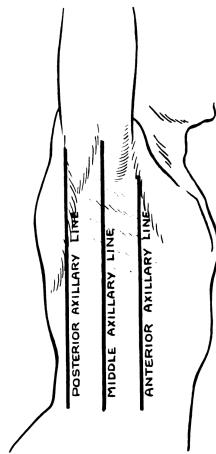
**Figure. 2.2:** The leads position on chest[Gre].

## Chest Electrodes

The chest electrodes are denoted as “V” and they all are numbered from V1 to V6 as can be seen in Figure 2.2. The electrodes are positioned at the following locations on the chest:

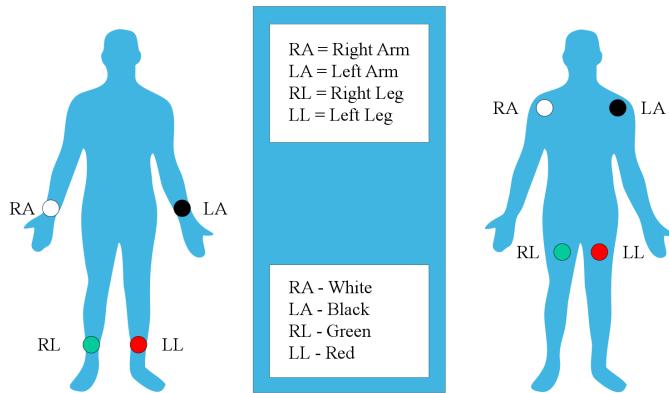
- V1 - Fourth intercostal space (between ribs 4 and 5) on the right sternum
- V2 - Fourth intercostal space (between ribs 4 and 5) on the left sternum
- V3 - Placed in the middle of V2 and V4
- V4 - Fifth intercostal space (between ribs 5 and 6) at the mid-clavicular line
- V5 - Placed horizontally on anterior axillary line with V4
- V6 - Placed horizontally on Mid-axillary line with V4 and V5

The 3 different axillary lines **anterior axillary line**, **midaxillary line**, and **posterior axillary line** can be seen in Figure 2.3.



**Figure. 2.3:** The axillary lines on the right side of chest[Com17a].

### Limb Electrodes



**Figure. 2.4:** The possible position of limb leads[Com17b].

The 4 limb electrodes are denoted as RA, LA, LL, RL and their respective positions are:

- RA - Anywhere on right arm between shoulder and elbow, but avoiding thick muscles.
- LA - Symmetric to the RA position, but on left arm
- RL - Anywhere on right leg between the torso and the ankle
- LL - Symmetric to the RL position, but on left leg

The limb electrodes are shown in Figure 2.4

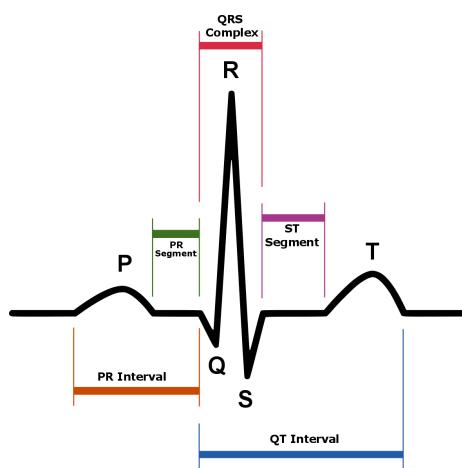
## 2.3 ECG Complex

ECG complex represents the electrical activity of the heart during one cardiac cycle [Wil05]. A normal cardiac cycle consists of five waveforms labeled with P, Q, R, S and T as can be seen in Figure 2.5. The Q, R and S waves are referred to as one unit, the QRS complex. The ECG signal represents the conduction of electrical impulses from the atria to the ventricles. The important parameters in the ECG signal are:

### 2.3.1 P Wave

The P wave is the first component of the ECG signal. It occurs due to contraction of both left and right atrium. This process is also known as atrial depolarization. A normal P wave has following characteristics (in lead II):

- Duration: less than 120 milliseconds
- Amplitude: less 0.25 mV in the limb leads and less than 0.15 mV in the precordial leads
- Location: before the QRS complex



**Figure. 2.5:** The ECG signal[Com17c].

### 2.3.2 QRS Complex

The QRS complex follows the P wave and represents a contraction of both right and left ventricles. This contraction results in the blood ejection from the heart which eventually pumps into the arteries and creates a pulse. The Q and S waves are relatively very

## *2 Background*

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small whereas, R wave is comparatively very big. A normal QRS complex has following characteristics (in lead II):

- Duration: 70 to 100 milliseconds
- Location: follows the P wave

### **2.3.3 T Wave**

The T wave represents the ventricles repolarization. It occurs during the last part of ventricle systole. The T wave has following characteristics (in lead II):

- Duration: 100 to 250 milliseconds or greater
- Location: follows the QRS complex

### **2.3.4 PR Interval**

The PR interval is the time interval between the end of contraction of the atria and the beginning of contraction of the ventricles. A normal PR interval has following characteristics:

- Duration: 120 to 200 milliseconds
- Location: From the beginning of P wave to the beginning of the QRS complex

### **2.3.5 ST Segment**

The ST segment represents the end of ventricular depolarization and the beginning of the ventricles relaxation. The point between the end of QRS complex and the beginning of ST segment is called as the J point. A normal ST segment has following characteristics:

- Duration: 80 to 120 milliseconds
- Location: From the end of QRS complex to the beginning of T wave

### 2.3.6 QT Interval

The QT interval is the time interval between the ventricular depolarization and repolarization. The QT duration varies according to the heart rate. Faster heart rate results in smaller QT interval whereas, slower heart rate may result in a bigger QT interval. The bigger QT interval may result in an irregular heartbeat. A normal QT interval has following characteristics:

- Duration: 360 to 440 milliseconds
- Location: From the beginning of QRS complex to the end of T wave

## 2.4 Disadvantages of Attached Electrodes

While it is easy to monitor the electrical heart activity by placing the electrodes directly on the body but it has several disadvantages as well.

1. It limits the patient's mobility.
2. Discomfort for the patient as electrodes are directly attached to the body.
3. Loss of cardiac monitoring in case if patient moves.
4. Long time contact of the electrodes may irritate the skin.

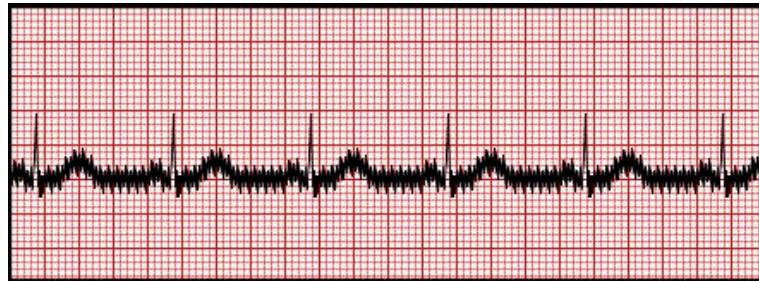
## 2.5 Noise in ECG Signal

Typically the ECG signal can be corrupted by the different types of noises and artifacts which changes the characteristics of the ECG signal [LD]. Hence, it is difficult to extract the useful information from the signal. Following are the major noises, which are present in the ECG signal.

### 2.5.1 Power Line Interference

Power line interference is a 50 Hz noise, which is present in ECG signal because of the improper grounding of the ECG equipment or interference from the nearby equipment. In order to remove this type of noise, a proper use of a filter is required. A 50 Hz notch filter

can be used to remove the power line interference. Figure 2.6 illustrates the 50 Hz power line interference in ECG signal.



**Figure. 2.6:** AC Interference of 50Hz[mau17].

### 2.5.2 Baseline wander

Baseline wander is a low-frequency component which corrupts the ECG signal because of breathing, body movements, dirty or lose electrodes or electrode impedance. Generally, they have a frequency lower than 2 Hz [Sch12]. A high pass filter can be used to remove the baseline wander. The baseline wandering in ECG signal can be seen in Figure 2.7.



**Figure. 2.7:** Baseline wandering in ECG signal[mau17].

### 2.5.3 Muscle Noise

This type of noise is caused by muscle contractions besides heart, which results in the change of heart electrical potential [MG13]. Whenever the other muscles near the electrodes depolarized and repolarized, they also generate waves, which can be monitored by the ECG. They generally occur in short time burst and have higher amplitude values than the ECG signal. It can be removed using Wavelet transform [MPS<sup>+</sup>11]. An example of ECG signal affected by muscle contractions can be seen in Figure 2.8.



**Figure. 2.8:** ECG signal combined with muscle noise[mau17].

## 2.6 Arrhythmias

Irregularity in the heartbeat is known as arrhythmia (also called dysrhythmia) [med17]. During an arrhythmia, a heart is out of normal rhythm and may feel like the heart has skipped a beat or beat with an irregular pattern. A normal heart rate lies between 60 to 100 beats per minute and arrhythmia can occur with normal heart rate, slow heart rate (called bradycardia), in which heart rate is less than 60 beats per minute or with rapid heart rate (called tachycardia) in which heart beats faster than 100 beats per minute.

### 2.6.1 Causes of Arrhythmia

Arrhythmia can be caused by one of the following reasons:

- Heart disease
- Electrolyte imbalance
- Changes in heart muscle
- After surgery effects

### 2.6.2 Types of Arrhythmias

The most common types of arrhythmias are:

### Premature Ventricular Contraction

It is one type of arrhythmia, in which the heartbeat is initiated by the ventricles rather than the SA node. It is generally referred as “skipped beat”. This is the most common type of arrhythmia, which occurs with or without any heart disease. It could be the result of too much stress, usage of too much cocaine or restless. Sometimes it can also be caused by heart disease. However, most of the time PVC is considered as harmless and rarely needs a treatment.



**Figure. 2.9:** Premature Ventricular Contraction[con17b].

### Atrial Fibrillation

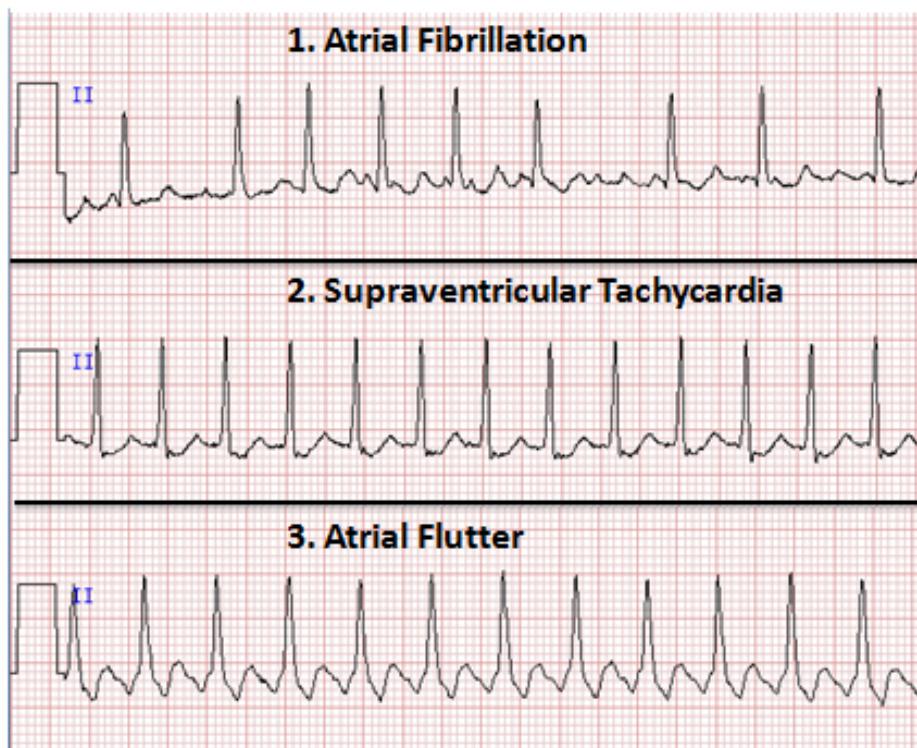
This type of arrhythmia caused by the abnormal contraction of the upper chamber of the heart. During atrial fibrillation, the atria beat irregularly without any coordination with the ventricles. This could results in heart palpitation, shortness of breath and weakness.

### Atrial Flutter

This type of arrhythmia caused by problems in the heart’s electrical system. It is similar to atrial fibrillation but rhythm in atria is more organized than the atrial fibrillation. The risk factors and causes of atrial flutter are similar to those of atrial fibrillation.

### Bradycardia

In this type of arrhythmia, the heart beats slower than the normal pace, usually less than 60 beats per minute. This could be because of the disease in electrical heart system.



**Figure. 2.10:** Atrial Fibrillation, Atrial Flutter and Tachycardia[sum17].

## Tachycardia

In this type of arrhythmia, the heart beats faster than the normal pace, usually, more than 100 beats per minute. When the heart beats too fast, it may not pump blood effectively to the body parts, which could result in shortness of breath.

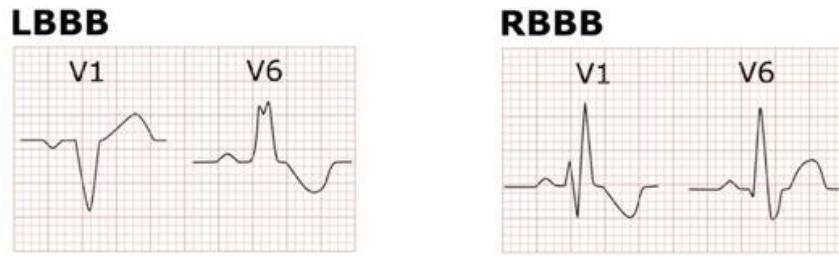
## Heart Block

In this type of arrhythmia, the heart beats slowly because of the delay or complete block of the electrical signal between the upper chambers and the lower chambers of the heart. It is also called atrial ventricular block (AV block).

## Bundle Branch Block

Bundle branch block can be of two types, left bundle branch block (LBBB) and right bundle branch block (RBBB). In a normal heart, both bundles depolarized simultaneously and contract at the same time. In this type of arrhythmia, the affected bundle depolarized

slowly whereas the un-affected bundle depolarized normally which results in a broader QRS complex, generally longer than 120 milliseconds duration. LBBB and RBBB can be seen in Figure 2.11. In RBBB, the delayed activation of the right ventricle gives rise to the ST depression and the T wave inversion in the lead V1 and the wide S wave in the lead V6. Similarly, in LBBB, the delayed activation of the left ventricle, results in the absence of Q wave and tall R wave appeared as M shaped in lead V6 and deep S wave in the lead V1 [cab17].



**Figure. 2.11:** LBBB vs RBBB[bil17].

# 3 Signal Processing and Feature Extraction

Wireless sensor devices and contact-less sensor devices are the current trends in the health informatics. The recent improvements in the sensor devices made it possible for the people to bring this idea into reality. When medical sensor devices are combined with cloud computing, it can be thought of as a complete solution for a healthcare system which can be used not only in hospitals but also can be utilized out of the hospital. These sensors can monitor some vital signs such as body temperature, respiration, heart rate, blood pressure, ECG or EEG.

## 3.1 Devices

Multiple contact-less sensors are used to implement a system for this thesis, which collects data of the user and processes them in real-time. The following devices are used in this work:

### 3.1.1 Magnetic Induction Sensor

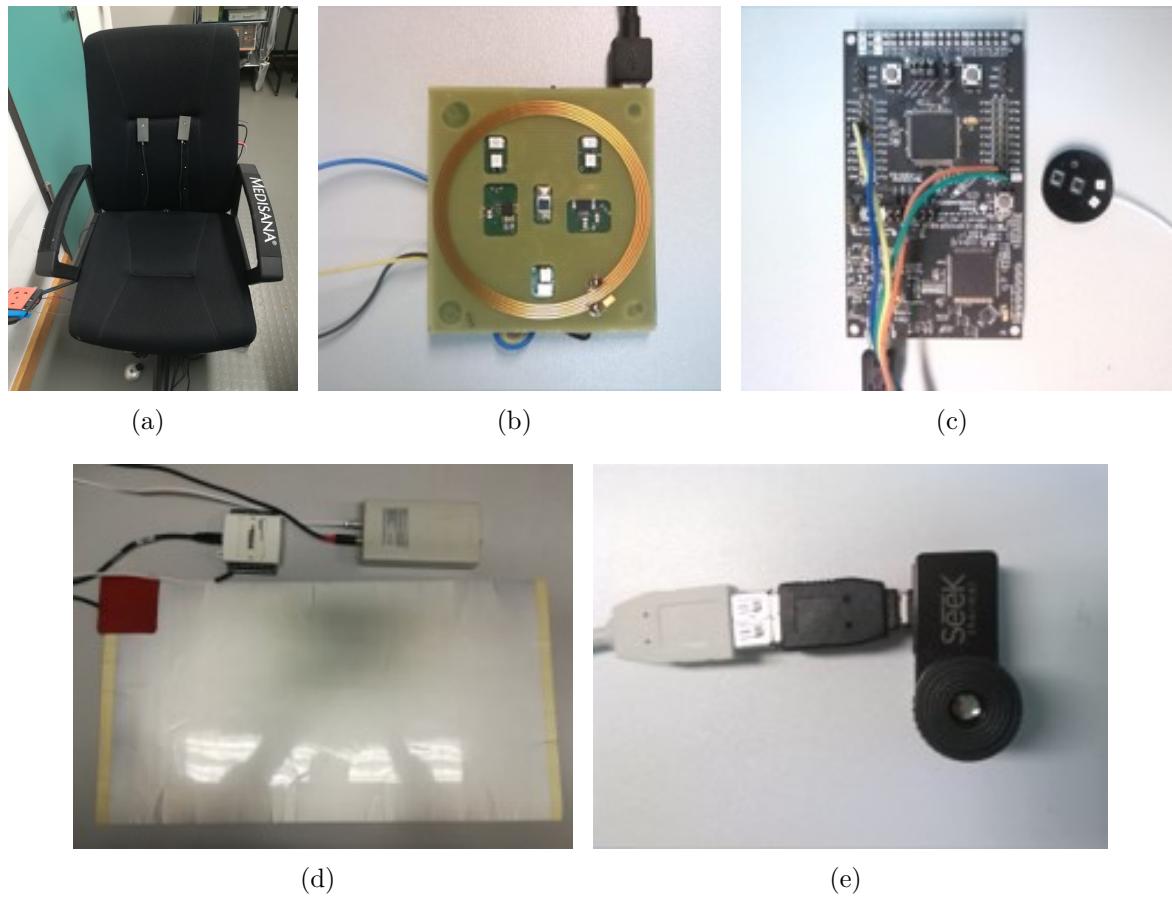
The magnetic induction (MI) sensor uses the magnetic fields to measures the small changes in electrical resistance of the thorax. A magnetic coil is used which induces eddy currents within the thorax. This eddy current reinduces a secondary magnetic field which can be measured with the same or another coil. The amplitude of the eddy current is directly proportional to the magnetic flux density and the conduction of the material. Based on this concept, the thorax conductivity, which changes according to the inflation and deflation of the lungs, enable us to capture the breathing of the patient [MRF13].

The MI sensor provides a data packet of 42 bytes, which splits into the attributes shown in Table 3.1 and the byte identifier is shown in Table 3.2.

As mentioned in Table 3.2, 0x81 and 0x82 represents the byte identifier, but in some cases, it also presents in the data as they are simply the hexadecimal number. The sensor algorithm replaces the 0x81 by 0x8101 and 0x82 by 0x8102 in order to differentiate the values from the byte identifiers. Therefore, to do the correct processing of the sensor data, the hexadecimal value 0x8101 should be replaced by 0x81 and 0x8102 by 0x82.

### 3 Signal Processing and Feature Extraction

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**Figure. 3.1:** A set of sensor devices: (a) an ECG sensor; (b) a MI sensor; (c) a PPG sensor; (d) a BCG sensor; and, (e) a thermal camera.

**Tab. 3.1:** Attributes of MI sensor.

Attributes	Size (Bytes)
MI_RAW	4
MI	4
RED_RAW	4
ECG_RAW	4
IR_RAW	4
RED_AVG	4
ECG_AVG	4
IR_AVG	4
ACC_X	2
ACC_Z	2
ECG_REF	2
RESP_REF	2
BATTERY	2

**Tab. 3.2:** Byte identifiers for the MI sensor.

2-Byte Identifier	Description
0x81	Header
0x82	Data Packet

### 3.1.2 Photoplethysmogram Sensor

The photoplethysmogram (PPG) sensor is used to measures the variations in blood flow in the body with each heartbeat. It is an optical, simple, low cost and non-invasive technique, which can measure various vital signs at the surface of the skin. A PPG sensor uses a light source to illuminate the skin and a photo-detector to measures the variations in the light intensity associated with changes in the oxygen level in blood. The decrease in light intensity indicates the increase in oxygen level in blood, whereas, increase in light intensity indicates the decrease of oxygen level in blood. They can provide valuable information about the cardiovascular system such as the pulse rate.

The sensor provides PPG signals with 4 different channels, a temperature, and accelerometer coordinates. The size of the data changes according to the attributes, as shown in Table 3.3. The temperature value is sent every one second, while, the frequency rate of PPG channels is 100 samples per second. For the accelerometer coordinates, the data rate is 50 samples per second.

**Tab. 3.3:** Attributes of PPG sensor.

2-Byte Identifier	Attributes	Size (Bytes)	Data
0x0050	ppg (8 Bytes)	2	Channel 1
		2	Channel 2
		2	Channel 3
		2	Channel 4
0x0054	Temperature (2 Bytes)	2	Temperature
0x0041	Accelerometer coordinates (6 Bytes)	2	X Coordinate
		2	Y Coordinate
		2	Z Coordinate

### 3.1.3 ECG Sensor

As described in Section 2.2, the ECG signal is usually collected by placing electrodes directly on the body but it has several disadvantages as described in Section 2.4. Therefore,

non-contact capacitive electrodes have been used to collect the ECG signals. Unlike traditional electrodes, which rely on galvanic contact, the capacitive electrodes are insulated from skin using a dielectric material, such as air gap or clothes [Bou17]. The ECG signal propagates via skin to the dielectric material and then to the electrodes through a capacitive coupling. The major drawback of this approach is that it is very sensitive to a body motion.

### 3.1.4 Ballistocardiogram Sensor

The ballistocardiogram (BCG) sensor measures the ballistic forces associated with cardiac contraction and ejection of blood. These ballistic forces are mainly measured by the electromechanical film (EMFi), which converts the mechanical energy into the electrical signal. Most of the time, the EMFi sensing device is placed on a chair or bed, which measures the pressure associated with the cardiac activity.

### 3.1.5 Thermal Camera

A thermal camera is also used to measure the temperature of the person. A thermal Seek camera captures the thermo temperature images from which the temperature is calculated.

## 3.2 ECG Signal Processing

The detection of QRS complex is the basis for processing ECG signal. Regardless of what application is required, the accurate detection of QRS complex is a prerequisite for feature extraction. In order to detect the QRS complex accurately, it is necessary to detect the R-peak position correctly. Once the QRS complex is identified, further operations can also be performed on the signal such as heart rate calculation, classification of ECG signal and P and T detection.

The “QRS Complex” is the combination of Q, R and S waves and it represents the contraction of the ventricles. It plays a significant role in the detection of cardiac arrhythmias.

Many methods have already been proposed for the detection of QRS complex. These methods fall into 3 categories [PZZ10]:

### 3.2.1 Filter Method

The filter method uses a bandpass filter to filter the ECG signal [PT85][RSN97]. In this method, a QRS complex is intensified by suppressing the P and T wave. This method is generally very quick and takes less time to implement. But the major drawback of this method is that the frequency band of QRS complex and of noise overlapping affect its performance.

### 3.2.2 Artificial Intelligence Method

The detection of QRS complex using this method is fast, accurate and more robust, but in reality, it is time-consuming and difficult to implement [XHT92][Pie91][CSCB90]. Therefore, this method is not very popular and not widely used as compared to the other methods.

### 3.2.3 Wavelet Transform Method

Wavelet transform method becomes popular in detecting the QRS complex. It is based on time-frequency analysis. It is efficient and takes less to implement. Many researchers have already used wavelet transform for detecting the QRS complex. Yazhu Qiu [QDFM06] used Mexican-hat wavelet to detect ECG signal. In the proposed method, although the processing was fast, it sometimes did not detect the onset and offset of QRS complex accurately. Nevertheless, it is considered as faster and easier to implement and it is used to extract the ECG signal features in this thesis.

## 3.3 Wavelet Transform

A wavelet transform is a very useful tool for analyzing the signal simultaneously in both time and frequency domain [Add17]. It uses a little wavelike functions known as **wavelets**. Wavelets are used to transform a signal into another representation where signal information can be viewed in a more useful form.

Generally, there are two operations involved with wavelet. Either they can be stretched or squeezed or can be translated to other locations on the signal and if the wavelet matches the shape of the signal at specific location or scale, it produces a large transform value. And similarly, if the signal and the wavelet do not correlate, it produces a low transformed value. There is a single function called “mother wavelet” which is stretched or translated

to produce a family of basis functions known as “daughter wavelet”. A mother wavelet is defined as:

$$\Psi_{a,b}(t) = \frac{1}{\sqrt{|a|}} \Psi\left(\frac{t-b}{a}\right), \quad a, b \in \mathbb{R}, a \neq 0 \quad (3.1)$$

where  $a$  is the scaling parameter which measures the degree of the scale, and  $b$  is the translation parameter, which measures the time location of the wavelet. If  $|a| < 1$ , then it mainly corresponds to higher frequencies. And on the other hand, if  $|a| > 1$ , it corresponds to lower frequencies. It is important to note here that the variation in time and frequency scale of the wavelet is supervised by the Heisenberg's uncertainty principle. At large scale, the time domain is not very clear, whereas, in the frequency domain is much finer. As the scale decreases, the frequency domain becomes worse, whereas, time domain becomes finer.

The wavelet transform of a signal  $f(x)$  is defined as:

$$X_W(a, b) = \frac{1}{\sqrt{|a|}} \int_{-\infty}^{\infty} \left( \frac{t-b}{a} \right) f(x) dx \quad (3.2)$$

If  $a = 2^j (j \in Z)$ , then the wavelet transform is called the dyadic wavelet transform or the binary wavelet transform [MH92]. To calculate the dyadic wavelet transform of a signal, a mother wavelet is first chosen and then dilated by a power of two. The Quadratic Spline wavelet is used with ECG signal as the mother wavelet. It has a property that the sharp edges occur at the zero crossing point in the transformation, which corresponds to the local maxima or minima of the smoothed signal. The dyadic wavelet transform of a signal  $f(n)$  can be calculated by using Mallat's Algorithm [PZZ10].

## 3.4 Mallat's Algorithm

Mallat algorithm [MH92] for the signal  $f(n)$  is defined as follows:

$$s_{2^j} f(n) = \sum h_k s_{2^{j-1}} f(n - 2^{j-1}k), \quad (3.3)$$

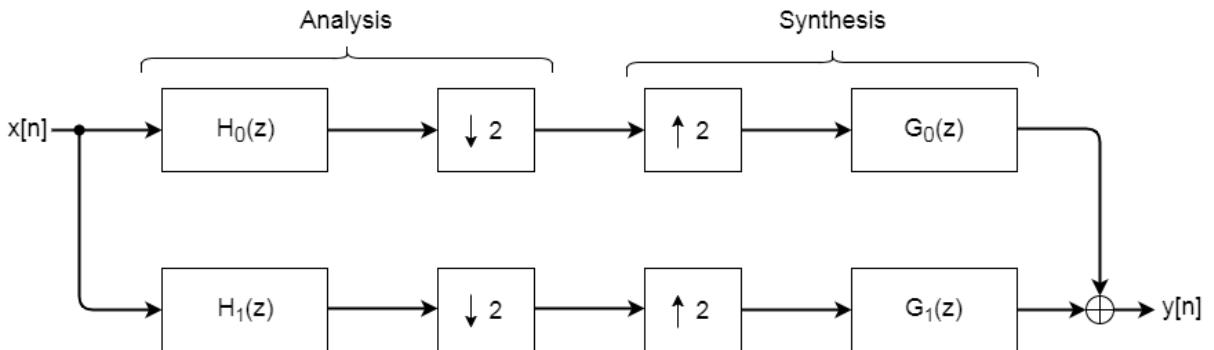
$$w_{2^j} f(n) = \sum g_k s_{2^{j-1}} f(n - 2^{j-1}k). \quad (3.4)$$

where,  $s_{2^0}f(n)$  is the original signal to be processed, in this case, it is the ECG signal.  $w_{2^j}f(n)$  is the wavelet transform of the input signal  $f(n)$  at scale  $2^j$ .  $h_k$  and  $g_k$  are the coefficients of a low-pass filter and high-pass filter respectively. The wavelet transform of a signal  $f(n)$  is obtained by passing the input signal through a digital filter bank, which consists of a low-pass and high-pass filters. The design and implementation of the Wavelet transform is based on perfect reconstruction filter banks. The coefficients of low-pass filter  $H(z)$  and high-pass filter  $G(z)$  can be calculated by constructing a filter bank.

### 3.5 Filter Bank Construction

A biorthogonal filter bank is designed based on Quadratic Spline wavelet. A filter bank is a set of filters and sampling operators [SN96]. The downsampling operators are decimators, whereas, upsampling operators are expanders. In a 2-channel filter bank, the analysis and synthesis phase both contain a low-pass and a high-pass filter. These filters are  $H_0(z)$  and  $H_1(z)$  for the analysis phase, and  $G_0(z)$  and  $G_1(z)$  for the synthesis phase respectively [WLH01], as shown in Figure 3.2. After passing the input signal  $X[n]$  from the filters, the resulting signal is first down-sampled by 2 and then up-sampled by 2 respectively, producing the final output signal  $Y[n]$ .

The filters  $H_0(z)$  and  $H_1(z)$  are not ideal filters, therefore, their responses overlap, there is aliasing in each channel and there is distortion. The synthesis filters  $G_0(z)$  and  $G_1(z)$  should be adjusted according to the analysis filters  $H_0(z)$  and  $H_1(z)$  to cancel out the error.



**Figure. 3.2:** Two-channel filter bank

The idea is to determine  $H_0$ ,  $H_1$ ,  $G_0$  and  $G_1$  such that,  $Y[n]$  is a delayed version of input signal  $X[n]$ . This is called as perfect reconstruction filter bank. A perfect reconstruction filter bank is also known as “biorthogonal” and the associated filters as biorthogonal filters. A perfect reconstruction with an  $l$ -step delayed in  $z$  domain without upsampling and downsampling represented as:

$$H_0(z)G_0(z) + H_1(z)G_1(z) = z^{-l} \quad (3.5)$$

The combination of downampler ( $\downarrow 2$ ) and an upsampler ( $\uparrow 2$ ) removes the odd number components. In  $z$  domain, it can be written as:

$$(\downarrow 2)(\uparrow 2)H_0X = \frac{1}{2}[H_0(z)X(z) + H_0(-z)X(-z)] \quad (3.6)$$

It contains only the even components as the odd components have already been removed. The term  $H_0(-z)X(-z)$  is an aliasing term. This aliasing term has to cancel the aliasing effect from the other channel to remove the alias.

After passing the input signal from the channel 1, it produces:

$$Y_0(z) = \frac{1}{2}G_0(z)[H_0(z)X(z) + H_0(-z)X(-z)] \quad (3.7)$$

Similarly, for the 2nd channel, it produces:

$$Y_1(z) = \frac{1}{2}G_1(z)[H_1(z)X(z) + H_1(-z)X(-z)] \quad (3.8)$$

Adding the output of these 2 channels produce the final output.

$$\begin{aligned} Y(z) &= Y_0(z) + Y_1(z) \\ &= \frac{1}{2}G_0(z)[H_0(z)X(z) + H_0(-z)X(-z)] + \frac{1}{2}G_1(z)[H_1(z)X(z) + H_1(-z)X(-z)] \end{aligned} \quad (3.9)$$

Arranging  $Y(z)$  in such a way so that, one part depends on  $X(z)$  and the other part on  $X(-z)$ . We get,

$$Y(z) = \frac{1}{2}[G_0(z)H_0(z) + G_1(z)H_1(z)]X(z) + \frac{1}{2}[G_0(z)H_0(-z) + G_1(z)H_1(-z)]X(-z) \quad (3.10)$$

In Equation 3.10, the part that depends on  $X(-z)$  is the aliasing part, and the part that depends on  $X(z)$  is the distortion part.

### 3 Signal Processing and Feature Extraction

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The perfect reconstruction for filter bank can be achieved if the following two conditions are satisfied.

1. No aliasing:

$$G_0(z)H_0(-z) + G_1(z)H_1(-z) = 0 \quad (3.11)$$

2. No distortion:

$$G_0(z)H_0(z) + G_1(z)H_1(z) = mz^{-k} \quad (3.12)$$

where  $m$  is a constant and  $k$  is a time delay.

In order to satisfy condition 1 i.e., to get rid of aliasing, choose:

$$\begin{aligned} G_0(z) &= H_1(-z), \\ G_1(z) &= -H_0(-z) \end{aligned} \quad (3.13)$$

Substituting the values of Equation 3.13 in 3.11 yields:

$$H_0(-z)H_1(-z) - H_0(-z)H_1(-z) = 0 \quad (3.14)$$

which implies to 0, hence the aliasing is removed.

In order to remove the distortion, i.e, to satisfy equation 3.12, lets assume that,

$$P_0(z) = G_0(z)H_0(z) \quad (3.15)$$

This is a low-pass product filter. The high-pass product filer is  $P_1(z) = G_1(z)H_1(z)$ . The relationship between the terms  $P_0$  and  $P_1$  can be deduce by Equation 3.13:

$$P_1(z) = G_1(z)H_1(z) = -H_0(-z)G_0(-z) = -P_0(-z) \quad (3.16)$$

The equation 3.12 can be re-written as:

$$P_0(z) - P_0(-z) = mz^{-k} \quad (3.17)$$

The design of 2-channel filter bank is now reduced to only two steps:

1. Design a low-pass filter which satisfy Equation 3.17.

2. Factorize  $P_0$  to find the values of  $H_0$  and  $G_0$ .

Equation 3.17 can be further simplified by normalizing  $P_0(z)$  by  $z^k$  to center it. Substituting  $P(z)$  by  $z^k P_0(z)$  and  $P(-z)$  by  $-z^k P_0(-z)$  produces:

$$P(z) + P(-z) = m \quad (3.18)$$

Equation 3.18 implies that  $P(z)$  is a half-band filter, in which all even powers of  $z$  in  $P(z)$  are zero except for the constant term (coefficient of the term  $z^0$ ). Furthermore, all the odd powers cancel out when  $P(z)$  and  $P(-z)$  are added.

One possibility to design the low-pass filter  $P_0(z)$  is to use the Daubechies construction [SN96]:

$$P_0(z) = (1 + z^{-1})^{2p} Q(z) \quad (3.19)$$

$P_0(z)$  is called “maxflat filter” where  $p$  can be any integer and has  $2p$  coefficients, i.e., the length of the filter.  $(1 + z^{-1})^{2p}$  is called *binomial filter* and it is a spline filter, and  $Q(z)$  be a polynomial of degree  $(2p - 2)$  is chosen such that  $P_0(z)$  satisfy the half-band filter property. Moreover, the order of  $P_0(z)$  is always an even number.  $p$  defines the number of zeros to be placed at  $\pi$  in a unit circle.

Any value of  $p$  can be chosen and the polynomial  $Q(z)$  depends on the value of  $p$ , i.e.,  $Q(z)$  should be chosen in such a way that it satisfies the half-band filter property. If  $p = 1$ , then this represents the Haar case and it has 2 coefficients.

In this case,  $p = 2$  is chosen. Therefore, the number of coefficients are 4 and degree of  $Q(z)$  be 2. Then Equation 3.19 becomes:

$$P_0(z) = (1 + z^{-1})^4 Q(z) \quad (3.20)$$

Let  $Q(z)$  be of form,

$$Q(z) = a + bz^{-1} + az^{-2} \quad (3.21)$$

Substituting Equation 3.21 in 3.20 produces:

$$P_0(z) = a + (4a + b)z^{-1} + (7a + 4b)z^{-2} + (8a + 6b)z^{-3} + (7a + 4b)z^{-4} + (4a + b)z^{-5} + az^{-6} \quad (3.22)$$

To satisfy the condition on  $P_0(z)$ , equating all the coefficients of odd power of  $z$  to 0, except for the center term, i.e., term at  $z^{-3}$  which equates to 1, produces:

$$4a + b = 0 \quad (3.23)$$

$$8a + 6b = 1 \quad (3.24)$$

Solving Equation 3.23 and 3.24 yields:

$$a = \frac{-1}{16}, b = \frac{1}{4} \quad (3.25)$$

From Equation 3.20, 3.21 and 3.25, we get:

$$P_0(z) = \frac{(1 + z^{-1})^4(-1 + 4z^{-1} - z^{-2})}{16} \quad (3.26)$$

Factorizing  $P_0(z)$  to get  $H_0(z)$  and  $G_0(z)$ :

$$\begin{aligned} H_0(z) &= \frac{(1 + z^{-1})^3}{4} \\ &= \frac{(1 + 3z^{-1} + 3z^{-2} + z^{-3})}{4} \end{aligned} \quad (3.27)$$

$$\begin{aligned} G_0(z) &= \frac{(1 + z^{-1})(-1 + 4z^{-1} - z^{-2})}{4} \\ &= \frac{(-1 + 3z^{-1} + 3z^{-2} - z^{-3})}{4} \end{aligned} \quad (3.28)$$

Then by equation 3.13, we have:

$$\begin{aligned} H_1(z) &= G_0(-z) \\ &= \frac{(-1 - 3z^{-1} + 3z^{-2} + z^{-3})}{4} \end{aligned} \tag{3.29}$$

$$\begin{aligned} G_1(z) &= -H_0(-z) \\ &= \frac{(-1 + 3z^{-1} - 3z^{-2} + z^{-3})}{4} \end{aligned} \tag{3.30}$$

Therefore, the filter coefficients are:

$$\begin{array}{llll} h_0(0) = & \frac{1}{4} & h_0(1) = & \frac{3}{4} \\ h_0(2) = & \frac{3}{4} & h_0(3) = & \frac{1}{4} \\ h_1(0) = & \frac{-1}{4} & h_1(1) = & \frac{-3}{4} \\ h_1(2) = & \frac{3}{4} & h_1(3) = & \frac{1}{4} \\ g_0(0) = & \frac{-1}{4} & g_0(1) = & \frac{3}{4} \\ g_0(2) = & \frac{3}{4} & g_0(3) = & \frac{-1}{4} \\ g_1(0) = & \frac{-1}{4} & g_1(1) = & \frac{3}{4} \\ g_1(2) = & \frac{-3}{4} & g_1(3) = & \frac{1}{4} \end{array} \tag{3.31}$$

The coefficients of filters are just simple fractions, therefore, the amount of computation and time needed for the transformation is small. As our interest is only in the decomposition of the signal, therefore, we will consider only the  $H_0$  and  $H_1$  filters coefficients.

Let  $f(n)$  be the ECG signal, then the wavelet transform of  $f(n)$  can be calculated by using Mallat algorithm as follows:

$$s_{2^0}f(n) = f(n) \tag{3.32}$$

$$s_{2^j}f(n) = \frac{1}{4}s_{2^{j-1}}f(n) + \frac{3}{4}s_{2^{j-1}}f(n - 2^{j-1}) + \frac{3}{4}s_{2^{j-1}}f(n - 2^j) + \frac{1}{4}s_{2^{j-1}}f(n - 2^j * 3) \tag{3.33}$$

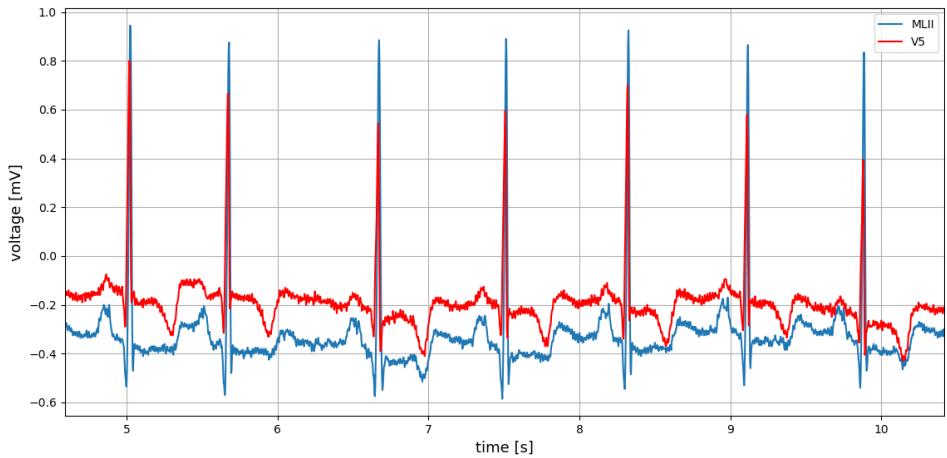
$$w_{2^j}f(n) = \frac{-1}{4}s_{2^{j-1}}f(n) + \frac{-3}{4}s_{2^{j-1}}f(n - 2^{j-1}) + \frac{3}{4}s_{2^{j-1}}f(n - 2^j) + \frac{1}{4}s_{2^{j-1}}f(n - 2^j * 3) \quad (3.34)$$

where  $w_{2^j}f(n)$  is the Biorthogonal Spline Wavelet Transform of ECG signal at scale  $2^j$ .

## 3.6 Dataset

The MIT-BIH Arrhythmia dataset is used for the implementation of the system. It contains 48 hours of recording of 47 subjects. Each record contains 2 signals, namely MLII and V5, with a recording of 30 minutes duration. The sample rate for the recording is 360 samples per second per channel with 11-bit resolution over a 10mV range. Each record consists of 3 files:

- Header file (.hea): It contains information such as the number of samples, sampling frequency, ECG signal format, number of ECG leads and their types, patient's history and the detailed clinical information.
- ECG signals (.dat): It contains the original signal values of both MLII and V5 leads. The signals from MLII lead are used in the analysis.
- Attribute file (.atr): It contains the annotation information of the ECG signal, annotated by the doctors.



**Figure. 3.3:** The ECG signals from MIT-BIH dataset.

There is a specific python package *wfdb-python* available for reading the data from the MIT-BIH dataset. The ECG signals of one of the patients can be seen in Figure 3.3. It contains 2 signals, namely, MLII and V5.

The signals are generally contaminated with noise or baseline drift. Therefore, they are required to be processed in order to achieve better signals.

## 3.7 Preprocessing

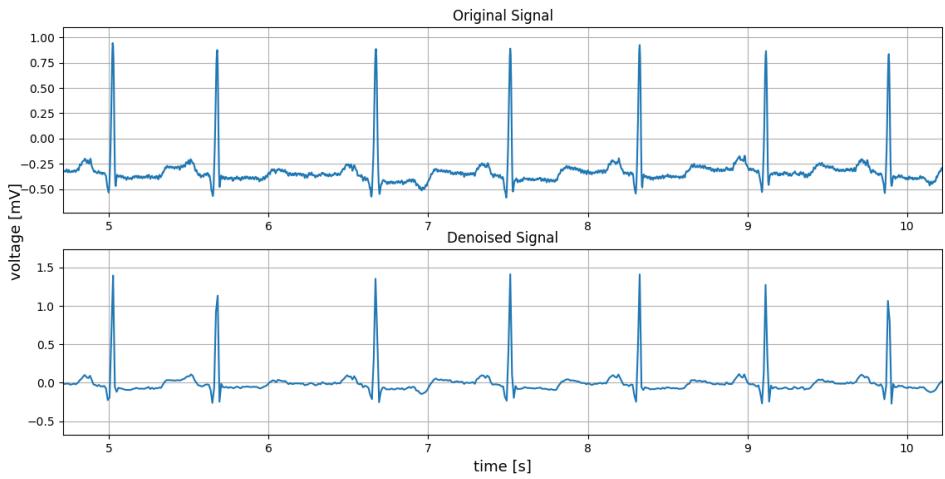
Two different methods have been used to remove the noise and artifacts from the signal in the system implementation.

1. Wavelet transform method
2. Band-pass filter method

### 3.7.1 Wavelet Transform Method

The wavelet transform decomposes the signal into different frequency bands by passing the signal through high-pass and low-pass filter respectively, which results in 2 sets of coefficients namely, approximation coefficients and detail coefficients. The approximation coefficients contain the low-pass filter coefficients and the detail coefficients contain the high-pass filter coefficients. The next step is to split the approximation coefficients again into 2 parts using the same procedure and so on.

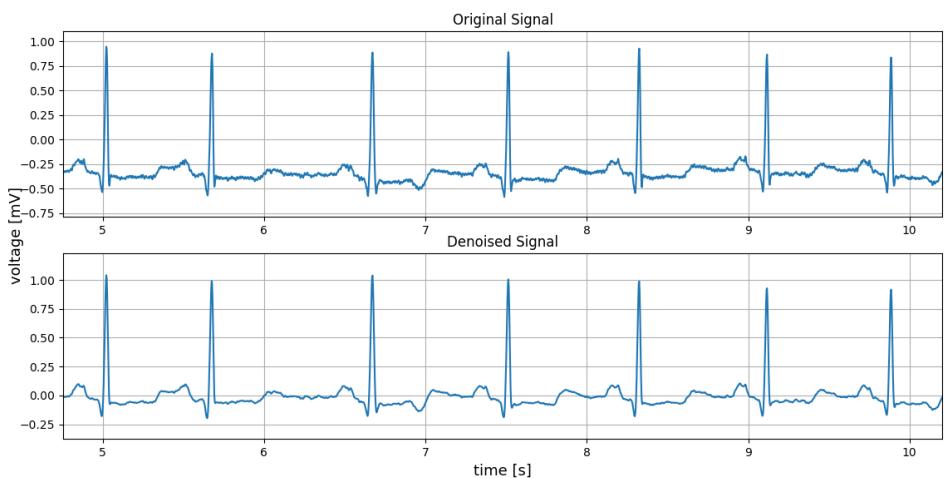
The original signal contains the high-frequency noise and the baseline drift. The wavelet transform can be used to remove the corresponding noises and the baseline drift. The process starts by decomposing the original signal into 8 layers using Wavelet type *bior2.6*, which results in the corresponding detail and approximation coefficients. Mostly, the layers 1 and 2 of the detail coefficients contain the high-frequency noise and the layer 8 of the approximation coefficients contain the baseline drift. Therefore, the layers 1 and 2 of the detail coefficients and layer 8 of the approximation coefficients are set to 0, which then results in the de-noised signal with no baseline drift. The resulting ECG signal is shown in Figure 3.4.



**Figure. 3.4:** The filtered ECG signal using wavelet.

### 3.7.2 Band-pass Filter Method

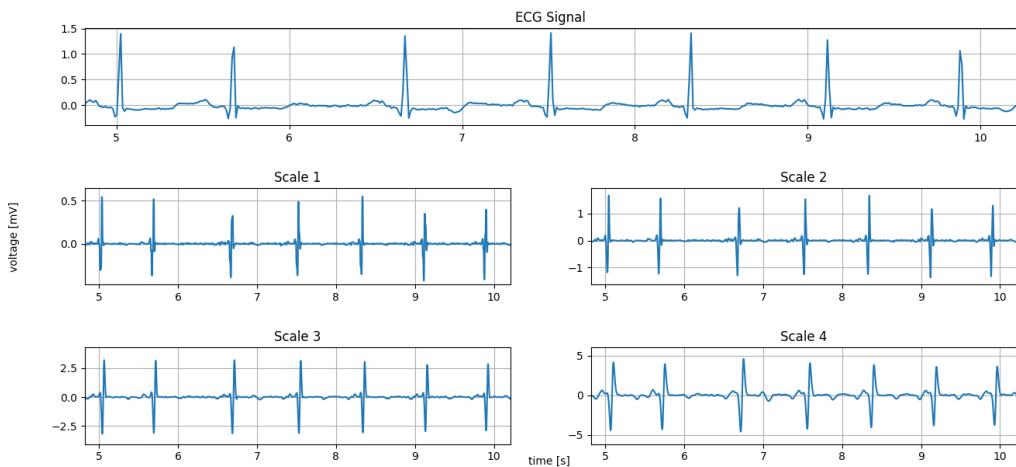
A band-pass filter is a type of filter, which passes frequencies only in a certain range or spread without disturbing the input signal. A band-pass filter can be used to reduce the baseline drift, motion artifacts and high-frequency noise from the ECG signal. A passband of 0.5 Hz to 40 Hz has been used. After applying the band-pass filter, this results in the denoised signal with no high-frequency and baseline drift. The denoised signal is shown in Figure 3.5.



**Figure. 3.5:** The filtered ECG signal using bandpass filter.

## 3.8 QRS Detection

From Equation 3.33 and 3.34, the Biorthogonal Spline Wavelet Transform of ECG signal is obtained, which is the first derivative of the signal at different scales. The signal is decomposed into 4 levels, as shown in Figure 3.6. The procedure starts by first locating the R peaks and then the onset and offset of QRS complexes, and finally the onset and offset of P and T waves. Due to Wavelet characteristic derivative, this wavelet transforms the signal maxima and minima into the zero crossing point at the different scales, which makes it easier to detect the location of P, QRS and T waves [E10].

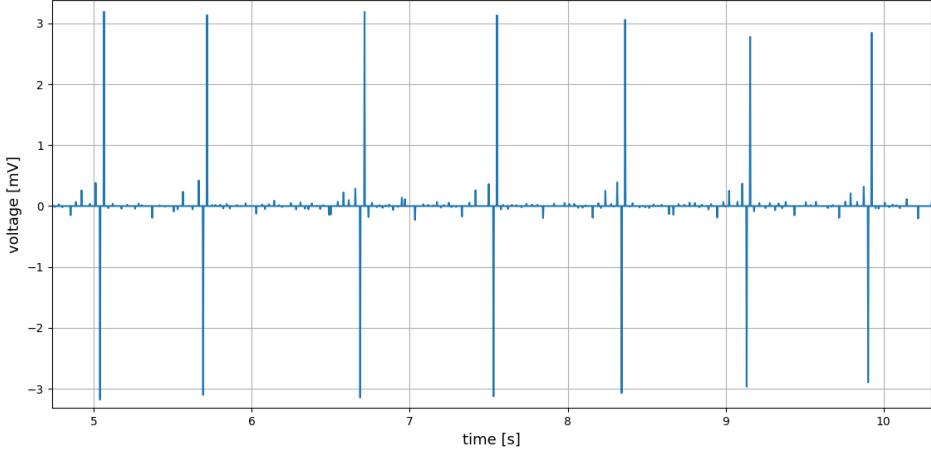


**Figure. 3.6:** ECG signal and its decomposition at different scales.

**Tab. 3.4:** Wavelet transform ECG signal frequency range[SLL14].

Transform Scale	Frequency Range (Hz)
$2^1$	90.0~180.0
$2^2$	29.92~84.24
$2^3$	1.52~38.88
$2^4$	5.76~19.44

Most of the QRS complex energy lies between 3 Hz and 40 Hz, and it corresponds to the 3<sup>rd</sup> scale as shown in Table 3.4. The R peaks correspond to the zero-crossing point of the modulus maxima pair, with a little delay, therefore, first all the positive and negative extrema on scale 3 be identified. The extrema are shown in Figure 3.7. To reduce the influence of noise and other interference in locating the R peaks, the scale 3 signal is



**Figure. 3.7:** Maximum and minimum values on scale 3.

divided into four parts, let's say,  $A1, A2, A3$  and  $A4$ . To find the average maximum and minimum values, the maximum and minimum values from each part are identified.

$$MAX = \frac{\max(A1) + \max(A2) + \max(A3) + \max(A4)}{4} \quad (3.35)$$

$$MIN = \frac{\min(A1) + \min(A2) + \min(A3) + \min(A4)}{4} \quad (3.36)$$

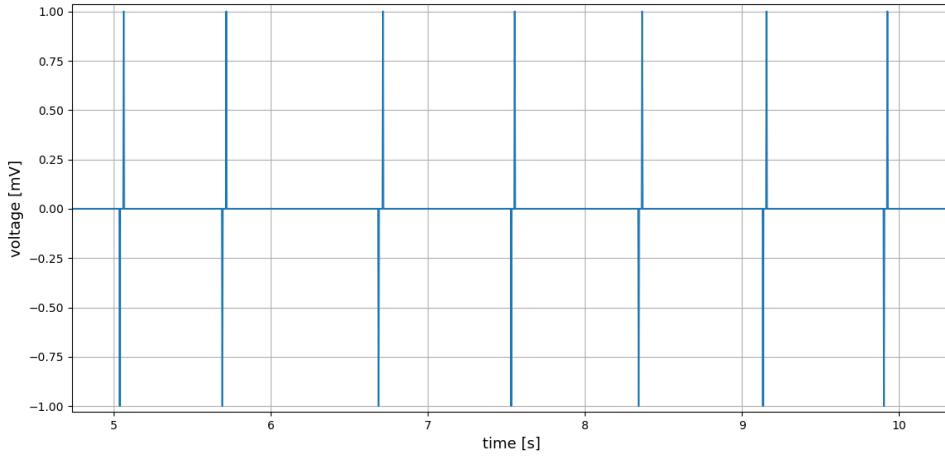
Not all the extrema are important, therefore, only modulus maxima pair in certain scope can be focused and the rest can be ignored. The threshold are calculated as:

$$Th_1 = \frac{MAX}{2}, Th_2 = \frac{MIN}{2} \quad (3.37)$$

The threshold values can be adjusted. If they are too big, then the missing probability of R peaks would be higher and if they are too low, then the noise or interference can be misdetected as R peaks. The thresholds defined above provided the best result in our experiment. The modulus maxima pair are shown in Figure 3.8.

The best modulus maxima pair corresponds to the R peaks and the value of R peaks lie at the zero-crossing point of modulus maxima pair with a little delay. For compensating the delay, a maximum value can be searched in the window of 20 points to the zero-crossing point to determine the accurate position of R peaks.

To compensate the false R peak detection or misdetection, the distance between the adjacent R peaks is calculated. If the distance is less than 40% of the average RR interval,

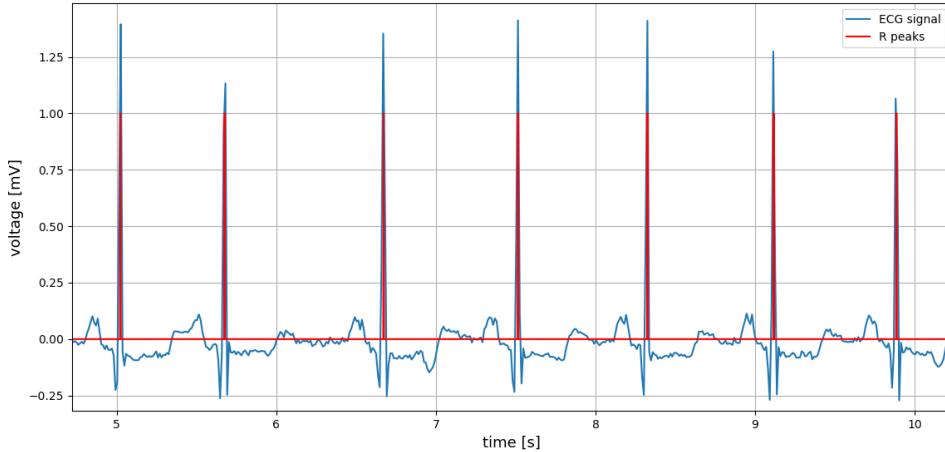


**Figure. 3.8:** Maximum and minimum values pair for finding the R peaks.

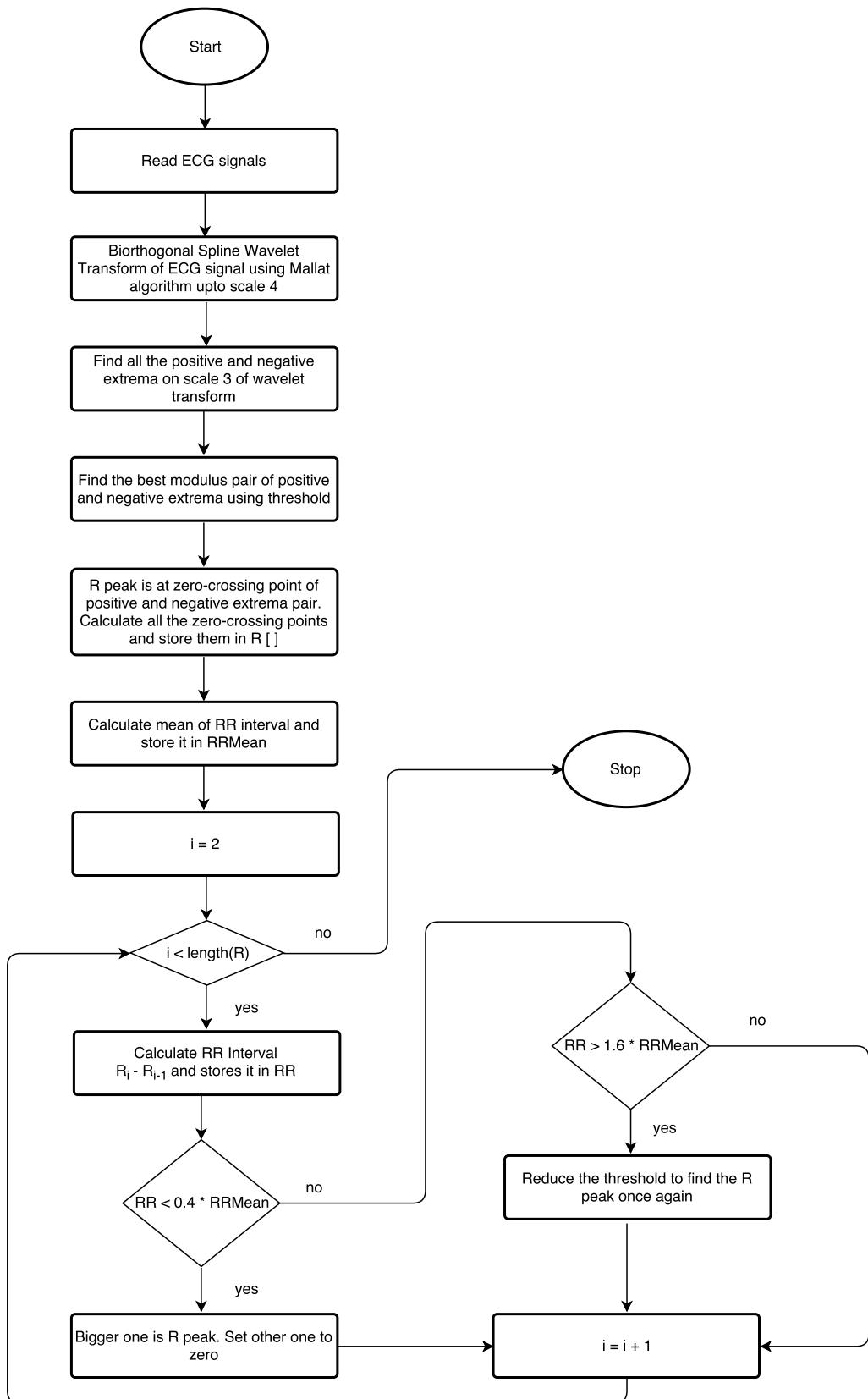
then one of the peaks is misdetected. Therefore, the larger one is kept as R peak and the smaller one is eliminated.

If the distance between adjacent R peaks is greater than 160% of the average RR interval, it is considered as misdetection. Therefore, the threshold values defined in Equation 3.37, are further reduced and R peak is searched again in the adjacent R peaks window or interval.

The detected R-peaks are shown in Figure 3.9. The flowchart for finding the R peaks is shown in Figure 3.10.



**Figure. 3.9:** Detected R peaks.



**Figure. 3.10:** Flowchart for locating R peaks.

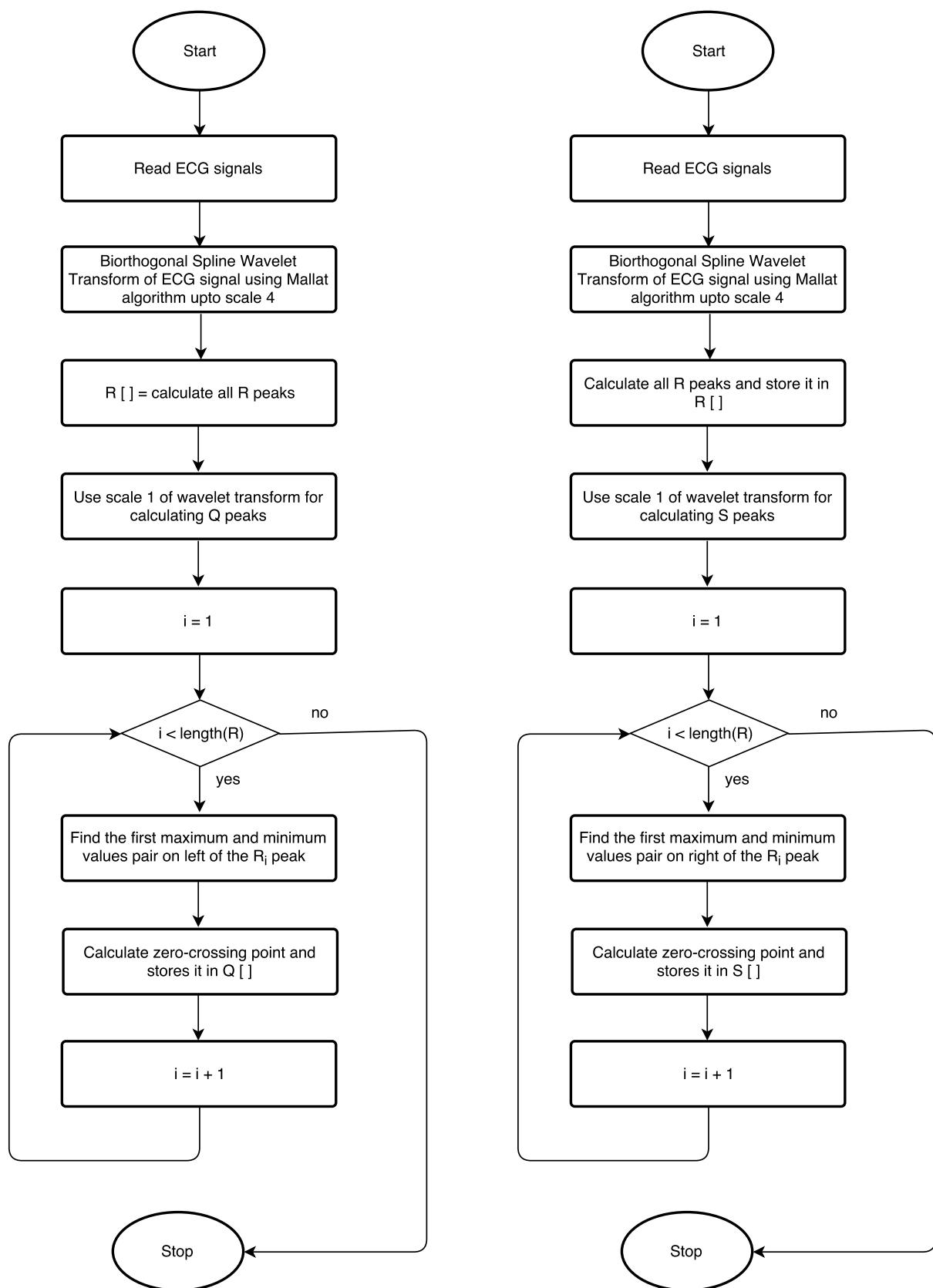
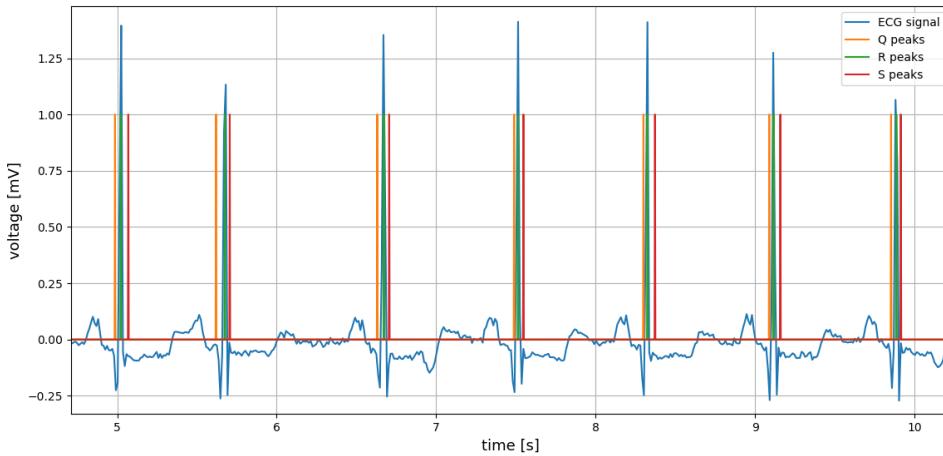


Figure. 3.11: Flowchart for locating Q and S peaks.

Q and S peaks generally are of high frequency. Therefore, their energies mainly lie at the 1<sup>st</sup> scale. For finding the Q wave, the algorithm starts by looking on the left side of the R wave and finds the first non-zero value i.e. the Q wave. And because of the delay, the minimum value is searched in the window of 10 points to the detected Q wave. The same process is executed for the S wave, but in this case, the direction was on the right side of the R wave. The detected QRS complex can be seen in Figure 3.12.



**Figure. 3.12:** Detected Q, R and S peaks.

After detecting the QRS complex, P and T waves are required to be detected as they are important for the identification of the arrhythmia. P wave occurred before the QRS complex and T wave after the QRS complex. Therefore, they can be detected based on the QRS location.

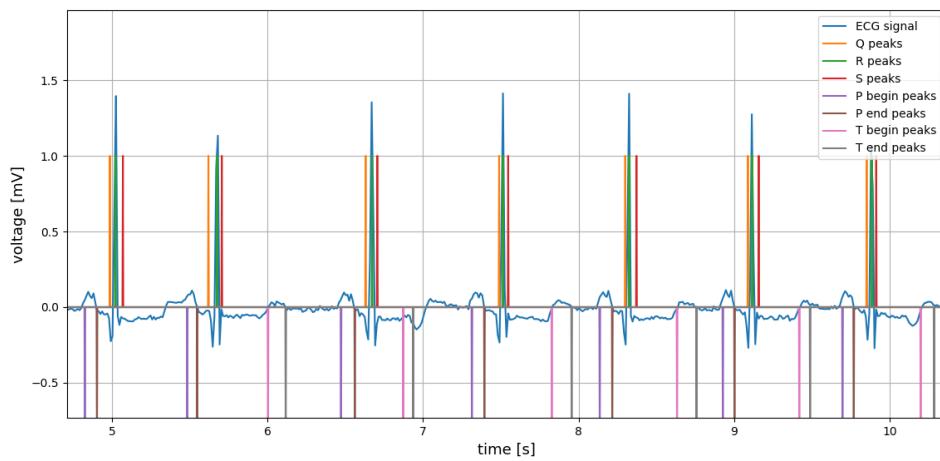
## 3.9 P and T Wave Detection

After the detection of QRS complex, the P and T waves are also detected. According to power spectra of ECG signal [TWT84] and Table 3.4, most of the P and T waves energy lies at scale 4. Therefore, the scale 4 is selected to detect P and T waves.

The corresponding modulus maxima pair of P and T waves can be seen in Figure 3.6 at scale 4 before and after the QRS complex. Therefore, P and T waves can be searched in a window before and after the QRS complex. A window size of 100 is used for detecting the P wave and T waves. The P wave is searched within the 33% of the average RR interval to the left of QRS complex and T wave is searched within the 67% to the right of QRS complex. The P and T waves lie at the zero-crossing point of the identified modulus maxima pair in their respective windows. Because of the delay, a maximum value is searched in the

window of 20 points to the zero-crossing point to determine the accurate position of P and T waves.

All detected waves are shown in Figure 3.13. The Flowchart for finding the P and T waves are shown in Figures 3.14 and 3.15 respectively.



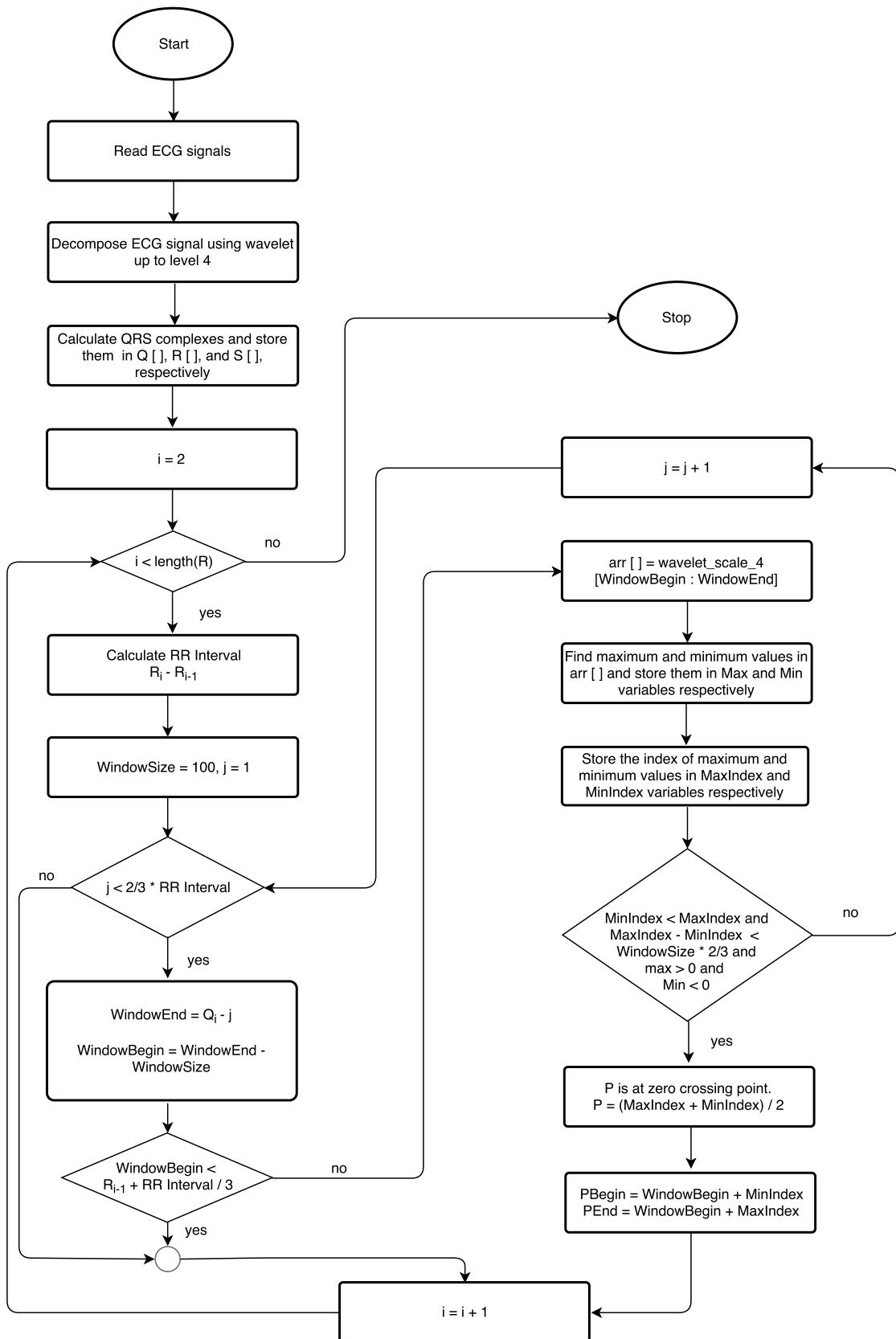
**Figure. 3.13:** Detected P,Q,R,S and T waves.

## 3.10 Heart Rate Calculation

The heart rate is calculated by using the RR interval. The formula to calculate the heart rate is:

$$HeartRate = sample\_rate \times \frac{60}{RRinterval} \quad (3.38)$$

where *sample\_rate* is the sample rate of the ECG signal and 60 is multiplied to convert the heart rate into beats per minute.



**Figure. 3.14:** Flowchart for locating P wave.

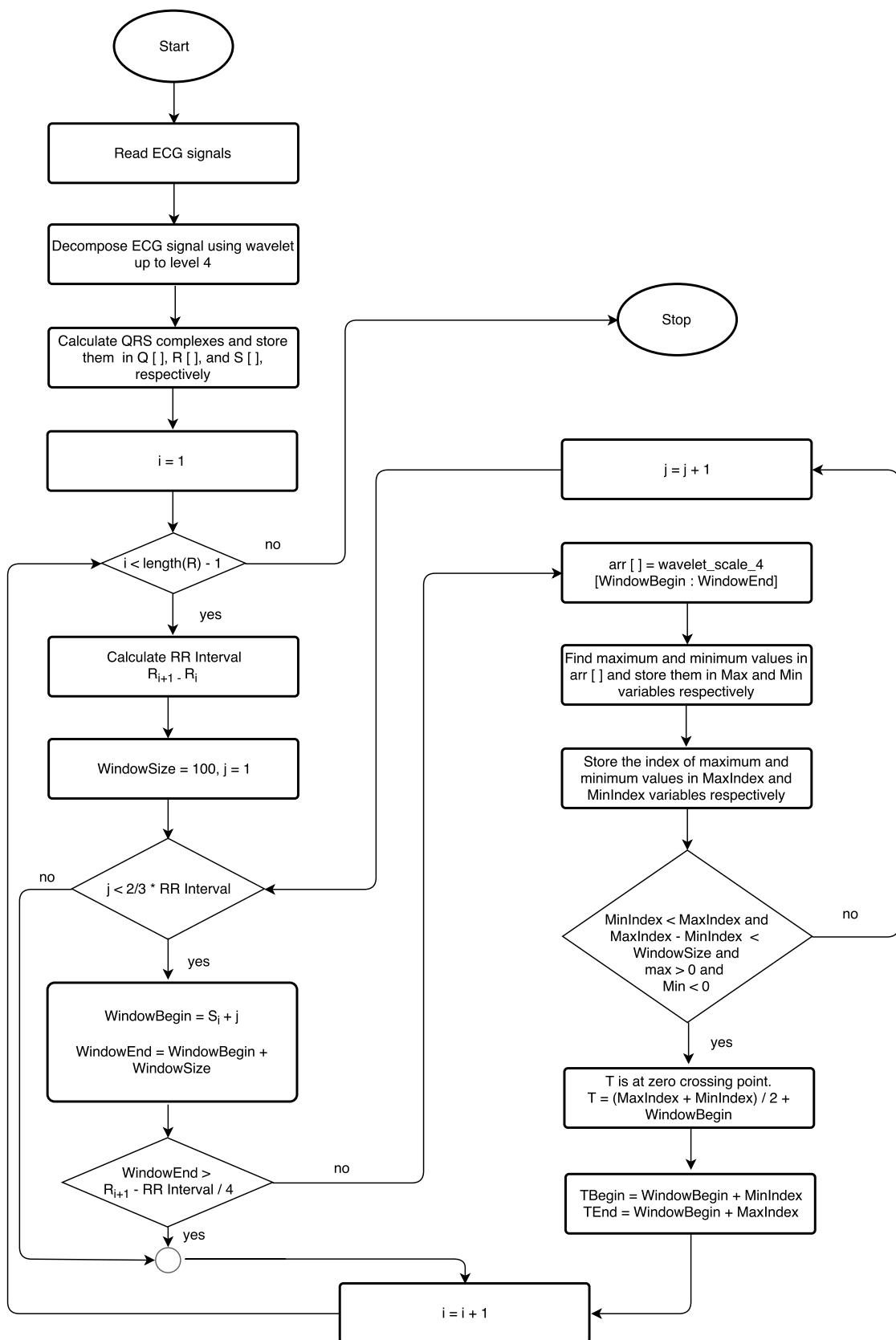
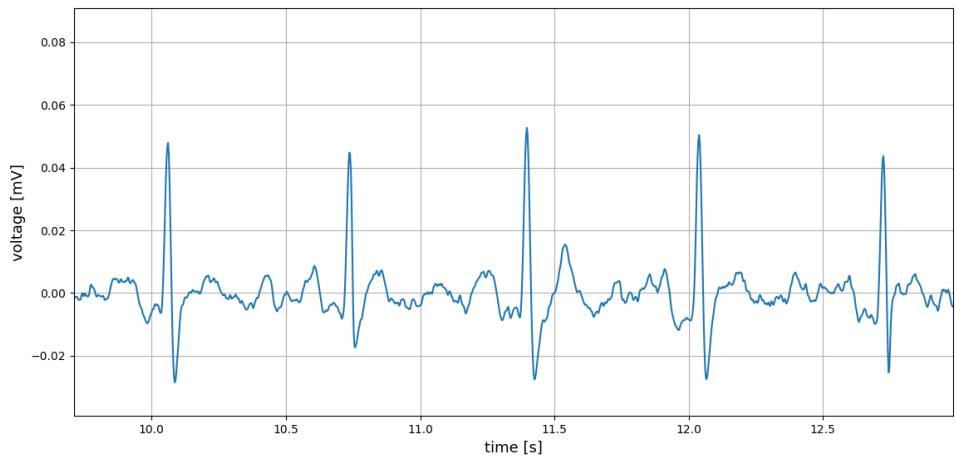


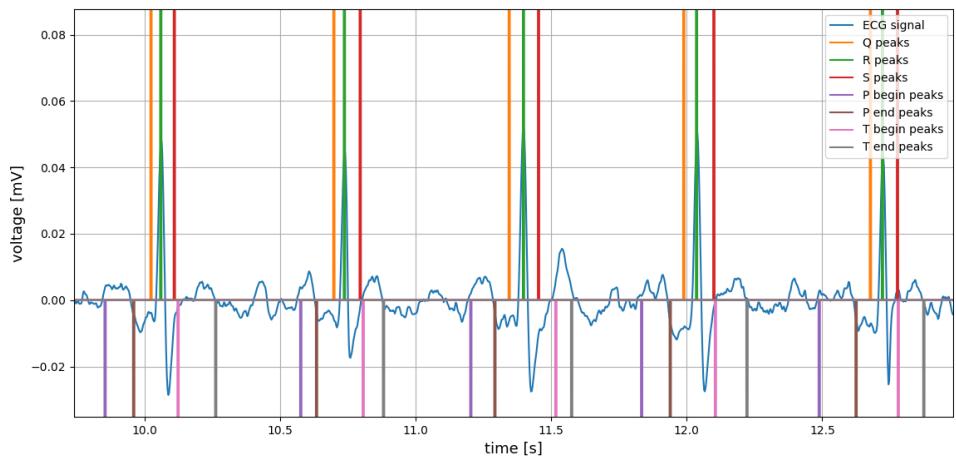
Figure. 3.15: Flowchart for locating T wave.

### 3.11 Algorithm Execution on ECG Chair Data

The data used in the development of ECG feature extraction algorithm is taken from MIT-BIH dataset and the algorithm works great with that dataset. The original ECG signal from the chair is shown in Figure 3.16 and the extracted features are shown in Figure 3.17.



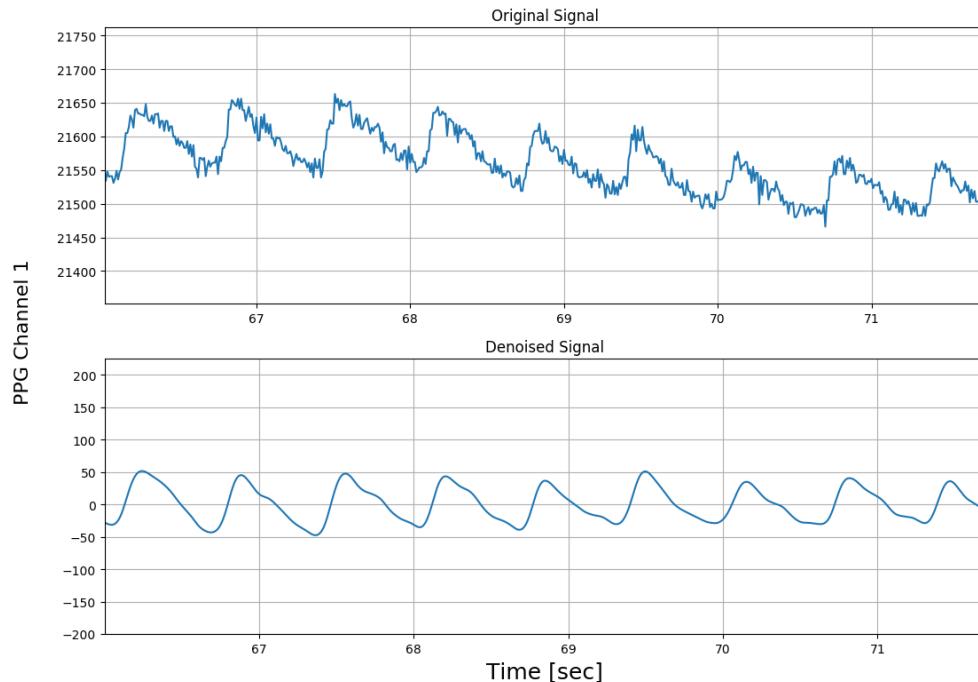
**Figure. 3.16:** Original ECG signal from the chair.



**Figure. 3.17:** Detected P,Q,R,S and T waves on the chair's ECG signal.

## 3.12 PPG Signal Processing

A band-pass filter can be used to reduce the baseline drift and high-frequency noise from the PPG signal. A passband of 0.5 Hz to 5 Hz has been used. After applying the band-pass filter, the resulting signal is the denoised PPG signal. The denoised channel 1 signal is shown in Figure 3.18.



**Figure. 3.18:** The denoised PPG signal using band-pass filter.



# 4 Deep Learning

Deep learning is a subfield of machine learning which is in fact, is a subfield of Artificial Intelligence (AI). Deep learning has emerged as one of the most exciting fields of computer science, and it keeps expanding its scope. It has been used in many technologies such as, in medical to identify the diseases, automatic game playing, self-driving cars, image recognition, natural language processing and many more. The reason why deep learning is successful in many different domains is its ability to understand multiple levels of representation of data. Its mean that, it not only has the ability to classify and predict but also has the ability to learn a different level of complexity. Before diving into deep learning, it is necessary to understand a broader field "machine learning".

## 4.1 Machine Learning

Machine Learning is a data analysis method [Bis06]. It gives the computer the ability to learn from data without being explicitly instructed. By using different machine learning algorithms, it helps to find hidden insights of data and allow us to build models to make predictions. It can be classified into 2 categories [Bro17].

1. Supervised Learning
2. Unsupervised Learning

### 4.1.1 Supervised Learning

In supervised learning, the labeled data is used to train the models. Here, labeled data represents that the input and output variables are known in advance. Thus, a supervised machine learning algorithm is used to come up with a mapping function which maps the input variables to the output variables. Learning is supposed to be stopped when the level of performance reaches the desired result. Supervised learning is generally divided into regression and classification.

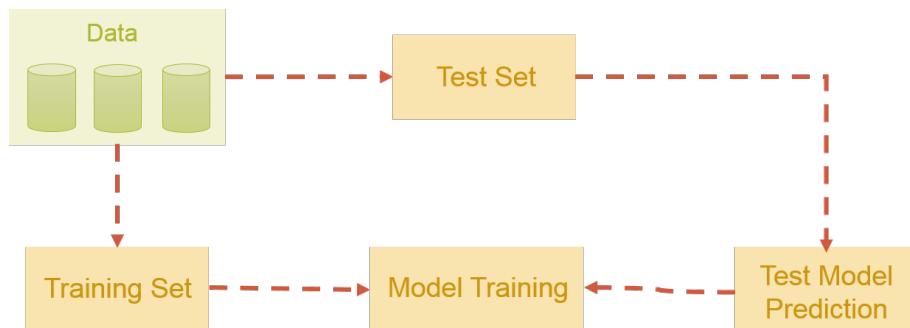
- **Regression:** A problem in which the output variable is a category.
- **Classification:** A problem in which the output variable is the real value.

### 4.1.2 Unsupervised Learning

In unsupervised learning, only the input variables are known and no corresponding output variables are known. Thus, there are no labels given and it is expected from unsupervised machine learning algorithm to find the structure in the data, i.e. finding hidden patterns to learn more about data. It is different from supervised learning in that the correct output value is not known. Unsupervised learning is generally divided into clustering and association.

- **Clustering:** Group objects in such a way that the objects, which are similar to each other, placed in the same cluster.
- **Association:** Discover rules that define the large portions of the data such as people who buy product X may buy Y as well.

The objective of machine learning is to analyze the past and present data and predict or make a decision for the future data. In supervised learning, the basic workflow is to build a model, evaluate or tune a model and then deploy it in the production environment where it will do the predictions. The workflow can be seen in Figure.



**Figure. 4.1:** Basic supervised machine learning workflow.

Machine learning is generally powered by a huge amount of data which is generally referred as Big Data. It is generally defined as a too big or complex data which cannot be processed on a single machine. As the data is growing day by day, the new tools are also required to process that big data on multiple machines and extract the useful insights from the data.

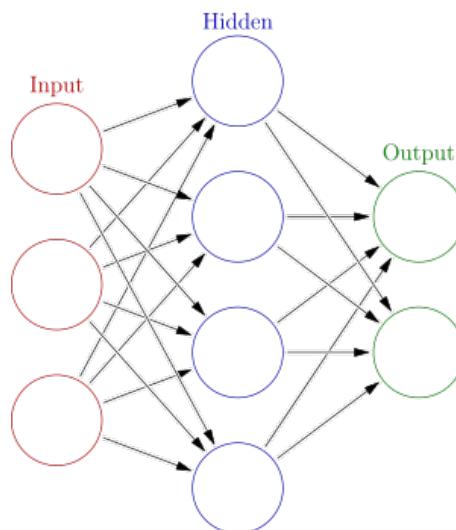
One of the problems with the traditional machine learning model is the feature extraction challenge. The model designer or the programmer need to specifically tell the model which features it should consider making a correct decision. The model heavily relies on the programmer's understanding of data and this was a huge burden on the programmers. For problems like object recognition, language translation, it was considered as a huge problem.

Deep learning comes into play to solve the problem of feature extraction. They have the capability to focus only on the right features by themselves by understanding as much data as possible, requiring very little input from the programmer. This feature of deep learning models makes it very powerful tool for the current machine learning era.

## 4.2 Artificial Neural Networks

Artificial neural networks (ANNs) are generally inspired by the biological neural networks that mimic brain functionality [con17a]. These systems generally learned by considering examples instead of specifically define rules for certain situations or cases. An ANN is a network of nodes called artificial neurons which are connected to other neurons using a link called *synapse*. Each neuron gets the input, process the input and pass the output to the next neuron. In the most basic state, an ANN consists of 3 layers:

1. Input Layer
2. Hidden Layer
3. Output Layer

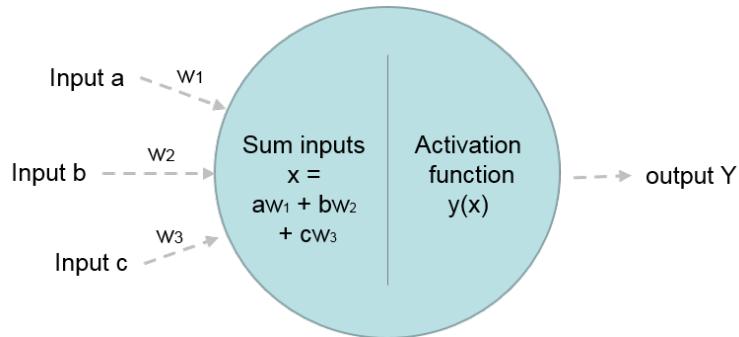


**Figure. 4.2:** An artificial neural network with its 3 basic layers[con17a].

### 4.2.1 Artificial Neuron

An artificial neuron is the most basic unit of ANN. It takes inputs and produces an output. Generally, the inputs are multiplied by some weights to specify which inputs are more

important. The higher the value of weights, the more important they are. The inputs are shown as a, b, and c, and weights as  $w_1$ ,  $w_2$  and  $w_3$  in Figure 4.3. After then the products are summed together and passed to the activation function. An activation function is a function which takes an input and generates an output based on a certain threshold. So, if the summed value is greater than the threshold value of that activation function, the output is produced or in other terms, the neuron fired else no output is produced and neuron does not fire.



**Figure. 4.3:** A single artificial neuron.

Artificial neurons adjust the weights as the learning proceeds and the process of finding weights is known as learning. ANN considers many different examples and finds the best possible combination of weights to provide the most accurate results. There are many other parameters involved as well to find a good combination of weights.

## 4.2.2 Activation Function

A function that takes an input and produces output based on threshold value is known as activation function [ujj17]. There are many activation functions available. Few of them are:

### Sigmoid

It takes a real value input and scales it to the range of 0 to 1. It is also known as the logistic function. It is represented as:

$$y = \frac{1}{1+e^{-x}}$$

Another variation of the sigmoid function is softmax function which is used for multiclass classification.

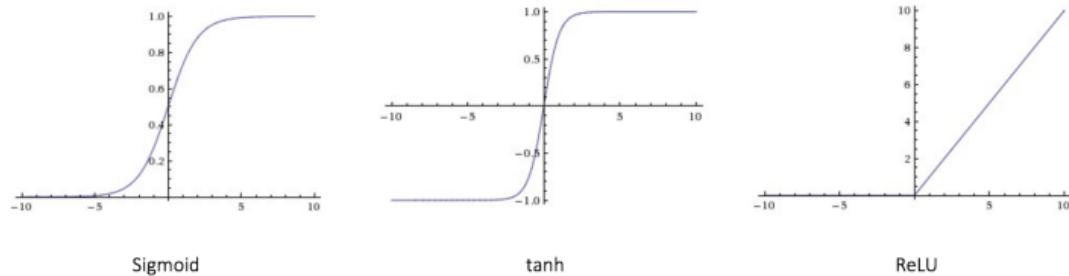
## Tanh

It takes a real value input and scales it to the range of -1 to 1. It is also a sigmoidal function as it also takes s-shaped.

## ReLU

It stands for Rectified Linear Unit. It is the most used activation function as it is the ideal choice to be used in convolutional neural networks. It takes the real value input and all negative values are mapped to zero. It is represented as:

$$f(x) = \max(0, x)$$



**Figure. 4.4:** Activation functions[ujj17].

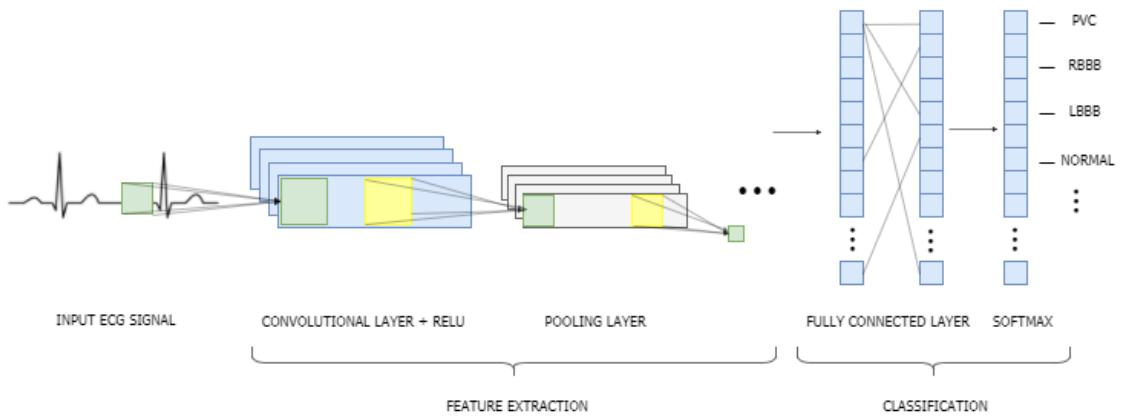
The graph of all the activation functions defined above can be seen in Figure 4.4.

### 4.2.3 Convolutional Neural Network

Convolutional neural network (CNN) is a class of deep neural network which uses multilayer perceptrons. It consists of an input layer, an output layer, and multiple hidden layers. The hidden layers can be convolutional, pooling or fully connected layer.

#### Convolutional Layer

In CNN, the first layer is always the convolutional layer. This layer applies a convolutional operation to the input and passes the output to the next layer. A filter (or sometimes referred as a kernel) is used which slides over all the area of the input and extract the features



**Figure. 4.5:** Convolutional neural network example.

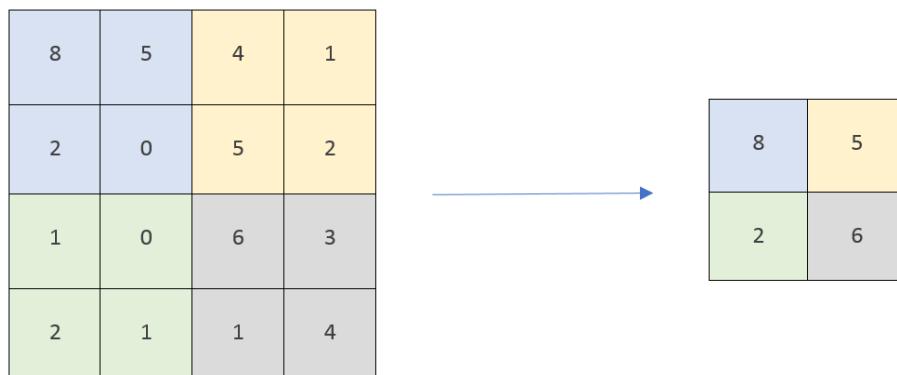
from it. The region where the filter is being applied at any instant of time is called as a receptive field. As the filter slides or convolves over the input signal, it multiples the filter with the original signal values (which can also be referred as element-wise multiplication) which results in a single value. The important point to note here is that this single result is just from a single receptive field. Therefore, the same operation will be carried out on other receptive fields by sliding the filter over the different areas of the input signal. The filter can slide for any unit and this sliding unit is known as stride. Every unique area of the input signal will produce an output and the combined output together is called as feature map or an activation map. If we assume that, the input size is  $32 \times 32$ , the filter size is  $5 \times 5$  and the stride is 1 unit, then the size of the activation map will be  $28 \times 28$ . In a 2D array, the filter can be moved in both directions.

## Pooling Layer

Pooling layer is used to downsampled the convolutional layer output. There are several pooling options, for example, average pooling, L2-norm pooling, etc., but max polling is the most popular. This layer basically takes a filter of size  $2 \times 2$  with the same stride size. It then applies the filter to the part of input and output the maximum number in that region. The same process is applied to the different sub-region by sliding the filter all over the input. By convolving the filter around the input, it drastically reduces the spatial size of the input. The example can be seen in Figure 4.6.

## Fully Connected Layer

In fully connected layer, the neurons of one layer are connected to all the neurons of the other second layer, as it can be seen in Figure 4.5. This layer can be seen in the regular neural network as well. The softmax function is applied to the output of the second layer



**Figure. 4.6:** Max pooling layer example.

to produce the probabilities for the classification of the input.

#### 4.2.4 Keras

Keras is an open source artificial neural network library written in python. It is very powerful and easy to use library to develop neural networks. It has a capability to run on top of TensorFlow, Microsoft Cognitive Toolkit (CNTK), or Theano, can run on both CPU and GPU. Before keras, it was really time-consuming to develop a network on TensorFlow or Theano and the aim to develop keras was to make it easy and fast to develop neural networks. Keras supports both convolutional neural networks and recurrent neural network, as well as a combination of both.

The model starts by defining the model as sequential using a *Sequential()*, which is a linear stack of layers. Then the layers are added into the model using *add()* method. Keras supports almost all kinds of layers. The input dimensions are needed to specify when the layers are added to the model. Once the layers are added, the model is compiled by using the *compile()* method, which additionally needs 3 arguments.

- Optimizer: To optimize the neural network, for example, rse, adagrad, adam, etc.
- Loss Function: This is the value that model tries to minimize to calculate the error, for example, categorical\_crossentropy, mse, etc.
- Metrics: It can be any existing metric or a custom defined metric function. But for classification problems metrics=['accuracy'] is recommended.

Then the model is trained by using the *fit()* method. This method lets the model iterate over the data and find the most optimal neural network for the given data.

This library has been used for training the CNN for the identification of Cardiac Arrhythmias.

### 4.2.5 Convolutional Neural Network for the Identification of Cardiac Arrhythmia

A 6-layer Convolutional Neural Network (CNN) has been trained for the identification of an arrhythmia in an ECG signal. The trained model can detect 3 different kinds of arrhythmia namely:

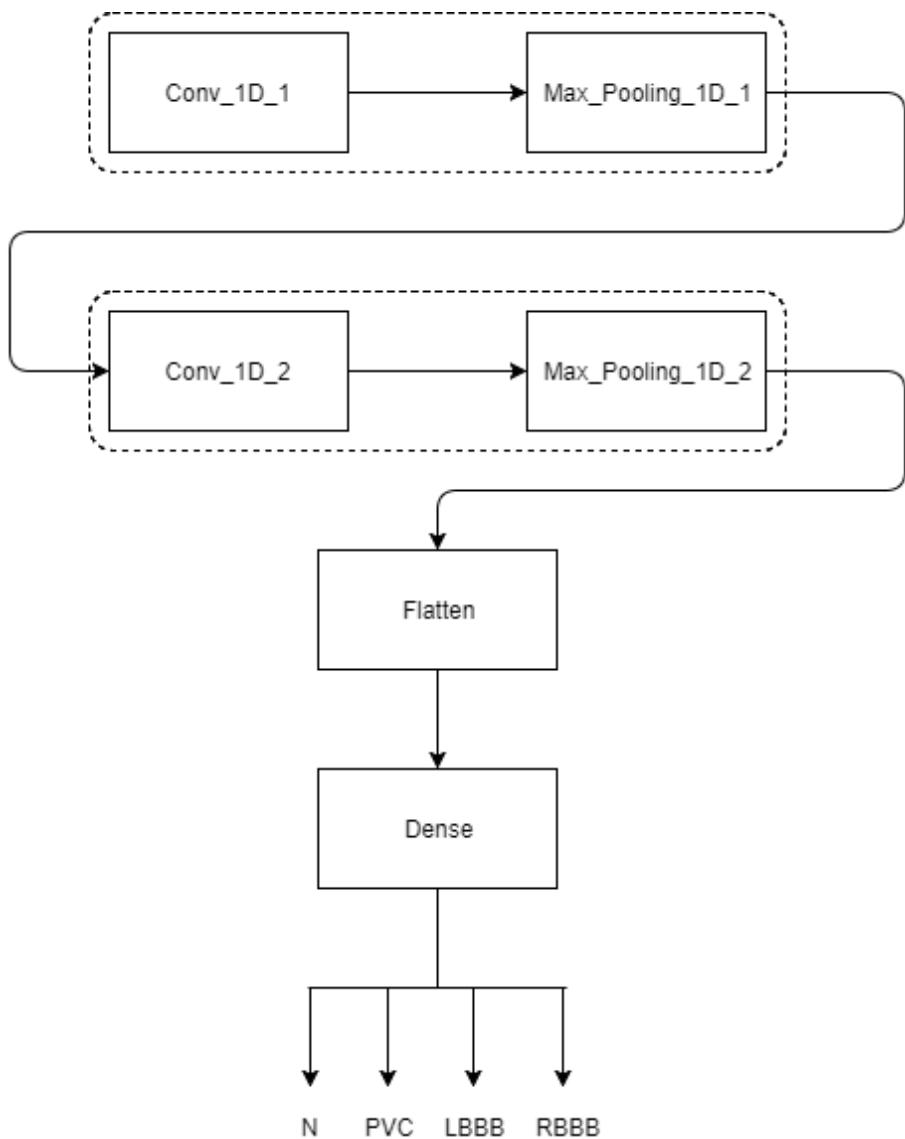
1. Normal
2. Left bundle branch block (LBBB)
3. Right bundle branch block (RBBB)
4. Premature ventricular contraction (PVC)

The CNN layers can be seen in Figure 4.7.

### Layers Explanation

The 1st convolutional layer (Conv\_1D\_1) consists of 64 filters, whereas, the 2nd convolutional layer (Conv\_1D\_2) consists of 32 filters with a kernel of size 3. For both convolutional layers, Relu has been used as an activation function each followed by a MaxPooling layer. The batch size of 1000 was used for the training, along with the Adam algorithm to optimize the CNN. Since the model is trained for performing the classification of an ECG signal, therefore, categorical cross-entropy loss function was used for calculating the loss of training and validation. After performing the convolutions, the flattening and dense layer has been used followed by a softmax activation function to produce the final probabilities with 4 classes.

The model was trained and tested for the several no. of iterations ranging from 10 to 100. The best model was found after the 20 iterations. After that, the model remained stable with the slight improvement in the training as well as in the validation accuracy. The training and validation accuracy can be seen in Figure 4.9.



**Figure 4.7:** A 6-layer Convolutional Neural Network model for the identification of cardiac arrhythmia.

Layer (type)	Output Shape	Param #
conv1d_1 (Conv1D)	(None, 300, 64)	256
max_pooling1d_1 (MaxPooling1	(None, 150, 64)	0
conv1d_2 (Conv1D)	(None, 150, 32)	6176
max_pooling1d_2 (MaxPooling1	(None, 75, 32)	0
flatten_1 (Flatten)	(None, 2400)	0
dense_1 (Dense)	(None, 4)	9604

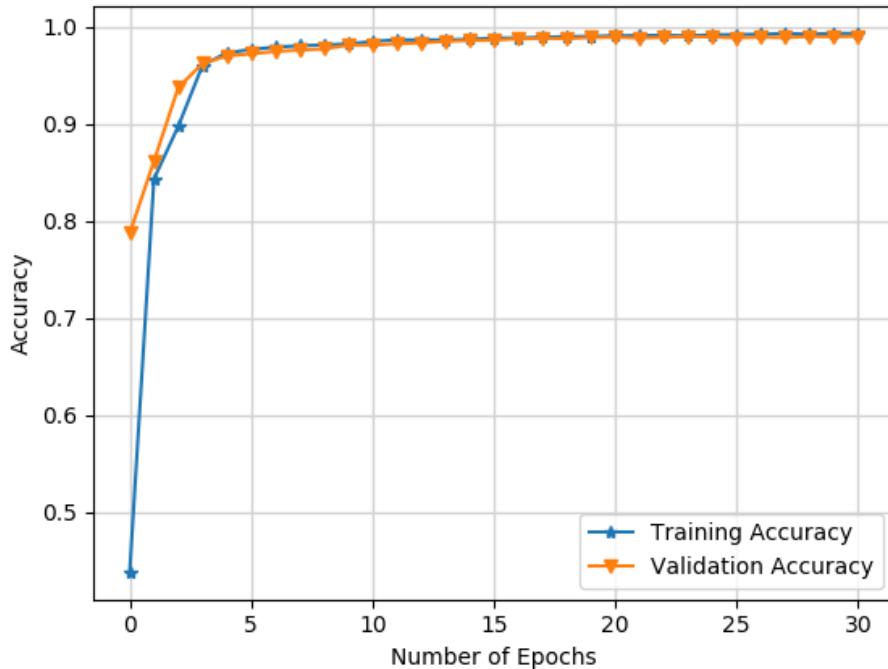
Total params: 16,036  
 Trainable params: 16,036  
 Non-trainable params: 0

**Figure. 4.8:** Layers used in the model and number of parameters to be optimized.

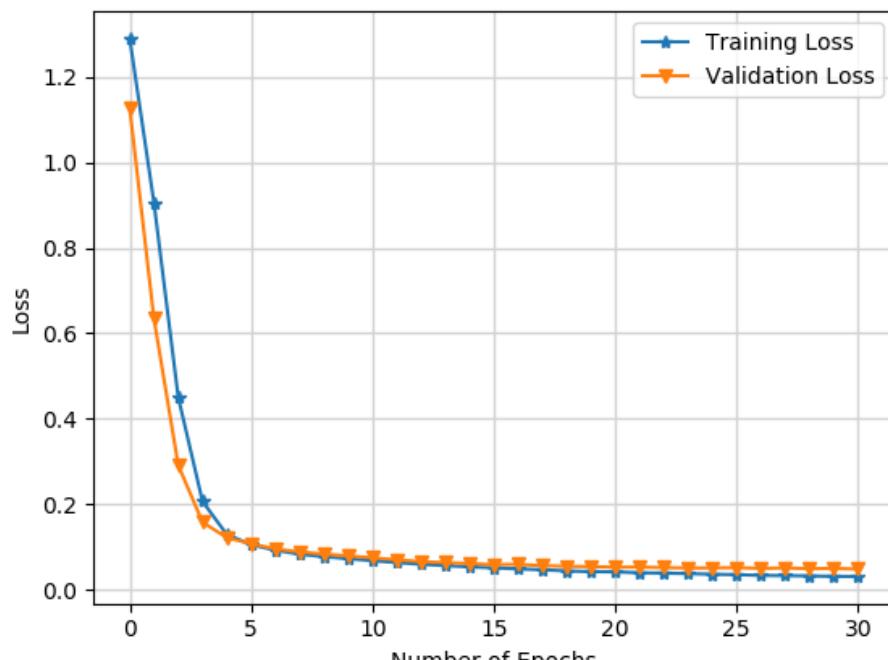
## Results

The CNN model has achieved an accuracy of 99.2% on MIT-BIH dataset. Total 16,415 ECG signals were extracted from the MIT-BIH dataset, out of which 10,998 (67% of the total signals) were used for the training, and the remaining 5,417 (33% of the total signals) were used for the testing of the model. The types count for training and testing data can be seen in Tables 4.1 and 4.2 respectively.

During the testing of the model, 42 ECG signals were classified wrong out of 5,417 ECG signals. The false predicted results can be seen in Table 4.3. In table,  $a \rightarrow b$  means is that  $a$  was classified as  $b$ .



(a)



(b)

**Figure. 4.9:** (a) Training and validation accuracy results; and, (b) Training and validation loss of CNN model for 30 iterations.

**Tab. 4.1:** Training data.

Type	Count
Normal	3,352
LBBB	2,641
RBBB	2,498
PVC	2,507
<b>Total</b>	<b>10,998</b>

**Tab. 4.2:** Test data.

Type	Count
Normal	1,648
LBBB	1,308
RBBB	1,285
PVC	1,176
<b>Total</b>	<b>5,417</b>

**Tab. 4.3:** False Prediction Counts.

False Prediction	Count
$0 \rightarrow 1$	1
$0 \rightarrow 2$	1
$0 \rightarrow 3$	3
$1 \rightarrow 3$	6
$2 \rightarrow 0$	5
$2 \rightarrow 3$	3
$3 \rightarrow 0$	9
$3 \rightarrow 1$	12
$3 \rightarrow 2$	2
<b>Total</b>	<b>42</b>



# 5 Visualization

*“A picture is worth a thousands words.”*

Raw numbers to the users do not make sense and therefore, require necessary tools to display the results. Visualization allows us to see the broader aspects of complex data by showing the data in graphical formats. It really helps in capturing the user’s attention and engage him through out the process. Complex data that could easily be ignored, can still be recognized and captured the attention of the user in a graphical reports [Iye17].

The visualization tool Grafana has been set up for displaying the real-time data received from the sensors. All devices send the data in real-time which first get stored in Influxdb and then Grafana tool loads the data from there and display it on the graph.

## 5.1 Grafana

Grafana is an open source real-time visualization tool for analytics and monitoring. It is one of the best tools for time series analytics, therefore, it has been used for visualizing the real-time data from sensor devices. It can be used for any kind of application analytics, for example, industrial sensors, home automation, hospitals, weather reports etc. It can connect to many data sources and pull data from it to do the analytics or the visualization. The most commonly used data sources these days are:

- Elasticsearch
- InfluxDB
- Graphite
- Prometheus

It allows us to connect to these data sources on just few click which makes it very convenient. Multiple dashboards can be created in Grafana to view different dimensions of the data. It also provides multiple tools for creating graphs in different fashion and styles which can be added to dashboards.

## 5.2 InfluxDB

Since the sensor data is always time critical, therefore, a time series database is required for storing the data. InfluxDB is one of the best time series database available, therefore, it has been chosen for storing the sensors data.

It is very easy install and manage, and does not require other dependencies to run. It also provides an HTTP/HTPPS interface to read and write data from the database. The retention policy can be set on the database to manage space conveniently. The basic terms in InfluxDB are:

- Database name
- Measurement (same as table name in traditional databases)
- Tags (to filter data)
- Fields (actual data values)

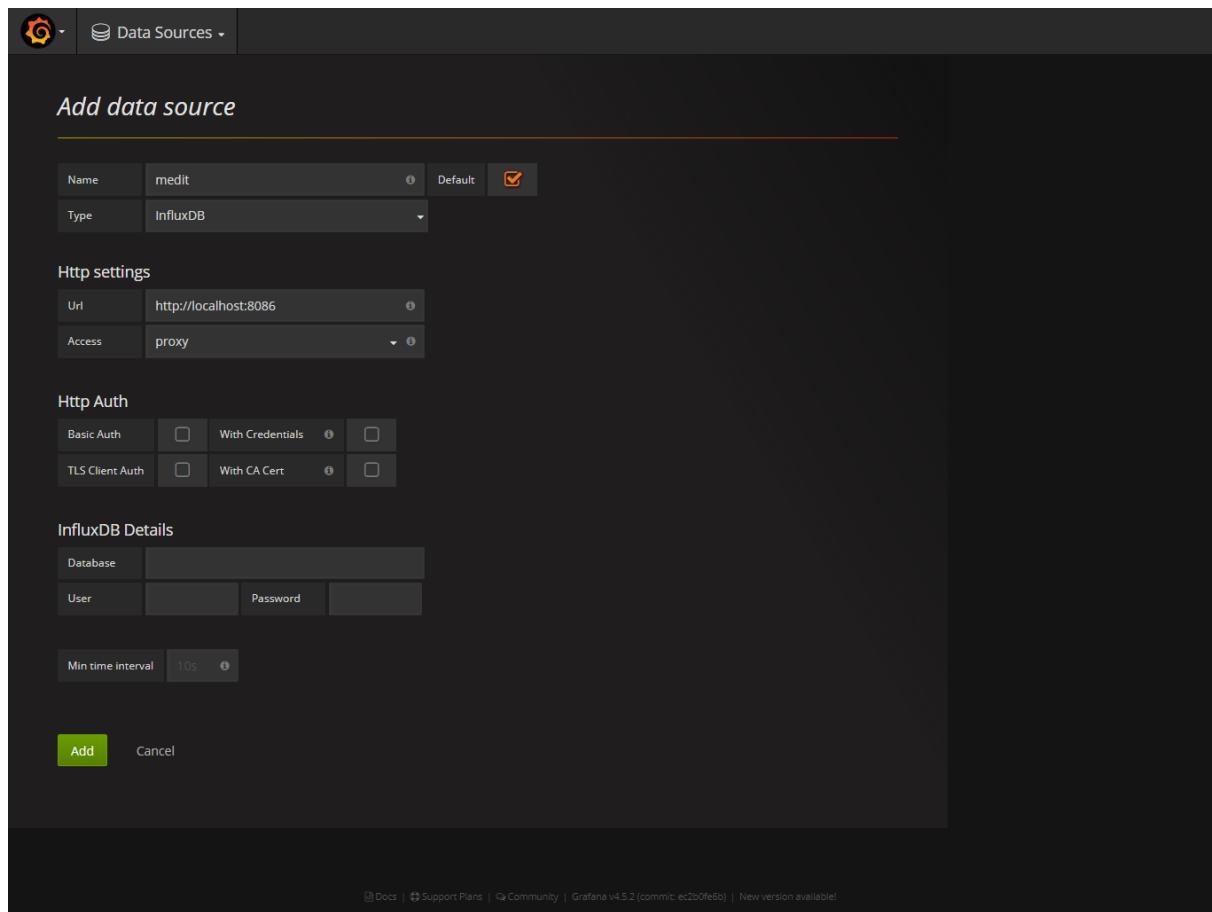
The fields are generally used as a key value pair, with a timestamp field. Only one point can be stored at any specific timestamp. The precision of a single field can be in s, ms,  $\mu$ s, ns. If the field does not contains a timestamp field, then the InfluxDB will generate a timestamp automatically.

## 5.3 Setting up Grafana with InfluxDB

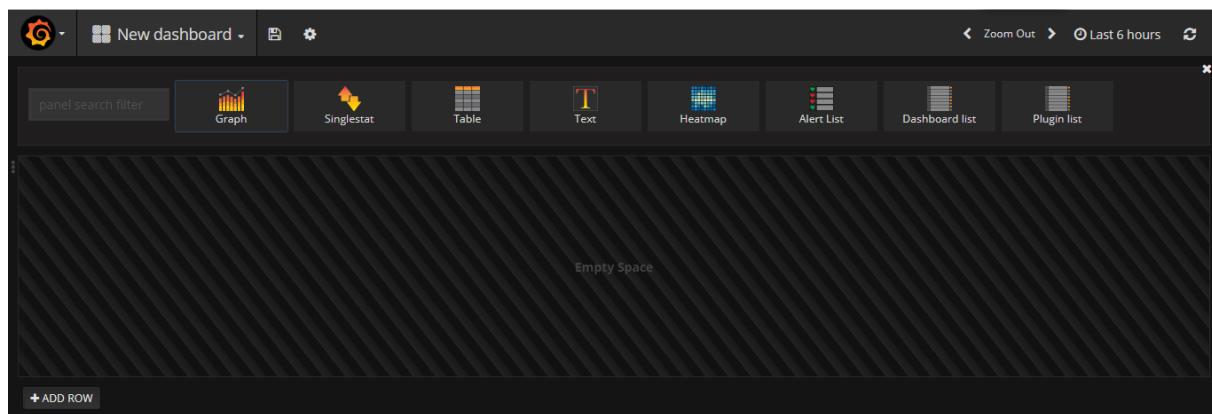
Another reason for choosing the InfluxDB is that, it is really easy to configure Grafana for using InfluxDB as a data source. It is so simple that, the setup can be done in just 5 minutes. First, a user needs to create a database in the InfluxDB. Once the database is ready, starts the Grafana server. Generally, it runs on port 3000 but because of ports conflict, it is recommended to change the port to some other address by editing the `conf\sample.ini` file.

Once the server is started, go to `localhost:3000` address to open the Grafana web interface. Select an option to add a new data source. Lets say the database name is “medit”, then configure the InfluxDB data source as shown in Figure 5.1.

Once the data source is setup, a dashboard is created to add the graphs and panels where the data is visualized. Multiple types of panels are available by default such as table, graphs, text, single stat, alert list, etc.

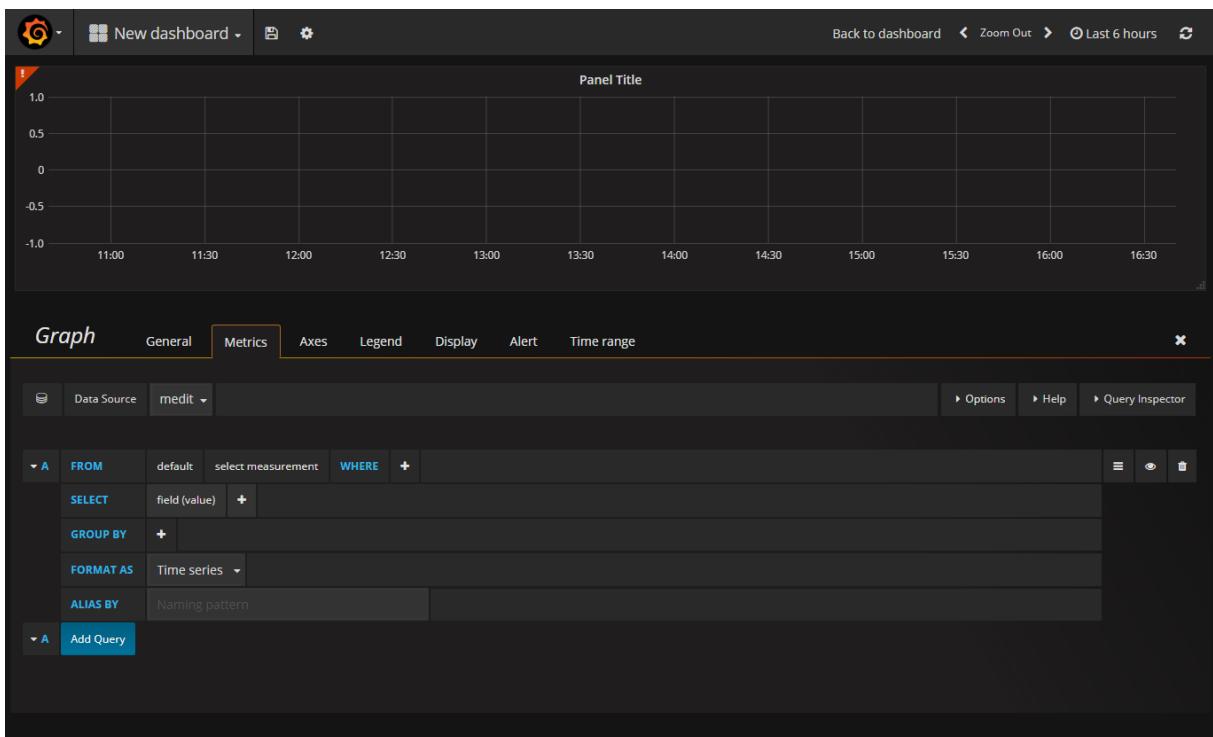


**Figure. 5.1:** InfluxDB data source setup in Grafana.



**Figure. 5.2:** Dashboard setup.

Lets say a graph is added to the dashboard. Now, a data source is need to be defined for the graph. That can be done by selecting the graph and edit it. The interface for setting up the data source for graph can be seen in Figure 5.3. A very user-friendly interface is available where one can define a query for the panel. A query can be build just by selecting the option from drop down. It will contains all the information from the database that is setted up in the data source, that shown in Figure 5.1. So user simply needs to select the data source, then from the measurements select the specific measurement that wants to be chosen. One measurement can have multiple fields therefore, select a specific field which needs to be displayed on graph. Once all the steps are done, the panel is ready to display the information from the InfluxDB.



**Figure. 5.3:** Interface to add query for the panel.

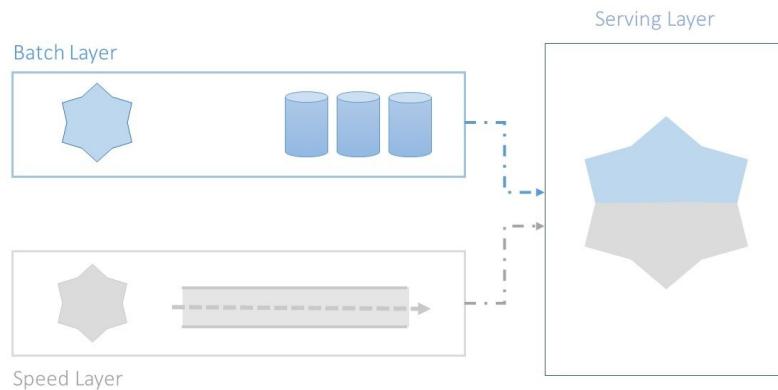
## 5.4 Lambda Architecture for Big Data Processing

The amount of data being processed nowadays is enormous, and this is often coined as Big Data. Big data is everywhere in the form of web logs, events, social networks, sensors data,etc, and these all are generating around petabytes of data each day. And because of this humongous amount of data, the traditional tools and storage technologies are unable to handle and cope with it. Therefore, this has led to a technology phase shift how we keep and manage our data, and to the development of Advance Analytics solutions.

Lambda Architecture [BSK16] [Kre17] [KMM<sup>+</sup>15] [Hau17] is getting involved in machine

learning and data science applications day by day by enabling the real-time data processing and analytics without using the traditional ETL approach. It is designed to address the fault-tolerance, scalability and robustness issues of big data systems. Moreover, Lambda Architecture also ensure the low-latency and accuracy of the result. It combines the power of stream processing with batch processing to provide such kind of system. Lambda architecture, as shown in Figure 5.4, consists of 3 main components:

1. Speed Layer
2. Batch Layer
3. Serving Layer



**Figure. 5.4:** Lambda architecture.

### 5.4.1 Batch Layer

The Batch layer will hold all of the master data which will be stored in Apache Hadoop. This data will be kept in its original state, untouched and in an immutable manner. This data will be processed and generate the batch views which then will be served in the serving layer. This is the place which will provide the most accurate results from the data using any of the available distributed platform tools.

### 5.4.2 Speed Layer

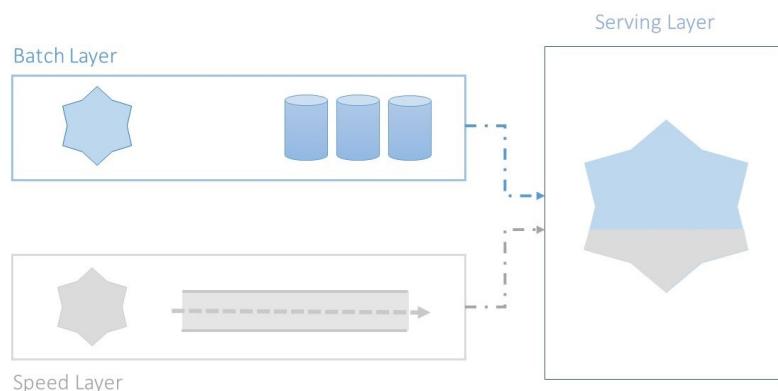
Typically, it is known that a Hadoop processing frameworks are slow and take a lot of time. To cope up with this problem, Lambda Architecture introduces the speed layer.

Speed layer process the real-time stream and generate the real-time views of a short time frame, which are then serve in a serving layer along with batch views. The main point to notice here is that the speed layer data is temporal in nature, i.e. it can only store that much amount of data that could be kept in the memory. And it is deleted as soon as one batch process is completed.

### 5.4.3 Serving Layer

This is a place where the final results and data are visualized. Serving layer provides an interface which integrates real-time views with batch views and unified them together. An accurate view of data will be presented by the batch layer, whereas the fresh view of the data will be presented by the speed layer. It also supports ad-hoc queries which are optimized for low-latency. Technologies which can be used in this layers are Cassandra, HBase, etc.

The data source will provide the data which will be streamed in the stream layer and at the same time to the batch layer. Batch layer will hold the data for a long time and stream layer will process the stream in a window of short time and then provide the calculated result. The serving layer will combine the data received from the batch layer, more specifically the batch views, and the data received from the speed layer and allow them to query from a single interface. The advantage of the Lambda Architecture is that if one layer is down, the other layer can be used to make system available. For example, in Figure ??, if a speed layer is down, which of course can happen in the production environment, The batch layer can be used to compensate the failure.



**Figure. 5.5:** Using more data from serving layer in case of speed layer having a problem.

The reason why it is called lambda architecture is because the lambda symbol splits into two parts which in case of this architecture represents the batch layer and the speed layer.

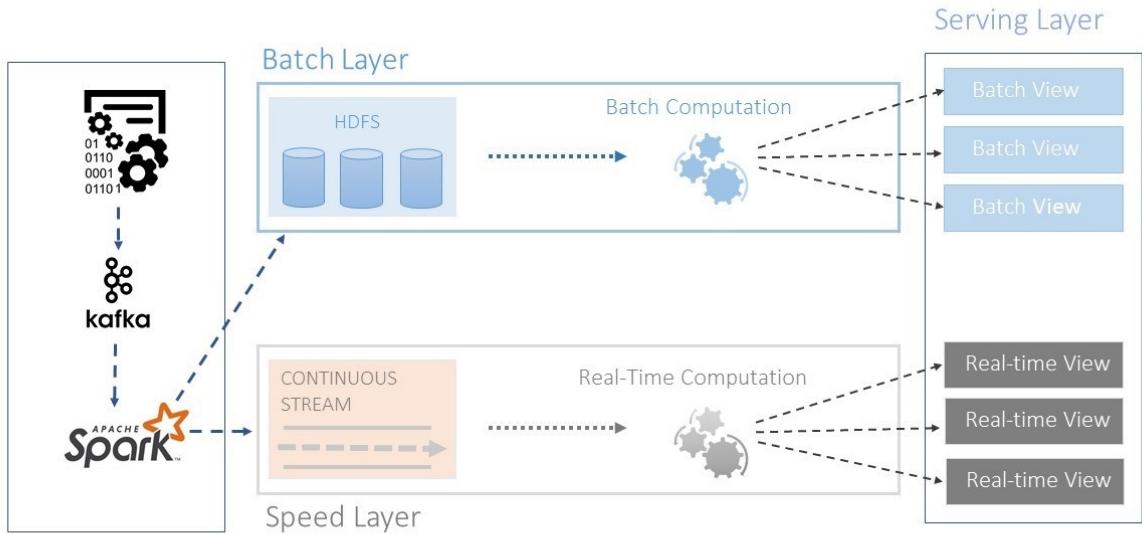


**Figure. 5.6:** Lambda symbol representing the lambda architecture.

Typically, the data stream is implemented using a publish-subscribe messaging system such as Kafka, which can easily scale for high velocity data ingestion. It can be thought of as a place where publishers publish their data and the consumers read data from it. This is different from the traditional queue as it keeps the data until we let it to hold. In contrast, the data will be removed from the queue, once it is delivered to the appropriate consumer of the data. It uses topics to publish and to subscribe for the data. Every Kafka server is known as broker and since it is a distributed system, therefore, there can be more than one broker. The more the number of brokers are, the higher the availability is. The advantage of having Kafka is that it can handle many different forms of data, such as sensors data, application events, server logs, social network events etc. Kafka is very fast despite of having heavy load.

The implementation of lambda architecture has been shown in Figure 5.7. The data will directly be published from data source to Kafka based on some topic. Data from multiple data sources can be collected via Kafka based on different topic names. Once the data is fed into the Kafka, the corresponding consumers will read the data from Kafka using the topic name where the data publish to. In this architecture, Apache Spark can be used in both the batch layer and the speed layer.

Apache Spark is a large-scale data processing tool, which runs 100 times faster than the Hadoop MapReduce by caching the data objects in the memory. Thus, it is a strong candidate to replace the MapReduce. It also creates a lineage graph. So, in case of failure, it can do the computations again and go back to the last state of the data. These are two of the fundamental things that Resilient Distributed Data Set (RDD) is all about. It is specially designed to schedule and execute a large amount of data. Apache Spark does not only provide the batch processing, but it also comes with real-time stream processing, machine learning tools, graph processing, Spark SQL, Spark R and complex analytics. It is designed to run everywhere, such as it can run on Hadoop YARN, apache Mesos or standalone as well. Apache Spark offers interface for several languages to write the applications. The available languages are Java, Scala, Python and R.



**Figure. 5.7:** Implementation of lambda architecture.

## 5.5 System Architecture

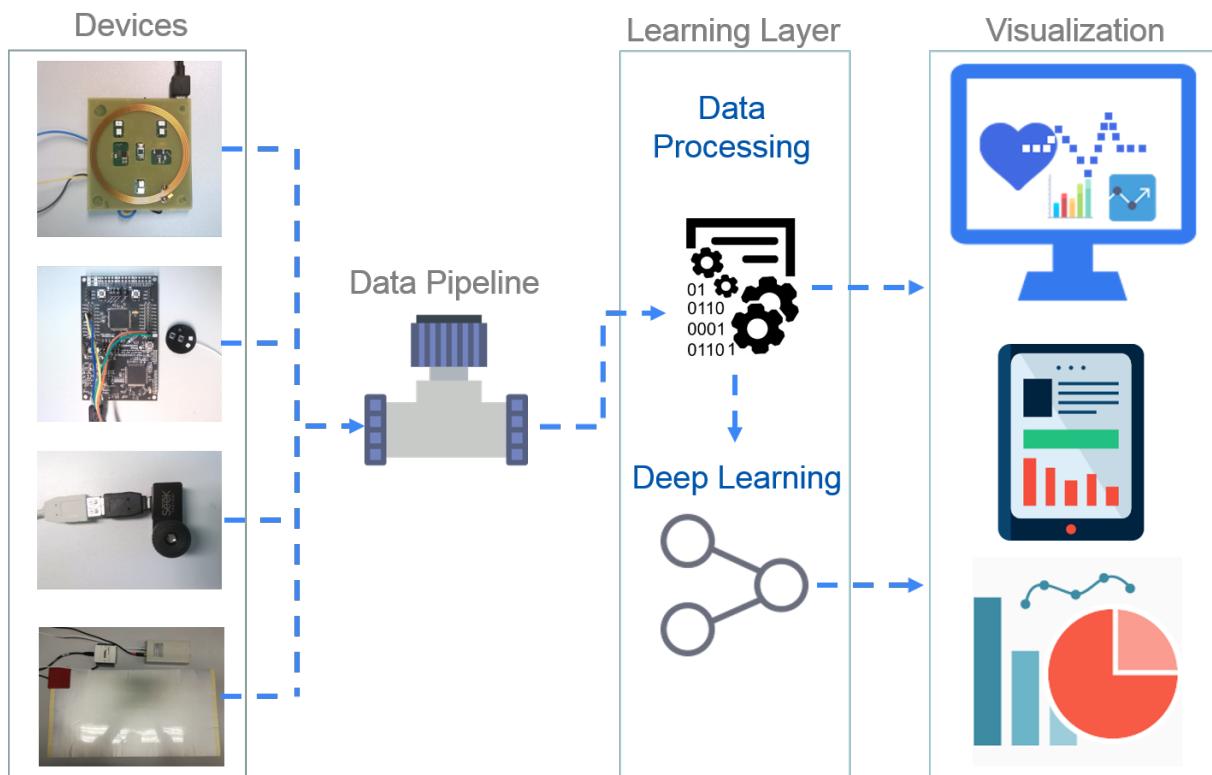
A system has been implemented to collect, process and visualize the data for all the sensors based on the lambda architecture defined in Section 5.4. But the system has been modified according to the requirements and because of the lack of enough resources to run all the big data tools. The system architecture can be seen in Figure 5.8 .

An architecture has been implemented in *python* language, which first collects the data from all sensors based on their protocol. The data is then immediately stored in InfluxDB in order to have the original state of the data, as shown in Figure 5.9. The data is then cleaned and processed to do the further operations on it, such as for the ECG signal, the feature extraction.

The main focus of this thesis is on cardiac, therefore, most of the implementation is based on ECG sensor. The NI USB-6259 is used for the signal acquisition. The sample rate of 360 Hz has been used as the deep learning model was trained on 360 Hz frequency data. The same feature extraction algorithm is used that is defined in Section 3.8. Once the R wave is detected, 100 points to the left and 150 points to the right of the R peaks are selected to make a single ECG signal of 250 sample points, which was then passed to the deep learning model to predict the arrhythmia. The window of 10 seconds is used for calculating the heart rate. The complete process is shown in Figure 5.9. Once the features are extracted, the cleaned signal and the extracted features are saved in InfluxDB immediately to save the

state of the signal.

Once all the information is stored in the InfluxDB, then the Grafana takes the job. It retrieves the desired data from InfluxDB and display it on the dashboard. Grafana provides many other options as well, such as, the refresh time, i.e, how much time retrieves the new data from InfluxDB. If the data is coming from other machine and the clock time is not same, Grafana gives an option to shift the time to adjust the panels and many other helpful functions.

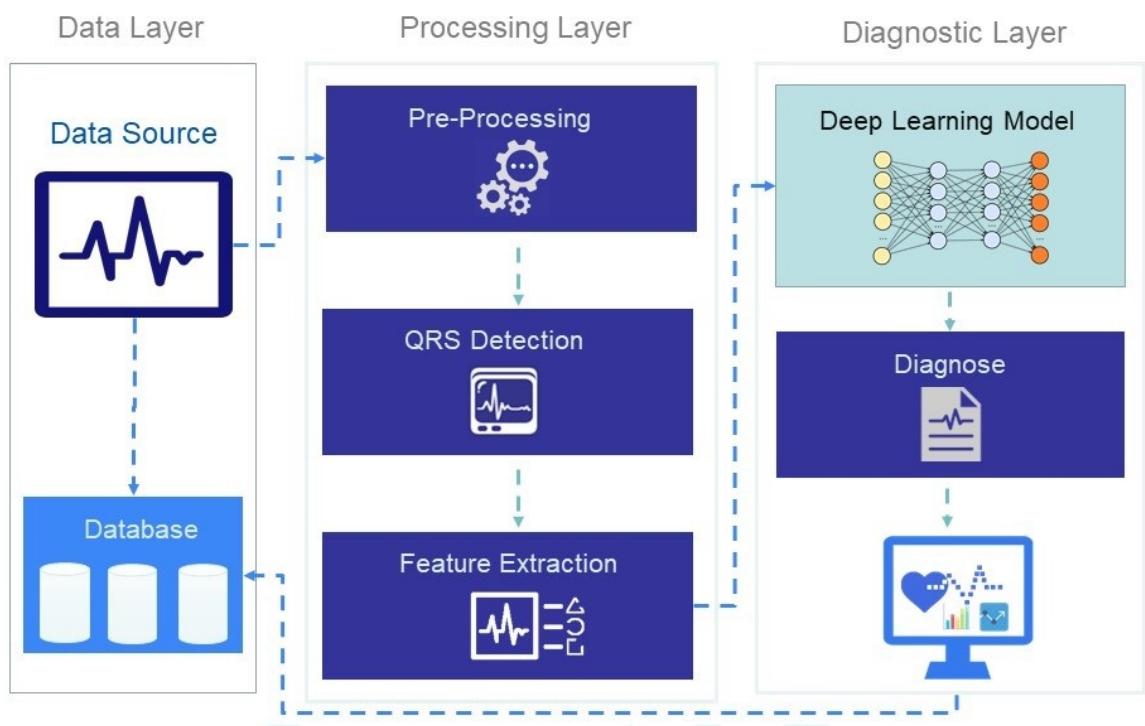


**Figure. 5.8:** System architecture for the sensors.

The Grafana dashboards for ECG, MI and PPG sensors can be seen in Figure 5.10, 5.11 and 5.12 respectively.

## 5.6 Device Management Interface

Starting the system via console is not a very convenient way to interact with the devices. Therefore, a simple web view interface has also been made to operate the sensor devices. The devices can be start, stop and in case of error, the logs can be viewed directly in the same interface. The interface pictures can be seen in Figure 5.13.

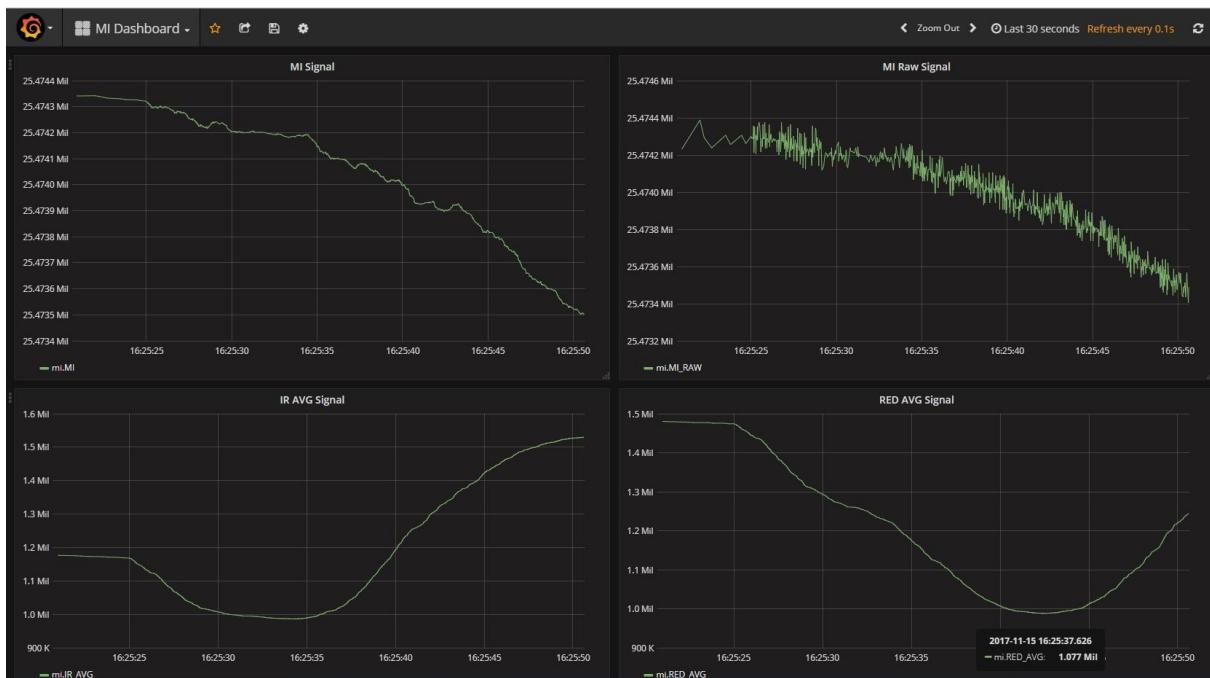


**Figure. 5.9:** Using the deep learning model in real-time environment.

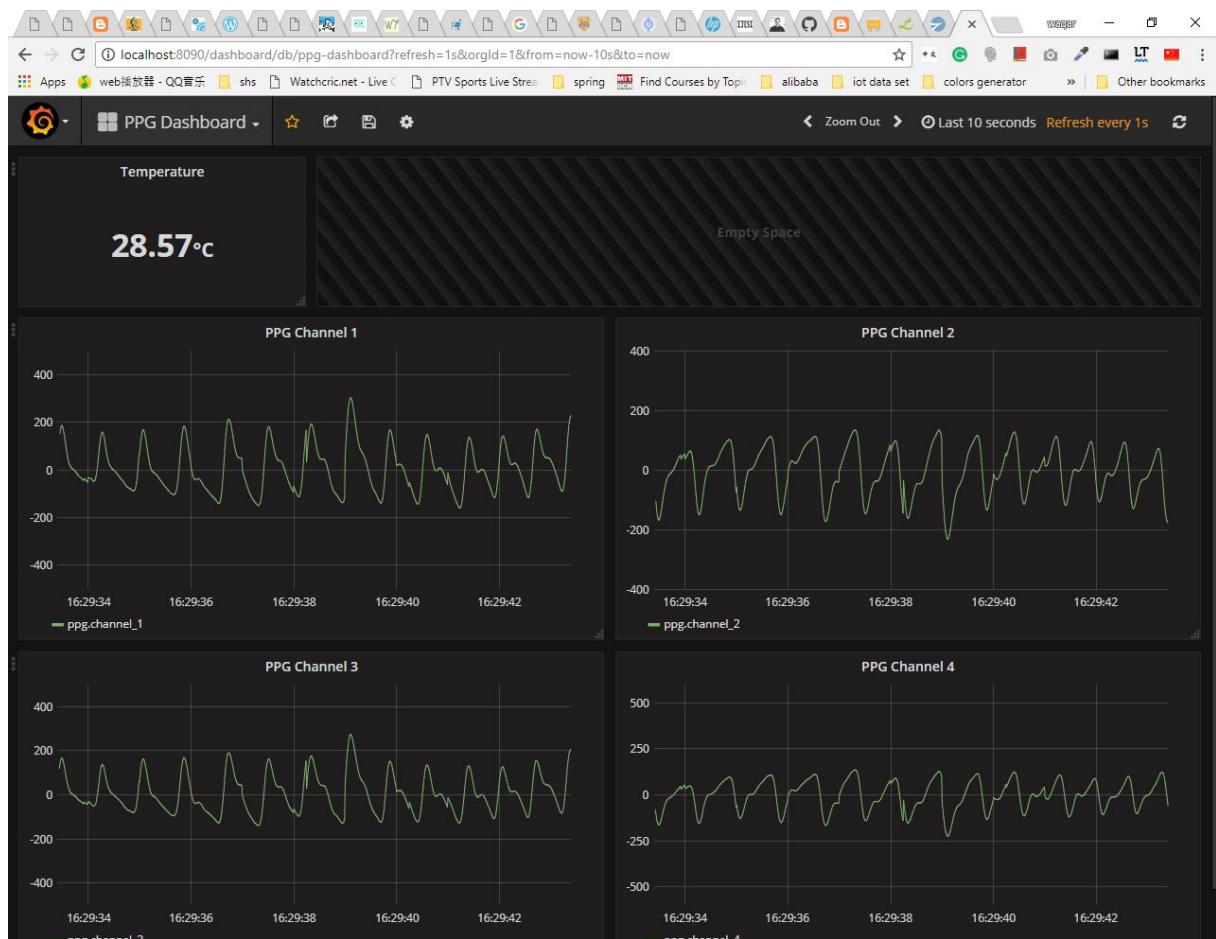
## 5.6 Device Management Interface



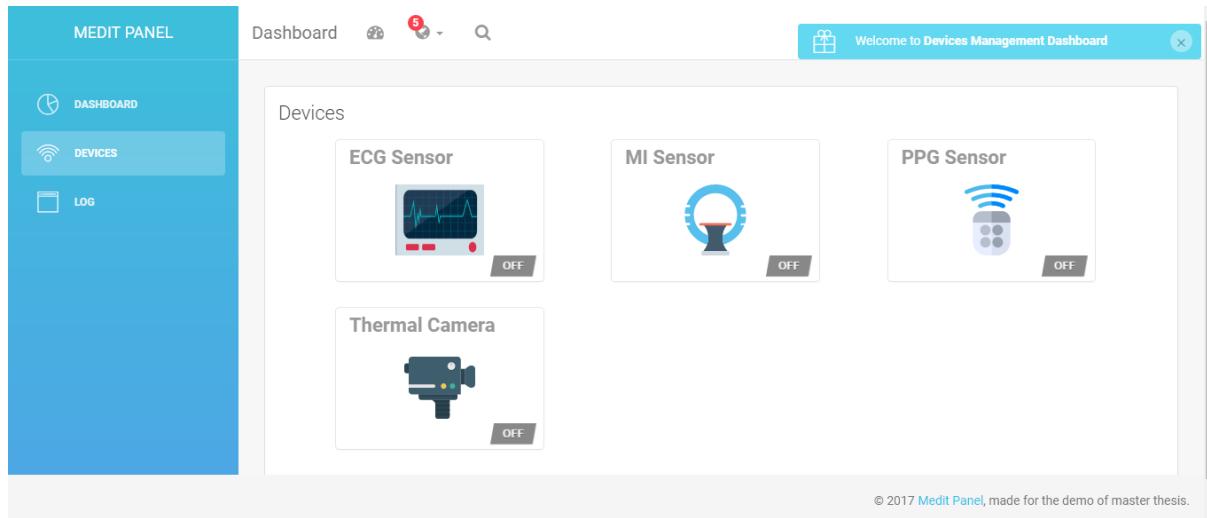
**Figure. 5.10:** Real-time ECG signal visualization.



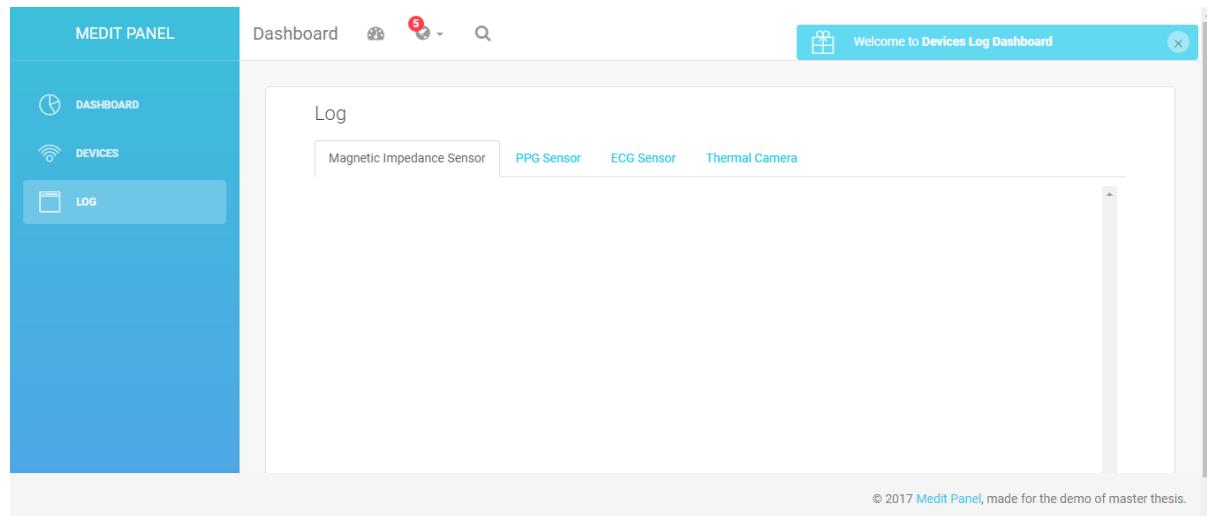
**Figure. 5.11:** Real-time MI signal visualization.



**Figure. 5.12:** Real-time PPG signal visualization.



(a)

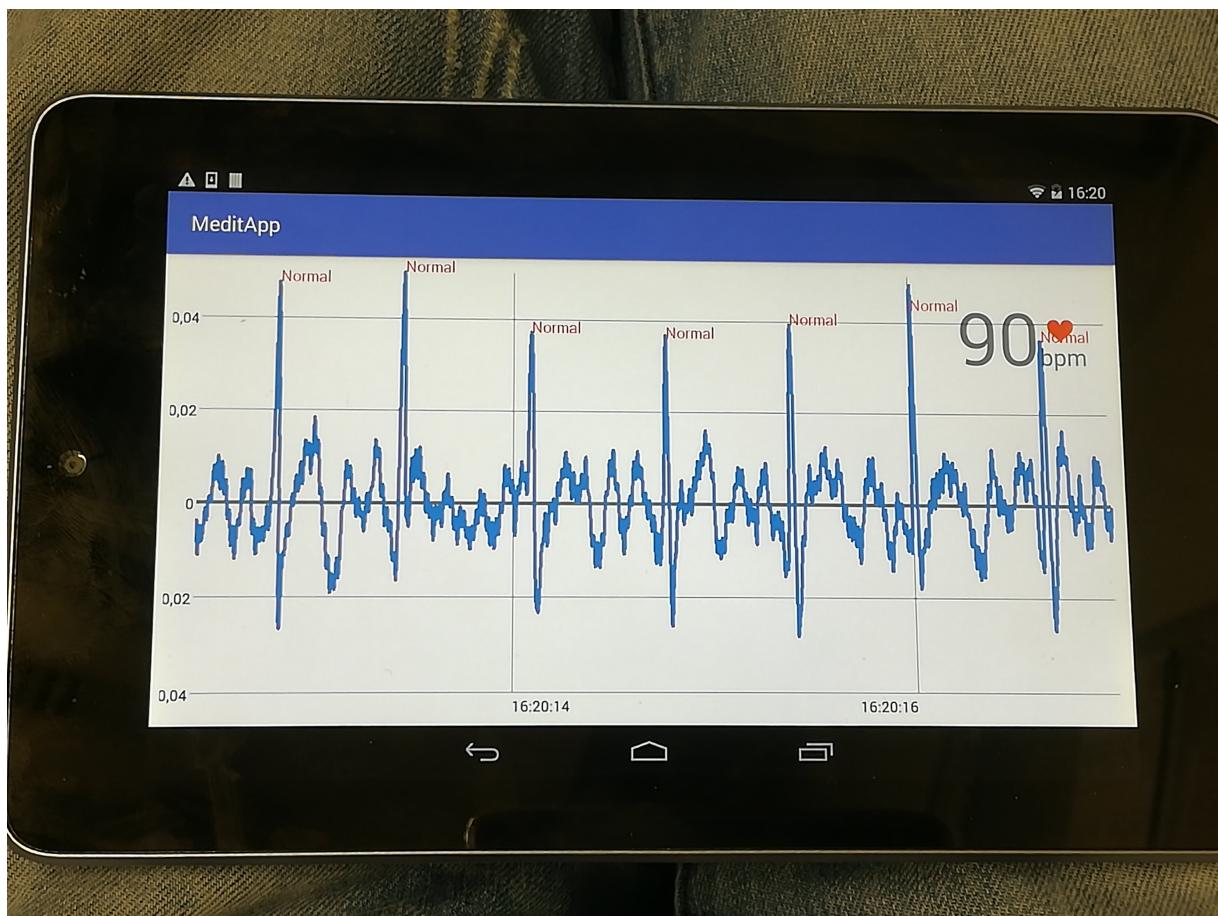


(b)

**Figure. 5.13:** (a) The device management view to interact with devices; and, (b) the log view to know the state of each device.

## 5.7 Android Application

The purpose of this thesis is to implement a system which allows to visualize the data from anywhere. Sometimes, it is not very convenient to visualize the data on laptop, therefore, an android application has been written so the sensors data can be visualized directly on your mobile device as well. The advantage of android application is that it is very light weight and does not require any dependency to visualize the data. The screen shot of android application can be seen in Figure 5.14.



**Figure. 5.14:** Real-time ECG signal visualization on android application.

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