

Verifying Quantum Error Correction Codes with SAT Solvers

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Abstract

Quantum error correction is essential for executing quantum algorithms under realistic noise. However, verifying the correctness of quantum error correction code implementations remains challenging due to the exponential size of the possible error patterns. In this paper, we present a SAT-based approach to formally verify quantum error correction codes by encoding the verification problem as a SAT problem. We apply our method to analyze surface code implementations and successfully identify bugs in a recently published paper, where codes claimed to correct k errors actually fail to do so for larger distances. Our approach demonstrates that SAT solvers can efficiently find counterexamples (bugs) in quantum error correction implementations, though verifying correctness (proving no bugs exist) remains computationally challenging due to the inherent difficulty of UNSAT problems combined with XOR constraints.

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1 Introduction

Quantum computing promises to solve certain problems exponentially faster than classical computers, with potential applications ranging from quantum chemistry [2], cryptography [20], machine learning [23], to finance [19]. However, quantum systems are inherently fragile: quantum bits (qubits) are susceptible to errors from decoherence, environmental noise, and imperfect gate operations [14]. Unlike classical systems where errors mainly occur during data transmission or storage, quantum errors occur *continuously during computation itself*, which intertwines quantum algorithms with quantum error correction, making the correctness of a code not only a static property but also a dynamic one [8].

Quantum error correction (QEC) codes address this challenge by spreading logical information across multiple physical qubits, ensuring that local errors cannot easily affect the logical information. The *distance* d of a code determines its error-correcting capability: a distance- d code can correct up to $\lfloor \frac{d-1}{2} \rfloor$ errors. Verifying that a code implementation achieves its claimed distance is crucial for ensuring fault tolerance, but exhaustively testing all possible error combinations is computationally infeasible for practical code sizes.

There is prior work using SMT solvers to verify the correctness of quantum error correction codes, but the performance is not satisfactory. For example, it takes 70 hours to verify a distance-7 code [6].

1.1 Contributions

In this paper, we make the following contributions:

1. We formulate quantum error correction verification as a SAT problem, enabling the use of highly optimized SAT solvers.



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- 43 2. We develop efficient encodings for XOR constraints arising from detector definitions using
- 44 Tseitin transformation with both chain and tree structures.
- 45 3. We apply our method to verify surface code implementations and discover bugs in a
- 46 recently published Nature paper [5], where codes claimed to achieve certain distances
- 47 actually fail.
- 48 4. We analyze the performance characteristics of our approach, identifying the computational
- 49 challenges that make verification (UNSAT problems) significantly harder than bug finding
- 50 (SAT problems).

51 2 Background

52 2.1 Quantum Computing Basics

53 A *qubit* (quantum bit) is the fundamental unit of quantum information. Unlike a classical bit
54 that exists in state 0 or 1, a qubit can exist in a *superposition* $\alpha|0\rangle + \beta|1\rangle$, where α and β
55 are complex amplitudes satisfying $|\alpha|^2 + |\beta|^2 = 1$ [18]. When measured, the qubit collapses
56 to $|0\rangle$ with probability $|\alpha|^2$ or $|1\rangle$ with probability $|\beta|^2$.

57 For n qubits, the system state lives in a 2^n -dimensional Hilbert space spanned by
58 computational basis states $|x_1 x_2 \cdots x_n\rangle$ where each $x_i \in \{0, 1\}$. A general n -qubit state is
59 $|\psi\rangle = \sum_{x \in \{0,1\}^n} \alpha_x |x\rangle$ with $\sum_x |\alpha_x|^2 = 1$. This exponential growth in state space makes
60 quantum systems both powerful and fragile.

61 2.2 The Surface Code

62 The surface code [11, 9] is one of the most promising quantum error correction codes due to:
63 (1) local nearest-neighbor interactions compatible with many hardware platforms, (2) high
64 error threshold ($\sim 1\%$, below which error correction becomes beneficial), and (3) efficient
65 decoding via almost linear-time algorithms [16] that are also near optimal. The surface
66 code has been successfully demonstrated on multiple experimental platforms, including
67 superconducting qubits [1] and neutral atoms [5].

68 2.3 Stabilizer Formalism

69 The stabilizer formalism [13] enables error detection without measuring the encoded quantum
70 state directly. A stabilizer code is defined by a set of commuting n -qubit Pauli operators
71 $\mathcal{S} = \{S_1, S_2, \dots, S_m\}$. Valid codewords $|\psi\rangle$ satisfy $S_i|\psi\rangle = |\psi\rangle$ for all $S_i \in \mathcal{S}$.

72 When an error E (a Pauli operator) occurs, the corrupted state $E|\psi\rangle$ may no longer be a
73 $+1$ eigenstate of all stabilizers. The syndrome is determined by the commutation relations:
74 measuring S_i yields $+1$ if $ES_i = S_iE$ (commute), and -1 if $ES_i = -S_iE$ (anti-commute).
75 Mathematically, if we define syndrome bit $s_i \in \{0, 1\}$ where $S_iE = (-1)^{s_i}ES_i$, then the
76 syndrome vector $\mathbf{s} = (s_1, \dots, s_m)$ can be used to determine the error.

77 A quantum code with parameters $[[n, k, d]]$ uses n physical qubits to encode k logical
78 qubits with distance d , meaning any error affecting fewer than d qubits produces a non-trivial
79 syndrome and can be detected.

80 2.4 Detectors and Decoders

81 A *detector* is a linear combination of measurement outcomes that is deterministic in the
82 absence of errors. When errors occur, detectors may produce unexpected values, providing
83 classical information about which errors likely occurred.

84 The *decoder* is a classical algorithm that uses detector information to infer the error
 85 pattern and apply corrections.

86 2.5 Detector Error Model (DEM)

87 We use Stim's Detector Error Model (DEM) format [12] to represent error mechanisms
 88 and their effects. A DEM file describes each error mechanism with its probability, affected
 89 detectors (D#), and affected logical observables (L#). For example:

```
90
91 1 error(0.027) D0 D1
92 2 error(0.101) D0 L0
```

94 The first line triggers detectors D0 and D1 with probability 0.027; the second line triggers
 95 D0 and flips logical observable L0 with probability 0.101. In this work, we only focus on the
 96 number of errors that occur and ignore the probability values.

97 2.6 Zero-Detector Verification

98 Most quantum error correction codes are *linear codes*: if error patterns E_1 and E_2 each
 99 produce syndromes s_1 and s_2 , then $E_1 \oplus E_2$ produces syndrome $s_1 \oplus s_2$. This linearity has
 100 an important consequence for code verification.

101 A *zero-detector logical error* is an error pattern that triggers no detectors (zero syndrome)
 102 but flips at least one logical observable. Such errors are undetectable and cause logical failures.
 103 Due to linearity, if E_1 and E_2 produce the same syndrome $s_1 = s_2$ but different logical
 104 outcomes, then $E_1 \oplus E_2$ triggers no detectors yet flips a logical observable—a zero-detector
 105 logical error.

106 The *code distance* d is defined as the minimum weight of any zero-detector logical error:

$$107 \quad d = \min\{|E| : E \text{ triggers no detectors and flips a logical observable}\}$$

108 A code with distance d can reliably correct up to $t = \lfloor (d - 1)/2 \rfloor$ errors. This is because any
 109 two correctable error patterns E_1 and E_2 with $|E_1|, |E_2| \leq t$ must have distinct syndromes;
 110 otherwise $E_1 \oplus E_2$ would be a zero-detector logical error with weight at most $2t < d$,
 111 contradicting the definition of distance. This guarantee assumes an *optimal decoder* that,
 112 given a syndrome, selects the minimum-weight error pattern consistent with that syndrome,
 113 thereby ensuring correct decoding for all errors up to weight t .

114 3 SAT Encoding Methodology

115 Given n error mechanisms, m detectors, and ℓ logical observables, we create a boolean
 116 variable e_i for each error mechanism and add the following constraints:

- 117 1. *Detector*: $\bigoplus_{i \in \text{affects}(D_j)} e_i = 0$ for each detector D_j ;
- 118 2. *Observable*: $\bigvee_k (\bigoplus_{i \in \text{affects}(L_k)} e_i = 1)$ for each logical observable L_k ;
- 119 3. *Cardinality*: $\sum_i e_i \leq k$.

120 If the SAT solver finds a solution, the solution represents an undetectable logical error with
 121 at most k errors, demonstrating that the distance of the code is at most k . Conversely, if the
 122 solver proves UNSAT, then no such error pattern exists, certifying that the code distance is
 123 at least $k + 1$.

124 3.1 XOR Encoding with Tseitin Transformation

125 XOR constraints must be converted to CNF using the Tseitin transformation. For a base- b
 126 XOR gate $c = e_1 \oplus e_2 \oplus \dots \oplus e_b$, we enumerate all 2^b input combinations and generate 2^{b-1}
 127 clauses enforcing $c = 1$ when an odd number of inputs are true. For the simplest case $b = 2$,
 128 the constraint $c = a \oplus b$ requires 4 clauses: $(\neg a \vee \neg b \vee \neg c) \wedge (a \vee b \vee \neg c) \wedge (a \vee \neg b \vee c) \wedge (\neg a \vee b \vee c)$.

129 To encode $e_1 \oplus \dots \oplus e_n = 0$, we recursively decompose it using base- b XOR gates as
 130 building blocks:

131 **Chain Structure:** Introduce auxiliary variables sequentially: $a_1 = e_1 \oplus \dots \oplus e_b$,
 132 $a_2 = a_1 \oplus e_{b+1} \oplus \dots \oplus e_{2b-1}$, etc. This produces a linear chain with depth $O(n/b)$.

133 **Tree Structure:** Reduce XORs in a balanced tree: first compute $a_i = e_{(i-1)b+1} \oplus \dots \oplus e_{ib}$
 134 for each group of b variables, then recursively combine a_i 's using the same method. This
 135 achieves depth $O(\log_b n)$ for better unit propagation.

136 Higher base values reduce the number of auxiliary variables but increase clause complexity
 137 exponentially (2^{b-1} clauses per gate).

138 3.2 Cardinality Constraints

139 To encode “at most k of n variables are true,” the naive approach adds a clause for each
 140 $(k+1)$ -subset, yielding $\binom{n}{k+1}$ clauses—exponential in k .

141 We use the *totalizer encoding* [3], which constructs a unary counting circuit via a binary
 142 tree. Each leaf represents an input variable e_i . Each internal node merges two sorted
 143 unary counters from its children: if the left child outputs (l_1, \dots, l_a) and the right outputs
 144 (r_1, \dots, r_b) , the merged output (o_1, \dots, o_{a+b}) satisfies $o_i = 1$ iff at least i inputs below are
 145 true. The merge operation uses clauses of the form $l_i \wedge r_j \Rightarrow o_{i+j}$. At the root, it is enforced
 146 that $o_{k+1} = 0$ to guarantee at most k variables are true. This encoding requires $O(n \log n)$
 147 auxiliary variables and $O(nk)$ clauses, and provides strong unit propagation.

148 4 Evaluation

149 Our implementation uses Python with PySAT and CaDiCaL [4], a state-of-the-art CDCL
 150 solver. We use Stim [12] to generate detector error models from quantum circuits.

151 4.1 Bug Discovery in Nature Paper

152 We applied our method to surface code implementations from a Nature paper [5], where
 153 the authors claimed to have implemented a variant of the surface code that can correct $\frac{d-3}{2}$
 154 errors for distance d .

155 Table 1 shows the problem scales for different code distances in the buggy version of the
 156 surface code.

157 Table 2 shows our findings: **distances 11 and 13 fail to correct the claimed number**
 158 **of errors**. The distance-11 code corrects only 3 errors (not 4), and the distance-13 code
 159 corrects only 4 (not 5).

160 Our SAT solver not only proves the existence of error patterns that trigger no detectors
 161 while flipping a logical observable but also provides explicit counterexamples. For the
 162 distance-11 code, an 8-error pattern (versus the expected minimum of 11) demonstrates a
 163 “shortcut” through the code. These counterexamples provide valuable debugging information,
 164 pinpointing exactly which error mechanisms combine to defeat error correction.

165 The root cause of this bug appears to be incorrect extrapolation from smaller code
 166 distances. While the observed sequence $(0, 1, 2, 3)$ for distances 3, 5, 7, 9 naturally suggests

■ **Table 1** Problem sizes for different code distances

Distance	Errors	Detectors	CNF Vars
3	1	16	438
5	3	72	3,392
7	4	192	11,824
9	6	400	29,058
11	7	720	58,704
13	9	1,176	104,856

■ **Table 2** Verification Results: Claimed vs Actual Correctable Errors

Distance	Actual	Claimed
3	0	0
5	1	1
7	2	2
9	3	3
11	3	4
13	4	5

the pattern continues with 4 for distance 11, our formal verification reveals this intuition is incorrect. This highlights the importance of formal verification in quantum error correction: properties that hold for small instances do not necessarily generalize to larger systems.

4.2 Performance Analysis: SAT vs UNSAT

Figure 1 compares SAT (bug finding) vs UNSAT (verification) performance. Finding counterexamples is fast, but the time required for proving correctness grows rapidly with problem size.

We notice that for small instances, SAT is sometimes slower than UNSAT. This might be because when the code is small, the relative difference between d and $d - 1$ is large, making UNSAT easier to prove. In an extreme case, when $d = 3$, we are trying to prove that 0 errors cannot trigger any detectors while flipping a logical observable, which is obviously impossible.

4.3 Performance Analysis: Different XOR Encoding Strategies

Figure 2 compares XOR encoding strategies (chain vs tree, base-2 vs base-3). Tree-based encodings provide better propagation and thus are faster in both SAT and UNSAT problems. However, we do not see a significant difference in performance between base-2 and base-3 encodings.

4.4 Performance Analysis: Different Solvers

We also tested the performance of solving the SAT and UNSAT problems using other solvers, including CryptoMiniSat [21], MaxSAT(RC2) [17], and Z3 [7].

We chose these solvers because CryptoMiniSat has native support for XOR constraints, MaxSAT(RC2) is optimized for cardinality constraints, and Z3 has the potential to leverage SMT reasoning for better performance.

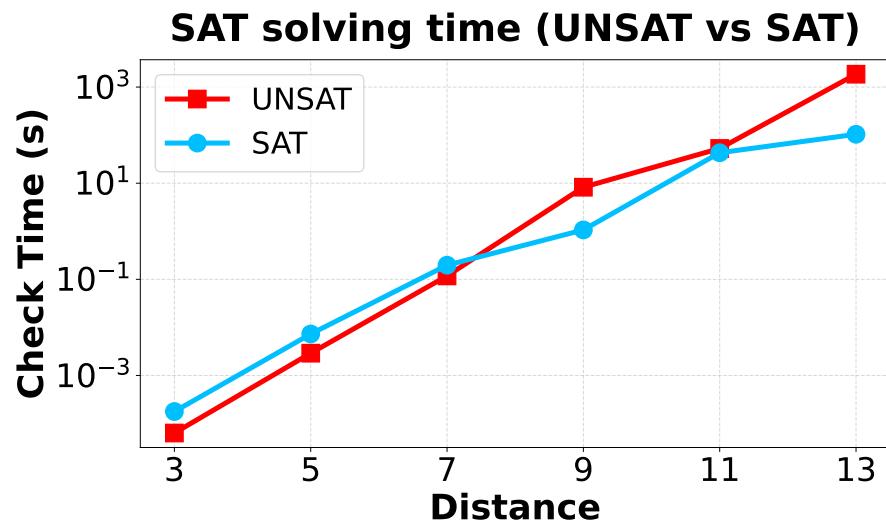


Figure 1 UNSAT performance: Verification is slow

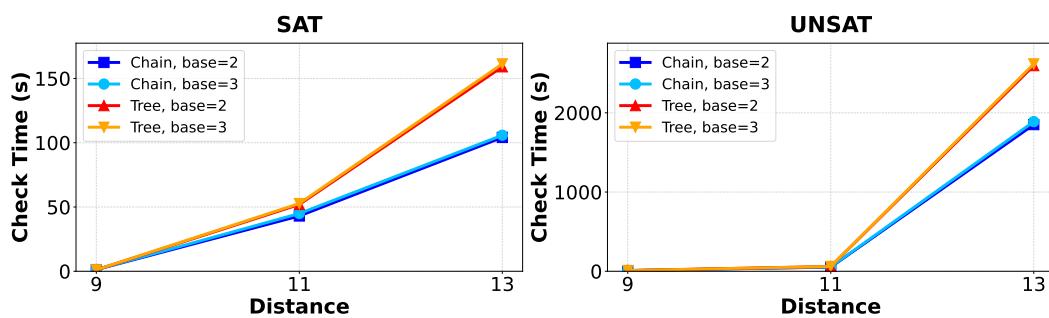


Figure 2 Comparison of XOR encoding strategies

¹⁸⁹ Throughout this subsection, we use the “correct” implementation of the surface code and
¹⁹⁰ base-2 chain XOR encoding when applicable.

¹⁹¹ 4.4.1 Results using CaDiCaL

¹⁹² Table 3 shows the results using CaDiCaL. CaDiCaL is able to solve the UNSAT problem up
¹⁹³ to distance 9 but fails to solve the UNSAT problem at distance 11. This is already the best
 performance among all solvers.

■ **Table 3** Results using CaDiCaL

Distance	Errors	Result	Num vars	Build Time	Solve Time
3	2	UNSAT	679	0.002	0.0001
3	3	SAT	679	0.002	0.0002
5	4	UNSAT	4479	0.063	0.024
5	5	SAT	4479	0.066	0.011
7	6	UNSAT	14461	0.218	1.623
7	7	SAT	14461	0.213	0.119
9	8	UNSAT	34160	0.986	72.82
9	9	SAT	34160	0.991	1.067
11	10	UNSAT	67004	4.748	>3600
11	11	SAT	67004	4.748	0.007

¹⁹⁴

¹⁹⁵ 4.4.2 Results using CryptoMiniSat

¹⁹⁶ Table 4 shows the results using CryptoMiniSat [21]. CryptoMiniSat is able to solve the
¹⁹⁷ UNSAT problem up to distance 7 but fails to solve the UNSAT problem at distance 9. We
 attribute this to the fact that CryptoMiniSat is not optimized for cardinality constraints.

■ **Table 4** Results using CryptoMiniSat

Distance	Errors	Result	Num vars	Build Time	Solve Time
3	2	UNSAT	539	0.016	0.150
3	3	SAT	539	0.012	0.0003
5	4	UNSAT	3691	0.063	272.9
5	5	SAT	3691	0.066	0.0025
7	6	UNSAT	12175	0.529	91.68
7	7	SAT	12175	0.467	0.019
9	8	UNSAT	29197	2.374	>3600
9	9	SAT	29197	2.554	0.059

¹⁹⁸

¹⁹⁹ 4.4.3 Results using Z3

²⁰⁰ Table 5 shows the results using Z3 [7]. Z3 is the worst among all solvers and can only solve
²⁰¹ the UNSAT problem up to distance 5.

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■ **Table 5** Results using Z3

Distance	Errors	Result	Build Time	Solve Time
3	2	UNSAT	0.016	0.150
3	3	SAT	0.012	0.066
5	4	UNSAT	0.063	272.9
5	5	SAT	0.066	0.697
7	6	UNSAT	0.187	>3600
7	7	SAT	0.006	0.007

202 4.4.4 Results using MaxSAT(RC2)

203 Table 6 shows the results using MaxSAT(RC2) [17]. RC2 is on par with CryptoMiniSat but
 204 has the advantage of not requiring any prior knowledge and can find the exact error-correcting
 capability in one shot.

■ **Table 6** Results using MaxSAT

Distance	Result	Num hard clauses	Num soft clauses	Build Time	Solve Time
3	3	506	74	0.001	0.002
5	5	2758	382	0.002	0.321
7	7	8034	1094	0.004	96.3
9	9	17606	2378	0.010	>3600

205

206 5 Challenges and Limitations

207 Through our experiments, we found that verification is significantly harder than bug finding.
 208 We believe the following factors explain this:

209 **UNSAT Problem Difficulty:** Verification requires proving UNSAT—that no satisfying
 210 assignment exists. This is inherently harder than finding satisfying assignments because the
 211 solver must exhaustively rule out all possibilities. While SAT problems can often be solved
 212 quickly by finding a single witness, UNSAT proofs require exploring (and pruning) the entire
 213 search space.

214 **XOR Constraints:** SAT solvers are known to struggle with parity constraints [22]. Our
 215 XOR constraints, while encoded into CNF via Tseitin transformation, retain their underlying
 216 parity structure that causes difficulty for resolution-based proof systems. The inability of
 217 resolution to efficiently handle XOR is a fundamental limitation.

218 **Cardinality Constraints:** The “at most k errors” constraint resembles the pigeonhole
 219 principle, which is known to require exponentially long resolution proofs [15]. Combined
 220 with XOR constraints, this creates a particularly challenging problem structure.

221 Together, these factors make verification substantially harder than bug finding, explaining
 222 the dramatic performance gap observed in our experiments.

223 5.1 A Proof Complexity Perspective

224 It is well known that resolution is intractable for the pigeonhole principle: any resolution
 225 refutation of PHP $_{n+1}^n$ has size $2^{\Omega(n)}$ [15]. This classical lower bound serves as a canonical

226 benchmark for reasoning about counting constraints in CNF.

227 A closely related structure arises in our setting. Consider variables x_1, \dots, x_{n+1} and the
228 contradictory formula

$$\bigwedge_{i=1}^{n+1} x_i \wedge \sum_{i=1}^{n+1} x_i \leq k.$$

230 This formula is an instance of the surface code problem when all detectors only detect two
231 errors, and captures a simple form of global counting inconsistency. The proof complexity
232 of the resulting CNF depends on the particular encoding of the cardinality constraint into
233 clauses.

234 Under the *pigeonhole encoding* of cardinality constraints [?], the formula above contains,
235 as a projection, an instance of the pigeonhole principle. Consequently, every resolution
236 refutation of this encoding has exponential size, by an immediate reduction to the lower
237 bound of [15].

238 The situation for other standard encodings (such as totalizer, sorting-network, or binary-
239 adder encodings) is less well understood. Existing lower bounds do not directly apply, and it
240 remains open whether these alternative encodings also admit exponential resolution lower
241 bounds or whether some of them may yield polynomial-size refutations. Establishing the
242 precise proof complexity of these cardinality encodings is an interesting direction for further
243 investigation.

244 6 Related Work

245 There has been prior work on verifying quantum error correction codes using SMT solvers,
246 for example, [10]. However, their proof relies on a specific decoder and cannot generalize to
247 other codes. A more general approach is proposed in [6] using SMT solvers. However, their
248 scalability is not satisfactory: it takes 70 hours to verify a distance-7 code.

249 7 Conclusion and Future Work

250 We presented a SAT-based approach to verifying quantum error correction codes, encoding the
251 verification problem as boolean satisfiability with XOR constraints for detectors, cardinality
252 constraints for error bounds, and disjunctive constraints for logical observables. Our method
253 discovered bugs in a published Nature paper’s surface code implementation, where distance-11
254 and distance-13 codes fail to achieve their claimed error correction capability.

255 Our experiments reveal a fundamental challenge: SAT solvers efficiently find counter-
256 examples in faulty implementations, but proving correctness (UNSAT) is significantly harder
257 due to the combination of XOR constraints, cardinality constraints, and the need to exhaustively
258 rule out all possibilities.

259 For future work, we propose a hybrid SAT and theorem prover approach. SAT solvers
260 excel at bug finding and search space pruning, while theorem provers (e.g., Lean) provide
261 formal correctness guarantees. A hybrid approach could use SAT for rapid counterexample
262 detection and pruning and then employ theorem provers to formally verify correctness.

263 References

- 264 1 Quantum error correction below the surface code threshold. *Nature*, 638(8052):920–926, 2025.

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- 265 2 Ryan Babbush, Jarrod McClean, Dave Wecker, Alán Aspuru-Guzik, and Nathan Wiebe.
266 Chemical basis of trotter-suzuki errors in quantum chemistry simulation. *Physical Review A*,
267 91(2):022311, 2015.
- 268 3 Olivier Bailleux and Yacine Boufkhad. Efficient cnf encoding of boolean cardinality constraints.
269 In *International conference on principles and practice of constraint programming*, pages 108–122.
270 Springer, 2003.
- 271 4 Armin Biere, Tobias Faller, Katalin Fazekas, Mathias Fleury, Nils Froleyks, and Florian Pollitt.
272 CaDiCaL 2.0. In Arie Gurfinkel and Vijay Ganesh, editors, *Computer Aided Verification - 36th
273 International Conference, CAV 2024, Montreal, QC, Canada, July 24-27, 2024, Proceedings,
274 Part I*, volume 14681 of *Lecture Notes in Computer Science*, pages 133–152. Springer, 2024.
275 doi:10.1007/978-3-031-65627-9_7.
- 276 5 Dolev Bluvstein, Alexandra A Geim, Sophie H Li, Simon J Evered, J Pablo Bonilla Ataides,
277 Gefen Baranes, Andi Gu, Tom Manovitz, Muqing Xu, Marcin Kalinowski, et al. A fault-
278 tolerant neutral-atom architecture for universal quantum computation. *Nature*, pages 1–3,
279 2025.
- 280 6 Kean Chen, Yuhao Liu, Wang Fang, Jennifer Paykin, Xin-Chuan Wu, Albert Schmitz, Steve
281 Zdancewic, and Gushu Li. Verifying fault-tolerance of quantum error correction codes. In
282 *International Conference on Computer Aided Verification*, pages 3–27. Springer, 2025.
- 283 7 Leonardo De Moura and Nikolaj Bjørner. Z3: An efficient smt solver. In *International
284 conference on Tools and Algorithms for the Construction and Analysis of Systems*, pages
285 337–340. Springer, 2008.
- 286 8 Nicolas Delfosse and Adam Paetznick. Spacetime codes of clifford circuits. *arXiv preprint
287 arXiv:2304.05943*, 2023.
- 288 9 Eric Dennis, Alexei Kitaev, Andrew Landahl, and John Preskill. Topological quantum memory.
289 *Journal of Mathematical Physics*, 43(9):4452–4505, 2002.
- 290 10 Wang Fang and Mingsheng Ying. Symbolic execution for quantum error correction programs.
291 *Proceedings of the ACM on Programming Languages*, 8(PLDI):1040–1065, 2024.
- 292 11 Austin G Fowler, Matteo Mariantoni, John M Martinis, and Andrew N Cleland. Surface codes:
293 Towards practical large-scale quantum computation. *Physical Review A—Atomic, Molecular,
294 and Optical Physics*, 86(3):032324, 2012.
- 295 12 Craig Gidney. Stim: a fast stabilizer circuit simulator. *Quantum*, 5:497, 2021.
- 296 13 Daniel Gottesman. *Stabilizer codes and quantum error correction*. California Institute of
297 Technology, 1997.
- 298 14 Daniel Gottesman. Surviving as a quantum computer in a classical world. *Textbook manuscript
299 preprint*, 8(8.1):8–2, 2024.
- 300 15 Armin Haken. The intractability of resolution. *Theoretical computer science*, 39:297–308, 1985.
- 301 16 Oscar Higgott. Pymatching: A python package for decoding quantum codes with minimum-
302 weight perfect matching. *ACM Transactions on Quantum Computing*, 3(3):1–16, 2022.
- 303 17 Alexey Ignatiev, António Morgado, and Joao Marques-Silva. Rc2: an efficient maxsat solver.
304 *Journal on Satisfiability, Boolean Modelling and Computation*, 11(1):53–64, 2019.
- 305 18 Michael A Nielsen and Isaac L Chuang. *Quantum computation and quantum information*.
306 Cambridge university press, 2010.
- 307 19 Román Orús, Samuel Mugel, and Enrique Lizaso. Quantum computing for finance: Overview
308 and prospects. *Reviews in Physics*, 4:100028, 2019.
- 309 20 Peter W Shor. Algorithms for quantum computation: discrete logarithms and factoring. In
310 *Proceedings 35th annual symposium on foundations of computer science*, pages 124–134. Ieee,
311 1994.
- 312 21 Mate Soos. The cryptominisat 5 set of solvers at sat competition 2016. *Proceedings of SAT
313 Competition*, 28, 2016.
- 314 22 Alasdair Urquhart. Hard examples for resolution. *Journal of the ACM (JACM)*, 34(1):209–219,
315 1987.

- ³¹⁶ 23 Xin-Ding Zhang, Xiao-Ming Zhang, and Zheng-Yuan Xue. Quantum hyperparallel algorithm
³¹⁷ for matrix multiplication. *Scientific reports*, 6(1):24910, 2016.