

$1.2 + 0.4 + 0.4 + 0.3$
NATIONAL TSING HUA UNIVERSITY
DEPARTMENT OF COMPUTER SCIENCE
CS 4100: Computer Architecture
Spring 2023, Mid-term Examination

1. (22%) Consider a specific computer called HAL running a program of 10 million instructions at a clock rate of 400 MHz. Among the instructions, 20% of them are INT instructions, 40% are FP instructions, 20% are load/store instructions, and the rest are branch instructions. Suppose that an INT instruction takes 1 cycle; an FP instruction takes 10 cycles; a load/store instruction takes 2 cycles; a branch instruction takes 3 cycles to execute.

- (a) (5%) What is the average CPI of this program running on HAL?
- (b) (7%) From (a), the architect wants to reduce the total time by improving the cycles of an FP instruction. Let n be the largest possible number of cycles for an FP instruction to reduce the total time by at least 50%, and n is an integer. What will n be?
- (c) (10%) From (a), to increase the cycle rate of HAL to 800 MHz, each branch instruction becomes 5 cycles. And 50% of the FP instructions must be executed in 14 cycles, whereas the rest remains the same. What is the overall speedup (i.e., the ratio of the enhanced performance over the original performance) after the enhancement?

2. (8%) The architect is evaluating two alternative processor implementations, P1 and P2, by using a benchmark set of two benchmark programs, B1 and B2. P1 operates at the clock rate of 800 MHz; P2 operates at 1.2 GHz. The execution cycles of the two benchmarks are summarized as follows:

Benchmark	Execution Cycles on P1	Execution Cycles on P2
B1	5M	12M
B2	10M	6M

- (a) (6%) What is the performance ratio of P1:P2, considering both benchmarks using geometric mean?
- (b) (2%) From (a), which processor implementation is faster? You must give the reason.

3. (25%) Modern computers are designed based on the stored-program concept, based on which programs are stored in and executed from the main memory, where data are also stored. One consequence is that program instructions and data may be manipulated in the same way. A good example to illustrate the idea is self-modifying code, which alters its own instructions while it is executing. Although most computers do not allow you to do it for robustness reasons, we assume here that you can do it, and the effect shows immediately. Consider the C statement shown below left. Assume that a and b have been loaded into registers $x28$ and $x29$, respectively. One possible implementation of the C statement with self-modifying code is shown below right. Note that the instruction encodings of add and sub in RISC-V differ by only one bit:

add 0000000 rs2 rs1 000 rd 0110011

sub 0100000 rs2 rs1 000 rd 0110011

```

if a < b
    a = a - b;
else
    a = a + b;
    
```

slt	x6, x28, x29	$x6 \leftarrow 1$ if $a < b$ else $x6 \leftarrow 0$
slli	x6, x6, 30	
auipc	x7, 0	
lw	x30, 16(x7)	
or	x30, x30, x6	
sw	x30, 16(x7)	

1. HAL: 10^7 instructions, clock rate: 400 MHz

20% INT, 40% FP, 20% load/store, 20% branch
1 cyc 10 cyc 2 cyc 3 cyc

(a) Average CPI = $0.2 \times 1 + 0.4 \times 10 + 0.2 \times 2 + 0.2 \times 3 = 5.2$

(b) Improve FP. n is at least $\downarrow 50\%$ time of max cycle

$$\frac{5.2}{2} = 2.6, \quad 5.2 - 4 = 1.2, \quad 2.6 - 1.2 = 1.4, \quad 0.4 \times n \leq 1.4$$

$$n = 3 \neq$$

(c) rate $\rightarrow 800$ MHz, branch $\rightarrow 5$ cyc, FP $\rightarrow \begin{cases} -\frac{1}{2} 14 \text{ cyc} \\ -\frac{1}{2} 10 \text{ cyc} \end{cases}$

$$\text{Avg CPI} = 0.2 \times 1 + 0.2 \times 10 + 0.2 \times 14 + 0.2 \times 2 + 0.2 \times 5 = 6.4$$

$$\text{Speedup} = \frac{5.2}{6.4 \div 2} = \frac{5.2}{3.2} = \frac{13}{8}$$

2. (a) $P1:P2 = \sqrt{\frac{12}{1.2} \times \frac{6}{1.2}} : \sqrt{\frac{5}{0.8} \times \frac{10}{0.8}} = 25\sqrt{2} : \frac{25\sqrt{2}}{4} = 4:5$

(b) P2 is faster.

3. (a)(i) load 31~12 bit to $x7$, sign extend 63~32 bit, 11~0 bit = 0, add PC

$$x7 = PC$$

(ii) add $x28, x28, x29$: $\underbrace{00000000}_7 \underbrace{-11101}_5 \underbrace{-11100000}_5 \underbrace{-11100}_3 \underbrace{-0110011}_7$

(iii) if $a < b$, $x30[30] \leftarrow \text{sub}$ of a remain, if $a \geq b$, $x30$ remains its value. $\rightarrow \text{add}$

(iv) $\underbrace{00000000}_7 \underbrace{-11101}_5 \underbrace{-11100000}_5 \underbrace{-11100}_3 \underbrace{-0110011}_7$

[000 0004]

add x28, x28, x29

(a) (8%) Explain how the above RISC-V code implements the C statement:

(i) What is loaded into **x7** after executing **auipc**?

(ii) Where is **16 (x7)** pointing to? What is loaded into **x30** after executing **lw**?

(iii) What is the effect of executing **or**, considering **a < b** and **a ≥ b**?

31 ~ 12

(iv) What instruction will be executed when the execution comes to **add**?

(b) (5%) Replace **auipc** with **lui** in the above RISC-V code, assuming that **add** is stored at memory location 0x0000 0000 1000 0004. This is an implementation that uses absolute addressing instead of PC-relative. Show all the instructions that are modified and your calculations of the addresses. You should not add other instructions.

(c) (7%) Note that the above RISC-V code does not use branch instructions, although the C statement is an if-then-else statement. Now, implement the C statement in RISC-V, particularly using the **blt** instruction to check the **a < b** condition. Show all the instructions. You may use labels, such as **EXIT**, to indicate locations of instructions.

(d) (5%) Give the encoding of the **blt** instruction according to your RISC-V code in (c).

blt imm[12|10:5] rs2 rs1 100 imm[4:1|11] 1100011

4. (10%) Translate the following C code into RISC-V assembly code. You can only use RV64I instructions and cannot use pseudoinstructions. Note that according to RISC-V spec, "In the standard RISC-V calling convention, the stack grows downward and the stack pointer is always kept 16-byte aligned." Also, the return address is stored in **x1** and the stack pointer is in **x2**.

long long int findGCD(long long int a, long long int b)

```
{
    if (a==b)
        return a;
    if (a>b)
        return findGCD(a-b,b);
    else
        return findGCD(a,b-a);
}
```

less than

X10

X11

X10 8

0100

X11 16

X1 24

5. (10%) In class we have described a 64-bit ALU, which has two 64-bit data inputs $A = a_{63}a_{62} \dots a_0$, $B = b_{63}b_{62} \dots b_0$, and one 4-bit control input ALUop (composed of 1-bit Ainvert, 1-bit Bnegate, and 2-bit Operation from left to right). Now if you want to remove the slt (set-less-than) operation and change the specification of the ALU as follows, what will the new ALU look like for bit 0?

Operation	ALUop
A + B	1101
A - B	1001
A and B	1110
A or B	1100
A nor B	0010

12

112

You can modify the following 1-bit ALU to show your answer.

01100

4321

0110

(b) `auipc ... → lui x7, 0x0FFFF`

(c) `b/t x28, x29, Sub`

`add x28, x28, x29`

`jal Exit`

`Sub: sub x28, x28, x29`

`Exit:`

(d) `rs1: 11100, rs2: 11101`

`imm = 0 0000 0000 1100`

`imm[12,10:5] = 0 00000`

`imm[4:1,11] = 0110 0`

4. func: addi x2, -16

sd x1, 8(x2)

bne x10, x11, a<b

addi x2, 16

jalr x0, 0(x1)

a<b: bge x10, x11, a>b

sub x10, x10, x11

jal x1, func

ld x1, 8(x2)

addi x2, 16

jalr x0, 0(x1)

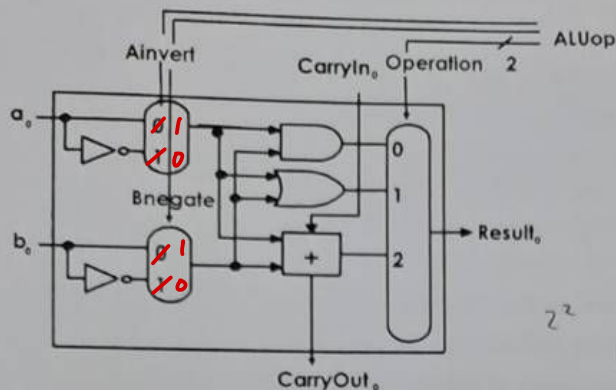
a>b: sub x11, x11, x10

jal x1, func

ld x1, 8(x2)

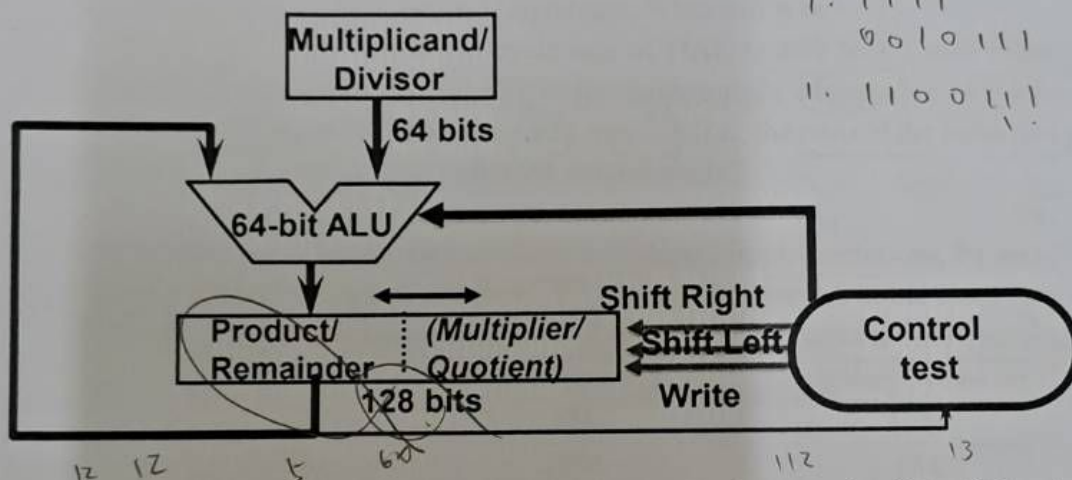
addi x2, 16

jalr x0, 0(x1)



Handwritten notes for problem 6:
 2^{24}
 100
 $24 \div 12 = 2$
 $24 \div 12 = 2$

6. (10%) The following hardware has been introduced in class for performing 64-bit unsigned integer multiplication and division.



Handwritten binary numbers for problem 6:
 1.1111
 0010111
 1.1100111

Let $M=1100$ and $N=0101$ be 4-bit unsigned integers. Perform each of the following operations using a 4-bit version of the hardware, respectively:

- $M \times N$
- $M \div N$

Handwritten binary numbers for problem 6:
 1000
 0011
 0111
 1101
 $1 + 12 + 112$

For each operation, you only need to show (1) the initial values of Multiplicand/Divisor register and Product/Remainder register, and (2) the updated value of Product/Remainder register at the end of each iteration. Besides, you also need to show the final value of Product/Remainder register for (ii).

7. (15%) Consider the IEEE 754 floating-point standard and its arithmetic operations.

- (3%) Does $0x7F839C5A$ represent a single precision normalized number? Why?
- (3%) Suppose the largest single precision denormalized number represents the decimal number $(A - 2^{-23}) \times 2^{-126}$. What is A ?
- (6%) Consider the following two single precision floating-point numbers:

$B = 0011\ 1111\ 0011\ 1000\ 0000\ 0000\ 0000\ 0000$

$C = 1100\ 0000\ 1111\ 1000\ 0000\ 0000\ 0000\ 0000$

Show all the work to perform $B + C$, and write the result in the single precision format.

- (3%) Let the decimal number, $(2^{24} - 1) \times 2^D$, denote the largest even integer that can be exactly represented by the single precision format. What is D ?

Handwritten binary numbers for problem 7:
 1.110001
 0010111
 1111101

Handwritten calculations for problem 7:
 $4/5$
 $16/32$
 24
 126

Handwritten binary numbers for problem 7:
 1.1111
 0112
 0010111
 110001
 1.1111
 0010111
 1.110001

6. $M = 1100$, $N = 0101$ unsigned

(i) $M \times N$

	iter.	Product	Mcand
init	0.	0000 0101	1100
	1.	0110 0010	1100
	2.	0011 0001	1100
	3.	0111 1000	1100
	4.	0011 1100	1100
$M \times N = 00111100_2 = 60_{10}$			

(ii) $M \div N$

	iter.	Rem	Divisor
init	0.	0000 1100	0101
	1.	0011 0000	0101
	2.	0110 0000	0101
	3.	0010 0001	0101
	4.	0100 0010	0101
	5.	<u>0010</u> <u>0010</u>	0101

$$M \div N = 0010_2 = 2_{10} \dots 2_{10}$$

7. (a) $0x7F839C5A \approx 0_1111\ 0000_011\ \dots$

normalized \therefore exponent = $1111\ 0000 \neq 0000\ 0000$

(b) $(2^{23}-1) \times 2^{-23} \times 10^{-126} = (1-2^{-23}) \times 10^{-126}, A=1$

(c) $B = 0\ 011\ 1111\ 0\ 011\ 1000\ 0000\ 0000\ 0000\ 0000$

$C = 1\ 100\ 0000\ 1\ 111\ 1000\ 0000\ 0000\ 0000\ 0000$

ExpB \Rightarrow $\overset{+3}{1\ 00\ 0000\ 1}$

$0.001\ 0111\ 0000\ \dots$

$-1.111\ 1000\ 0000\ \dots$

$-1.110\ 0001\ 0000\ \dots$

Exp $\Rightarrow 100\ 0000\ 1$, frac $\Rightarrow 110\ 0001\ 0000\ 0000\ 0000\ 0000$

sign bit $\Rightarrow 1$

$\Rightarrow B+C = 1100\ 0000\ 1110\ 0001\ 0000\ 0000\ 0000\ 0000_2$

(d) $(2^{24}-1) \times 2^{-23} \times 2^{127} = (2^{24}-1) \times 2^{104}, D=104$

$\overset{(2^8)}{1\ 111\ 1111\ \dots}$

$1111\ 1111 \rightarrow \text{keep}$

$1111\ 1110 = 254$

$254 - 127 = 127$