

function

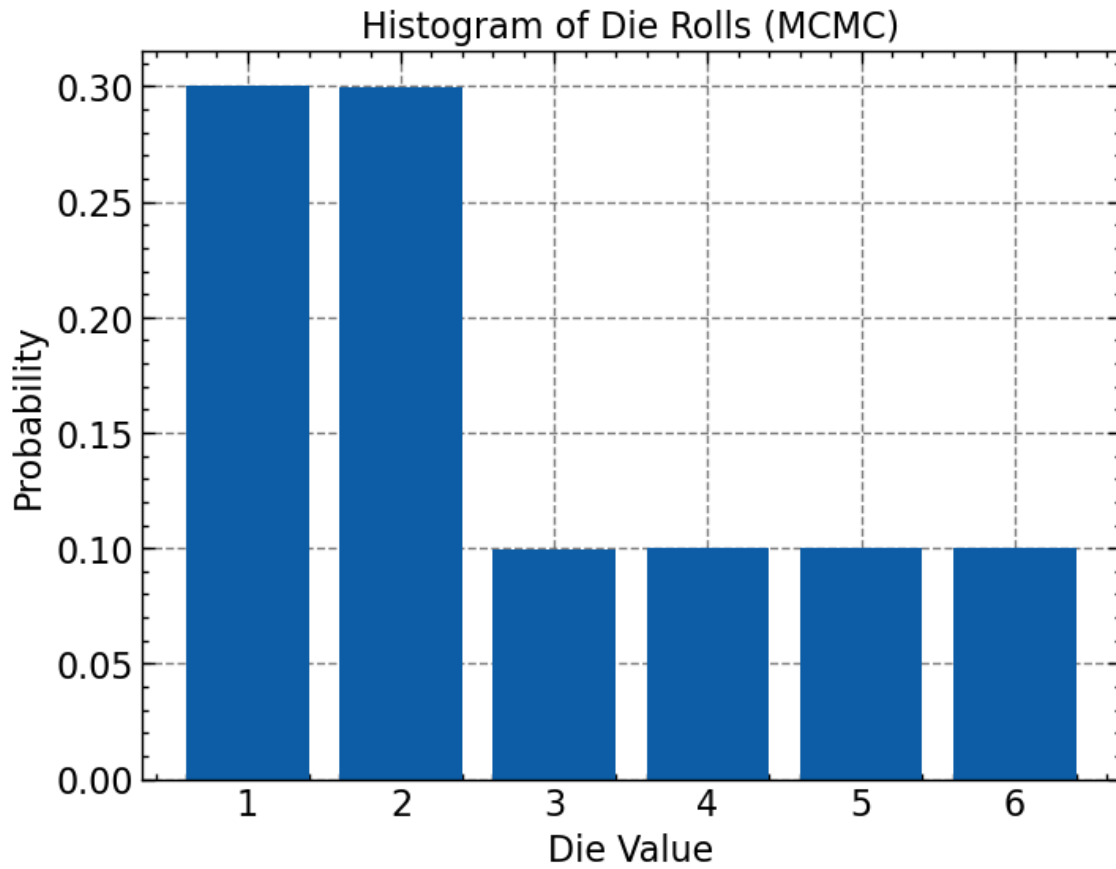
May 27, 2024

```
[ ]: from numba import jit, njit
import numpy as np
import matplotlib.pyplot as plt
import scienceplots
import random
from modula import *
plt.style.use(['science', 'grid', 'notebook'])
```

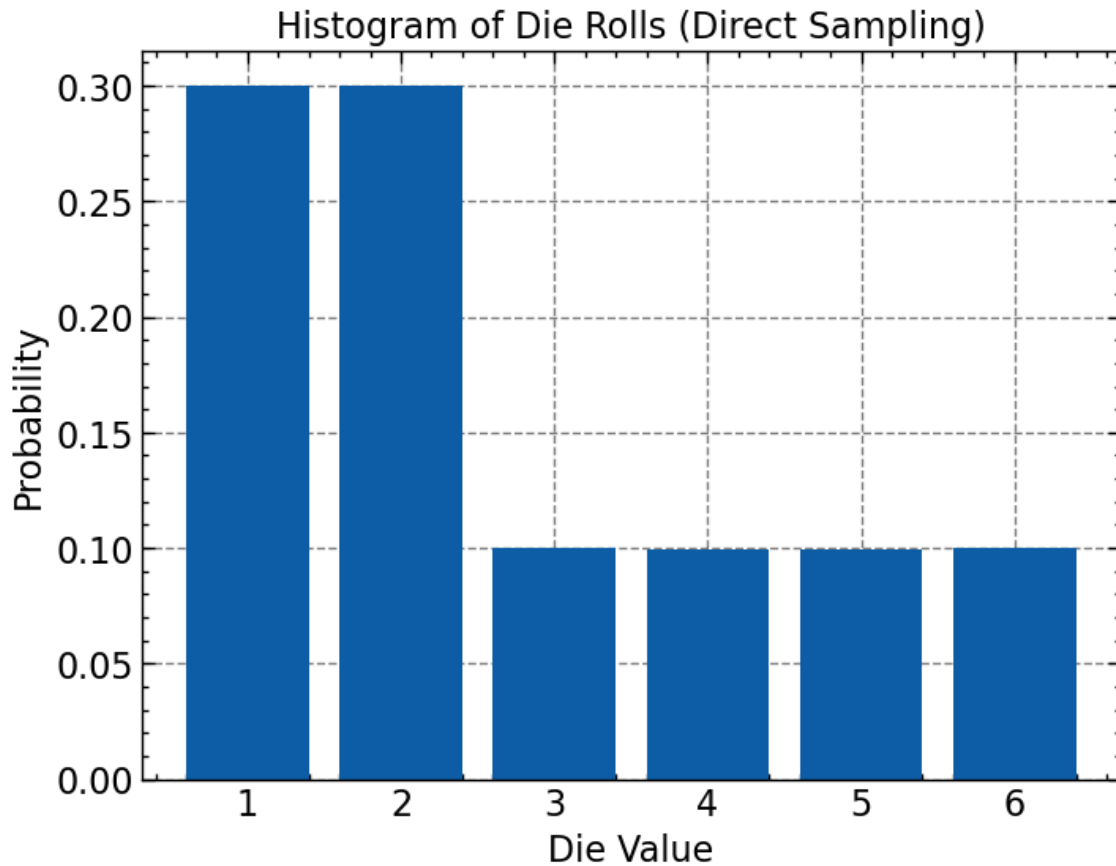
0.0.1 Weighted die

```
[ ]: num_simulation = int(1e6)
result_mcmc = weighted_die(num_simulation)
result_python = weighted_die_direct_sampling(num_simulation)
```

```
[ ]: # Set bins to explicitly represent each die value from 1 to 6
bins = [0.5, 1.5, 2.5, 3.5, 4.5, 5.5, 6.5] # Setting bins between the integers
plt.hist(result_mcmc, bins=bins, density=True, rwidth=0.8)
plt.xticks(range(1, 7))
plt.xlabel('Die Value')
plt.ylabel('Probability')
plt.title('Histogram of Die Rolls (MCMC)')
plt.show()
```



```
[ ]: plt.hist(result_python, bins=bins, density=True, rwidth=0.8)
plt.xticks(range(1, 7)) # Set x-ticks to be centered on each integer
plt.xlabel('Die Value')
plt.ylabel('Probability')
plt.title('Histogram of Die Rolls (Direct Sampling)')
plt.show()
```



0.0.2 plotting time series' of intensive quantities

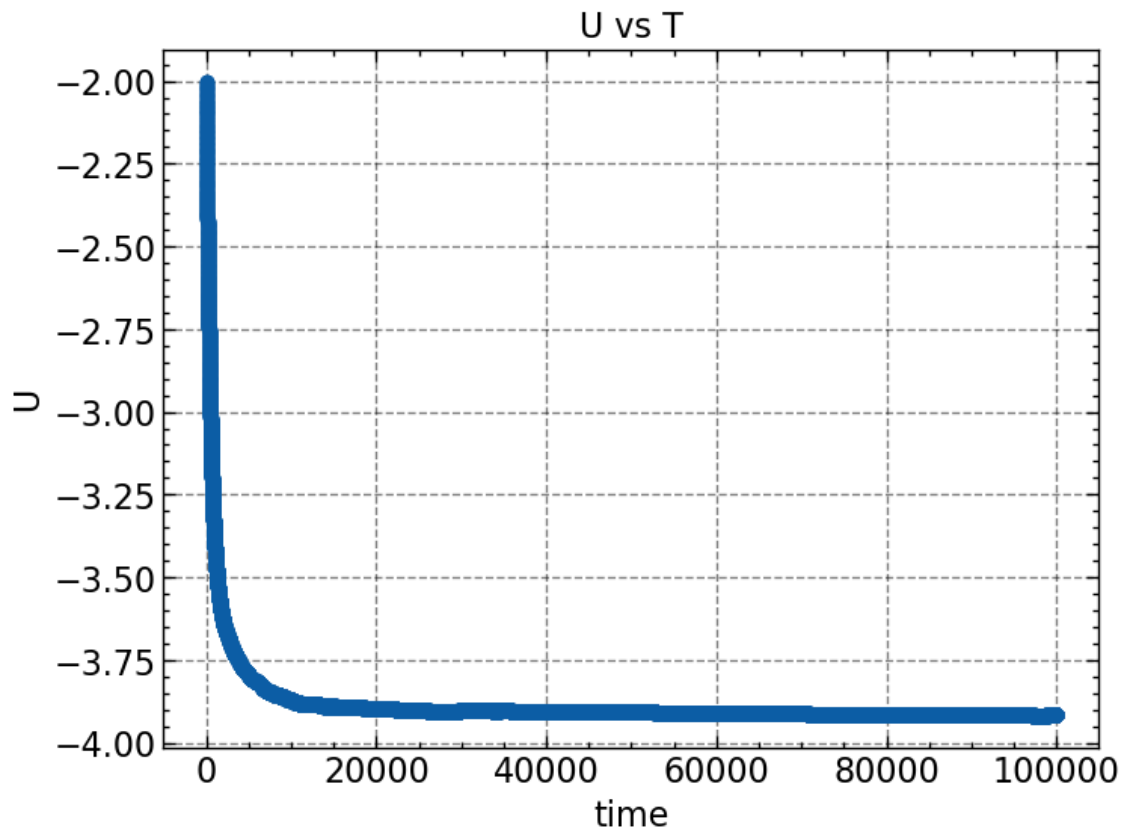
- Choose system sizes $L = 16, 32$ and a temperature of your choosing not too close to the critical temperature, and run the simulation. Plot U and M as functions of t , the update step per site defined above.
- Roughly how long does it seem to take for the simulation to converge?
- Does the time it takes seem to depend on the system size?

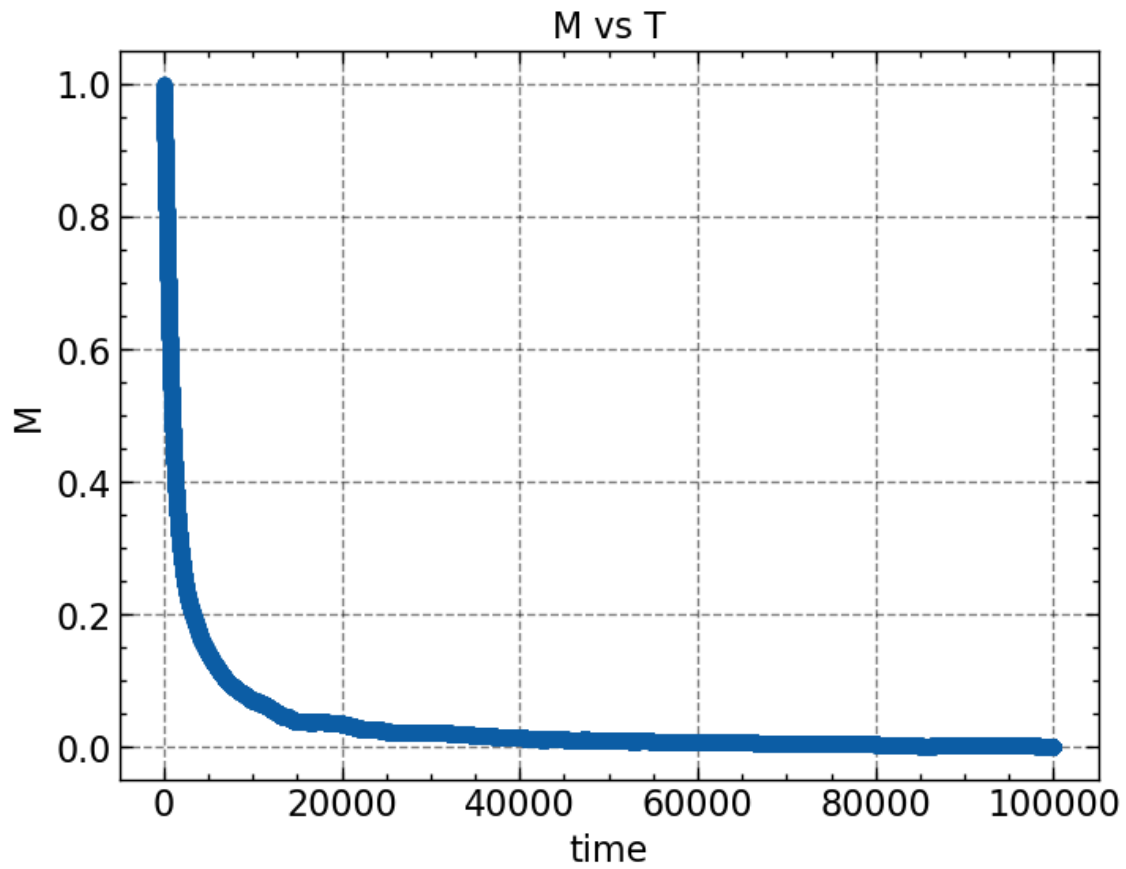
```
[ ]: arr, E, S = two_dim_ising(L = 32, temp = 25, num_steps = int(1e6))
U = U_series(E, int(1e6), 32)
M = M_series(S, int(1e6), 32)
points = U.size // 10

plt.figure()
plt.plot(np.arange(points), U[:points], 'o')
plt.xlabel('time')
plt.ylabel('U')
plt.title(f'U vs T')
```

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plt.show()

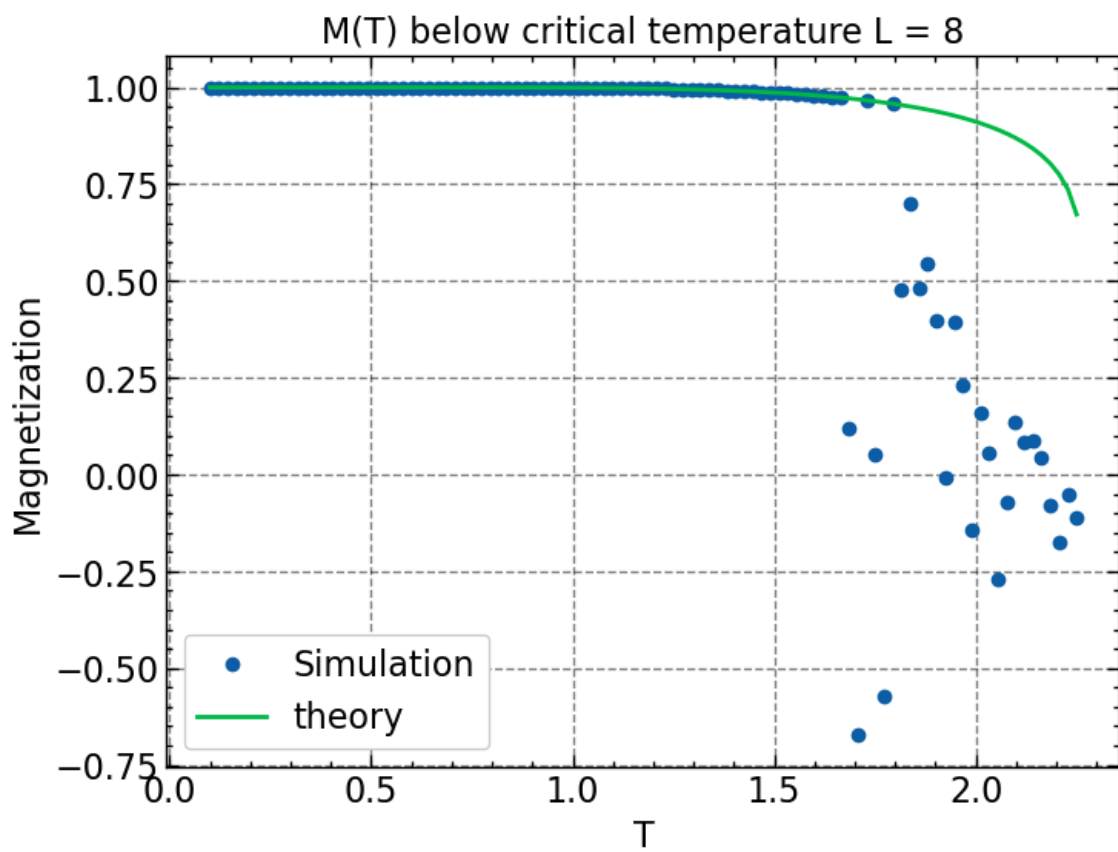
plt.figure()
plt.plot(np.arange(points), M[:points], 'o')
plt.xlabel('time')
plt.ylabel('M')
plt.title(f'M vs T')
plt.show()
```

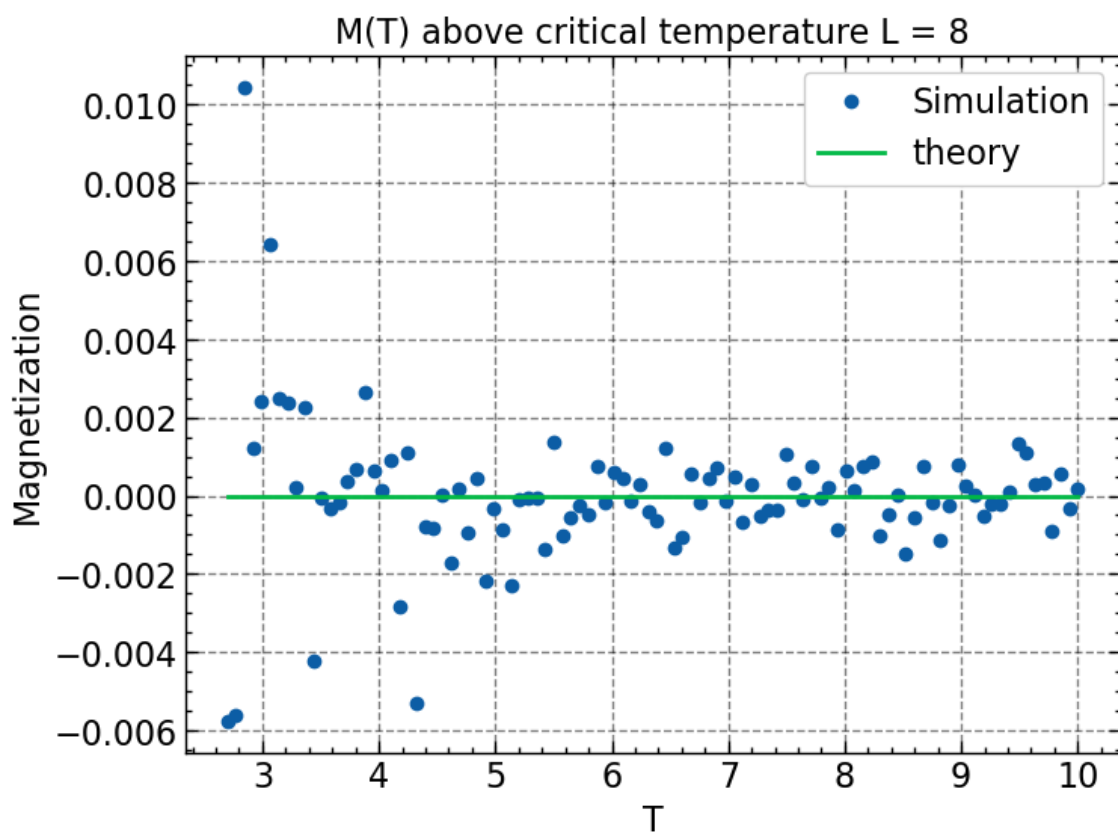


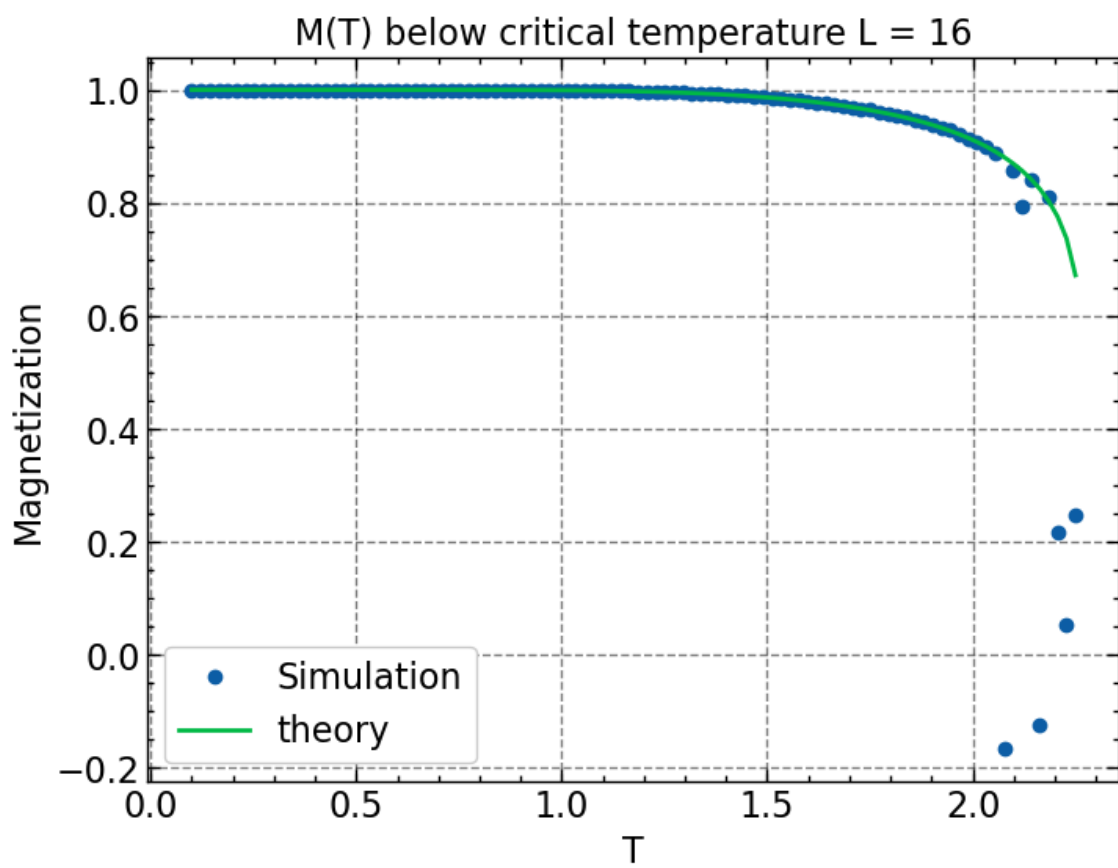


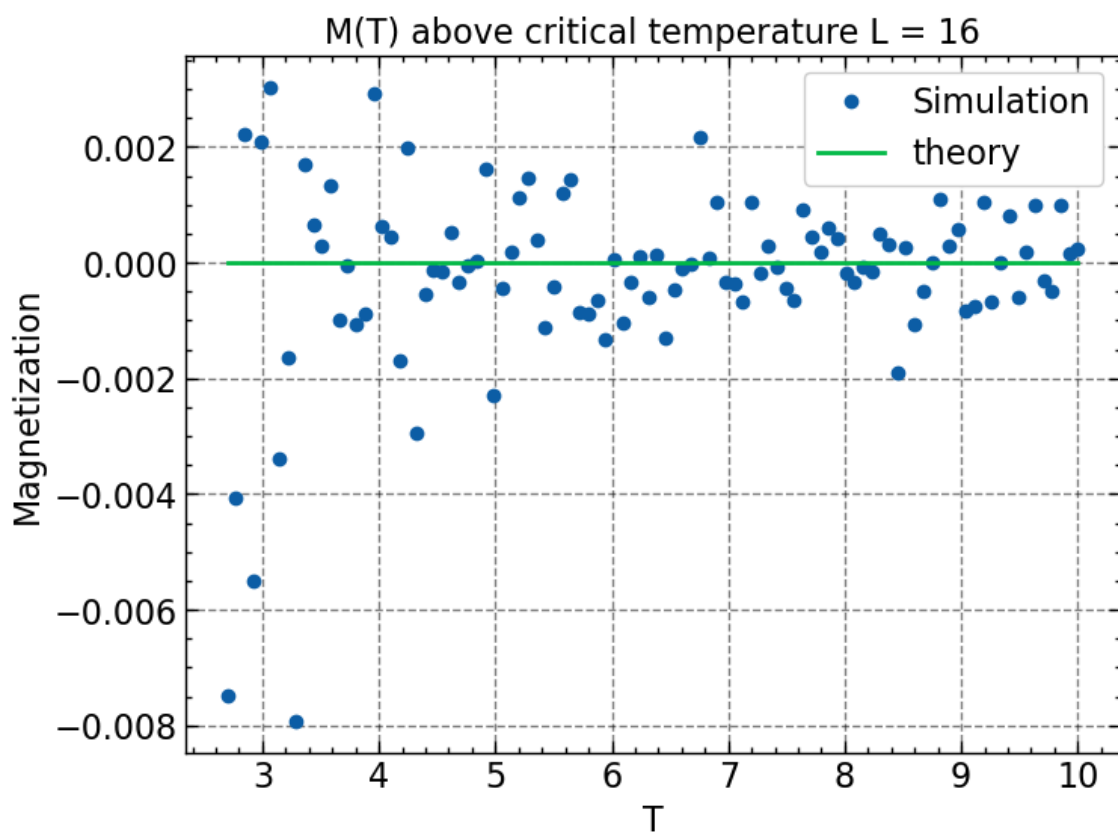
0.0.3 Magnetization curves for different lattice sizes

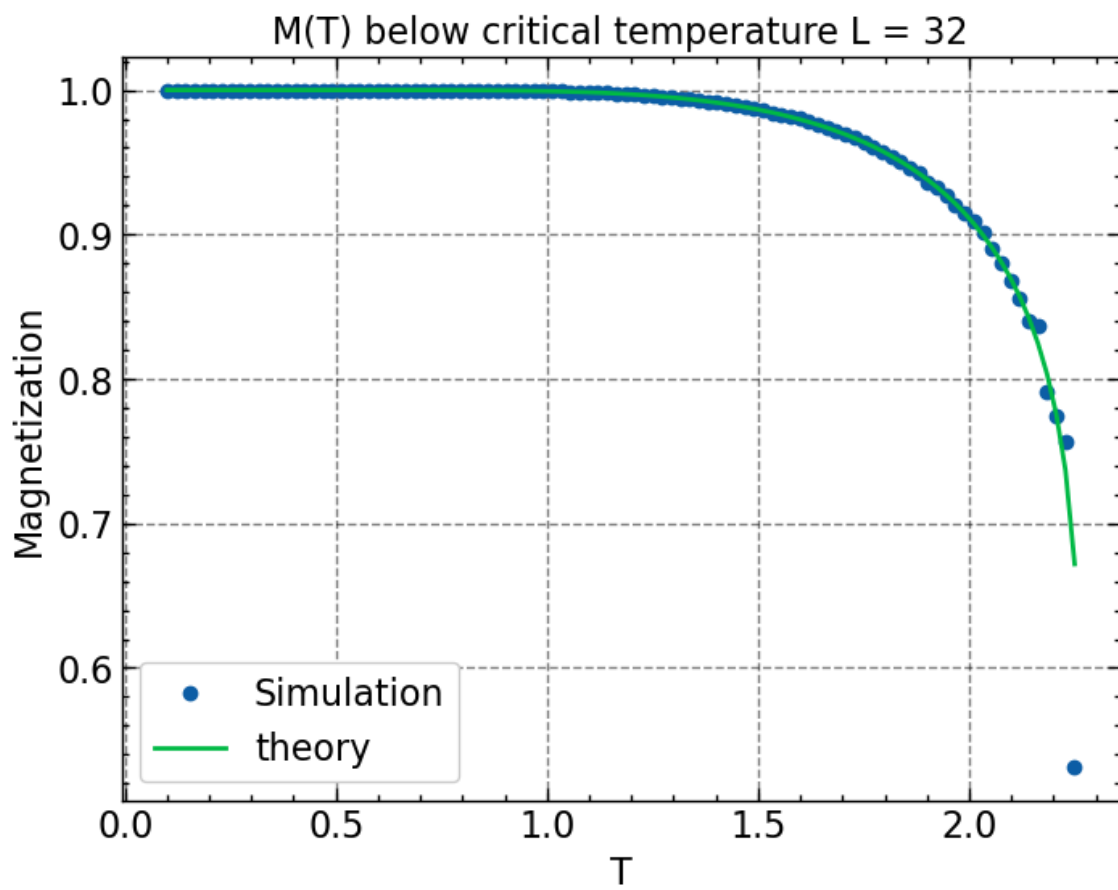
```
[ ]: Magnetization(L_arr = [8, 16, 32, 64])
```

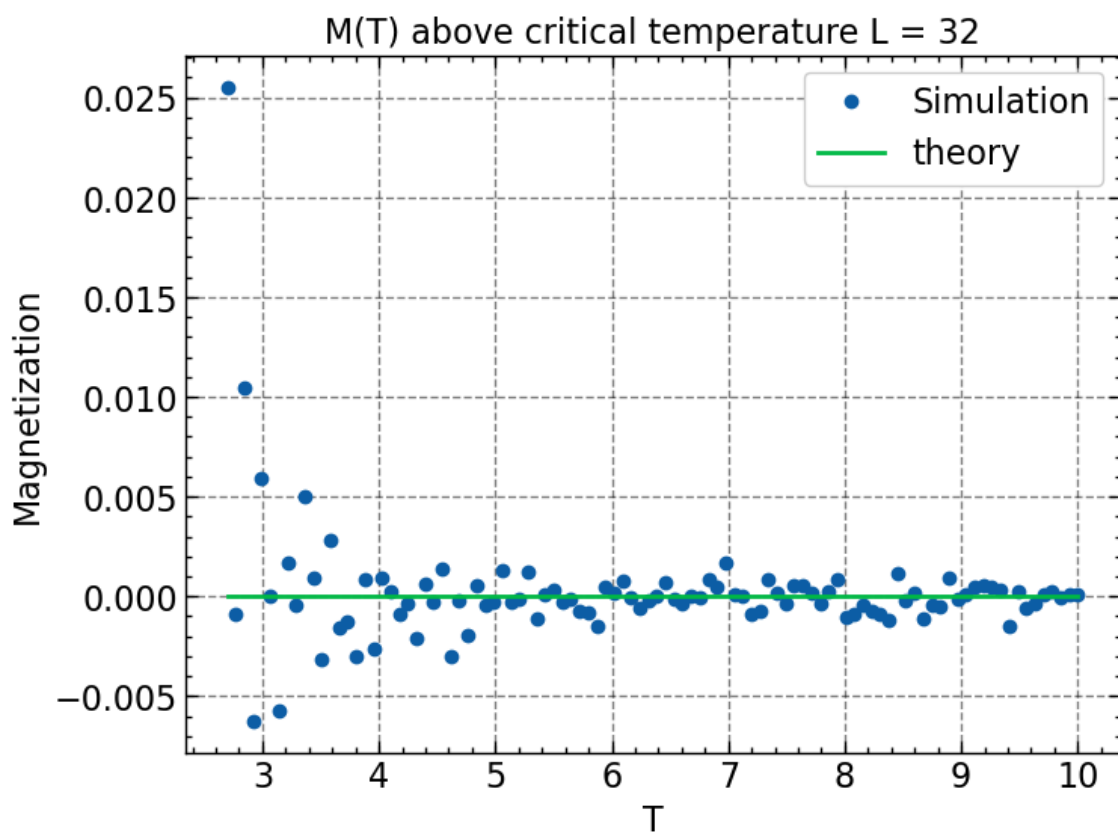


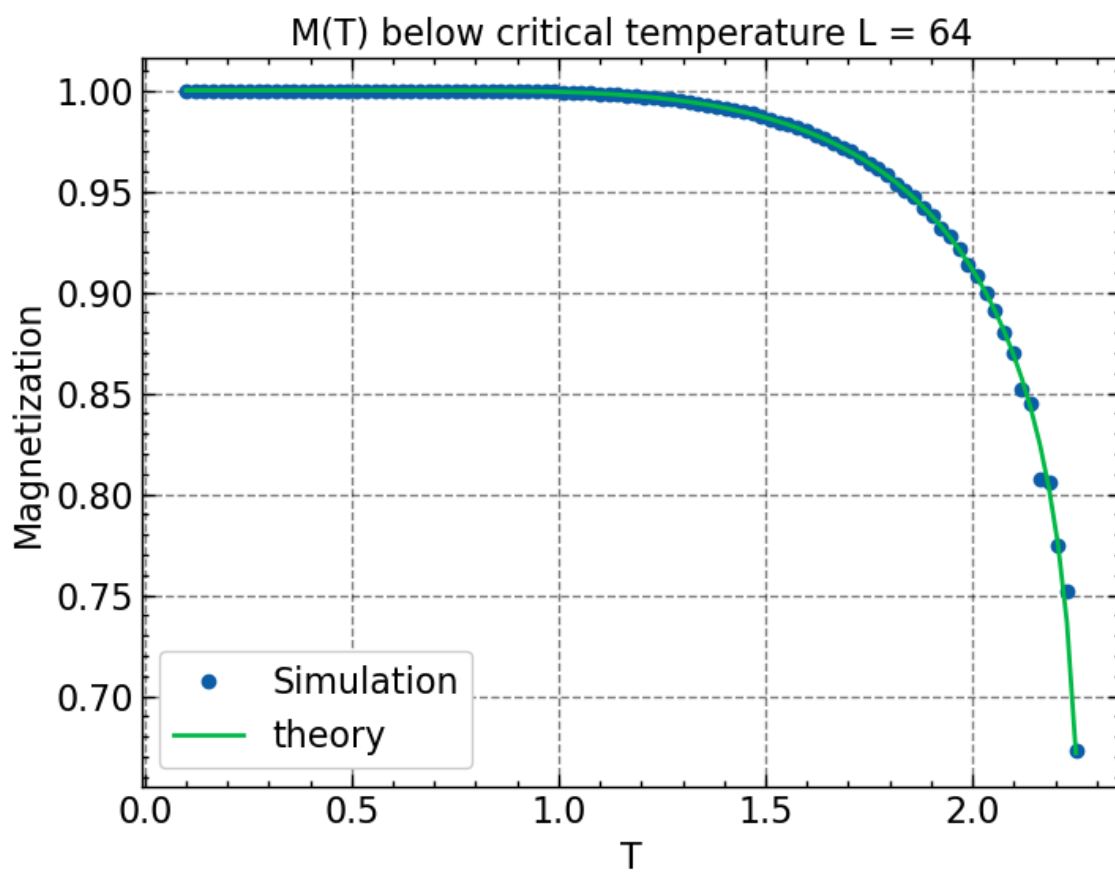


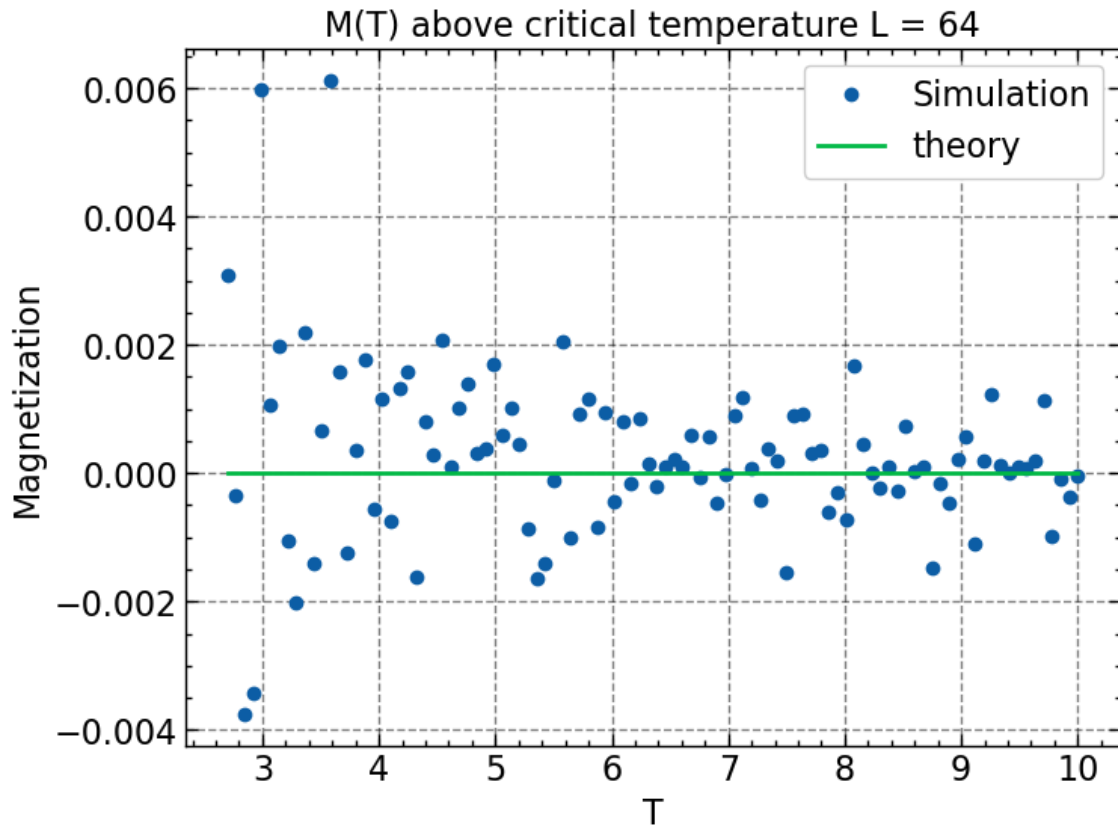








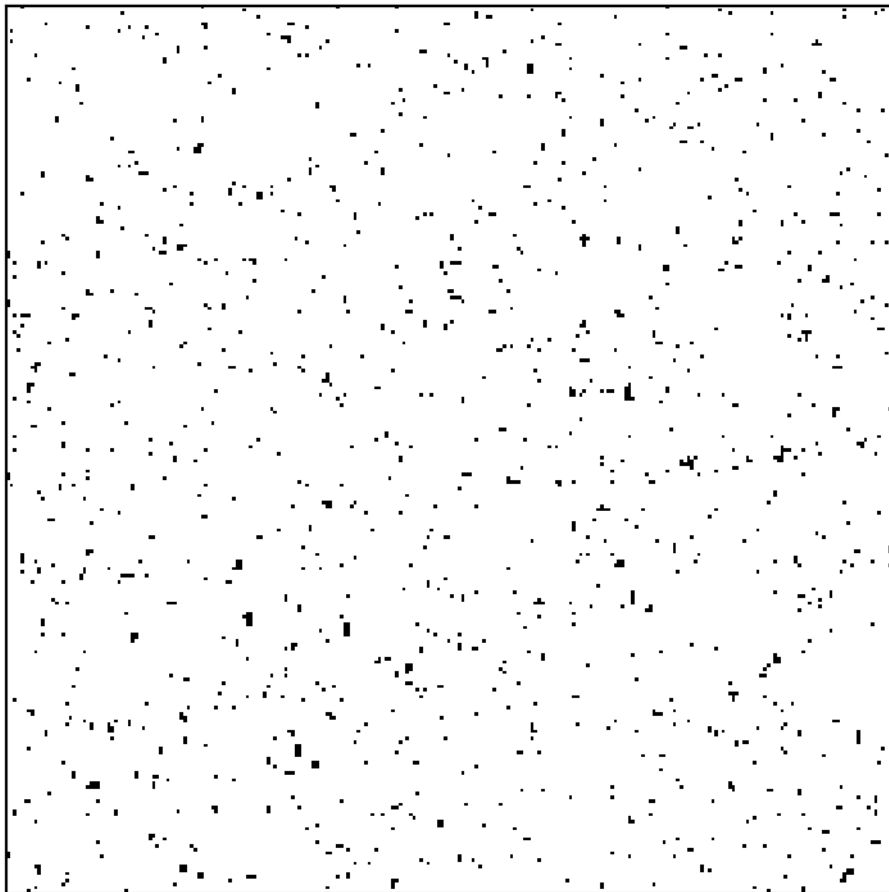




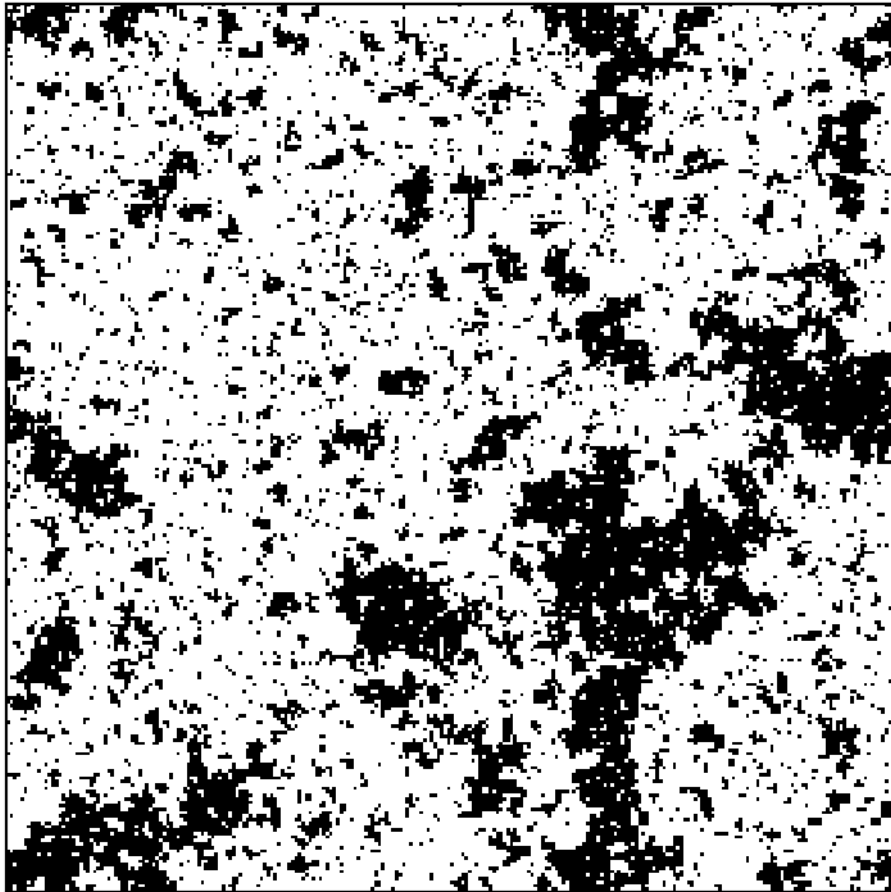
0.0.4 Typical spin configuration at different temperatures

```
[ ]: plot_configuration(temp_arr=[1.8, 2.3, 4.0])
```

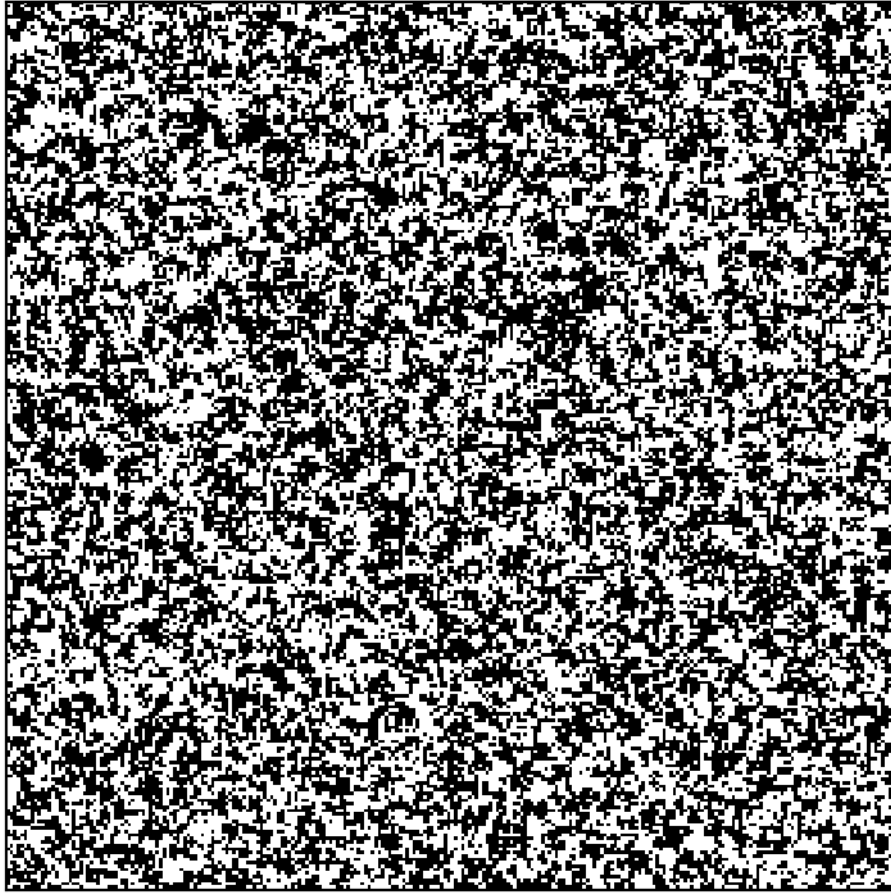
Spin configuration for $T = 1.8$



Spin configuration for $T = 2.3$



Spin configuration for $T = 4.0$



- Comment on how the patterns differ at different temperatures and what they might physically tell us about how the system behaves at temperatures below, near, and above the critical temperature.

At 1.8K, we are seeing mostly -1 spins for the lattice site. At 2.3K, we are still observing more -1 spin than +1 spin, but we are seeing some lumps of +1 spin. At 4.0K, it's mostly random and there's no real pattern to be observed.