PHYSICAL ATTACKS (V1.2)

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Agenda

Mathematical knowledge

Circuit knowledge

Cryptography knowledge

Attack methods

Case analysis

MATHEMATICAL KNOWLEDGE

Definition

A vector is *a list of numbers*. There are at least two ways to interpret what this list of numbers mean: One way to think of the vector as being appoint in a space. Then this list of numbers is a way of identifying that point in space, where each number represents the vector's component that dimension. Another way to think of a vector is magnitude and direction, e.g. a quantity like velocity.

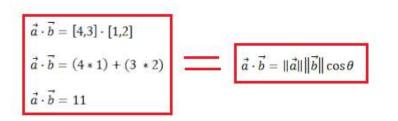
Vector addition and subtraction

Numerically, we add vectors component-by-component. That is to say, we add the x components together, and then separately we add the y components together.

$$\vec{c} = \vec{a} + \vec{b}$$
 $\vec{c} = [4,3] + [1,2]$ $\vec{c} = [4+1,3+2]$ $\vec{c} = [5,5]$ $\vec{c} = [3,1]$

Vector multiplication: dot product

A dot product(or scalar product) is the numerical product of the lengths of the two vectors, multiplied by the cosine of angle between them.



Vector multiplication: cross product

A cross product of two vectors **a** and **b** is defined only in three-dimensional space and is denoted by **a x b**. The cross product is defined by the formula:

$$\mathbf{a} \times \mathbf{b} = \|\mathbf{a}\| \|\mathbf{b}\| \sin(\theta) \mathbf{n}$$

Where θ is the angle between a and b in the plane containing them. $\|a\|$ and $\|b\|$ are the magnitudes of vector \mathbf{a} and \mathbf{b} , and \mathbf{n} is a unit vector perpendicular to the plane containing a and b in the direction given by the right-hand rule.

$$\mathbf{a} \times \mathbf{b} = -a_{1}b_{1}\mathbf{0} + a_{1}b_{2}\mathbf{k} - a_{1}b_{3}\mathbf{j}
- a_{2}b_{1}\mathbf{k} - a_{2}b_{2}\mathbf{0} + a_{2}b_{3}\mathbf{i}
+ a_{3}b_{1}\mathbf{j} - a_{3}b_{2}\mathbf{i} - a_{3}b_{3}\mathbf{0}
= (a_{2}b_{3} - a_{3}b_{2})\mathbf{i} + (a_{3}b_{1} - a_{1}b_{3})\mathbf{j} + (a_{1}b_{2} - a_{2}b_{1})\mathbf{k}$$

$$= (a_{2}b_{3} + a_{3}b_{1}\mathbf{j} + a_{1}b_{2}\mathbf{k}) - (a_{3}b_{2}\mathbf{i} + a_{1}b_{3}\mathbf{j} + a_{2}b_{1}\mathbf{k})
= (a_{2}b_{3} - a_{3}b_{2})\mathbf{i} + (a_{3}b_{1} - a_{1}b_{3})\mathbf{j} + (a_{1}b_{2} - a_{2}b_{1})\mathbf{k}.$$

Determinant

Definition

A **square array** of numbers bordered on the left and right by a vertical line and having a value equal to the algebraic sum of all possible products where the number of factors in each product is the same as the number of rows or columns, each factor in a given product is taken from a different row and column, and sign of a product is positive or negative depending upon whether the number of permutations necessary to place the indices representing each factor's position in its row or column in the order of the natural numbers is odd or even.

Determinant

How to get the result of determinant.

$$|A| = det(A) = \left|egin{array}{c} a & b \ c & d \end{array}
ight| = ad - bc$$

$$|B|=det(B)=\left|egin{array}{ccc} a&b&c\d&e&f\g&h&k \end{array}
ight|=a\left|egin{array}{ccc} e&f\h&k \end{array}
ight|-b\left|egin{array}{ccc} d&f\g&k \end{array}
ight|+c\left|egin{array}{ccc} d&e\g&h \end{array}
ight|$$

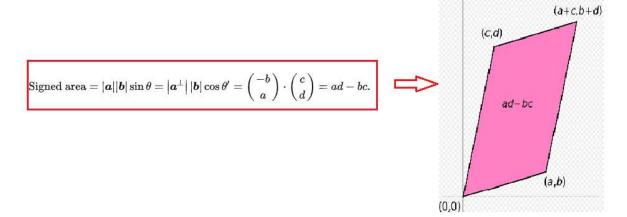


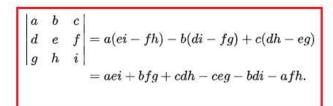
$$|A| = a_{11} (-1)^{1+1} \begin{vmatrix} a_{22} & a_{23} \\ a_{32} & a_{33} \end{vmatrix} + a_{21} (-1)^{2+1} \begin{vmatrix} a_{12} & a_{13} \\ a_{32} & a_{33} \end{vmatrix} + a_{31} (-1)^{3+1} \begin{vmatrix} a_{12} & a_{13} \\ a_{22} & a_{23} \end{vmatrix}$$

$$= a_{11} (a_{22} a_{33} - a_{23} a_{32}) - a_{21} (a_{12} a_{33} - a_{13} a_{32}) + a_{31} (a_{12} a_{23} - a_{13} a_{22})$$

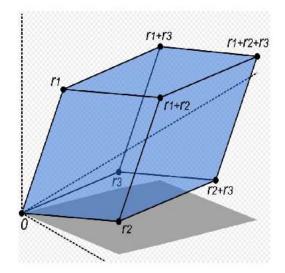
Determinant

• Geometric meaning.









Definition

In mathematics, a matrix is a rectangular array of numbers, symbols, or expressions, arranged in rows and columns. The numbers, symbols, or expressions in the matrix are called its entries or its elements. Matrix is commonly written in box brackets or parentheses.

Symmetric		Diagonal			Upper Triangular			Lower Triangular			Zero				Identity							
1	2	3]	T	1	0	0	[:	l	2	3]		1	0	٥٦	ſ	0	0	0]		1	0	0]
2	0	-5		0	4	0)	7	-5		-4	7	0		0	0	0		0	1	0
3	-5	6	l	0	0	6)	0	-4]		12	5	3]	L	0	0	0]	L	0	0	1

$$A = \begin{pmatrix} a_{11} & a_{12} & \dots & a_{1n} \\ a_{21} & a_{22} & \dots & a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{m1} & a_{m1} & \dots & a_{mn} \end{pmatrix}$$

Matrix addition

Two matrices **A** and **B** can be added or subtracted if and only if their dimensions are the same(both matrices have the equal numbers of rows and columns). The sum of two matrices **A** and **B** will be a matrix which has the same number of rows and columns as do **A** and **B**.

$$\mathbf{A} + \mathbf{B} = \begin{bmatrix} a_{11} & a_{12} & \cdots & a_{1n} \\ a_{21} & a_{22} & \cdots & a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{m1} & a_{m2} & \cdots & a_{mn} \end{bmatrix} + \begin{bmatrix} b_{11} & b_{12} & \cdots & b_{1n} \\ b_{21} & b_{22} & \cdots & b_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ b_{m1} & b_{m2} & \cdots & b_{mn} \end{bmatrix}$$

$$= \begin{bmatrix} a_{11} + b_{11} & a_{12} + b_{12} & \cdots & a_{1n} + b_{1n} \\ a_{21} + b_{21} & a_{22} + b_{22} & \cdots & a_{2n} + b_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{m1} + b_{m1} & a_{m2} + b_{m2} & \cdots & a_{mn} + b_{mn} \end{bmatrix}$$

Matrix multiplication

In mathematics, matrix multiplication or matrix product is a binary operation that produces a matrix from two matrices with entries in a filed, or, more generally, in a ring or even a semiring.

If **A** is an $m \times n$ matrix and **B** is an n x p matrix, the matrix product **C** = **AB** is defined to be the $m \times p$ matrix.

$$\mathbf{A} = \begin{pmatrix} a_{11} & a_{12} & \cdots & a_{1n} \\ a_{21} & a_{22} & \cdots & a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{m1} & a_{m2} & \cdots & a_{mn} \end{pmatrix}, \quad \mathbf{B} = \begin{pmatrix} b_{11} & b_{12} & \cdots & b_{1p} \\ b_{21} & b_{22} & \cdots & b_{2p} \\ \vdots & \vdots & \ddots & \vdots \\ b_{n1} & b_{n2} & \cdots & b_{np} \end{pmatrix} \qquad \qquad \qquad \qquad \qquad \mathbf{C} = \begin{pmatrix} c_{11} & c_{12} & \cdots & c_{1p} \\ c_{21} & c_{22} & \cdots & c_{2p} \\ \vdots & \vdots & \ddots & \vdots \\ c_{m1} & c_{m2} & \cdots & c_{mp} \end{pmatrix}$$

$$c_{ij}=a_{i1}b_{1j}+\cdots+a_{in}b_{nj}=\sum_{k=1}^n a_{ik}b_{kj},$$

$$\begin{pmatrix} a & b & c \\ d & e & f \\ g & h & i \end{pmatrix} \begin{pmatrix} j & k & l \\ m & n & o \\ p & q & r \end{pmatrix} = \begin{pmatrix} (aj+bm+cp) & (ak+bn+cq) & (al+bo+cr) \\ (dj+em+fp) & (dk+en+fq) & (dl+eo+fr) \\ (gj+hm+ip) & (gk+hn+iq) & (gl+ho+ir) \end{pmatrix}$$

Matrix transposition

In linear algebra, the transpose of a matrix is an operator which flips a matrix over its diagonal, that is switches the row and column indices of the matrix by producing another matrix denoted.

Some properties of transpose:

$$(\mathbf{A}^{\mathrm{T}})^{\mathrm{T}} = \mathbf{A}.$$

$$(\mathbf{A} + \mathbf{B})^{\mathrm{T}} = \mathbf{A}^{\mathrm{T}} + \mathbf{B}^{\mathrm{T}}.$$

$$(\mathbf{A}\mathbf{B})^{\mathrm{T}} = \mathbf{B}^{\mathrm{T}}\mathbf{A}^{\mathrm{T}}.$$

$$(c\mathbf{A})^{\mathrm{T}} = c\mathbf{A}^{\mathrm{T}}.$$

$$\det (\mathbf{A}^{\mathrm{T}}) = \det(\mathbf{A}).$$

$$\mathbf{A} = \begin{bmatrix} 5 & 2 & 3 \\ 4 & 7 & 1 \\ 8 & 5 & 9 \end{bmatrix} \quad \mathbf{A}^{\mathrm{T}} = \begin{bmatrix} 5 & 4 & 8 \\ 2 & 7 & 5 \\ 3 & 1 & 9 \end{bmatrix}$$

$$[\mathbf{a} \cdot \mathbf{b}] = \mathbf{a}^{\mathrm{T}}\mathbf{b},$$

The dot product of two column vectors a and b can be computed as the single entry of the matrix product.

$$\left(\mathbf{A}^{\mathrm{T}}\right)^{-1} = \left(\mathbf{A}^{-1}\right)^{\mathrm{T}}.$$

• Invertible matrix

In linear algebra, an n-by-n square matrix A is called invertible if there exists an n-by-n square matrix B such that $AB = BA = I_n$, where I_n denotes the n-by-n identity matrix and the multiplication used is ordinary matrix multiplication.

If A is an n x n invertible matrix , then $A^{-1} = \frac{1}{\det(A)} \operatorname{adj}(A)$.

Where adj(A) is the transpose of the cofactor matrix **C** of **A**.

Mean(expected value)

Definition

In probability theory, the expected value of a random variable is a key aspect of its probability distribution. Intuitively, a random variable's expected value represents the average of a large number of independent realizations of the random variable. It is often represented μ, \overline{X} .

Let X be a random variable with a finite number of finite outcomes x1, x2, \cdots xk occurring with probabilities p1, p2, \cdots pk. The expectation of X is defined as :

$$\mathrm{E}[X] = \sum_{i=1}^k x_i \, p_i = x_1 p_1 + x_2 p_2 + \dots + x_k p_k.$$

Where all probabilities pi add up to 1 (p1 + p2 + \cdots + pk = 1).

If all outcomes xi are equiprobable, then the expected value is average(arithmetic mean):

$$A=rac{1}{n}\sum_{i=1}^n a_i=rac{a_1+a_2+\cdots+a_n}{n}$$

Variance

Definition

In probability theory and statistics, variance is the expectation of the squared deviation of a random variable from its mean. Informally, it measures how far a set of (random) numbers are spread out from their average value. The variance is the square of the standard deviation. It is often represented by σ^2 , s^2 , or Var(X).

The variance of a random variable X is the expected value of the squared deviation from the mean of X, $\mu = E[X]$:

$$\mathrm{Var}(X) = \mathrm{E}\big[(X-\mu)^2\big]$$

Covariance

• In probability theory and statistics, covariance is a measure of the joint variability of two random variables. If the greater values of one variable mainly correspond with the greater values of the other variable, and the same holds for the lesser values, (i.e., the variables tend to show similar behavior), the covariance is positive. In the opposite case, when the greater values of one variable mainly correspond to the lesser values of the other, the covariance is negative. The sign of the covariance shows the tendency in the linear relationship between the variables.

$$\operatorname{cov}(X,Y) = \operatorname{E}\left[(X - \operatorname{E}[X])(Y - \operatorname{E}[Y])\right]$$

$$cov(X,Y) = \frac{1}{n} \sum_{i=1}^{n} (x_i - E(X))(y_i - E(Y))$$

Normal distribution

Definition

Normal distribution, also known as the Gaussian distribution, is a probability and is that is symmetric about the mean, showing that data near the mean are more frequent in occurrence than data far

from the mean.

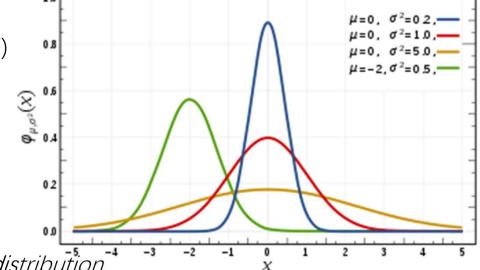
The probability density of the normal distribution is(PDF)

$$f(x\mid \mu,\sigma^2) = rac{1}{\sqrt{2\pi\sigma^2}}e^{-rac{(x-\mu)^2}{2\sigma^2}}$$

Whe.

 μ is the mean or expectation of the distribution σ^2 is the variance

when $\mu = 0$ and $\sigma = 1$, called as standard normal distribution.



Normal distribution

• The normal distribution is often revered to as $N(\mu, \sigma^2)$, Thus when a random variable X is distributed normally with mean μ and variance σ^2 , one may write

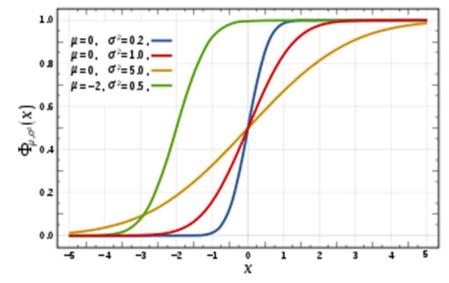
$$X \sim N(\mu, \sigma^2)$$

• The cumulative distribution function(CDF) of a real-valued random variable X, or just distribution function of X, evaluated at x, is the probability that X will take a value less

than or equal to x.

$$F_X(x) = \int_{-\infty}^x f_X(t) \, dt.$$

$$\lim_{x o -\infty} F_X(x) = 0, \quad \lim_{x o +\infty} F_X(x) = 1.$$



Multivariate distribution Statistics

- Multivariate distributions let us model multiple random variables that may or may not be correlated.
- A whole matrix of covariances. E.g three random variables(X,Y,Z).

• A mean for each random variable: $\mu = \begin{bmatrix} Var(\mathbf{X}) & Cov(\mathbf{X}, \mathbf{Y}) & Cov(\mathbf{X}, \mathbf{Z}) \\ Cov(\mathbf{Y}, \mathbf{X}) & Var(\mathbf{Y}) & Cov(\mathbf{Y}, \mathbf{Z}) \\ Cov(\mathbf{Z}, \mathbf{X}) & Cov(\mathbf{Z}, \mathbf{Y}) & Var(\mathbf{Z}) \end{bmatrix}$

• About the PDF, it uses a vector with all of the variables $x = [x, y, z, ...]^T$, The equation for k random variables is

$$f(\mathbf{x}) = \frac{1}{\sqrt{(2\pi)^k |\mathbf{\Sigma}|}} e^{-((\mathbf{x} - \mu)^T \mathbf{\Sigma}^{-1} (\mathbf{x} - \mu)/2}$$

• The SciPy package in Python can do all for this.

Welch's t-test

- In statistics, welch's t-test, or unequal variances t-test, is a two-sample location test which is used to test the hypothesis that two populations have equal means.
- Welch's t-test defines the $t=\frac{\overline{X}_1-\overline{X}_2}{\sqrt{\frac{s_1^2}{N_1}+\frac{s_2^2}{N_2}}}$ following formula:

Where $\overline{X1}$, s_1^2 and N_1 are the 1st sample mean, sample variance and sample size.

Finite field

- In mathematics, a finite field or Galois field is a field that contains a finite number of elements.
- The number of elements of finite field is called its order, or size.
- A finite field of order q exists if and only if the order q is a prime power p^k (where p is a prime number and k is a positive integer).

```
\begin{aligned} &F_2 \text{ or } GF(2) \text{ is } [0,1] \\ &F_{11} \text{ or } GF(11) \text{ is } [0,1,2,3,4,5,6,7,8,9,10,11] \\ &F_{23} \text{ or } GF(23) \text{ is } [0,1,2,3,4,5,6,7,8,9,10,11,12...22] \end{aligned}
```

Chinese remainder theorem

• If the n_i are pairwise coprime, and if $a_1, ..., a_k$ are any integers, then there exists an integer x such that

$$x \equiv a_1 \pmod{n_1}$$

$$\vdots$$

$$x \equiv a_k \pmod{n_k}$$

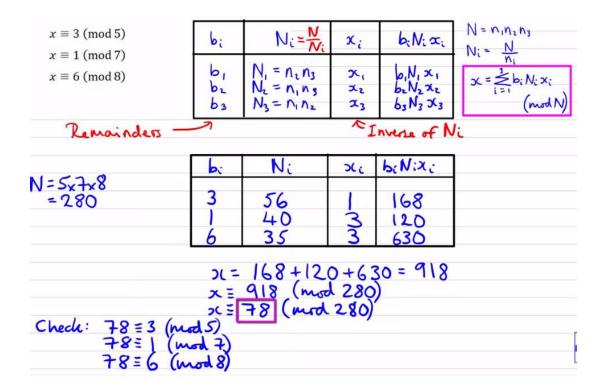
$$x = \left(\sum_{i=1}^k x_i r_i s_i\right) \mod n$$

$$= (x_1 r_1 s_1 + x_2 r_2 s_2 + \dots + x_k r_k s_k) \mod n$$

$$n = n_1 n_2 \dots n_k,$$

$$r_i = \binom{n}{n_i},$$

$$s_i = r_i^{-1} \mod n_i.$$



Note: a and b are coprime if and only if gcd{a, b} = 1.

CIRCUIT KNOWLEDGE

Power Consumption of CMOS Circuits

- Power consumption is divided into two parts: static power consumption P_{stat} and dynamic power consumption P_{dyn} .
- The static power consumption is calculated $P_{stat} = I_{leak} \cdot V_{DD}$.
- The static power consumption of CMOS circuits is typically very low.
- Dynamic power consumption occurs if an internal signal or an output signal of a logic cell switches.
- The dynamic power consumption depends on the data that is processed by the CMOS circuit.

Transition	Power consumption	Type of power consumption	V_{DD} PI	[A] 2 - 0 - 0 - 0	Input a Output q	
0→0	P_{00}	static		0 2	4 6 8 10 1 Time [ns]	12
$0\rightarrow 1$	P_{01}	static + dynamic	a □ • • □ q		()	_
1→0	P_{10}	static + dynamic		150	A .	1
1→1	P_{11}	static	\square N1 \square C _L	¥ 100 -		1
			→ →	(£) 50 -		1
			GND	•	/ L / \	1
25		刘维峰(sa	awver). 86-18001126984. liuweifen	a168@126.com	4 6 8 10 1 Time [ns]	12

Hamming weight

• Hamming weight: the number of non-zero symbols in a symbol sequence. Note: for binary signaling, hamming weight is the number of "1" bits in the binary sequence.

String	Hamming weight
11101	4
11101000	4
00000000	0
789012340567	10

Hamming Distance

- In information theory, the hamming distance between two strings of equal length is the number of positions at which the corresponding symbols are different.
- For binary strings a and b the hamming distance is equal to the number of ones in a XOR b.

$$HD(v0, v1) = HW(v0 XOR v1)$$

- Hamming distance model is very well suited to describe the power consumption of data buses.
- Attackers commonly use the hamming distance model to describe the power consumption of buses and registers.

Noise distributions

Electrical signals are inherently noisy.

$$X = X_{actual} + N$$

• The probability density function(PDF) of Gaussian distribution is

$$f(x) = \frac{1}{\sigma\sqrt{2\pi}}e^{-(x-\mu)^2/2\sigma^2}$$
, where μ is the mean and σ is the standard deviation.

python: stats.norm.pdf(x, μ, σ)

Find probability using the CDF(cumulative distribution function).

```
mu = 5
sigma = 0.5

from scipy import stats
pval = stats.norm.cdf(6.0, mu, sigma)
print("%.2f %%"%(pval*100))

97.72 %
```

SNR

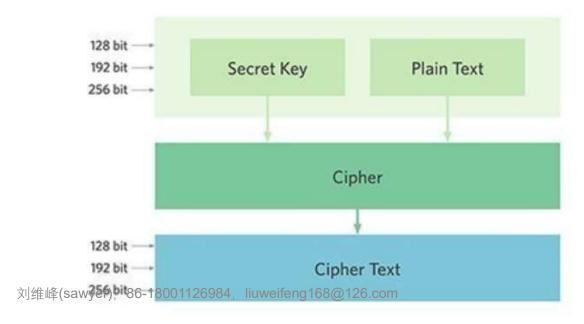
• The "Signal to Noise Radio" is defined as:

$$SNR = \frac{Var(Signal)}{Var(Noise)}$$

when $\mu = 0$.

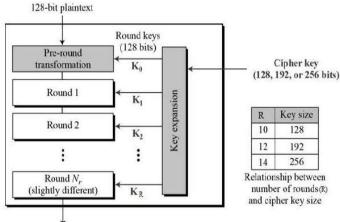
CRYPTOGRAPHY KNOWLEDGE

- The advanced encryption standard, or AES, is a symmetric block cipher chosen by the U.S. government to protect classified information and is implemented in software and hardware throughout the world to encrypt sensitive data.
- AES comprises three block ciphers: AES-128, AES-192 and AES-256. Each cipher encrypts and decrypt data in blocks of 128 bits using cryptographic key of 128-, 192- and 256-bits.



- High-level description of the algorithm, see https://nvlpubs.nist.gov/nistpubs/FIPS/NIST.FIPS.197.pdf
 - 1. key expansion round keys are derived from the cipher key using Rijndael's key schedule.
 - 2. initial round key addition:
 - 1 AddRoundKey each byte of the state is combined with a block of the round key using bitwise xor.
 - 3. 9, 11 or 13 rounds:
 - ① Subbytes—a non-linear substitution step where each byte is replaces with another according to lookup table.
 - 2 ShiftRows— a transposition step where the last three rows of the states are shifted cyclically a certain number of steps.
 - (3) Mixcolumns— a linear mixing operation which operates on the columns of the state, combining the four bytes in each column.

 128-bit plaintext
 - 4 AddRoundKey
 - 4. Final round(making 10, 12 or 14 rounds in total):
 - 1 subBytes
 - 2 shiftRows
 - 3 AddRoundKey

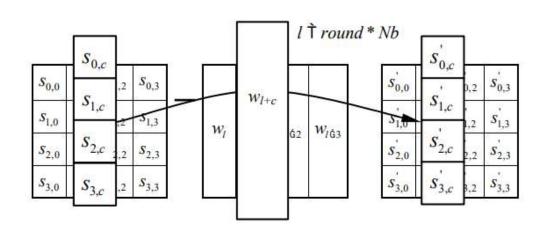


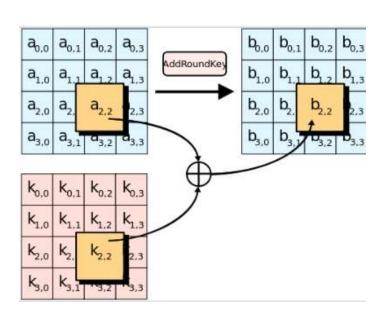
```
AES-128(byte in[16], byte out[16], word w[44])
byte state[4,4];
state = in;
AddRoundKey(state, w[0,3])
for round = 1 step 1 to 9
SubBytes(state)
ShiftRows(state)
MixColumns(state)
AddRoundKey(state, w[round*4,(round+1)*4-1])
end
SubBytes(state)
ShiftRows(state)
AddRoundKey(state, w[40,43])
out = state;
```

 KeyExpansion(key Schedule)

```
KeyExpansion(byte key[4*Nk], word w[Nb*(Nr+1)], Nk)
          begin
                                         w[44]/w[52]/w[60] as output
               word temp
                                         key[16]/key[24]/key[32] as input
               i = 0
               while (i < Nk)
                    w[i] = word(key[4*i], key[4*i+1], key[4*i+2], key[4*i+3])
                    i = i+1
               end while
               i = Nk
               while (i < Nb * (Nr+1)]
                    temp = w[i-1]
                    if (i \mod Nk = 0)
                        temp = SubWord(RotWord(temp)) xor Rcon[i/Nk]
                    else if (Nk > 6 \text{ and i mod } Nk = 4)
                        temp = SubWord(temp)
                    end if
                    w[i] = w[i-Nk] xor temp
                    i = i + 1
               end while
          end
           Note: Nk = 4, or 6, or 8.
                    Nb: Nb words of key data for each round, Nb = 4 for AES.
                    Nr: number of ounds, Nr = 10, 12 or 14
  SubWord(): SubWord(\begin{bmatrix} b_0 & b_1 & b_2 & b_3 \end{bmatrix}) = \begin{bmatrix} S(b_0) & S(b_1) & S(b_2) & S(b_3) \end{bmatrix}
  RotWord(): RotWord(\begin{bmatrix} b_0 & b_1 & b_2 & b_3 \end{bmatrix}) = \begin{bmatrix} b_1 & b_2 & b_3 & b_0 \end{bmatrix}
       Rcon[]: rcon_i = [rc_i \quad 00_{16} \quad 00_{16} \quad 00_{16}]
rc_i = egin{cases} 1 & 	ext{if } i = 1 \ 2 \cdot rc_{i-1} & 	ext{if } i > 1 	ext{ and } rc_{i-1} < 80_{16} \ (2 \cdot rc_{i-1}) \oplus 1B_{16} & 	ext{if } i > 1 	ext{ and } rc_{i-1} \geq 80_{16} \end{cases} egin{cases} i & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 \ rc_i & 01 & 02 & 04 & 08 & 10 & 20 & 40 & 80 & 1B & 36 \ \end{cases}
```

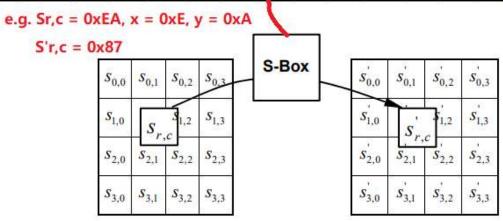
AddRoundKey





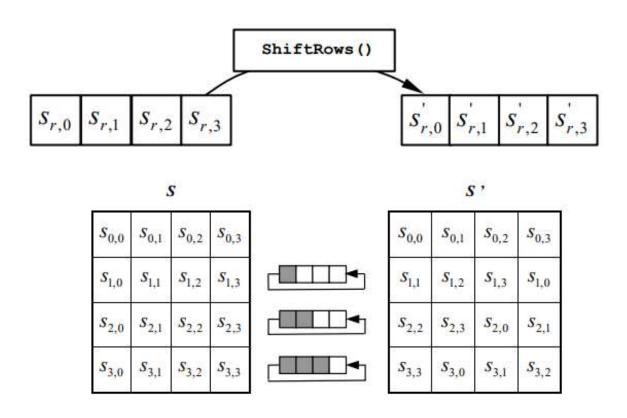
Subbytes

	Ī								7	7							
50		0	1	2	3	4	5	6	7	8	9	a	b	С	d	е	f
	0	63	7c	77	7b	f2	6b	6f	c5	30	01	67	2b	fe	d7	ab	76
	1	ca	82	c9	7d	fa	59	47	f0	ad	d4	a2	af	9c	a4	72	c0
	2	b7	fd	93	26	36	3f	f7	CC	34	a5	e5	f1	71	d8	31	15
	3	04	c7	23	с3	18	96	05	9a	07	12	80	e2	eb	27	b2	75
	4	09	83	2c	1a	1b	6e	5a	a0	52	3b	d6	b3	29	e 3	2f	84
	5	53	d1	00	ed	20	fc	b1	5b	6a	cb	be	39	4a	4c	58	cf
	6	d0	ef	aa	fb	43	4d	33	85	45	f9	02	7f	50	3с	9f	a8
2	7	51	a3	40	8f	92	9d	38	f5	bc	b6	da	21	10	ff	f3	d2
x	8	cd	0c	13	ec	5f	97	44	17	c4	a7	7e	3d	64	5d	19	73
	9	60	81	4f	dc	22	2a	90	88	46	ee	b8	14	de	5e	0b	db
	a	e0	32	3a	0a	49	06	24	5c	c2	d3	ac	62	91	95	e4	79
	b	e7	c8	37	6d	8d	d5	4e	a9	6c	56	f4	ea	65	7a	ae	08
1 0	C	ba	78	25	2e	1c	a6	b4	c6	e8	dd	74	1f	4b	bd	8b	8a
	d	70	3e	b5	66	48	03	f6	0e	61	35	57	b9	86	c1	1d	9e
	е	e1	f8	98	11	69	d9	8e	94	9b	1e	(87)	e9	ce	55	28	df
	f	8c	a1	89	0d	bf	e6	42	68	41	99	2d	0f	ь0	54	bb	16



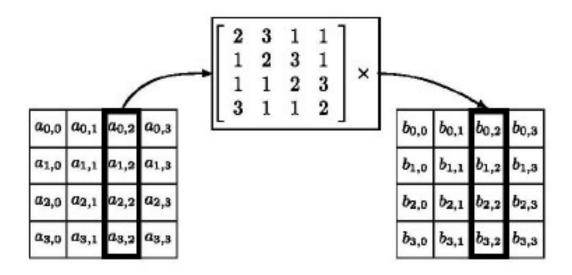
AES

• Shiftrows



AES

Mixcolumns



$$b_{0,0} = 2a_{0,0} + 3a_{1,0} + a_{2,0} + a_{3,0}$$

RSA

- 1. Generate two large random primes, p and q, of approximately equal size such their product n = pq is of the required bit length, e.g. 1024 bits.
- 2. Compute n = pq and $\emptyset = (p 1)(q 1)$
- 3. Choose an integer e, $1 < e < \emptyset$, such gcd(e, \emptyset) = 1. Compute the secret exponent d, $1 < d < \emptyset$, such that $ed \equiv 1 \mod \emptyset$.
- 4. The public key is (n, e) and the private key (d, p, q). Sometimes the private key is written as (n, d)
- n is known as the modulus, bit length of n is 1024, 2048, 3072, 4096.
- e is known as the public exponent or encryption exponent or just the exponent. e = 3,5,17,257,65537.
- d is known as the secret exponent or decryption exponent.

RSA

- Encrypting message
 - The message M is turned into a number m small than n by using an agree-upon reversible protocol known as a <u>padding scheme</u>(such as PKCS).
 - Compute the ciphertext **c**:

$$c = m^e \mod n$$

Decrypting message

```
m = c^d \mod n
```

RSA

Signature

- The massage M is digested with digest algorithm to give an octet string MD.
- Data encoding. MD and digest algorithm identifier are combined into an ASN.1 value, which shall be BER-encoded to give an octet string D.
- The data D is encrypted with RSA private key($s = m^d \mod n$) to give an octet string ED.
- The ED is converted into a bit string S, the signature.

Verification

- Signature S is converted into an octet string ED.
- The ED is decrypted with RSA public key($c = m^e \mod n$) to give an octet string D.
- The D is BER-decoded to give an ASN.1 value type DigestInfo(message digest MD and message-digest algorithm identifier).
- The massage M is digested with the selected message-digest algorithm to MD'.
- If MD' is the same as the MD, the verification shall be succeeded.

ECC

- ECC(Elliptic-curve cryptography) is an approach to public-key cryptography based on the algebraic structure of elliptic curves over finite fields.
- Elliptic curves are applicable for key agreement, digital signatures, pseudo-random generators and other task.
- The primary benefit promised by elliptic curve cryptography is a smaller key size. A 256-bit elliptic curve public key should provide comparable security to 3072-bit RSA public key.

ECC

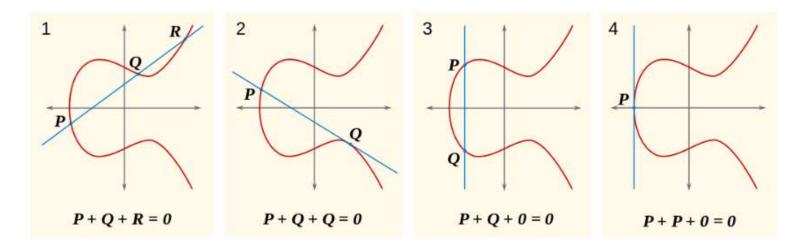
• Elliptic curve

In mathematics, an elliptic curve is a plane algebraic curve defined by an equation of the form $y^2 = x^3 + ax + b$

Where \boldsymbol{a} and \boldsymbol{b} are real numbers. This type of equation is called a Weierstrass equation.

Algebraically, this holds if and only if the discriminant $-16(4a^3 + 27b^2) \neq 0$.

In finite filed(F_p), If P+Q+R=0, Then $P+Q\equiv R(mod\ p)$, $P\times Q\equiv R(mod\ p)$, $P\div Q\equiv R(mod\ p)$.



ECC

Implementation

- 1. Define a base point G in the elliptic curve, the order of G, that is the smallest positive number n such that nG = 0,
- 2. Since n is the size of a subgroup of E[Fp] it follows from Lagrange's theorem that the number $h = \frac{1}{n} |E(Fp)|$ is an integer.
- 3. In the prime case, the domain parameters are (p, a, b, G, n, h).
- 4. Key pair, K = kG(k < n), K is public key, k is private key.
- 5. e.g. parameters secp256k1(http://www.secg.org/sec2-v2.pdf)

secp256k1

$$= 2^{256} - 2^{32} - 2^9 - 2^8 - 2^7 - 2^6 - 2^4 - 1$$

The curve $E: y^2 = x^3 + ax + b$ over \mathbb{F}_p is defined by:

The base point G in compressed form is:

G=02.79BE667E F9DCBBAC 55A06295 CE870B07 029BFCDB 2DCE28D9 59F2815B 16F81798

and in uncompressed form is:

G=04.79BE667E F9DCBBAC 55A06295 CE870B07 029BFCDB 2DCE28D9 59F2815B 16F81798 483ADA77 26A3C465 5DA4FBFC 0E1108A8 FD17B448 A6855419 9C47D08F FB10D4B8

Finally the order n of G and the cofactor are:

n = FFFFFFF FFFFFFF FFFFFFF FFFFFFF BAAEDCE6 AF48A03B BFD25E80 D0364141

01

ATTACK METHODS

SPA--definition

• Simple power analysis (SPA) is a <u>side-channel attack</u> which involves visual examination of graphs of the <u>current</u> used by a device over time. Variations in power consumption occur as the device performs different operations. For example, different instructions performed by a microprocessor will have differing power consumption profiles. As a result, in a power trace from a smart card using <u>DES</u> encryption, the sixteen rounds can be seen clearly. Similarly, squaring and multiplication operations in RSA implementations can often be distinguished, enabling an adversary to compute the secret key. Even if the magnitude of the variations in power consumption are small, standard digital <u>oscilloscopes</u> can easily show the data-induced variations. Frequency filters and averaging functions (such as those built into oscilloscopes) are often used to filter out high-frequency components.

SPA—example(password check)

- Input password via UART, then check if the password inputted is correct.
- Attack the full password(keep guessing letters until we no longer see the distinctive spike).
- Input password guess and capture trace "cap_pass_trace".
- Analyze trace(checkpass function)

```
刘维峰(sawyer), 86-18001126984, liuweifeng168@126.com
```

```
for(uint8_t i = 0; i < sizeof(correct_passwd); i++){
    if (correct_passwd[i] != passwd[i]){
       passbad = 1;
       break;
    }
}</pre>
```

```
trylist = "abcdefghijklmnopqrstuvwxyz0123456789"
password = | ""
for i in range(5):
    for c in trylist:
        next_pass = password + c + "\n"
        trace = [cap_pass_trace(next_pass)]
        if checkpass(trace, i):
            password += c
            print("Success, pass now {}".format(password))
            break

Success, pass now h0
Success, pass now h0a
```

Success, pass now h0aa

DPA—definition

• **Differential power analysis** (**DPA**) is a <u>side-channel attack</u> which involves statistically analyzing power consumption measurements from a <u>cryptosystem</u>. The attack exploits biases varying power consumption of microprocessors or other hardware while performing operations using secret keys. DPA attacks have *signal processing* and *error correction* properties which can extract secrets from measurements which contain too much noise to be analyzed using simple power analysis. Using DPA, an adversary can obtain secret keys by analyzing power consumption measurements from multiple cryptographic operations performed by a vulnerable smart card or other device.

DPA—example(AES DPA Attack)

- Capture traces(5000 traces).
- Separate traces based on the least significant bit.
- Calculate the difference of means, the highest absolute value corresponds to the guessed sub key.
- Repeat this with each possible key guess.

```
N=5000
for i in thrange N, desc='Capturing traces'):
    key, text = ktp.next() # manual creation of a key, text pair can be substituted here
    trace = cw.capture_trace(scope, target, text, key)
    if trace is None:
        continue
    traces.append(trace)
```

```
for subkey in thrange(0, 16, desc="Attacking Subkey"):
                                                              16 subkeys attacking
    for kguess in thrange(255, desc="Keyguess", leave=False):
       one list = []
                                                                              def intermediate(pt, keyguess):
        zero list = []
                                                                                  return sbox[pt ^ keyguess]
       for thum in range(numtraces):
           if (intermediate(textin array[tnum][subkey], kguess) & 1): #LSB is 1
                one list.append(trace array[tnum])
                                                                                 separate traces
                zero list.append(trace array[tnum])
       one avg = np.asarray(one list).mean(axis=0)
       zero avg = np.asarray(zero list).mean(axis=0)
       mean diffs[kguess] = np.max(abs(one_avg - zero_avg)) find highest absolute value
   guess = np.argsort(mean diffs)[-1] highest value as matched/guessed key
    key guess.append(guess)
    print(hex(guess) + "(real = 0x{:02X})".format(known key[subkey]))
    #mean diffs.sort()
    print(mean diffs[guess])
    print(mean diffs[known key[subkey]])
```

CPA—definition

- Correlation Power Analysis(CPA) is an attack that allows us to find a secret encryption key that is stored on a victim device.
- There are 4 steps to a CPA attack:
 - Write down a model for the victim's power consumption.
 - Get the victim to encrypt several different plaintexts. Record a trace of the victim's power consumption during each of these encryptions.
 - Attack small parts(subkeys) of the secret key:
 - Consider every possible option for the subkey. For each guess and each trace, use the known plaintext and the guessed subkey to calculate the power consumption according to our model.
 - Calculate the pearson correlation coefficient between the modeled and actual power consumption.
 - Decide which subkey guess correlates best to the measured traces.
 - Put together the best subkey guesses to obtain the full secret key.

CPA—modeling power consumption

- One of the simplest models for power consumption is the **Hamming Distance**.
 - -e.g HammingDistance(00110000, 00100011) = 3
 - Hamming Distance(x, y) = Hamming Weight(x \land y)

CPA—pearson's correlation coefficient

Pearson's correlation coefficient:

$$\rho_{X,Y} = \frac{Cov(X,Y)}{\sigma_X \sigma_Y} = \frac{E[(X - \mu_X)(Y - \mu_Y)]}{\sqrt{E[(X - \mu_X)^2]E[(Y - \mu_Y)^2]}}$$

This correlation coefficient will always be in the range[-1, 1], it describes how closely the random variables X and Y are related:

If Y always increases when X increases, it will be 1;

If Y always decreases when X increases, it will be -1;

If Y is totally independent of X, it will be 0.

CPA—attack with correlation

- After taking our measurements, we'll have D power traces, and each trace will have T data points. $t_{d,j}$ will refer to point j in the trace $d(1 \le d \le D, 0 \le j \le T)$
- There are I different subkeys that we want to try. had will refer to our power estimate in trace d.
- Calculate this is(how well model and measurements match for each guess i and time j).

$$r_{i,j} = \frac{\sum_{d=1}^{D} \left[\left(h_{d,i} - \overline{h_i} \right) \left(t_{d,j} - \overline{t_j} \right) \right]}{\sqrt{\sum_{d=1}^{D} \left(h_{d,i} - \overline{h_i} \right)^2 \sum_{d=1}^{D} \left(t_{d,j} - \overline{t_j} \right)^2}}$$

$$r_{i,j} = \frac{D \sum_{d=1}^{D} h_{d,i} t_{d,j} - \sum_{d=1}^{D} h_{d,i} \sum_{d=1}^{D} t_{d,j}}{\sqrt{\left(\left(\sum_{d=1}^{D} h_{d,i}\right)^{2} - D \sum_{d=1}^{D} h_{d,i}^{2}\right) \left(\left(\sum_{d=1}^{D} t_{d,j}\right)^{2} - D \sum_{d=1}^{D} t_{d,j}^{2}\right)}}$$

CPA—Picking a subkey

- Use the values of $r_{i,j}$ to decide which subkey matches our traces most closely.
 - For each subkey i, find the highest value of $|r_{i,j}|$.
 - Looking at the maximum values for each subkey, find the highest value of $|r_{i,j}|$, the location i of this maximum is our best guess.
- Note that we're only working with absolute values here because we don't care about the sign of the relationship. All we need to know is that a linear correlation exists.

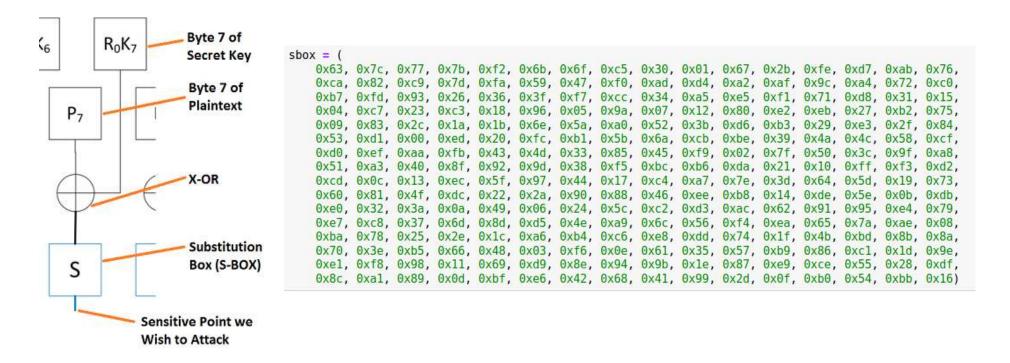
CPA—example1(manual CAP AES)

Capturing traces.

```
from tqdm import thrange
import numpy as np
                              Note: num traces = 50
import time
                                    key is same everytime
ktp = cw.ktp.Basic()
                                    text is random data
traces = []
for i in thrange(num traces, desc='Capturing traces'):
    key, text = ktp.next() # manual creation of a key, text pair can be substituted here
    trace = cw.capture trace(scope, target, text, key)
    if trace is None:
        continue
    traces.append(trace)
#Convert traces to numpy arrays
trace array = np.asarray([trace.wave for trace in traces]) # if you prefer to work with numpy array for number crunc
textin array = np.asarray([trace.textin for trace in traces])
known keys = np.asarray([trace.key for trace in traces]) # for fixed key, these keys are all the same
```

CPA—example1(manual CAP AES) cont'd

Review how AES works, attack point at the bottom of the figure.



CPA—example1(manual CAP AES) cont'd

Performing the check

```
for bnum in tqdm(range(0, 16), desc='Attacking subkeys'):
                                                                             16 subkeys attacking
    cpaoutput = [0] * 256
    maxcpa = [0] * 256
    for kguess in range(0, 256):
                                                                       guessed key: 0~255
         # Initialize arrays & variables to zero
         sumnum = np.zeros(numpoint)
         sumden1 = np.zeros(numpoint)
         sumden2 = np.zeros(numpoint)
        hyp = np.zeros(numtraces)
                                                                        same text with previous trace
         for thum in range(0, numtraces):
             hyp[tnum] = HW[intermediate(pt[tnum][bnum], kguess)]
         # Mean of hypothesis
         meanh = np.mean(hyp, dtype=np.float64)
         # Mean of all points in trace
         meant = np.mean(trace array, axis=0, dtype=np.float64)
         # For each trace, do the following
         for tnum in range(0, numtraces):
         hdiff = (hyp[tnum] - meanh)
             tulff = trace array[tnum, :] - meant
                                                                         \sum_{d=1}^{D} [(h_{d,i} - \bar{h_i})(t_{d,i} - \bar{t_i})]
            sumnum = sumnum + (hdiff * tdiff)
                                                                       \sum_{d=1}^{D} (h_{d,i} - \bar{h_i})^2
           sumden1 = sumden1 + hdiff * hdiff
                                                                      \sum_{d=1}^{D} (t_{d,j} - \bar{t_j})^2
           sumden2 = sumden2 + td1ff * td1ff
                                                                                             \frac{\sum_{d=1}^{D}[(h_{d,i}-\bar{h_i})(t_{d,j}-\bar{t_j})]}{\sqrt{\sum_{d=1}^{D}(h_{d,i}-\bar{h_i})^2\sum_{d=1}^{D}(t_{d,j}-\bar{t_j})^2}}
       cpaoutput[kguess] = sumnum / np.sqrt(sumden1
         maxcpa[kguess] = max(abs(cpaoutput[kguess]))
    bestguess[bnum] = np.argmax(maxcpa)
                                                                            find highest value
    cparefs[bnum] = np.argsort(maxcpa)[::-1]
```

CPA—example2(resynchronizing jittery AES Power traces)

- Add some random delay before encrypting. This is a countermeasure for CPA.
- The traces are not aligned. How to fix that? Figure out a very unique area, like A
 in the picture.
 - A window with the "unique" area defined.
 - How far we will shift the window to search for the best match.
- Then, attack like CAP-example1.

```
uint8_t get_pt(uint8_t* pt)
{
    trigger high();
        for(volatile uint8_t k = 0; k < (*pt & 0x0F); k++);
    aes_inde_enc(pt); /* encrypting the data block */
    trigger_low();
    simpleserial_put('r', 16, pt);
    return 0x00;
}</pre>
```

Template Attack—definition

- Template attacks are a powerful type of side-channel attack. These attacks are a subset of profiling attacks, where an attacker creates a "profile" of a sensitive device and applies this profile to quickly find a victim's secret key.
- To perform a template attack, the attacker must have access to another copy of the protected device that they can fully control.
- To create the template, this may take dozens of thousands of power traces.
- A very small number of traces from the victim to complete the attack.

Template Attack—steps

- Using a copy of the protected device, record a large number of power traces using many different inputs(plaintexts and keys).
- Create a template of device's operation. This template notes a few "points of interest" in the power traces and a multivariate distribution of the power traces at each point.
- On the victim device, record a small number of power traces. Use multiple plaintexts.(we have no control over the secret key, which is fixed.)
- Apply the template to attack traces. For each subkey, track which value is most likely to the correct subkey. Continue until the key has been recovered.

Template Attack—example

- Capture and find POI(Points of interest)
 - Capture traces on device fully controlled(Random Key, Random Text, 6000 traces)
 - Separate each trace into a different group according to the resulting hamming weights.
 - Find averages.
 - Find sum of differences
 - Find POI(Points of interest)

```
# 5: Find POIs
POIs = []
numPOIs = 5
POIspacing = 5
for i in range(numPOIs):
# Find the max
nextPOI = tempSumDiff.argmax()
POIs.append(nextPOI)

# Make sure we don't pick a nearby value
poiMin = max(0, nextPOI - POIspacing)
poiMax = min(nextPOI + POIspacing, len(tempSumDiff))
for j in range(poiMin, poiMax):
    tempSumDiff[j] = 0

print (POIs)

11174, 1165, 2522, 2650, 2502]

**Quantitation**

**POIspacing**
**POIspacing*
```

```
ktp.fixed key = False #RANDOM KEY in addition to RANDOM TEX
                            N = 6000 # Number of traces
                             for i in thrange(N, desc='Capturing traces'):
                                 key, text = ktp.next()
                                 trace = cw.capture trace(scope, target, text, key)
                                 if trace is None:
                                     continue
                                 project.traces.append(trace)
                                HammingWeight=text[0] ^key[0] every trace, just work for Key(
                                for i in range(len(project template.traces)):
                                    HW = tempHW[i]
                                    tempTracesHW[HW].append(project template.waves[i])
                          tempMeans = np.zeros((9, len(project template.waves[0])))
                           for i in range(9):
                               tempMeans[i] = np.average(tempTracesHW[i], 0)
                                  all of the pairs of traces, subtract them, and add
                                  them to the sum of differences
                               # 4: Find sum of differences
                               tempSumDiff = np.zeros(len(project template.waves[0]))
                               for i in range(9):
                                   for i in range(i):
                                       tempSumDiff += np.abs(tempMeans[i] - tempMeans[j])
                               hv.Curve(tempSumDiff).opts(height=600, width=600)
刘维峰(sawver),86-18001126984,liuweifeng168@126.com
```

Template Attack—example, cont'd

- Generate a Template
 - Build multivariate distributions at each point(POI) for each Hamming weight.
 - A mean matrix(1 x numPOIs) which stores the mean at each POI.
 - A covariance matrix(numPOIs x numPOIs) which stores the variances and covariances between each of the POIs.

Template Attack—example, cont'd

- Applying the Template
 - Capture traces on victim device.
 - Build a multivariate_normal object using the relevant mean and covariance matrices.
 - Calculate the log of the PDF and add it to the running total.
 - Find the highest value of Pk

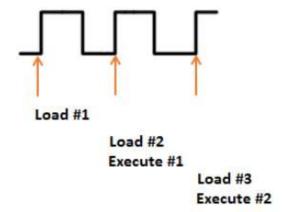
```
N = 20 # Number of traces
              for i in thrange(N, desc='Capturing traces'):
                 key, text = ktp.next()
                                               key is fixed.
                  trace = cw.capture trace(scope, target, text, key)
                  if trace is None:
                       continue
                  project.traces.append(trace)
 from scipy.stats import multivariate normal
 # 2: Attack
 # Running total of log P k
 P k = np.zeros(256)
 for j in range(len(project validate.traces)):
     # Grab key points and put them in a small matrix
  a = [project validate.waves[j][POIs[i]] for i in range(len(POIs))]
     # Test each key
     for k in range(256):
         # Find HW coming out of sbox
         HW = hw[sbox[project validate.textins[j][target byte] ^ k]]
         rv = multivariate normal(meanMatrix[HW], covMatrix[HW])
         p kj = rv.logpdf(a)
         # Add it to running total
         P k[k] += p kj
     # Print our top 5 results so far
     # Best match on the right
     print(" ".join(["%02x"%j for j in P k.argsort()[-5:]]))
guess = P k.argsort()[-1]
                                find the max value
```

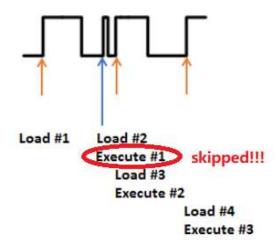
Note: we just attack one byte for the key.

print(hex(quess))

Fault Attack – clock Glitch

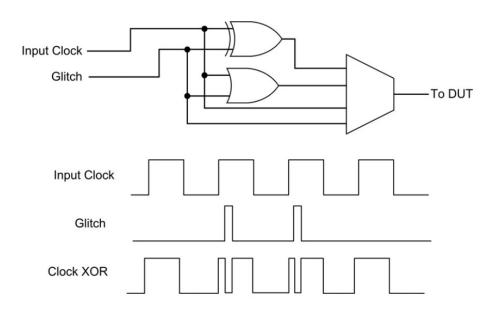
- Background
 - Most MCUs have pipeline to speed up the execution process.
 - Modify the clock, the system doesn't have enough time to perform an instruction.

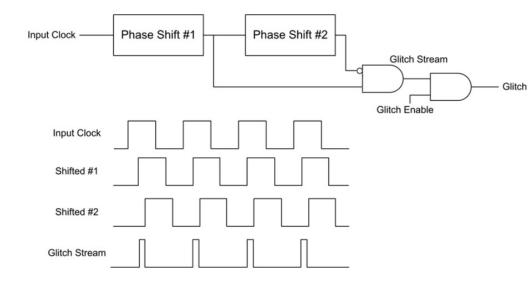




Fault Attack – clock Glitch, cont'd

- Glitch Hardware
 - The generation of glitches is done with two variable phase shift modules.
 - Input clock and Glitch XRO, the glitches can be inserted continuously.





Fault Attack – clock Glitch, cont'd

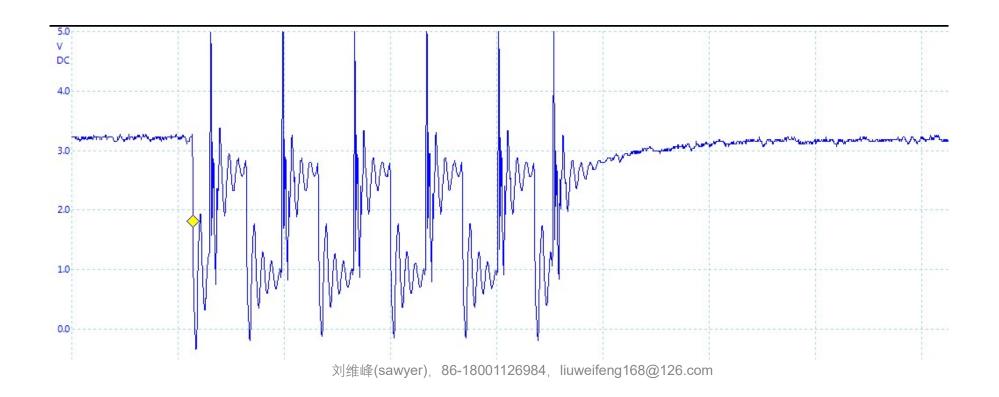
- Example
 - Code. When MCU enters an infinite loop, insert glitch on clock. UART will output "1234" after attacking successfully.

```
//External trigger logic
trigger_high();
trigger_low();

//Should be on infinite loop
while(a != 2){
    Attack here
    ;
}
uart_puts("1234");
```

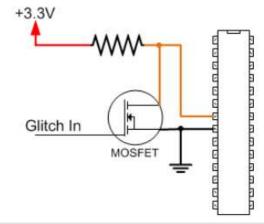
Fault Attack - Power Glitch

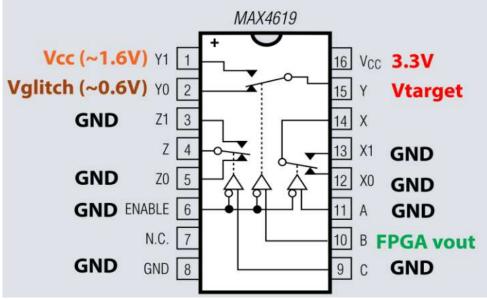
- Background
 - Insert glitch on voltage of device.
 - Can cause a failure to correctly read a memory or havoc with the proper functioning.



Fault Attack – Power Glitch, cont'd

- Hardware
 - A MOSFET to short the power line to GND at specific instances.
 - Use high-speed/CMOS analog switch(e.g MAX4619) to generate glitch.





Fault Attack - Power Glitch, cont'd

- Example
 - During normal operation, UART will output "40000 200 200 \$k". The numbers are incorrect, when inserting VCC glitch.

```
void glitch infinite(void)
    char str[64];
    unsigned int k = 0;
    //Declared volatile to avoid optimizing away loop.
    //This also adds lots of SRAM access
    volatile uint16 t i, j;
    volatile uint32 t cnt;
    while(1){
        cnt = 0;
        trigger high();
        trigger low():
       for(i=0; i<200; i++){</pre>
                                     Add power glitch
            for(j=0; j<200; j++){
                cnt++;
        sprintf(str, "%lu %d %d %d\n", cnt, i, j, k++);
        uart puts(str);
```

Fault Attack – Buffer Glitch

- Background
 - Occur this when more data is put into a fixed-length buffer than the buffer can handle.
 - Do this by well-timed clock or power glitch.
 - Usually result a system crash, or create the opportunity for an attacker to run arbitrary code or manipulate the coding errors

Fault Attack – Buffer Glitch, cont'd

- Example
 - The code is compiled, then check the ARM disassembly.
 - The check is whether i == ascii_idx.
 - Insert power or clock glitch, skip the check.
 - Note: for a small number of repetitions, size-speed tradeoff is skewed towards the latter(Wikipedia page on loop unrolling).

```
if(state == RESPOND)
    // Send the ascii buffer back
    trigger high();
                      attack here
   for(i = 0; i < ascii idx; i++</pre>
                                             8000268:
                                                          5d28
                                                                         ldrb
                                                                                 r0, [r5, r4]
                                             800026a:
                                                          3401
                                                                                 r4, #1
                                                                         adds
        putch(ascii buffer[i]);
                                             800026c:
                                                          f000 f8f2
                                                                               8000454 <putch>
                                             8000270:
                                                          2c08
                                                                                r4, #8
    trigger low();
                                             8000272:
                                                          d1f9
                                                                                  8000268 <main+0x64>
    state = IDLE;
```

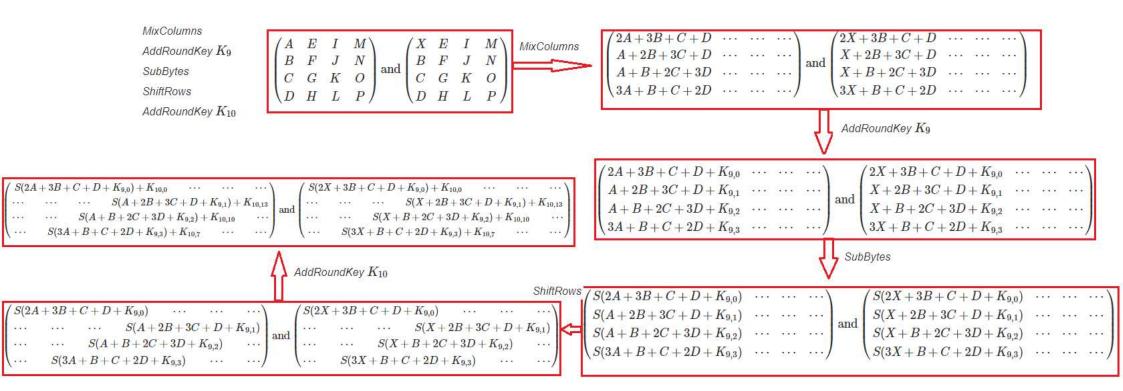
```
for (int i = 0; i < 3; i++)
    do_something();
    do_something();
    do_something();
    do_something();</pre>
```

Fault Attack - Buffer Glitch, cont'd

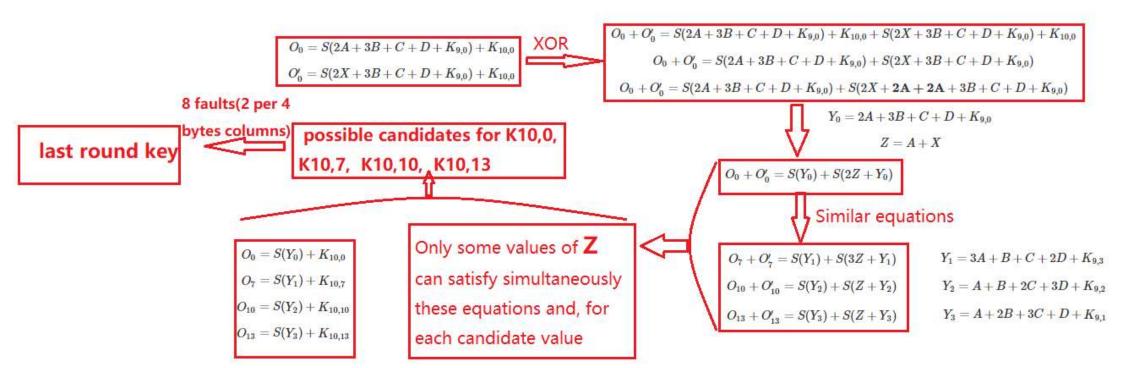
- Buffer overrun check
 - Insert a guard carriable onto the stack frame for each vulnerable function
 - Tools chains support this function.
 - *MCUXpresso IDE:* https://mcuoneclipse.com/2019/09/28/stack-canaries-with-gcc-checking-for-stack-overflow-at-runtime/
 - Keil: http://www.keil.com/support/man/docs/armcc/armcc_chr1359124940593.htm
 - IAR: https://www.iar.com/support/resources/articles/stack-protection-in-iar-embedded-workbench-for-arm/
 - Note: this is not a 100% check, because it relies on if the program/attacker writes to a memory address on the program's call stack outside of the intended data structure.

- Introduction
 - The basis of attack is that one byte of the state needs to be corrupted somewhere between the two last *MixColumns* operations, which take place in the last 3 rounds.
 - In this situation, the fault will be propagated to exactly 4 bytes of the output.

- Introduction
 - fault the first byte just before the last *MixColumns* operation



- Introduction
 - the following equations for the normal and faulty cases.



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- Example(AES-128, clock glicthing)
 - Attack the 8th or 9th round.
 - Collecting faulty outputs.
 - Cryptanalysis of the faulty outputs using phoenixAES. And get last round key.
 - Revert the AES keyscheduling and reveal the actual AES key.

Fault Attack – RSA Fault Attack

RSA-CRT system

```
primes p and q, N = pq i_q = q^{-1} \mod p n = pq \text{ and } \phi = (p-1)(q-1) \quad d_q = e^{-1} \mod (q-1) ed \equiv 1 \mod \phi \qquad \qquad d_p = e^{-1} \mod (p-1) Input: message m, key (p,q,d_p,d_q,i_q)
```

Output: signature $m^d \in \mathbb{Z}_N = S$ $S_p = m^{d_p} \mod p$

```
S_p = m^{d_p} \mod p

S_q = m^{d_q} \mod q

S = S_q + q \cdot (i_q \cdot (S_p - S_q) \mod p)

return (S)
```

Fault Attack – RSA Fault Attack

RSA-CRT fault attack

A fault happens in one of the equations mod p or q. P divides this value, but q does not divide this value. This means that $\tilde{s}^e - m$ is of the form pk with some integer k, $gcd(\tilde{s}^e - m, N)$ will give out p! q = N/P!

$$\begin{vmatrix}
s_1 = m^{d_p} \pmod{p} \\
\widetilde{s_2} = m^{d_q} \pmod{q}
\end{vmatrix} \Longrightarrow \widetilde{s} \pmod{pq}$$

$$\begin{cases} \widetilde{s}^e = m \pmod{p} \\ \widetilde{s}^e \neq m \pmod{q} \end{cases} \implies \begin{cases} \widetilde{s}^e - m = 0 \pmod{p} \\ \widetilde{s}^e - m \neq 0 \pmod{q} \end{cases} \implies \begin{cases} p \mid \widetilde{s}^e - m \\ q \nmid \widetilde{s}^e - m \end{cases}$$

Fault Attack – RSA Fault Attack

- Applying the RSA-CRT attack
 - Insert a glitch
 - Read the signature back
 - Verify that it is correct
 - Extract the PKCS#xx padded hash.
 - $p = gcd(\tilde{s}^e m, N)$
 - q = N/p
 - $ed \equiv 1 \mod \emptyset$, $\emptyset = (p-1)(q-1)$, **d** is private key.

TVLA

Definition

- TVLA(Test Vector Leakage Assessment) which was proposed at NIST sponsored NIAT workshop 2011, is one of such conformance style testing mechanism which seeks to detect and analyze leakage directly in a device under test.
- The statistical measurement used with TVLA is welch's t-test for significance of "difference of means" with a threshold of 4.5 standard deviations.
- TVLA test can be useful for validating your crypto implementation. If the TVLA value is within \pm 4.5, we can claim that the crypto-implementation is secure with high confidence.

TVLA

- Example
 - See Test Vector Leakage Assessment (TVLA) Derived Test Requirements (DTR) with AES.



SNR

Example

- Capture the trace
- Sort the traces as Hamming Weight and compute means for every HW.
- Remove any groups with zero traces.
- Use hwarray[4] to calculate the noise.

```
hwarray = [[], [], [], [], [], [], [], []]
#For each byte we are looking at - let's split into multiple groups Sort the trace
for tnum in range(0, len(traces)):
    hw_of_byte = HW[intermediate(traces[tnum].textin[bnum], traces[tnum].key[bnum])]
    hwarray[hw_of_byte].append(traces[tnum].wave)

hwmean = np.zeros((9, npoints))

for i in range(0, 9):
    hwmean[i] = np.mean(hwarray[i], axis=0)
compute means for every HW
```

```
N = 1500
for i in thrange(N, desc='Capturing traces'):
    key, text = ktp.next()
    trace = cw.capture_trace(scope, target, text, key)
    if trace is None:
        continue
    traces.append(trace)
```

```
inc_list = []
for i in range(0, len(hwarray)):
    if len(hwarray[i]) > 0:
        inc_list.append(i)
    with zero traces

hwmean_valid = hwmean[inc_list]

signal_var = np.var(hwmean_valid, axis=0)
noise_var_onehw = np.var(hwarray[4], axis=0)
variance
snr = signal_var / noise_var_onehw
```

CASE ANALYSIS

