

Quiz 2:

Problem 1: 2'

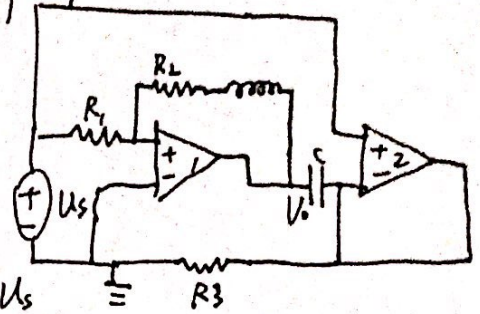
(1) ① Isolate two stages

② Reduce the influence between two circuits

(2) By the property

$$\frac{V_2 - V_1}{R_1} = \frac{V_1 - V_0}{R_2} \Rightarrow V_0 = V_1 - \frac{R_2}{R_1} \cdot (V_2 - V_1)$$

Since $V_1 = 0$ (gnd) $\Rightarrow V_0 = -\frac{R_2}{R_1} \cdot V_2$



Since + (positive) side of op-amp 2 is connected to V_2

So the right side of capacitor is V_2 .

$$V_C = V_2 - (-V_2 \cdot \frac{R_2}{R_1}) = \frac{R_1 + R_2}{R_1} V_2$$

So the energy stored in capacitor C is

$$\frac{1}{2} C \cdot \left(\frac{R_1 + R_2}{R_1} V_2 \right)^2$$

Problem 2: 1.5'

$$V_0 = -RC \frac{dV_i}{dt} = -20000 \Omega \times 0.01 \times 10^{-6} F \cdot \frac{dV_i}{dt}$$

I. $\frac{dV_i}{dt} = 10 \times 10^3 \frac{V}{s}$ $0 < t < 1 \text{ ms}$

II. $\frac{dV_i}{dt} = -10 \times 10^3 \frac{V}{s}$ $1 < t < 3 \text{ ms}$

III. $\frac{dV_i}{dt} = 10 \times 10^3 \frac{V}{s}$ $3 < t < 4 \text{ ms}$

So $V_0 = -2 \text{ V}$ $0 < t < 1 \text{ ms}$

$V_0 = 2 \text{ V}$ $1 < t < 3 \text{ ms}$

$V_0 = -2 \text{ V}$ $3 < t < 4 \text{ ms}$

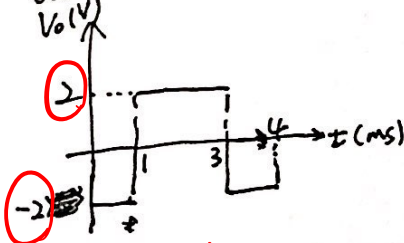
$0 < t < 1 \text{ ms}$

$1 < t < 3 \text{ ms}$

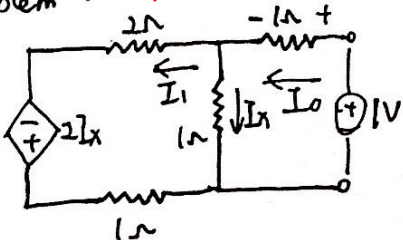
$3 < t < 4 \text{ ms}$

1' for shape

0.5' for 2 values.



Problem 3: 1.5'



Assume input voltage 1V. and input current I_0

By KVL:

$$\begin{cases} -2I_1 + I_x - I_1 + 2I_x = 0 \\ I_0 + I_x - 1 = 0 \end{cases} \Rightarrow \begin{cases} I_x - I_1 = 0 \\ I_0 + I_x = 1 \end{cases}$$

$$\Rightarrow I_0 = \frac{2}{3} \text{ A} \quad I_x = \frac{1}{3} \text{ A}$$

$$I_0 = I_x + I_1$$

Since there is no independent source, to calculate V_{TH} . $I_N = 0$.

$$I_x \cdot 1 + I_x \cdot 1 + I_x \cdot 2 + 2I_x = 0 \Rightarrow V_{TH} = 0$$

$$\text{And } R_N = \frac{1V}{I_0} = \frac{1V}{\frac{2}{3}A} = \frac{3}{2} \Omega$$

So equivalent circuit:

