

Quiz 2:

Problem 1: 2'

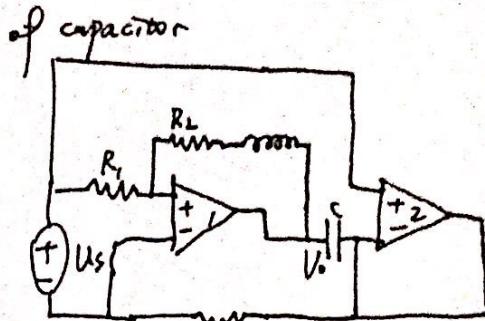
(1) ① Isolate two stages

② Reduce the influence between two circuits

(2) By the property V_o is the voltage of left side of capacitor

$$\frac{V_G - V_1}{R_1} = \frac{V_1 - V_o}{R_2} \Rightarrow V_o = V_1 - \frac{R_2}{R_1} \cdot (V_s - V_1)$$

$$\text{Since } \frac{V_1 - V_o}{R_1} = 0 \cdot (\text{ground}) \Rightarrow V_o = -\frac{R_2}{R_1} \cdot V_s$$



Since + (positive) side of op-amp 2 is connected to V_s $\frac{V_o}{R_3} = V_s$

So the right side of capacitor is V_s . $V_C = V_s - (-V_s \cdot \frac{R_2}{R_1}) = \frac{R_1 + R_2}{R_1} V_s$

So the energy stored in capacitor C is

$$\frac{1}{2} C \cdot \left(\frac{R_1 + R_2}{R_1} V_s \right)^2$$

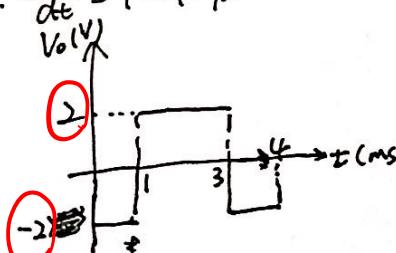
Problem 2: 1.5'

$$V_o = -RC \frac{dV_i}{dt} = -20000 \Omega \times 0.01 \times 10^{-6} F \cdot \frac{dV_i}{dt}$$

$$\text{I. } \frac{dV_i}{dt} = 10 \times 10^3 \frac{V}{s} \quad 0 < t < 1 \text{ ms}$$

$$\text{II. } \frac{dV_i}{dt} = -10 \times 10^3 \frac{V}{s} \quad 1 < t < 3 \text{ ms}$$

$$\text{III. } \frac{dV_i}{dt} = 10 \times 10^3 \frac{V}{s} \quad 3 < t < 4 \text{ ms}$$

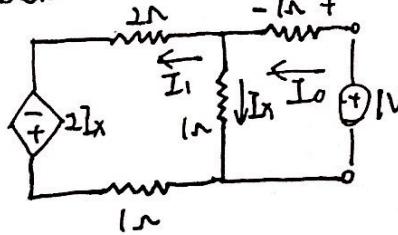


$$\text{So } V_o = -2 \text{ V. } \quad 0 < t < 1 \text{ ms}$$

$$V_o = 2 \text{ V. } \quad 1 < t < 3 \text{ ms}$$

$$V_o = -2 \text{ V. } \quad 3 < t < 4 \text{ ms}$$

Problem 3: 1.5'



Assume input voltage 1V. and input current I_o

By KVL:

$$\begin{cases} -2I_1 + I_x - I_1 + 2I_x = 0 \\ I_o + I_x - 1 = 0 \end{cases} \Rightarrow \begin{cases} I_x - I_1 = 0 \\ I_o + I_x = 1 \end{cases} \Rightarrow I_o = \frac{2}{3} A \quad I_x = \frac{1}{3} A.$$

$$I_o = I_x + I_1$$

Since there is no independent source, to calculate V_{TH} . $0.5'$

$$I_x \cdot 1 + I_x \cdot 1 + I_x \cdot 2 + 2I_x = 0 \Rightarrow V_{TH} = 0 \text{ for norton } I_N = 0.$$

$$\text{And } R_N = \frac{1V}{I_o} = \frac{1V}{\frac{2}{3} A} = \frac{3}{2} \Omega$$

0.5'

So equivalent circuit:

$$I_N = 0 \quad R_N = \frac{3}{2} \Omega$$

0.5'