Noah Arthurs CS 109 Section #4 July 25, 2019

Section 4: Code Analysis

Congratulations on making it through the midterm!:)

1. **Binary Tree**: Consider the following function for constructing binary trees:

```
struct Node {
    Node *left;
    Node *right;
};

Node *randomTree(float p) {
    if (randomBool(p)) { // returns true with probability p
        Node *newNode = new Node;
        newNode->left = randomTree(p);
        newNode->right = randomTree(p);
        return newNode;
    } else {
        return nullptr;
    }
}
```

The if branch is taken with probability p (and the else branch with probability 1 - p). A tree with no nodes is represented by nullptr; so a tree node with no left child has nullptr for the left field (and the same for the right child).

Let *X* be the number of nodes in a tree returned by randomTree. You can assume 0 . What is <math>E[X], in terms of p?

- 2. **Girl Scout Cookies** Three girl scouts are out selling cookies. The number of boxes of cookies each girl sells in a day in the neighborhood is randomly distributed with mean μ and standard deviation σ .
 - a. Noa and Chaya are sisters, but each out selling cookies on their own today. What are the parameters for the distribution of the total number of boxes sold by families that have two daughters both out selling cookies? Assume they are in different neighborhoods and their sales results are independent.
 - b. Maria's grandmother has told her that for every box Maria sells today, her grandmother will also buy a box to donate to the food bank. What are the parameters for the distribution of the total number of boxes Maria will sell?

3. Timing Attack:

In this problem we are going to show you how to crack a password in linear time, by measuring how long the password check takes to execute (see code below). Assume that our server takes T ms to execute any line in the code where $T \sim N(\mu = 5, \sigma^2 = 0.5)$ seconds. The amount of time taken to execute a line is always independent of other values of T.

On our site all passwords are length 5 through 10 (inclusive) and are composed of lower case letters only. A hacker is trying to crack the root password which is "gobayes" by carefully measuring how long we take to tell them that her guesses are incorrect.

- a. What is the distribution of time that it takes our server to execute k lines of code? Recall that each line independently takes $T \sim N(\mu = 5, \sigma^2 = 0.5)$ ms.
- b. First the hacker needs to find out the length of the password. What is the probability that the time taken to test a guess of correct length (server executes 6 lines) is longer than the time taken to test a guess of an incorrect length (server executes 4 lines)? Assume that the first letter of the guess does not match the first letter of the password. Hint: P(A > B) is the same as P(A B > 0).
- c. Now that our hacker knows the length of the password, to get the actual string she is going to try and figure out each letter one at a time, starting with the first letter. The hacker tries the string "aaaaaaa" and it takes 27s. Based on this timing, how much more probable is it that first character did not match (server executes 6 lines) than the first character did match (server executes 8 lines)? Assume that all letters in the alphabet are equally likely to be the first letter.
- d. If it takes the hacker 6 guesses to find the length of the password, and 26 guesses per letter to crack the password string, how many attempts does she need to crack our password, "gobayes"? Yikes!