The problem tries to change the amortized cost from 1 per bit to  $2^d$  for the d-th bit. I've decided to use the aggregated method.

We can consider how often we flip each individual bit, and sum those up to bound the total, rather than individually obtaining a worst case bound for each bit. From the analysis in class, we know that d-th bit toggled every  $2^d$  time, e.g. the second bit toggle every twice time.

If the counter now counts up to n, we can write down how frequent the bits are toggled,

$$n + \lfloor \frac{n}{2} \rfloor + \lfloor \frac{n}{4} \rfloor + \cdots$$

$$\leq n + \frac{n}{2} + \frac{n}{4} + \cdots$$

$$\leq 2n$$
(1)

so the time to count to n is 2n.

But the amortized cost is changed from 1 to  $2^d$  to flip a bit, where d is the position of the bit in the counter. For every increment, it needs two flip to perform a toggle, therefore, the price is  $2^{d+1}$ . Divide it and we can know the answer.