

1.k=1 (the function of "my_knn_R()" is the the R file "knn1.R" and "my_knn_C()" is the the R file "k1.cpp")

```
> my_knn_R(X, X0, y)
[1] 17.5
> my_knn_C(X, X0, y)
[1] 17.5
> FNN::knn.reg(X, matrix(X0, nrow = 1), y, k=1)
Prediction:
[1] 17.5
> microbenchmark(my_knn_R(X, X0, y),my_knn_C(X, X0, y),FNN::knn.reg(X, matrix(X0, nrow = 1), y, k=1))
Unit: microseconds
```

	expr	min	1q	mean	median	uq	max	neval
	my_knn_R(X, X0, y)	6931.132	7631.5390	8940.06988	8056.200	8991.2235	21018.692	100
	my_knn_C(X, X0, y)	14.588	20.8685	36.14508	34.038	53.4880	76.991	100
	FNN::knn.reg(X, matrix(X0, nrow = 1), y, k = 1)	594.039	612.8815	784.47223	797.455	875.8635	1889.499	100

*the results of these three versions of R,c++ and FNN::knn.reg() are the same, and the method of C++ is fastest.

2.k=2 (the function of "my_knn2_R()" is the the R file "knn2.R" and "my_knn2_C()" is the the R file "k2.cpp")

```
> my_knn2_R(X, X0, y)
[1] 17.85
> my_knn2_C(X, X0, y)
[1] 17.85
> FNN::knn.reg(X, matrix(X0, nrow = 1), y, k=2)
Prediction:
[1] 17.85
> microbenchmark(FNN::knn.reg(X, matrix(X0, nrow = 1), y, k=2),my_knn2_R(X, X0, y),my_knn2_C(X, X0, y))
Unit: microseconds
```

	expr	min	1q	mean	median	uq	max	neval
	FNN::knn.reg(X, matrix(X0, nrow = 1), y, k = 2)	597.281	646.514	822.27840	844.257	877.8895	1567.355	100
	my_knn2_R(X, X0, y)	14047.040	15045.884	17721.91693	16079.374	17900.1895	34435.629	100
	my_knn2_C(X, X0, y)	25.933	27.555	72.02647	45.384	67.2655	2437.344	100

*In the R Code of "knn2.R", firstly do the same in "knn1.R" to compare the distance between X0 and every row of X, find the minimum distance, the first closest neighbor and its output(y_1). Except the first closest neighbor, use the loop again to find the second closest neighbor

and its output(y_2).

*the prediction of the 2-nearest-neighbor is the average value of the first closest output and the second closest output($\frac{y_1 + y_2}{2}$).

*the results of these three versions of R,c++ and FNN::knn.reg() are the same, and the method of C++ is fastest.

3.Extra (the function of "my_knn_inverse_R()" is the the R file "knn_extra.R" and "my_knn_inverse_C()" is the the R file "knn_extra.cpp")

```
> my_knn_inverse_R(X, X0, y,2)
[1] 17.70935
> #[1] 17.5
> my_knn_inverse_C(X, X0, y,2)
[1] 17.70935
> microbenchmark(my_knn_inverse_R(X, X0, y,1),my_knn_inverse_C(X, X0, y,1))
Unit: microseconds
```

	expr	min	1q	mean	median	uq	max	neval
	my_knn_inverse_R(X, X0, y, 1)	7038.918	7521.727	8715.11314	7900.801	8497.6770	18287.166	100
	my_knn_inverse_C(X, X0, y, 1)	15.398	16.613	37.63622	50.652	56.3245	107.381	100

```
> microbenchmark(my_knn_inverse_R(X, X0, y,2),my_knn_inverse_C(X, X0, y,2))
Unit: microseconds
```

	expr	min	1q	mean	median	uq	max	neval
	my_knn_inverse_R(X, X0, y, 2)	14359.457	15310.892	18834.45581	16397.6675	17759.784	165358.849	100
	my_knn_inverse_C(X, X0, y, 2)	25.934	27.757	51.89554	32.8225	69.899	243.532	100

*in the extra problem, the function has one more parameter k, the number of closest neighbor,

When k=1,the prediction is first closest output(y_1).

When k=2,it is better to weight the neighbors so that the nearer neighbors contribute more,,so the prediction is

(d_1 is the first closest distance and d_2 is the second closest distance).

$$\frac{\frac{y_1}{d_1} + \frac{y_2}{d_2}}{\frac{1}{d_1} + \frac{1}{d_2}}$$

*the results of the versions of R,c++ are the same, and the method of C++ is faster.