

# Stochastic Boosting

## Algorithm: Gradient Boosted Trees for Classification

Input: training set  $Z = \{(\mathbf{x}_1, y_1), \dots, (\mathbf{x}_n, y_n)\}$ ,  
M – number of iterations

1.  $f_0(x) = \log \frac{p_1}{1-p_1}$   $p_1$ - part of objects of first class
2. For  $m=1 \dots M$ :
3.  $g_i = \frac{dL(y_i, f_m(\mathbf{x}_i))}{df_m(\mathbf{x}_i)}$
4. Fit a decision tree  $h_m(\mathbf{x}_i)$  to the target  $g_i$   
(auxiliary training set  $\{(\mathbf{x}_1, g_1), \dots, (\mathbf{x}_n, g_n)\}$ )
5.  $\rho_m = \underset{\rho}{\operatorname{argmax}} Q[f_{m-1}(\mathbf{x}) + \rho h_m(\mathbf{x})]$
6.  $f_m(\mathbf{x}) = f_{m-1}(\mathbf{x}) + \mathbf{v} \rho_m h_m(\mathbf{x}_i)$
7. Return:  $f_M(\mathbf{x})$

$\mathbf{v}$  - regularization (learningRate), recommended  $\leq 0.1$

## Algorithm: Gradient Boosted Trees for Classification **+Stochastic Boosting**

Input: training set  $\{(\mathbf{x}_1, y_1), \dots, (\mathbf{x}_n, y_n)\}$ , M – number of iterations

1.  $f_0(x) = \frac{1}{n} \sum_{i=1}^n y_i$
2. For  $m=1 \dots M$ :
3.  $g_i = \frac{dL(y_i, f_m(x_i))}{df_m(x_i)}$
4. Fit a decision tree  $h_m(\mathbf{x}_i)$  to the target  $g_i$   
(auxiliary training set  $\{(\mathbf{x}_1, g_i), \dots, (\mathbf{x}_k, g_k)\}$ ),  **$k=0.5n$   
created by random sampling with replacement**
5.  $\rho_m = \underset{\rho}{\operatorname{argmax}} Q[f_{m-1}(\mathbf{x}) + \rho h_m(\mathbf{x})]$
6.  $f_m(\mathbf{x}) = f_{m-1}(\mathbf{x}) + v \rho_m h_m(\mathbf{x}_i)$
7. Return  $f_M(\mathbf{x})$

$v$  - regularization (learningRate), recommended  $\leq 0.1$

# Sampling with Replacement

n=8

1	2	3	4	5	6	7	8
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k=4

7	3	1	3
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# Stochastic Boosting

- ▶ Improved performance
- ▶ Improved predictive power