

IK Terminology and Workflow

An IK **chain** is a collection of IK **bones** which are connected to each other. The very first bone in the chain is called the **basebone**, and the start location of the basebone is called the **base location**.

Each bone has a start location and an end location which, depending on whether we are working in 2D or in 3D, will be defined in either 2D or 3D space. The end location of the final bone in a chain is called the **end-effector**.

Each bone also has a single **joint** which may control the allowable movement of the bone.

The typical workflow of an IK setup is that:

- A chain is created,
- One or more bones are added to this chain, then
- An attempt is made to **solve** the chain for a given target location.

It is during this solve attempt that, in this case, the FABRIK algorithm is executed which may alter the configuration of the chain so that the end-effector is as close to the target location as possible.

During this solve attempt:

- The length of the bones does not change, and
- The end location of one bone and the start location of the following bone overlap precisely.

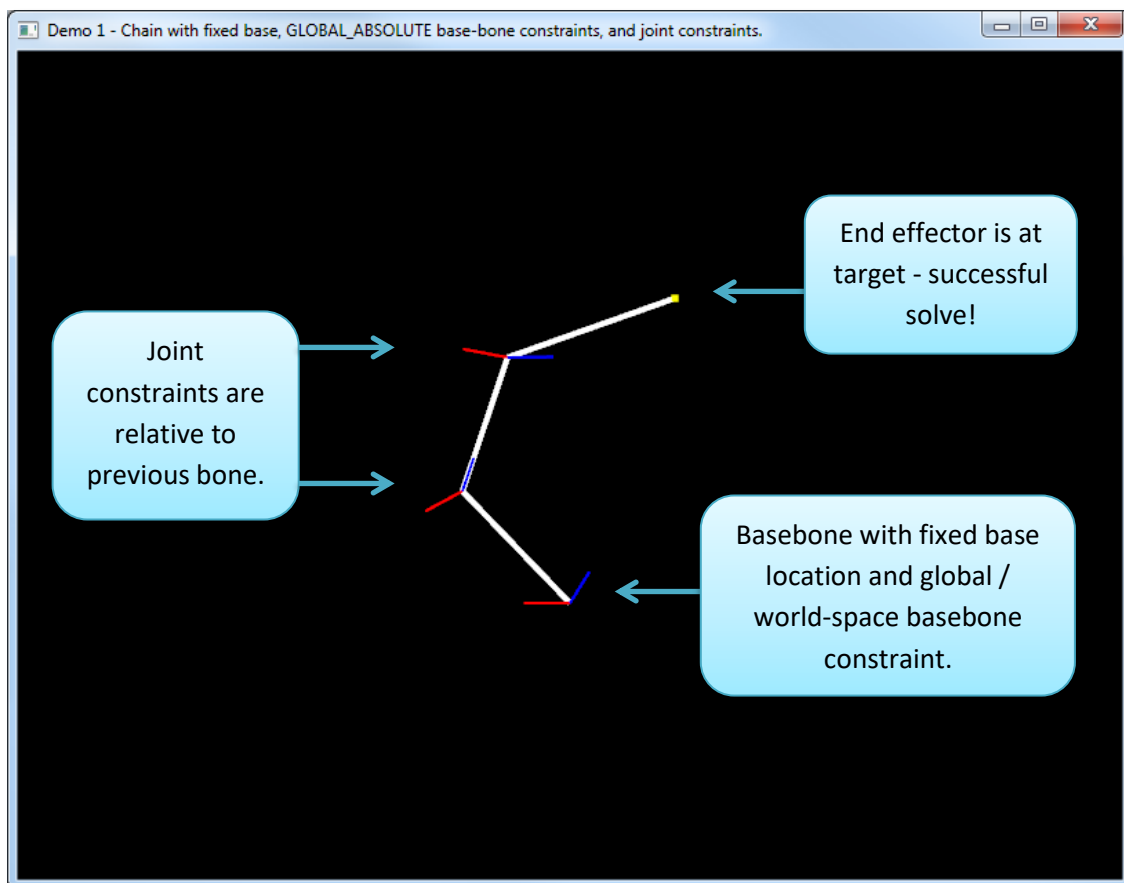


Figure 5 - A simple IK chain in 2D. It contains three bones, has a fixed base location, and has been successfully solved.

Structures

In the Caliko library, multiple IK chains may be connected to each other by placing them into a special 'holder' object called a **structure**. For example, after adding an initial chain to a structure, we might decide to add a second chain to the structure where the basebone of that second chain is connected to the end joint of the third bone in the initial chain (or the start joint of the second bone etc. - it's entirely up to you).

As such, when the first chain moves, the second chain's base location also moves in order to remain attached.

Joints and Restrictions

Each bone in a chain may be configured to allow only a restricted subset of motion. In the Caliko library there are two specific types of restriction:

- **Basebone restrictions** - which are applied to the **chain**, and
- **Joint restrictions** - which are applied to individual **bones**.

Depending on whether you are working in 2D or 3D there are a variety of different basebone and standard joint restriction types.

Basebone Restrictions

A basebone restriction is a special-case of standard restriction, and is required because the basebone itself is the very first bone in a chain and as such does not have a previous bone which it may be restricted about.

In 2D, the basebone restriction types are:

- **NONE** - No constraint,
- **GLOBAL_ABSOLUTE** - Constrained about a global / world-space direction,
- **LOCAL_ABSOLUTE** - Constrained about the direction of the connected bone, and
- **LOCAL_RELATIVE** - Constrained about a direction relative to that of the connected bone.

The LOCAL_ABSOLUTE and LOCAL_RELATIVE basebone constraint types are only available to be used by chains which are connected to other chains.

In 3D, the basebone restriction types are:

- **NONE** - No constraint,
- **GLOBAL_ROTATOR** - Ball-joint constrained about a global / world-space direction,
- **LOCAL_ROTATOR** - Ball-joint constrained about the direction of the connected bone,
- **GLOBAL_HINGE** - Hinge constrained about a world-space axis, and
- **LOCAL_HINGE** - Hinge constrained about an axis relative to that of the connected bone.

As before, the LOCAL_ROTATOR and LOCAL_HINGE basebone constraint types are only available to be used by chains which are connected to other chains. In addition, hinge constraints may have an additional **reference axis** constraint which is the direction within the axis of the hinge about which clockwise/anticlockwise movement is allowed.

To put this in perspective - if you think of the front door of your house rotating on its hinges: its reference axis would be when the door is closed, and it can likely rotate zero degrees one way (i.e. it doesn't open outwards) and maybe up to 100 degrees or such the other way to let people in and out.

Joint Restrictions

As previously mentioned, each bone has a single joint which can be thought of as being at the start of the bone. In 2D there are no specific joint types as the bones may only rotate clockwise and anticlockwise, however, 2D joint constraints may be configured to operate in a GLOBAL or LOCAL manner - where a local constraint is relative to the coordinate system of the previous bone in the chain.

In 3D, there are three distinct types of joint, which are:

- **BALL** - A 'rotor' / ball-joint constraint about the previous bone in the chain,
- **GLOBAL_HINGE** - A world-space hinge constraint, or
- **LOCAL_HINGE** - A hinge constraint relative to the previous bone in the chain.

The default joint type of a 3D bone is BALL, and the default constraint angle is 180 degrees - which in effect means that no constraint is applied. Ball joints only have a single constraint angle which describes the 'rotor' arc the joint allows, while hinges both have clockwise and anticlockwise constraint angles which may be enforced about a given reference axis that falls within the plane of the hinge.

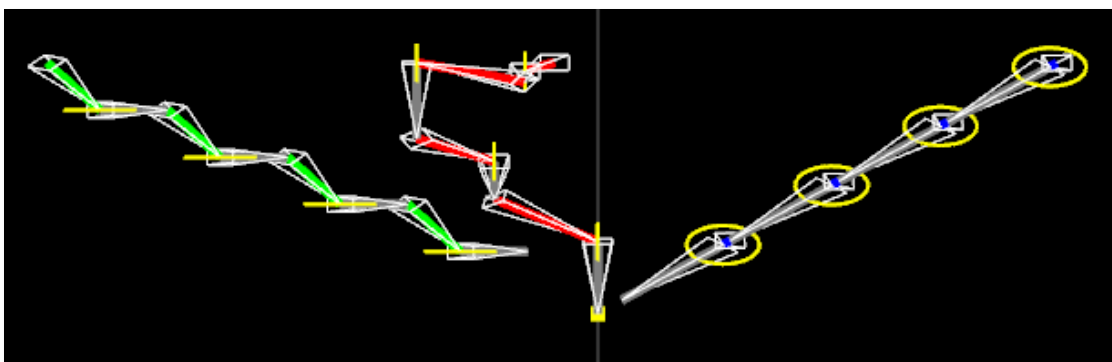
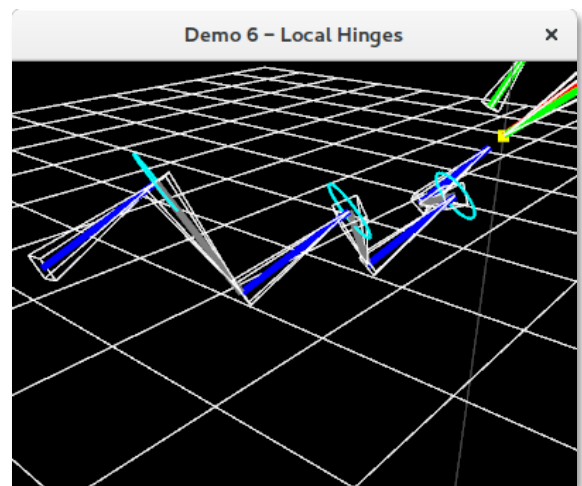
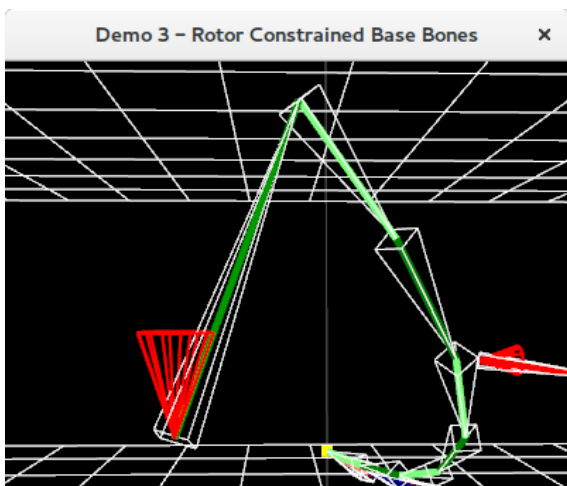


Figure 6 - Rotor / ball-joint constraints (top left) allow movement up to a given angle about the rotor constraint axis, local hinge constraints allow movement about the hinge axis in the coordinate system of the previous bone in the chain, while global hinge constraints (bottom) allow movement about a given world-space axis only.

Solving IK Chains and Structures

Once a chain exists and contains one or more bones, it can be solved by calling the **solveForTarget()** method and providing it a target location to solve the chain for. Targets may be specified as Vec2f or Vec3f objects, or as floats.

If multiple chains exist in a structure, then calling **solveForTarget()** along with a target location results in each chain in the structure being solved in a first-in-first-solved manner for the same target location. However, if a chain in a structure has the **useEmbeddedTarget** mode enabled, then the chain will be solved for its own embedded target location rather than any provided target. In this manner, a structure may contain a combination of chains which can be solved for the specified target or their own embedded target location with a single call to **solveForTarget()** on the structure. If all chains in a structure use embedded targets then the provided target location is effectively ignored.

Chains that use embedded targets may update their targets via the chain's **updateEmbeddedTarget()** method, and individual chains may be solved for their embedded targets via a call to **solveForEmbeddedTarget()**.

Vectors and Matrices

The Caliko library uses a series of custom 2D and 3D vector classes (Vec2f, Vec3f) 3x3 and 4x4 matrices (Mat3f, Mat4f). These classes can be found in the **au.edu.federation.utils** package.

Array getters and setters exist to allow you to interact via the vector/matrix classes of your choice - but all Caliko vector and matrix properties are publicly accessible for ease of customisation purposes.

Both orthographic (2D) and perspective (3D) matrices can be created with ease through the provided Mat4f class, and the Vec3f and Vec2f classes offer a wide variety of methods to assist with manipulation of directions and locations. Please see the class source code and provided Javadoc for full API specifications.

Reproducible Sequences

If you'd like to experiment with modifications to the Caliko source code, in particular, the results of solving 3D chains in a reproducible manner - then you can set a fixed seed for the random number generator (which is used by the MovingTarget3D class) by calling:

```
Utils.setSeed(SOME_FIXED_INTEGER);
```

For example:

```
Utils.setSeed(123);
```

Obtaining Pitch, Yaw and Roll Angles for 3D Vectors / Bones

The Vec3f class has **getGlobalPitchDegs()** and **getGlobalYawDegs()** methods which provide the pitch and yaw, and the FabrikBone3f class has the same functions which just call those Vec3f methods on the direction of the bone.

Obtaining **roll** is not directly supported at the present time because 3D bones are stored as a two points in space, which is insufficient to calculate consistent roll angles. To reliably keep track of roll, the Caliko library must be refactored to store the 3D bone directions in quaternions, or it must store a rotation matrix along with each bone (as opposed to the current system of generating a valid but not guaranteed consistent rotation matrix on demand).

Usage Examples

The Caliko demo application provides a number of usage examples which exercise various aspects of the library functionality. The examples below demonstrate how a variety of IK scenarios may be constructed.

In these 2D examples, UP/DOWN/LEFT/RIGHT are defined as the vectors (0.0f, 1.0f) / (0.0f, -1.0f) / (-1.0f, 0.0f) and (1.0f, 0.0f) respectively. In the 3D examples X_AXIS is (1.0f, 0.0f, 0.0f), the Y_AXIS is (0.0f, 1.0f, 0.0f) and Z_AXIS is (0.0f, 0.0f, 1.0f). The Z-axis points directly outwards from the screen.

2D Demo 1 - Chain with GLOBAL_ABSOLUTE basebone constraint and joint constraints

```
// Instantiate our structure, create a new chain and set it as fixed-base
FabrikStructure2D structure = new FabrikStructure2D();
FabrikChain2D chain = new FabrikChain2D();
chain.setFixedBaseMode(true);

// Default bone length
float boneLength = 40.0f;

// Create the basebone, set constraints and add it to the chain
FabrikBone2D base = new FabrikBone2D(new Vec2f(0.0f, -boneLength), new Vec2f() );
base.setClockwiseConstraintDegs(25.0f);
base.setAnticlockwiseConstraintDegs(90.0f);
chain.addBone(base);

// Fix the basebone and constrain it to the positive Y-axis
chain.setBaseboneConstraintType(BaseboneConstraintType2D.GLOBAL_ABSOLUTE);
chain.setBaseboneConstraintUV(UP);

// Create and add the second bone - 50 clockwise, 90 anticlockwise
chain.addConsecutiveConstrainedBone(UP, boneLength, 50.0f, 90.0f);

// Create and add the third bone - 75 clockwise, 90 anticlockwise
chain.addConsecutiveConstrainedBone(UP, boneLength, 75.0f, 90.0f);

// Finally, add the chain to the structure
structure.addChain(chain);
```

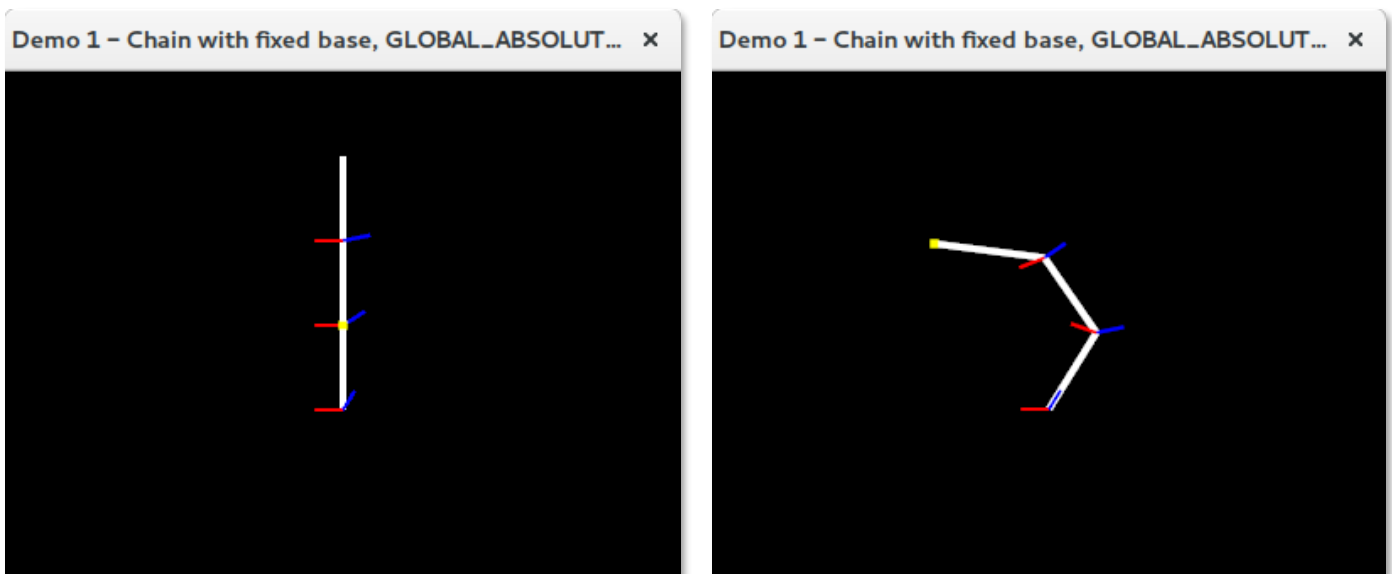


Figure 7 - Chain with GLOBAL_ABSOLUTE basebone constraint and joint constraints (left) original configuration (right) example solve configuration

2D Demo 2 - Chain with fixed base and multiple unconstrained bones

```
// Instantiate our structure, create a new chain and set it as fixed-base
FabrikStructure2D structure = new FabrikStructure2D();
FabrikChain2D chain = new FabrikChain2D();
chain.setFixedBaseMode(true);

// Create the basebone and add it to the chain.
// Params: Start location, direction, length
FabrikBone2D base = new FabrikBone2D(new Vec2f(), RIGHT, 10.0f);
chain.addBone(base);

// Add a series of additional bones which initially form a circle
float boneLength = 10.0f;
float numBones = 15;
float rotStep = 360.0f / numBones;
for (int loop = 0; loop < numBones; loop++){
    // Rotate each bone by 10 degrees and add it to the chain
    Vec2f rotatedUV = Vec2f.rotateDegs(RIGHT, loop * rotStep);
    chain.addConsecutiveBone(rotatedUV, boneLength);
}

// Finally, add the chain to the structure
structure.addChain(chain);
```

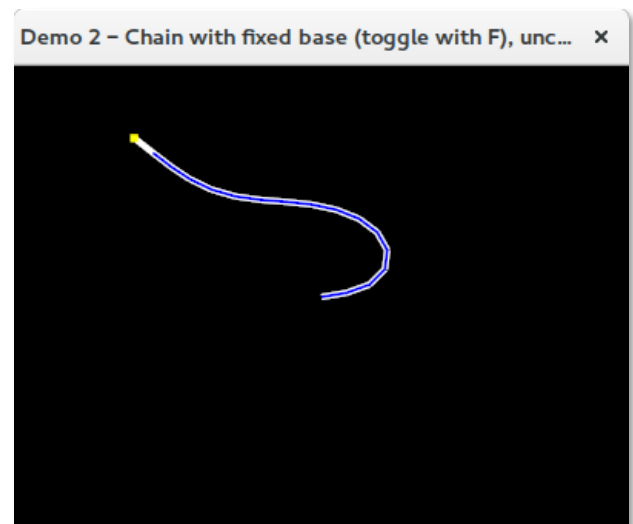
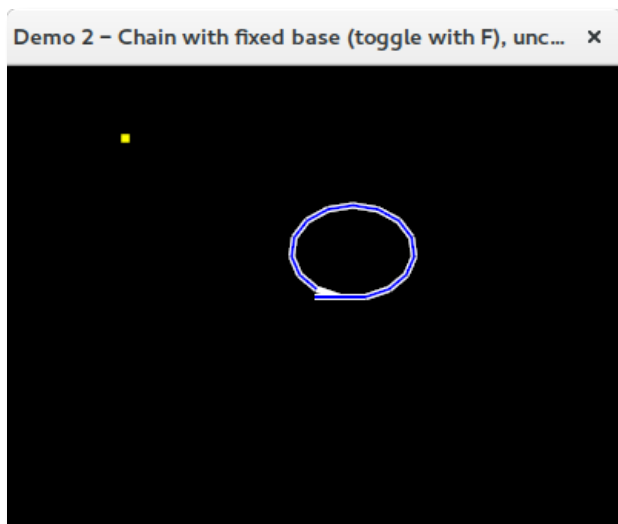


Figure 8 - Unconstrained chain (left) original configuration (right) example solve configuration

2D Demo 3 - Chain with fixed base and multiple constrained bones

```
// Instantiate our structure, create a new chain and set it as fixed-base
FabrikStructure2D structure = new FabrikStructure2D();
FabrikChain2D chain = new FabrikChain2D();
chain.setFixedBaseMode(true);

// Create the basebone and add it to the chain.
// Params: Start location, direction, length
FabrikBone2D base = new FabrikBone2D(new Vec2f(), RIGHT, 10.0f);
chain.addBone(base);

// Add a series of additional bones which initially form a circle
float boneLength = 10.0f;
float numBones = 15;
float rotStep = 360.0f / numBones;
for (int loop = 0; loop < numBones; ++loop) {
    // Rotate each bone by 10 degrees and add it to the chain with constraint angles
```

```
// Note: Anticlockwise rotation is positive, clockwise rotation is negative.
Vec2f rotatedUV = Vec2f.rotateDegs(RIGHT, loop * rotStep);
chain.addConsecutiveConstrainedBone(rotatedUV, boneLength, 60.0f, 60.0f);
}

// Finally, add the chain to the structure
structure.addChain(chain);
```

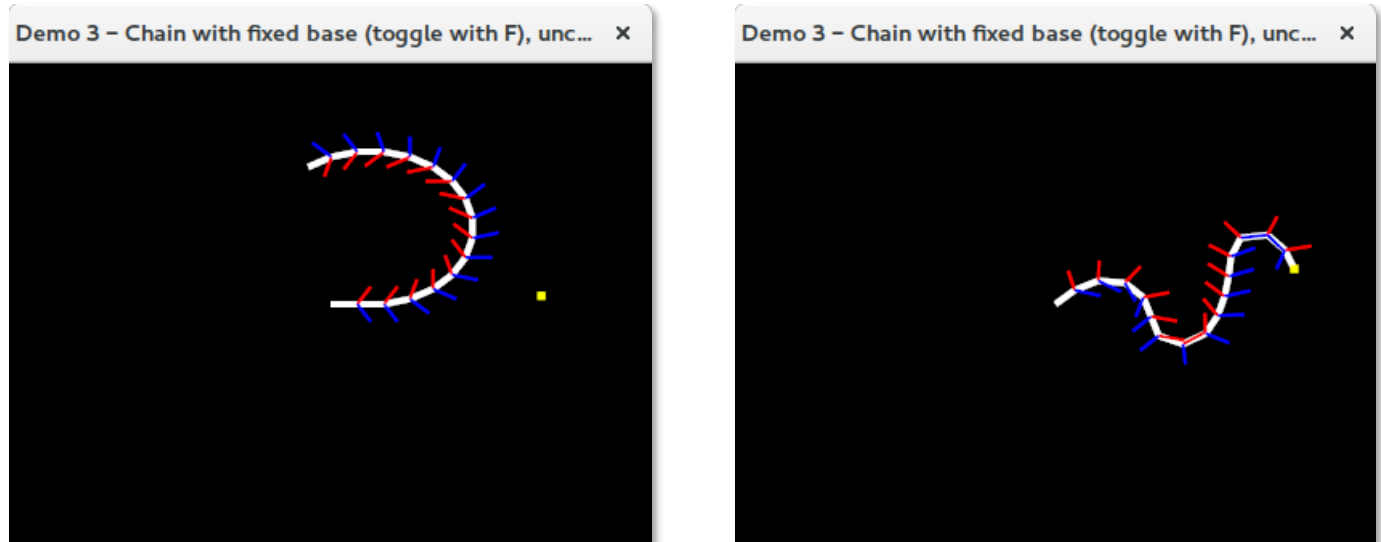


Figure 9 - Constrained chain in (left) original configuration and (right) example solve configuration. No bone may exceed its anticlockwise or clockwise constraint angles, shown in red and blue respectively.

2D Demo 4 - Chain with fixed base and multiple constrained bones

```
// Instantiate our FabrikStructure2D
FabrikStructure2D structure = new FabrikStructure2D();

// ----- Vertical chain -----
float boneLength = 50.0f;
FabrikChain2D verticalChain = new FabrikChain2D();
FabrikBone2D basebone = new FabrikBone2D( new Vec2f(0.0f, -50.0f), UP, boneLength);

// Note: Default basebone constraint type is NONE
verticalChain.addBone(basebone);

// Add two additional consecutive bones
verticalChain.addConsecutiveConstrainedBone(UP, boneLength, 90.0f, 90.0f);
verticalChain.addConsecutiveConstrainedBone(UP, boneLength, 90.0f, 90.0f);

// Add our main chain to structure
structure.addChain(verticalChain);

// ----- Left branch chain -----
boneLength = 30.0f;

// Create the base bone and set its colour
basebone = new FabrikBone2D( new Vec2f(), new Vec2f(-boneLength, 0.0f) );
basebone.setColour(Utils.MID_GREEN);

// Create the chain and add the basebone to it
FabrikChain2D leftChain = new FabrikChain2D();
leftChain.addBone(basebone);

// Add consecutive constrained bones
// Note: The base-bone is unconstrained, but these bones ARE constrained
leftChain.addConsecutiveConstrainedBone(LEFT, boneLength, 90.0f, 90.0f,
Utils.MID_GREEN);
```

```

leftChain.addConsecutiveConstrainedBone(LEFT, boneLength, 90.0f, 90.0f,
Utils.MID_GREEN);

// Add the chain to the structure, connecting to the end of bone 0 in chain 0
structure.addConnectedChain(leftChain, 0, 0, BoneConnectionPoint2D.END);

// ----- Right branch chain -----

// Create the base bone
basebone = new FabrikBone2D( new Vec2f(), new Vec2f(boneLength, 0.0f) );
basebone.setColour(Utils.GREY);

// Create the chain and add the basebone to it
FabrikChain2D rightChain = new FabrikChain2D();
rightChain.addBone(basebone);

// Add two consecutive constrained bones to the chain
// Note: The base-bone is unconstrained, but these bones ARE constrained
rightChain.addConsecutiveConstrainedBone(RIGHT, boneLength, 60.0f, 60.0f,
Utils.GREY);
rightChain.addConsecutiveConstrainedBone(RIGHT, boneLength, 60.0f, 60.0f,
Utils.GREY);

// Add the chain to the structure, connecting to the end of bone 1 in chain 0
structure.addConnectedChain(rightChain, 0, 2, BoneConnectionPoint2D.START);

```

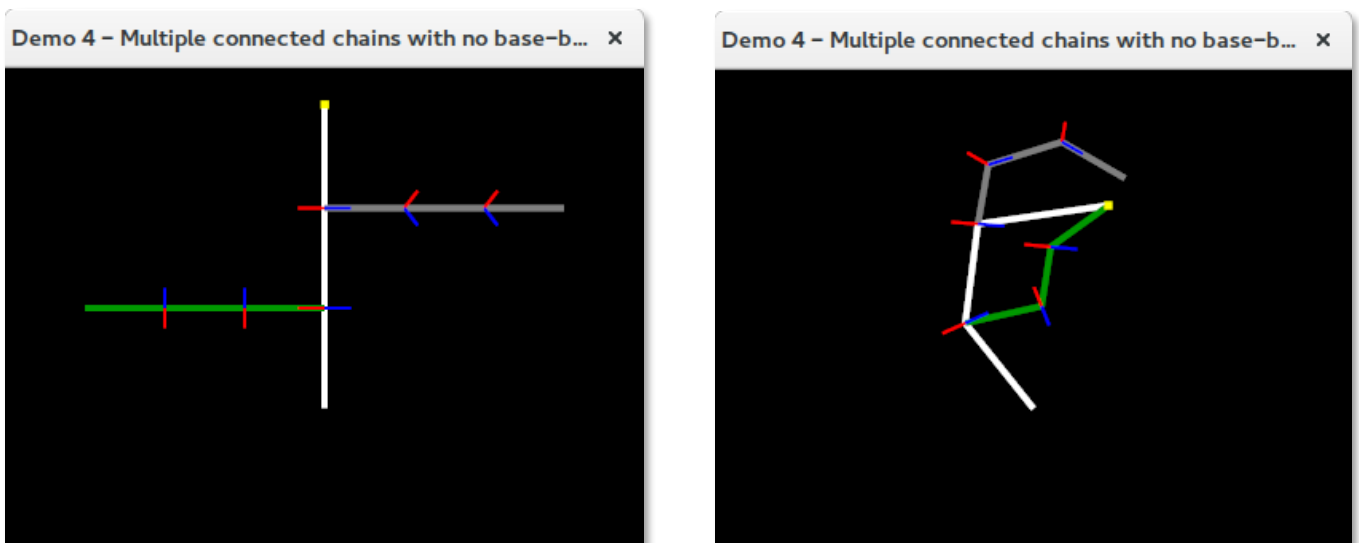


Figure 10 - Connected chains with fixed basebones, joint constraints and no basebone constraints. (left) original configuration (right) example solve configuration. The joint constraints on the grey chain prevent a successful solve in this instance.

2D Demo 5 - Multiple connected chains with LOCAL_RELATIVE basebone constraints

```

FabrikStructure2D structure = new FabrikStructure2D();

// ----- Vertical chain -----
float boneLength = 50.0f;
FabrikChain2D verticalChain = new FabrikChain2D();
FabrikBone2D basebone = new FabrikBone2D( new Vec2f(0.0f, -100.0f), UP,
boneLength);
basebone.setClockwiseConstraintDegs(15.0f);
basebone.setAnticlockwiseConstraintDegs(15.0f);

verticalChain.addBone(basebone);
verticalChain.addConsecutiveConstrainedBone(UP, boneLength, 30.0f, 30.0f);
verticalChain.addConsecutiveConstrainedBone(UP, boneLength, 30.0f, 30.0f);

```



```
verticalChain.setBaseboneConstraintType(BaseboneConstraintType2D.GLOBAL_ABSOLUTE);
verticalChain.setBaseboneConstraintUV(UP);

// Add chain to structure
structure.addChain(verticalChain);

// ----- Left branch chain -----
boneLength = 30.0f;

// Create the base bone
basebone = new FabrikBone2D( new Vec2f(), new Vec2f(-boneLength, 0.0f) );
basebone.setClockwiseConstraintDegs(60.0f);
basebone.setAnticlockwiseConstraintDegs(60.0f);
basebone.setColour(Utils.MID_GREEN);

// Create the chain, add the basebone and enable base bone constraint mode
FabrikChain2D leftChain = new FabrikChain2D();
leftChain.setBaseboneConstraintType(BaseboneConstraintType2D.LOCAL_RELATIVE);
leftChain.addBone(basebone);

// Add consecutive constrained bones
leftChain.addConsecutiveConstrainedBone(LEFT, boneLength, 60.0f, 60.0f,
                                         Utils.MID_GREEN);
leftChain.addConsecutiveConstrainedBone(LEFT, boneLength, 60.0f, 60.0f,
                                         Utils.MID_GREEN);

// Add the chain to the structure, connecting at the end of bone 0 in chain 0
structure.addConnectedChain(leftChain, 0, 0, BoneConnectionPoint2D.END);

// ----- Right branch chain -----
// Create the base bone
basebone = new FabrikBone2D( new Vec2f(), new Vec2f(boneLength, 0.0f) );
basebone.setClockwiseConstraintDegs(30.0f);
basebone.setAnticlockwiseConstraintDegs(30.0f);
basebone.setColour(Utils.GREY);

// Create the chain, add the basebone and enable base bone constraint mode
FabrikChain2D rightChain = new FabrikChain2D();
rightChain.setBaseboneConstraintType(BaseboneConstraintType2D.LOCAL_RELATIVE);
rightChain.addBone(basebone);

// Add two consecutive constrained bones to the chain
rightChain.addConsecutiveConstrainedBone(RIGHT, boneLength, 15.0f, 15.0f,
                                         Utils.GREY);
rightChain.addConsecutiveConstrainedBone(RIGHT, boneLength, 15.0f, 15.0f,
                                         Utils.GREY);

// Add the chain to the structure, connecting at the end of bone 1 in chain 0
structure.addConnectedChain(rightChain, 0, 1, BoneConnectionPoint2D.END);
```

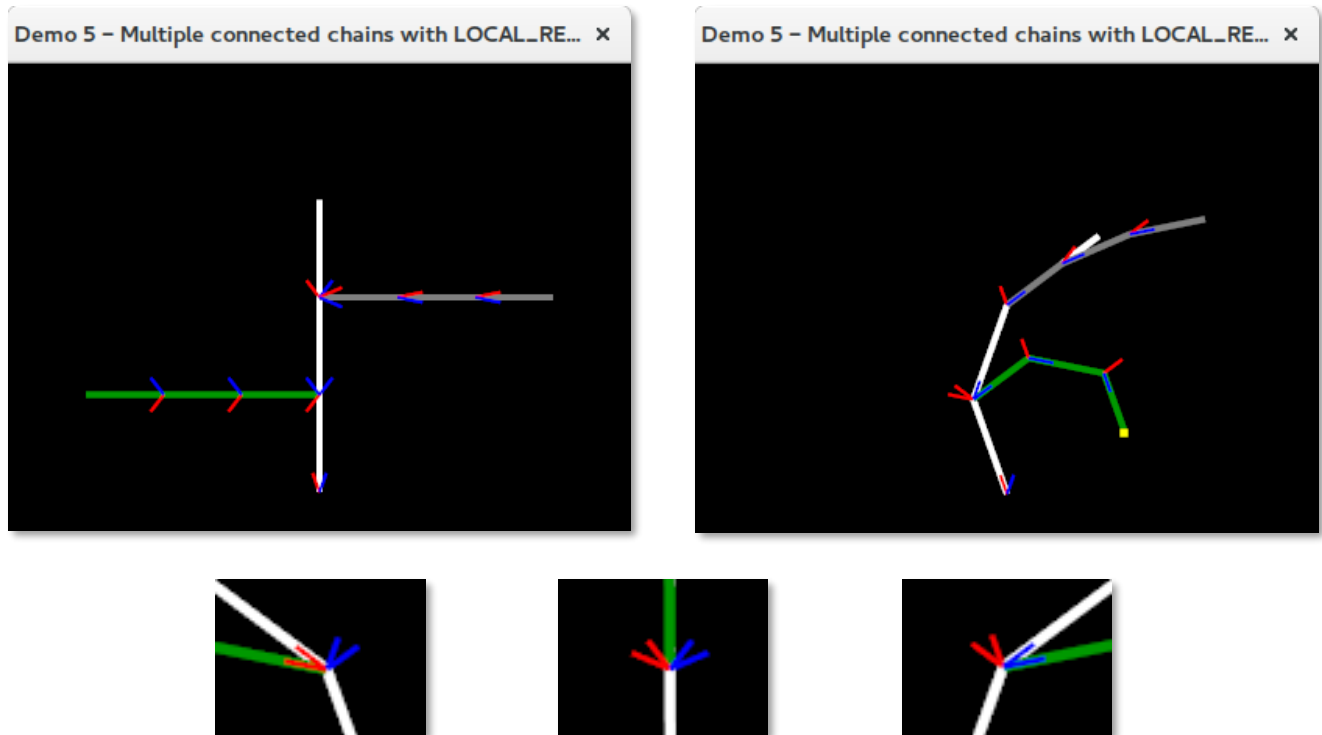


Figure 11 - Connected chains with local relative basebone constraints. (left) original configuration (right) example solved configuration. The white and grey chains are highly constrained in this example. The bottom row shows how the basebone constraints of the green chain move relative to the direction of the first bone in the white chain to which it is attached. Notice that the relative basebone constraints in the original configuration are not being honoured - this is because the structure as a whole has not been solved yet. When a solve attempt is made, all constraints are honoured.

2D Demo 6 - Multiple connected chains with LOCAL_ABSOLUTE basebone constraints

While LOCAL_RELATIVE basebone constraints are applied relative to the direction of the bone a chain is connected to, LOCAL_ABSOLUTE basebone constraints are applied as directions in the local coordinate space of the bone a chain is connected to.

For example, if a basebone constraint is the vector $(-1.0f, 0.0f)$ [i.e. LEFT], then:

- If the bone the chain is connected to is pointing directly upwards, then the 'local' left remains **left**,
- If the bone the chain is connected to is pointing directly left, then 'local' left is now **down**,
- If the bone the chain is connected to is pointing directly right, then 'local' left is now **up**.

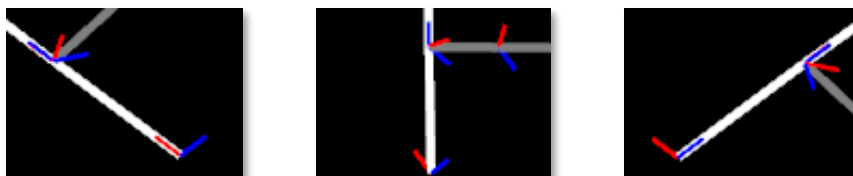


Figure 12 - The LOCAL_ABSOLUTE basebone constraint on the grey chain is set to RIGHT, but is maintained in the local space of the white 'host' bone that it's connected to.

LOCAL_ABSOLUTE basebone constraints can be set on a chain by specifying the constraint type **and** a constraint direction unit vector:

```
FabrikChain2D chain = new FabrikChain2D();
chain.setBaseboneConstraintType(BaseboneConstraintType2D.LOCAL_ABSOLUTE);
chain.setBaseboneConstraintUV(RIGHT);
// ...add bones to the chain here...
```

```
// If a chain has LOCAL basebone constraints it MUST be connected to another chain!  
structure.addConnectedChain(chain, 0, 0, BoneConnectionPoint2D.END);
```

2D Demo 7 – Chains with embedded targets

```
float boneLength = 50.0f;  
float startY    = -100.0f;  
mStructure = new FabrikStructure2D();  
  
FabrikChain2D chain = new FabrikChain2D();  
  
// ----- Central white chain -----  
// Create the first bone, configure it, and add it to the chain  
FabrikBone2D basebone;  
basebone = new FabrikBone2D(new Vec2f(0.0f, startY), new Vec2f(0.0f, startY +  
boneLength) );  
basebone.setClockwiseConstraintDegs(65.0f);  
basebone.setAnticlockwiseConstraintDegs(65.0f);  
chain.addBone(basebone);  
  
// Fix basebone to its current location, and constrain it to the positive Y-axis  
chain.setFixedBaseMode(true);  
chain.setBaseboneConstraintType(BaseboneConstraintType2D.GLOBAL_ABSOLUTE);  
chain.setBaseboneConstraintUV(UP);  
  
// Add second and third bones  
chain.addConsecutiveBone(UP, boneLength);  
chain.addConsecutiveBone(UP, boneLength);  
  
// Finally, add the chain to the structure  
mStructure.addChain(chain);  
  
// ----- Left green chain with embedded target -----  
FabrikChain2D leftChain = new FabrikChain2D();  
leftChain.setEmbeddedTargetMode(true); // Embedded target loc. set in demo loop  
basebone = new FabrikBone2D(new Vec2f(), new Vec2f(-boneLength / 6.0f, 0.0f) );  
  
// Add fifteen bones  
leftChain.addBone(basebone);  
for (int boneLoop = 0; boneLoop < 15; ++boneLoop)  
{  
    leftChain.addConsecutiveConstrainedBone(RIGHT, boneLength / 6.0f, 25.0f,  
25.0f);  
}  
  
// Set chain colour and basebone constraint type  
leftChain.setColour(Utils.MID_GREEN);  
  
// Add the left chain to the structure, connected to the start of bone 1 in chain 0  
mStructure.addConnectedChain(leftChain, 0, 1, BoneConnectionPoint2D.START);  
  
// ----- Right grey chain with embedded target -----  
FabrikChain2D rightChain = new FabrikChain2D();  
rightChain.setEmbeddedTargetMode(true); // Embedded target loc. set in demo loop  
basebone = new FabrikBone2D(new Vec2f(), new Vec2f(boneLength / 5.0f, 0.0f) );  
basebone.setClockwiseConstraintDegs(60.0f);  
basebone.setAnticlockwiseConstraintDegs(60.0f);  
  
// Add ten bones  
rightChain.addBone(basebone);  
for (int boneLoop = 0; boneLoop < 10; ++boneLoop)  
{  
    rightChain.addConsecutiveBone(RIGHT, boneLength / 5.0f);  
}
```

```

}

// Set chain colour and basebone constraint type
rightChain.setColour(Utils.GREY);
rightChain.setBaseboneConstraintType(BaseboneConstraintType2D.LOCAL_ABSOLUTE);
rightChain.setBaseboneRelativeConstraintUV(RIGHT);

// Add the right chain to the structure, connected to the start of bone 2 in chain
// 0
mStructure.addConnectedChain(rightChain, 0, 2, BoneConnectionPoint2D.START);

```

Chains that use embedded targets can have those targets updated by calls to the **updateEmbeddedTarget()** method.

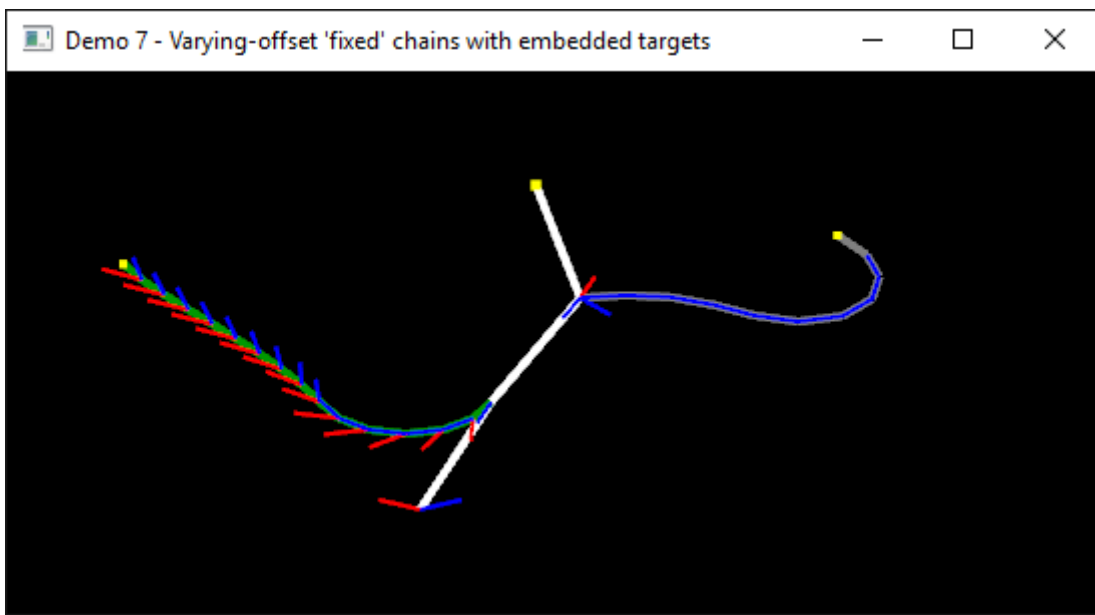


Figure 13 - Multiple connected chains with 'fixed' bases. The left and right chains use embedded targets which are updated separately via calls to the chain's **updateEmbeddedTarget** method.

2D Demo 8 – Multiple Nested Chains in a Semi Random Configuration

Just an example of nesting chains.

```

// Instantiate our FabrikStructure2D
this.structure = new FabrikStructure2D("Demo 8 - Multiple nested chains in a semi-
random configuration");

this.structure.addChain( createRandomChain() );
int chainsInStructure = 1;

int maxChains = 3;
for (int chainLoop = 0; chainLoop < maxChains; chainLoop++)
{
    FabrikChain2D tempChain = createRandomChain();

    tempChain.setBaseboneConstraintType(BaseboneConstraintType2D.LOCAL_RELATIVE);
    tempChain.setBaseboneConstraintUV(UP);

    this.structure.connectChain( createRandomChain(), Utils.randRange(0,
chainsInStructure++), Utils.randRange(0, 5) );
}

private FabrikChain2D createRandomChain()

```

```

{
    float boneLength          = 20.0f;
    float boneLengthRatio     = 0.8f;
    float constraintAngleDegs = 20.0f;
    float constraintAngleRatio = 1.4f;

    // ----- Vertical chain -----
    FabrikChain2D chain = new FabrikChain2D();
    chain.setFixedBaseMode(true);

    FabrikBone2D basebone = new FabrikBone2D( new Vec2f(), UP, boneLength);
    basebone.setClockwiseConstraintDegs(constraintAngleDegs);
    basebone.setAnticlockwiseConstraintDegs(constraintAngleDegs);

    chain.setBaseboneConstraintType(BaseboneConstraintType2D.LOCAL_RELATIVE);
    chain.addBone(basebone);

    int numBones = 6;
    float perturbLimit = 0.4f;
    for (int boneLoop = 0; boneLoop < numBones; boneLoop++)
    {
        boneLength      *= boneLengthRatio;
        constraintAngleDegs *= constraintAngleRatio;
        Vec2f perturbVector = new Vec2f( Utils.randRange(-perturbLimit,
        perturbLimit), Utils.randRange(-perturbLimit, perturbLimit) );

        chain.addConsecutiveConstrainedBone( UP.plus(perturbVector),
        boneLength, constraintAngleDegs, constraintAngleDegs );

    }

    chain.setColour( Colour4f.randomOpaqueColour() );

    return chain;
}

```

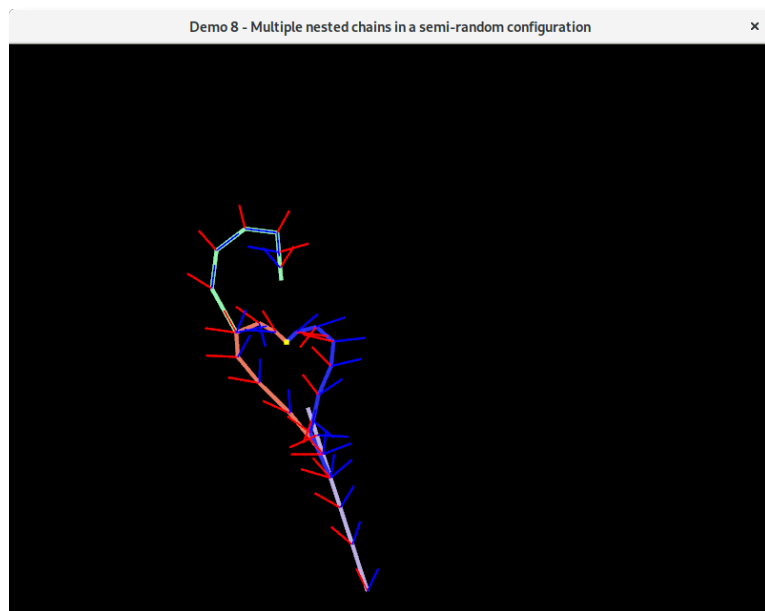


Figure 14 - Multiple nested chains all being solved for the same target location.

2D Demo 9 - World-Space 2D Constraints

An example of specifying that 2D joint constraints should be interpreted in world-space coordinates rather than in the coordinate system of the previous bone in the chain (which is the default).

```
// Instantiate our FabrikStructure2D
this.structure = new FabrikStructure2D("Demo 9 - Chain with fixed base and world
space (GLOBAL) bone constraints.");

// Create a new chain
FabrikChain2D chain = new FabrikChain2D();

float boneLength = 40.0f;

// Create and add first bone - 25 clockwise, 90 anti-clockwise
FabrikBone2D basebone;
basebone = new FabrikBone2D(new Vec2f(0.0f, -boneLength), new Vec2f(0.0f, 0.0f) );
basebone.setClockwiseConstraintDegs(90.0f);
basebone.setAnticlockwiseConstraintDegs(90.0f);
chain.addBone(basebone);

// Fix the base bone to its current location, and constrain it to the positive Y-
axis
chain.setFixedBaseMode(true);
chain.setBaseboneConstraintType(BaseboneConstraintType2D.GLOBAL_ABSOLUTE);
chain.setBaseboneConstraintUV( new Vec2f(0.0f, 1.0f) );

chain.addConsecutiveBone(UP, boneLength);
chain.addConsecutiveBone(UP, boneLength);

// Create and add the fourth 'gripper' bone - locked in place facing right (i.e. 0
// degree movement allowed both clockwise & anti-clockwise)
// Note: The start location of (50.0f, 50.0f) is ignored because we're going to add
// this to the end of the chain, wherever that may be.
FabrikBone2D gripper = new FabrikBone2D(new Vec2f(50.0f, 50.0f), RIGHT, boneLength
/ 2.0f, 30.0f, 30.0f);

gripper.setJointConstraintCoordinateSystem(ConstraintCoordinateSystem.GLOBAL);
gripper.setGlobalConstraintUV(RIGHT);
chain.addConsecutiveBone(gripper);

// Finally, add the chain to the structure
this.structure.addChain(chain);
```

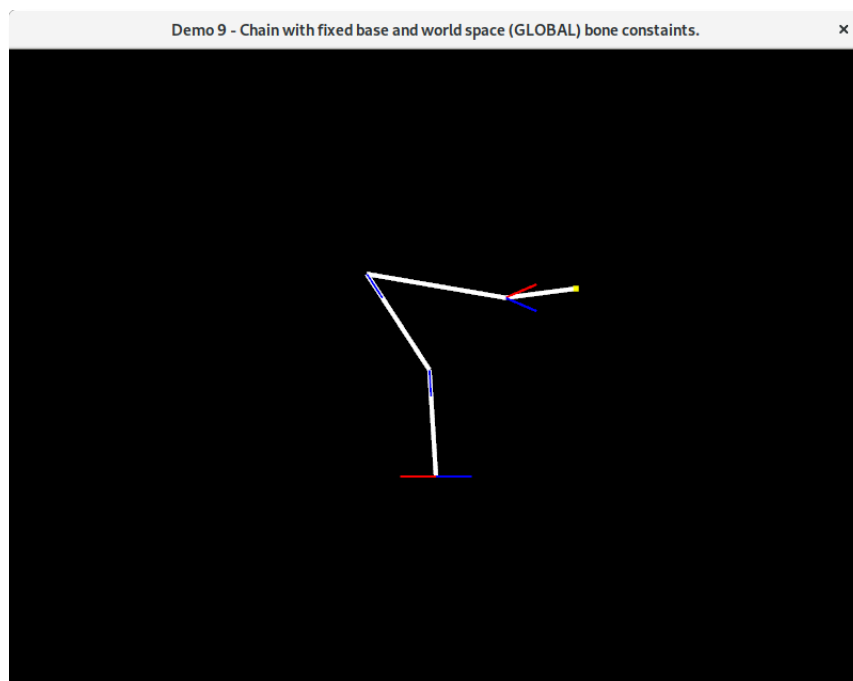


Figure 15 - An example of creating a chain with bones where the constraint angles are always treated to be about a world-space direction rather than relative to the direction of the previous bone in the chain.

3D Demo 1 - Unconstrained bones

```
FabrikStructure3D structure = new FabrikStructure3D();
FabrikChain3D chain        = new FabrikChain3D();
Colour4f colour            = new Colour4f(Utils.GREEN);
float boneLength           = 10.0f;
Vec3f boneDirection        = Z_AXIS.negated(); // i.e. into the screen

// Create a basebone and then add it to the chain
Vec3f start = new Vec3f(0.0f, 0.0f, 40.0f);
Vec3f end   = start.plus( defaultBoneDirection.times(boneLength) );
FabrikBone3D basebone = new FabrikBone3D(start, end);
basebone.setColour(colour);
chain.addBone(basebone);

// Add additional consecutive, unconstrained bones to the chain
for (int boneLoop = 0; boneLoop < 7; boneLoop++) {
    colour = (boneLoop % 2 == 0) ? colour.lighten(0.4f) : colour.darken(0.4f);
    chain.addConsecutiveBone(boneDirection, boneLength, colour);
}

// Finally, add the chain to the structure
structure.addChain(chain);
```

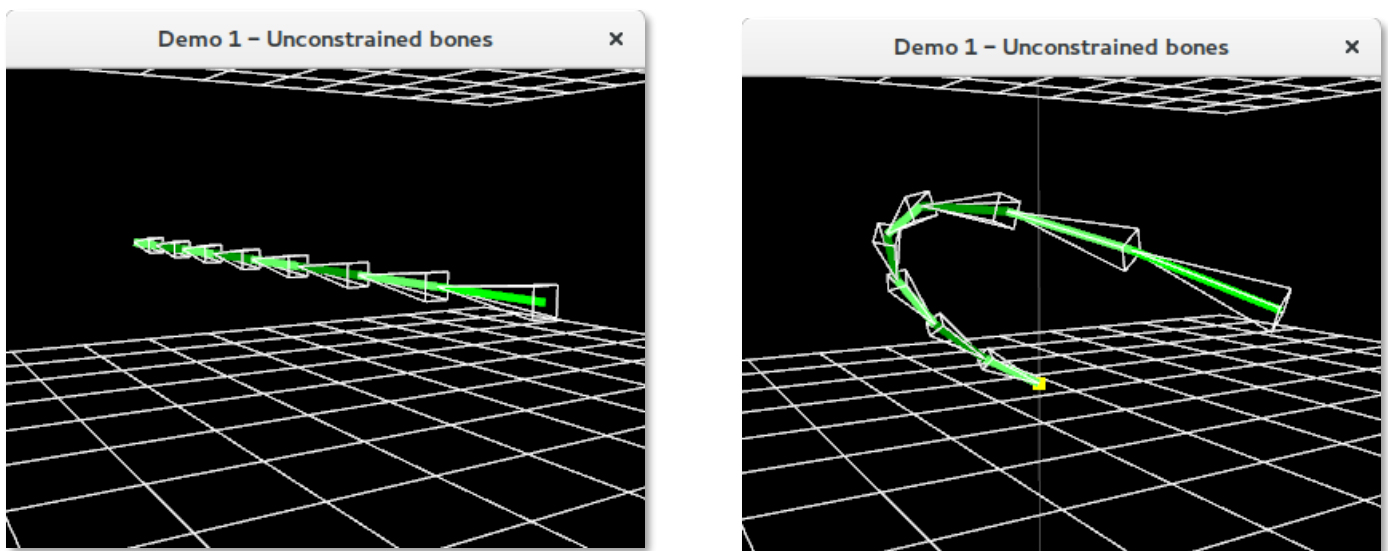


Figure 16 - A 3D chain containing unconstrained bones (left) in their initial and (right) in an example solved state.

3D Demo 2 - Rotor / ball joint constrained bones

```
FabrikStructure3D structure = new FabrikStructure3D();
int numChains              = 3;
float rotStep               = 360.0f / (float)numChains;
float constraintDegs        = 45.0f;
Colour4f colour             = new Colour4f();
float boneLength            = 10.0f;
Vec3f boneDirection        = Z_AXIS.negated(); // i.e. into the screen

// Create chains and set colours
for (int chainLoop = 0; chainLoop < numChains; ++chainLoop) {
    FabrikChain3D chain = new FabrikChain3D();
    switch (chainLoop % numChains) {
        case 0: boneColour.set(Utils.MID_RED); break;
        case 1: boneColour.set(Utils.MID_GREEN); break;
        case 2: boneColour.set(Utils.MID_BLUE); break;
    }
}
```

```

// Set up the initial base bone location...
Vec3f startLoc = new Vec3f(0.0f, 0.0f, -40.0f);
startLoc      = Vec3f.rotateYDegs(startLoc, rotStep * (float)chainLoop);
Vec3f endLoc   = new Vec3f(startLoc);
endLoc.z      -= defaultBoneLength;

// ...then create a base bone, set its colour and add it to the chain.
FabrikBone3D basebone = new FabrikBone3D(startLoc, endLoc);
basebone.setColour(colour);
chain.addBone(basebone);

// Add additional consecutive rotor constrained bones to the chain
for (int boneLoop = 0; boneLoop < 7; ++boneLoop) {
    colour = (boneLoop % 2 == 0) ? colour.lighten(0.4f) :
                                     colour.darken(0.4f);

    chain.addConsecutiveRotorConstrainedBone(boneDirection, boneLength,
                                              constraintDegs, colour);
}
// Finally, add the chain to the structure
structure.addChain(chain);
}

```

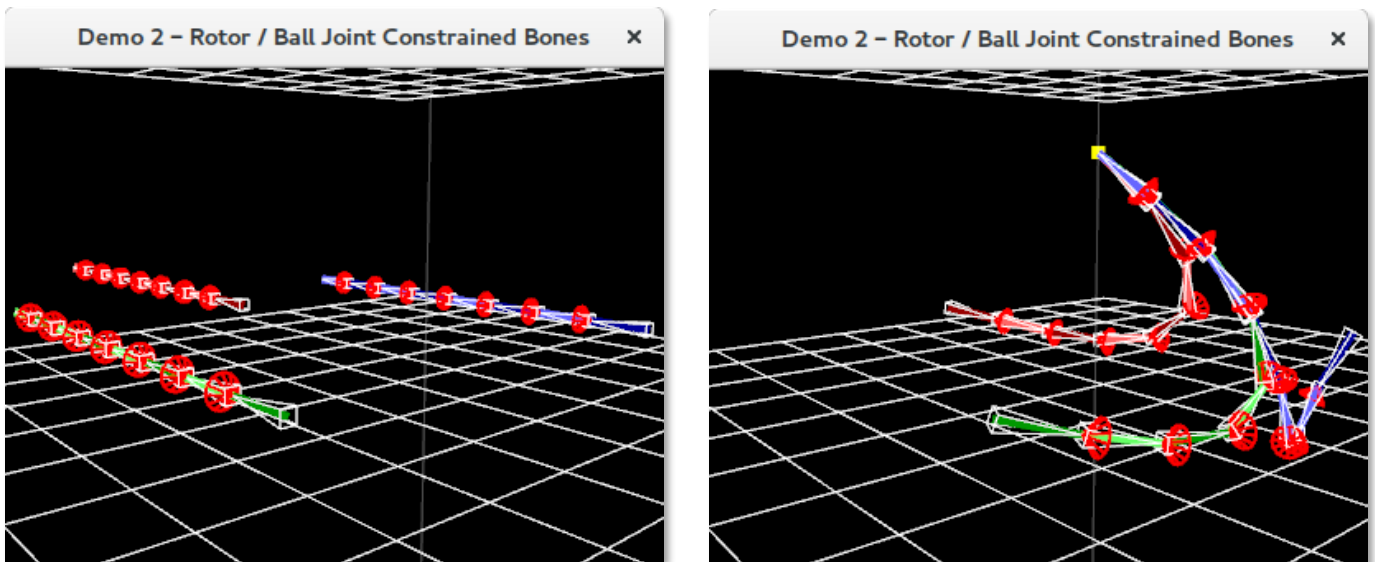


Figure 17 - Chains with 45 degree rotor constrained bones (left) in their initial state and (right) in an example solved state.

3D Demo 3 - Chains with rotor constrained basebones

```

FabrikStructure3D structure = new FabrikStructure3D();
int numChains              = 3;
float rotStep               = 360.0f / (float)numChains;
Colour4f colour             = new Colour4f();
Colour4f bbColour           = new Colour4f();
Vec3f bbConstraintAxis      = new Vec3f();
float bbConstraintDegs      = 20.0f;

for (int chainLoop = 0; chainLoop < numChains; ++chainLoop) {
    // Set bone colours and basebone constraint axes
    switch (chainLoop % 3) {
        case 0:
            colour.set(Utils.MID_RED);
            bbColour.set(Utils.RED);
            bbConstraintAxis = X_AXIS;
            break;
    }
}

```



```

    case 1:
        colour.set(Utils.MID_GREEN);
        bbColour.set(Utils.MID_GREEN);
        bbConstraintAxis = Y_AXIS;
        break;
    case 2:
        colour.set(Utils.MID_BLUE);
        bbColour.set(Utils.BLUE);
        bbConstraintAxis = Z_AXIS.negated();
        break;
}

// Create a new chain and set up the basebone start/end locations
FabrikChain3D chain = new FabrikChain3D();
Vec3f start = new Vec3f(0.0f, 0.0f, -40.0f);
start = Vec3f.rotateYDegs(start, rotStep * (float)chainLoop);
Vec3f end = start.plus( bbConstraintAxis.times(defaultBoneLength * 2.0f) );

// ...then create a base bone, set its colour, add it to the chain
FabrikBone3D basebone = new FabrikBone3D(start, end);
basebone.setColour(baseBoneColour);
chain.addBone(basebone);

// EITHER: Set the basebone to be global rotor constrained:
chain.setRotorBaseboneConstraint(BaseboneConstraintType3D.GLOBAL_ROTOR,
                                baseBoneConstraintAxis, baseBoneConstraintAngleDegs);

// OR: Freely-rotating global hinge constrained:
chain.setFreelyRotatingGlobalHingedBasebone(Y_AXIS);

// OR: Non-freely-rotating global hinge constrained
// Params: hinge axis, clockwise angle, anticlockwise angle, reference axis
chain.setGlobalHingeBaseboneConstraint(Y_AXIS, 90.0f, 45.0f, X_AXIS);

// Add additional consecutive, unconstrained bones to the chain
for (int boneLoop = 0; boneLoop < 7; ++boneLoop) {
    colour = (boneLoop % 2 == 0) ? colour.lighten(0.5f) :
                                   colour.darken(0.5f);
    chain.addConsecutiveBone(defaultBoneDirection, defaultBoneLength,
                             colour);
}
// Finally, add the chain to the structure
structure.addChain(chain);
}

```

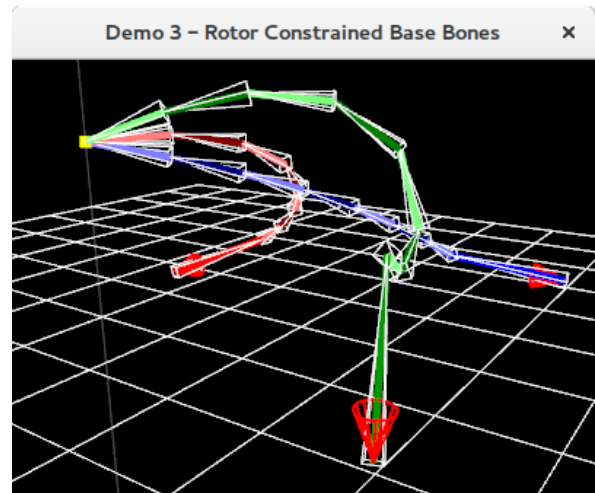
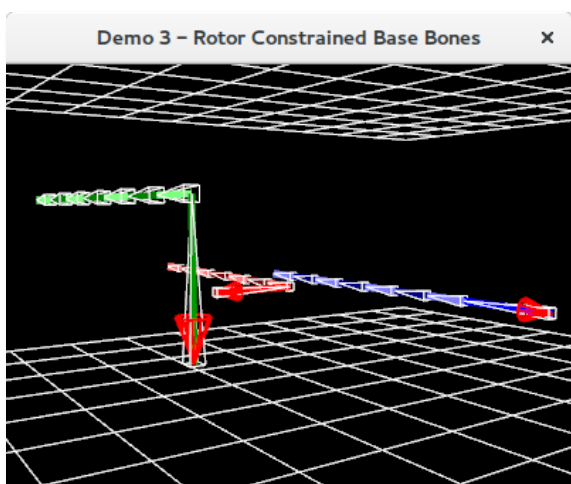


Figure 18 - Chains with rotor constrained basebones (left) in their initial configuration and (right) in an example solved configuration.

3D Demo 4 - Chains with freely rotating global hinges

```

FabrikStructure3D structure = new FabrikStructure3D();
int numChains              = 3;
float rotStep               = 360.0f / (float)numChains;
Vec3f boneDirection         = Z_AXIS.negated(); // i.e. into the screen
float boneLength             = 10.0f;

// Create a circular arrangement of 3 chains with varying global hinged bones
Vec3f hingeAxis = new Vec3f();
for (int chainLoop = 0; chainLoop < numChains; ++chainLoop) {
    // Set colour and axes
    Colour4f chainColour = new Colour4f();
    switch (chainLoop % numChains) {
        case 0:
            chainColour.set(Utils.RED);    hingeAxis = X_AXIS; break;
        case 1:
            chainColour.set(Utils.GREEN);  hingeAxis = Y_AXIS; break;
        case 2:
            chainColour.set(Utils.BLUE);   hingeAxis = Z_AXIS; break;
    }

    // Create a new chain and set the start and end locations...
    FabrikChain3D chain = new FabrikChain3D();
    Vec3f start = new Vec3f(0.0f, 0.0f, -40.0f);
    start = Vec3f.rotateYDegs(start, rotStep * (float)chainLoop);
    Vec3f end = startLoc.plus( boneDirection.times(boneLength) );

    // ...then create a base bone, set its colour, and add it to the chain.
    FabrikBone3D basebone = new FabrikBone3D(startLoc, endLoc);
    basebone.setColour(chainColour);
    chain.addBone(basebone);

    // Add alternating global hinge and unconstrained bones to the chain
    for (int boneLoop = 0; boneLoop < 7; ++boneLoop) {
        if (boneLoop % 2 == 0) {
            chain.addConsecutiveFreelyRotatingHingedBone(boneDirection,
                boneLength, JointType.GLOBAL_HINGE, globalHingeAxis, Utils.GREY);
        } else {
            chain.addConsecutiveBone(boneDirection, boneLength, chainColour);
        }
    }

    // Finally, add the chain to the structure
    structure.addChain(chain);
}

```

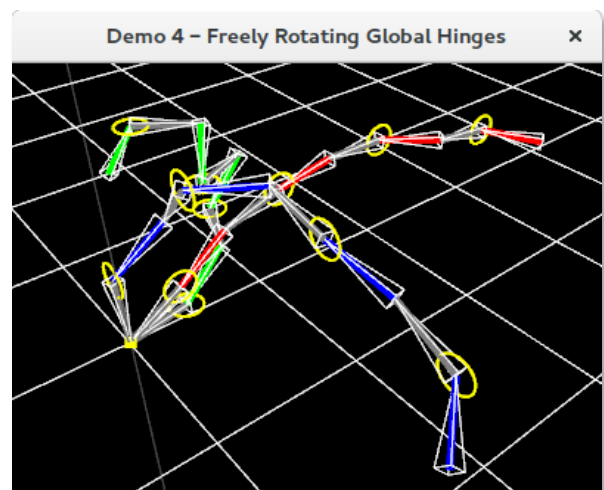
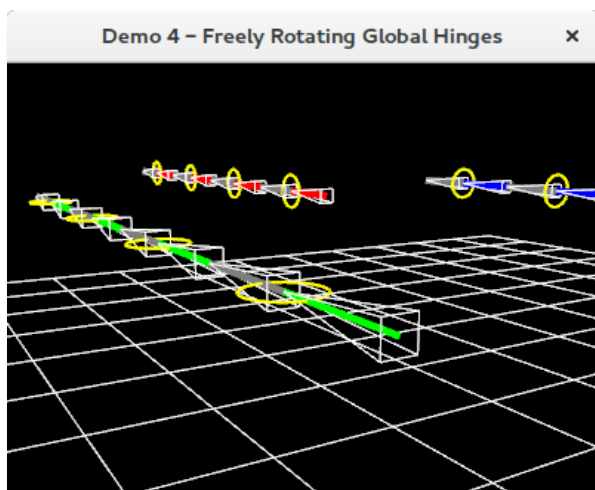


Figure 19 - Chains with global hinged bones (left) in their original and (right) in an example solved configuration.

3D Demo 5 - Global hinges with reference axis constraints

```

FabrikStructure3D structure = new FabrikStructure3D();
FabrikChain3D chain       = new FabrikChain3D();
Vec3d down               = Y_Axis.negated();
float boneLength          = 10.0f;

// Set up the initial base bone location...
Vec3f startLoc = new Vec3f(0.0f, 30f, -40.0f);
Vec3f endLoc   = new Vec3f(startLoc);
endLoc.y      -= defaultBoneLength;

// ...then create a base bone, set its colour, and add it to the chain.
FabrikBone3D basebone = new FabrikBone3D(startLoc, endLoc);
basebone.setColour(Utils.YELLOW);
chain.addBone(basebone);

// Add alternating global hinge constrained, and unconstrained bones to the chain
float cwDeps = 120.0f;
float acwDeps = 120.0f;
for (int boneLoop = 0; boneLoop < 8; ++boneLoop) {
    if (boneLoop % 2 == 0) {
        // Params: bone direction, bone length, joint type, hinge rotation
        // axis, clockwise constraint angle, anticlockwise constraint angle,
        // hinge constraint reference axis, colour
        // Note: There is a version of this method where you do not specify the
        // colour - the default is to draw the bone in white.
        chain.addConsecutiveHingedBone(down, boneLength, JointType.GLOBAL_HINGE,
                                         Z_AXIS, cwDeps, acwDeps, down, Utils.GREY);
    } else {
        chain.addConsecutiveBonedown(down, defaultBoneLength, Utils.MID_GREEN);
    }
}

// Finally, add the chain to the structure
structure.addChain(chain);

```

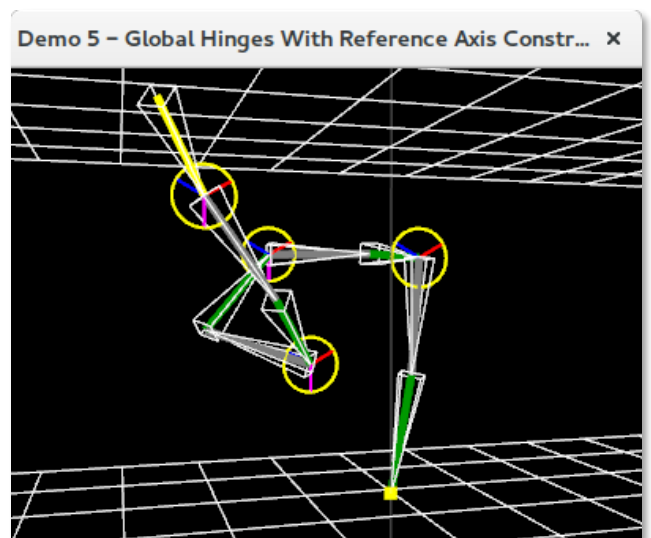
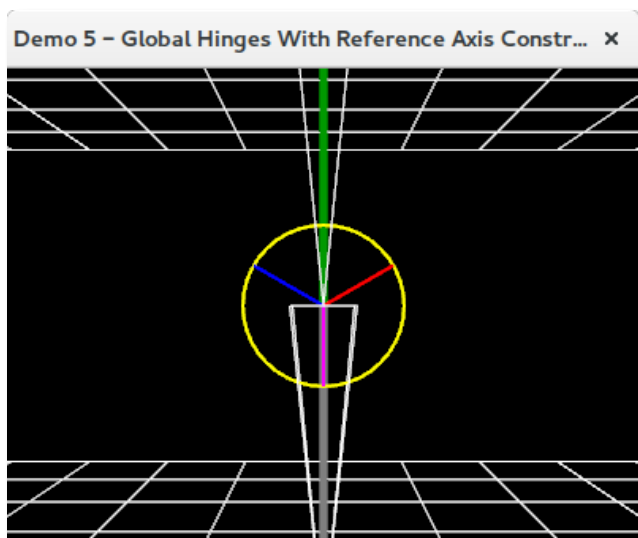


Figure 20 - A chain containing global hinges with reference axes. Anticlockwise (red) and clockwise (blue) constraint angles are measured with respect to the hinge reference axis (cyan). On the left is close-up of a hinge, while the right images show an example solved configuration.

3D Demo 6 - Chains with local hinges

```

FabrikStructure3D structure = new FabrikStructure3D();
int numChains              = 3;
float rotStep              = 360.0f / (float)numChains;
Vec3f rotationAxis        = new Vec3f();
Vec3f referenceAxis        = new Vec3f();
Vec3f boneDirection        = Z_AXIS.negated(); // i.e. into the screen
float boneLength           = 10.0f;

// We'll create a circular arrangement of 3 chains with alternate bones each
// constrained about different local axes. Note: Local hinge rotation axes are
// relative to the generated rotation matrix of the previous bone in the chain.
for (int chainLoop = 0; chainLoop < numChains; ++chainLoop) {
    // Set colour and axes. Reference axes must be in the plane of hinge axes.
    Colour4f chainColour = new Colour4f();
    switch (loop % numChains) {
        case 0:
            chainColour = Utils.RED;
            rotationAxis = new Vec3f(X_AXIS);
            referenceAxis = new Vec3f(Y_AXIS);
            break;
        case 1:
            chainColour = Utils.GREEN;
            rotationAxis = new Vec3f(Y_AXIS);
            referenceAxis = new Vec3f(X_AXIS);
            break;
        case 2:
            chainColour = Utils.BLUE;
            rotationAxis = new Vec3f(Z_AXIS);
            referenceAxis = new Vec3f(Y_AXIS);
            break;
    }

    // Create a new chain and set the basebone start and end locations
    FabrikChain3D chain = new FabrikChain3D();
    Vec3f start = new Vec3f(0.0f, 0.0f, -40.0f);
    start = Vec3f.rotateYDegs(start, rotStep * (float)chainLoop);
    Vec3f end = start.plus(boneDirection.times(boneLength));

    // ...then create a base bone, set its colour, and add it to the chain.
    FabrikBone3D basebone = new FabrikBone3D(startLoc, endLoc);
    basebone.setColour(chainColour);
    chain.addBone(basebone);

    // Add alternating local hinge and unconstrained bones to the chain
    float constraintDegs = 90.0f;
    for (int boneLoop = 0; boneLoop < 6; ++boneLoop) {
        if (boneLoop % 2 == 0) {
            // EITHER: For no reference constraints:
            chain.addConsecutiveFreelyRotatingHingedBone(boneDirection,
                boneLength, JointType.LOCAL_HINGE, hingeAxis, Utils.GREY);

            // OR: To apply reference constraints:
            chain.addConsecutiveHingedBone(boneDirection, boneLength,
                JointType.LOCAL_HINGE, rotationAxis, constraintDegs,
                constraintDegs, referenceAxis, Utils.GREY);
        } else {
            chain.addConsecutiveBone(boneDirection, boneLength, chainColour);
        }
    }
    // Finally, add the chain to the structure
    structure.addChain(chain);
}

```

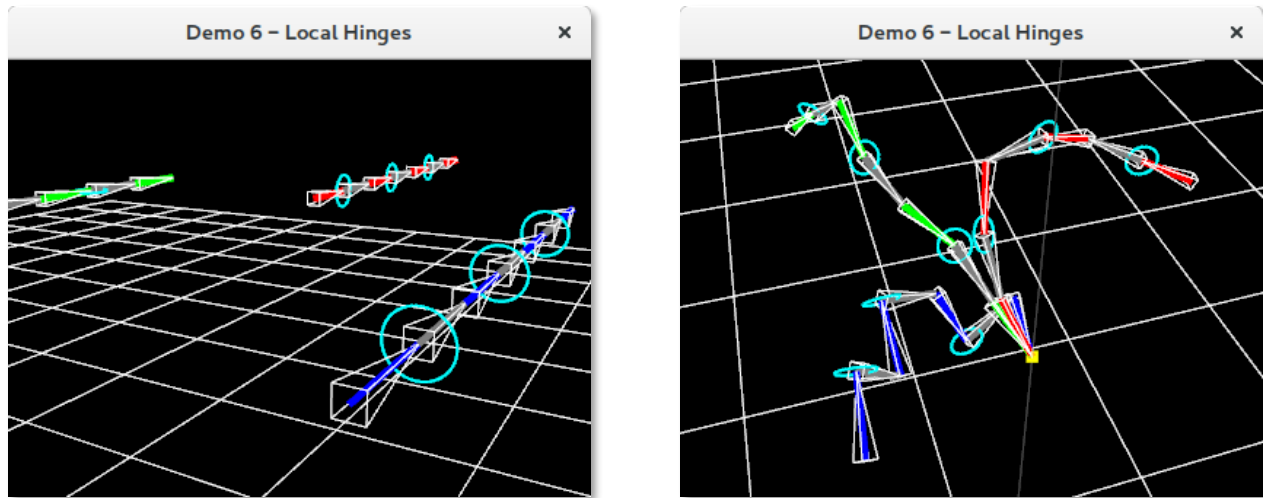


Figure 21 - Chains with local hinges shown (left) in their initial configuration and (right) in an example solved configuration. Each local hinge's rotation axis and reference axis are converted into the coordinate system of the previous bone in the chain before being enforced.

3D Demo 7 - Connecting chains

```
FabrikStructure3D structure = new FabrikStructure3D();
FabrikChain3D chain = new FabrikChain3D();
Colour4f colour = new Colour4f(Utils.GREEN);
Vec3f boneDirection = Z_AXIS.negated(); // i.e. into the screen
float boneLength = 10.0f;

// Create a new chain, set basebone start and end locations then add to chain
Vec3f start = new Vec3f(0.0f, 0.0f, 40.0f);
Vec3f end = start.plus( boneDirection.times(boneLength) );
FabrikBone3D basebone = new FabrikBone3D(start, end);
basebone.setColour(colour);
chain.addBone(basebone);

// Add additional consecutive, unconstrained bones to the chain
for (int boneLoop = 0; boneLoop < 5; boneLoop++) {
    colour = (boneLoop % 2 == 0) ? colour.lighten(0.4f) : colour.darken(0.4f);
    chain.addConsecutiveBone(defaultBoneDirection, defaultBoneLength, colour);
}

// Add the chain to the structure and create a second chain (base location isn't
// particularly important, it'll 'snap' to the connection point on the first chain)
structure.addChain(chain);
FabrikChain3D secondChain = new FabrikChain3D();
FabrikBone3D base = new FabrikBone3D( new Vec3f(100.0f), new Vec3f(110.0f) );
secondChain.addBone(base);

// We may optionally choose to constrain the chain we are connecting to the first
// chain about a global rotor constraint, for example, 45 degrees about the X-axis.
secondChain.setRotorBaseboneConstraint(BaseboneConstraintType3D.GLOBAL_ROTOR,
                                       X_AXIS, 45.0f);

secondChain.addConsecutiveBone(X_AXIS, 20.0f);
secondChain.addConsecutiveBone(Y_AXIS, 20.0f);
secondChain.addConsecutiveBone(Z_AXIS, 20.0f);

// Set the colour of all bones in the chain then connect it to the first chain...
// Params: chain we're connecting, host chain number, host bone number, conn. point
secondChain.setColour(Utils.RED);
```

```

structure.connectChain(secondChain, 0, 0, BoneConnectionPoint3D.START);

// We can keep adding the same chain at various points if we like, because the
// chain we connect is actually a clone of the one we provide, and not the
// original 'secondChain' object
secondChain.setColour(Utils.WHITE);

// Basebone constraints may be set on the connecting chain as desired prior to
// connection by using the following methods:

// For GLOBAL_ROTOR:
secondChain.setRotorBaseboneConstraint(BaseboneConstraintType3D.GLOBAL_ROTOR,
X_AXIS, 45.0f);

// For LOCAL_ROTOR:
secondChain.setRotorBaseboneConstraint(BaseboneConstraintType3D.LOCAL_ROTOR,
X_AXIS, 45.0f);

// For GLOBAL_HINGE:
secondChain.setFreelyRotatingGlobalHingedBasebone(Y_AXIS);

// For GLOBAL_HINGE with reference constraints:
secondChain.setGlobalHingeBaseboneConstraint(Y_AXIS, 90.0f, 45.0f, X_AXIS);

// For LOCAL_HINGE:
secondChain.setFreelyRotatingLocalHingedBasebone(Y_AXIS);

// For LOCAL_HINGE with reference constraints:
secondChain.setLocalHingeBaseboneConstraint(Y_AXIS, 90.0f, 45.0f, X_AXIS);

// Once any basebone constraints have been applied, we're free to add the chain to
// the structure - in this case we're connecting our secondChain to the end of bone
// 1 in chain 0.
structure.connectChain(secondChain, 0, 1, BoneConnectionPoint3D.END);

```

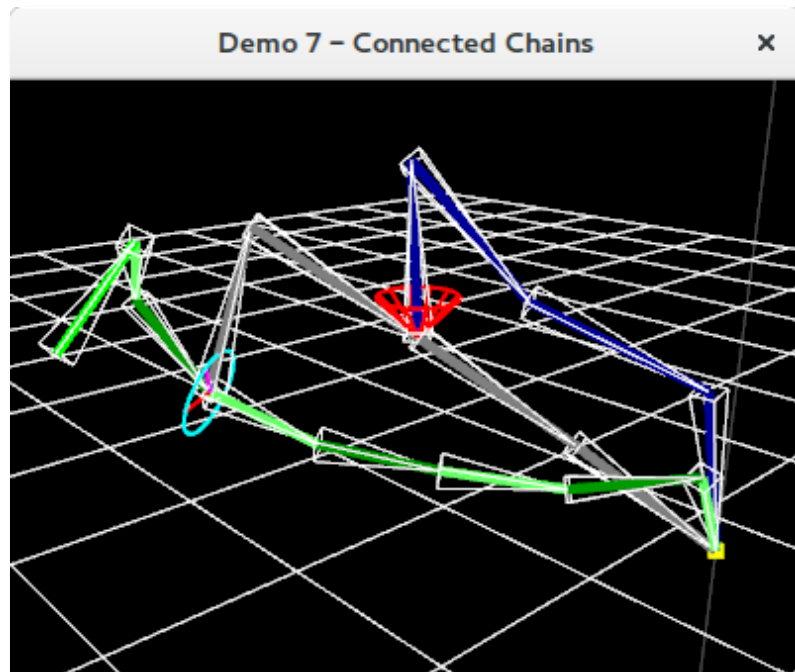


Figure 22 - A chain with a global rotor basebone constraint (in blue) attached to a chain with a local hinge with reference axis basebone constraint (in grey) attached to a chain without any basebone constraint (in green).

3D Demo 12 – Connected chains with embedded targets

Note: We jump from demo 7 to demo 12 here as demos 8 through 11 show variations on a theme

```
mStructure                = new FabrikStructure3D(demoName);
Colour4f boneColour       = new Colour4f(Utils.GREEN);

// Create a new chain...
FabrikChain3D chain = new FabrikChain3D();

// ...then create a basebone, set its draw colour and add it to the chain.
Vec3f startLoc          = new Vec3f(0.0f, 0.0f, 40.0f);
Vec3f endLoc             = startLoc.plus(
    defaultBoneDirection.times(defaultBoneLength) );
FabrikBone3D basebone = new FabrikBone3D(startLoc, endLoc);
basebone.setColour(boneColour);
chain.addBone(basebone);

// Add additional consecutive, unconstrained bones to the chain

for (int boneLoop = 0; boneLoop < 7; boneLoop++)
{
    boneColour = (boneLoop % 2 == 0) ? boneColour.lighten(0.4f) :
                                           boneColour.darken(0.4f);
    chain.addConsecutiveBone(defaultBoneDirection, defaultBoneLength,
    boneColour);
}

// Finally, add the chain to the structure
mStructure.addChain(chain);

// Create a second chain which will be connected to the first and will use an
// embedded target (specified in the main loop)
FabrikChain3D secondChain = new FabrikChain3D("Second Chain");
secondChain.setEmbeddedTargetMode(true);
FabrikBone3D base = new FabrikBone3D( new Vec3f(), new Vec3f(15.0f, 0.0f, 0.0f) );
secondChain.addBone(base);

// Set this second chain to have a freely rotating global hinge which rotates about
// the Y axis. Note: We MUST add the basebone to the chain before we can set the
// basebone constraint on it.
secondChain.setHingeBaseboneConstraint(BaseboneConstraintType3D.GLOBAL_HINGE,
Y_AXIS, 90.0f, 45.0f, X_AXIS);

// Add some additional bones
secondChain.addConsecutiveBone(X_AXIS, 20.0f);
secondChain.addConsecutiveBone(X_AXIS, 20.0f);
secondChain.addConsecutiveBone(X_AXIS, 20.0f);
secondChain.setColour(Utils.GREY);

// Connect this second chain to the start point of bone 3 in chain 0 of the struct
mStructure.connectChain(secondChain, 0, 3, BoneConnectionPoint3D.START);
```

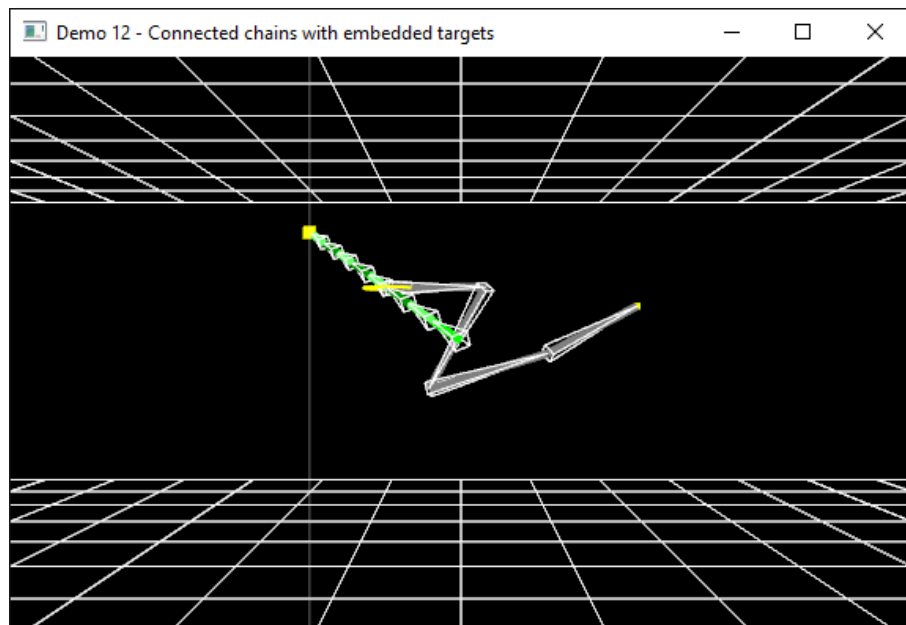


Figure 23 - Connected chains with embedded target locations (i.e. multiple end-effectors in a single structure). When embedded target mode is enabled for a chain then solving that chain uses the embedded target rather than any provided target location.
