Data Abstraction	Announcements
Data Abstraction	Data Abstraction -Compound values combine other values together -A date: a year, a month, and a day -A geographic position: latitude and longitude -Data abstraction lets us manipulate compound values as units -Isolate two parts of any program that uses data: -How data are represented (as parts) -How data are manipulated (as units) -Data abstraction: A methodology by which functions enforce an abstraction barrier between representation and use

Rational Numbers

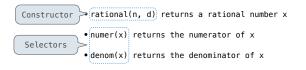
numerator

Exact representation of fractions

A pair of integers

As soon as division occurs, the exact representation may be lost! (Demo)

Assume we can compose and decompose rational numbers:



Rational Number Arithmetic

$$\frac{3}{2} * \frac{3}{5} = \frac{9}{10}$$

Example

General Form

Rational Number Arithmetic Implementation

• rational(n, d) returns a rational number x

 \bullet numer(x) returns the numerator of x

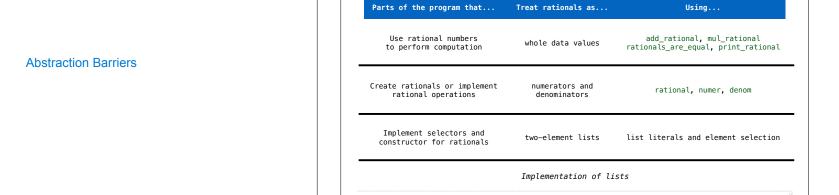
• denom(x) returns the denominator of x

These functions implement an abstract representation for rational numbers

Representing Rational Numbers

```
Representing Rational Numbers
    def rational(n, d): """Construct a rational number that represents N/D.""" return ([n, \ d])
           Construct a list
    def numer(x):
         """Return the numerator of rational number X."""
         return x[0]
   def denom(x):
    """Return the denominator of rational number X."""
        return x[1]
        Select item from a list
                                                 (Demo)
```

Reducing to Lowest Terms Example: 1/25 15 1/3 5 25 6 1/3 50 1/25 from math import gcd Greatest common divisor def rational(n, d): """Construct a rational that represents n/d in lowest terms.""" g = gcd(n, d) return [n//g, d//g] (Demo)



Abstraction Barriers

```
Violating Abstraction Barriers

Does not use constructors

add_rational( [1, 2], [1, 4] )

def divide_rational(x, y):
    return [x[0] * y[1], x[1] * y[0]]

No selectors!

And no constructor!
```

```
Data Representations
```

What are Data?

- *We need to guarantee that constructor and selector functions work together to specify the right behavior
- *Behavior condition: If we construct rational number x from numerator n and denominator d, then numer(x)/denom(x) must equal n/d
- •Data abstraction uses selectors and constructors to define behavior
- If behavior conditions are met, then the representation is valid

You can recognize an abstract data representation by its behavior

(Demo)

