第一题

- 1) find_name_value 的主要功能是从一个数据目录名中提取变量名和变量值,并将它们作为一个元组 (其中变量值为浮点型) 返回,目录名的格式是 <name><value> ,如果是负值则在变量值后会有 n 表示。
- 2) 编写测试函数如下,经过测试,函数功能实现如预期。

```
def test_find_name_value():
   test_cases = [
       # 正常输入(正浮点数)
       ("phi0.1"),
       # 正常输入(整数)
       ("xN14"),
       # 正常输入(负浮点数,后缀 'n')
       ("kappa0.5n"),
       # 正常输入(负整数,后缀 'n')
       ("yN30n"),
       # 边界输入(仅变量名,无数值)
       ("alpha"),
       # 边界输入(数值为零)
       ("beta0"),
       # 异常输入(数值格式不正确)
       ("g2ammaabn"),
       # 异常输入(带有额外字符但没有数值)
       ("zeta-xyz_"),
       # 边界输入(空字符串)
       (""),
       # 异常输入(只有数值)
       ("20.5n"),
   ]
   for i, input_data in enumerate(test_cases):
       result = find_name_value(input_data)
       print(result)
```

输出如下

```
('phi', 0.1)
('xN', 14.0)
('kappa', -0.5)
('yN', -30.0)
('alpha', None)
('beta', 0.0)
('g', 2.0)
('zeta-xyz_', None)
('', None)
('', -20.5)
```

3) 对于用下划线连接的文件名,原函数并不能正确解析,原函数仅能解析单个目录名,因此修改如下:

```
def find_name_value(folder_name):
    '''Split the name of a data directory into a list of (name, value) tuples.
```

```
The format of each segment in ``folder_name``:
    <name><value>
If the value is negative, it should be followed by a 'n'.
Args:
    folder_name (str): the name of a :term: `data directory`.
Returns:
    list: A list of tuples, where each tuple contains:
        * name (str): variable name.
        * value (float): value of the variable.
# 分割输入字符串
segments = folder_name.split('_')
results = []
# 解析每个部分
pattern = '([-+]?\d*\.\d+|[-+]?\d+)'
for segment in segments:
    rst = re.split(pattern, segment)
    if len(rst) < 2:</pre>
        results.append((segment, None))
        continue
    name = rst[0]
    valuestr = rst[1]
    sign_str = ''
    if len(rst) > 2:
        sign_str = rst[2]
    if sign_str == 'n':
       value = '-' + valuestr
    else:
        value = valuestr
    results.append((name, float(value)))
return results
```

运行后得到结果

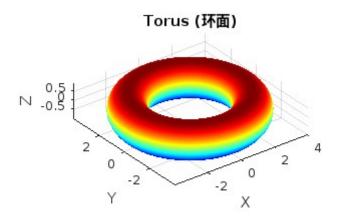
```
[('phi', 0.1), ('xN', 14.2), ('kappa', -0.5)]
[('a', 1.0), ('b', -14.0), ('n', 0.0), ('c', 0.2)]
```

第二题

```
R = 3;
r = 1;
theta = linspace(0, 2*pi, 100);
phi = linspace(0, 2*pi, 100);
[Theta, Phi] = meshgrid(theta, phi);
```

```
X = (R + r * cos(Theta)) .* cos(Phi);
Y = (R + r * cos(Theta)) .* sin(Phi);
Z = r * sin(Theta);

figure;
surf(X, Y, Z);
shading interp;
colormap jet;
axis equal;
xlabel('X');
ylabel('Y');
zlabel('Z');
title('Torus (环面)');
```



第三题

$$Sum[1/(n^3 + n^2), \{n, 1, Infinity\}]$$

结果为 $-1 + \frac{\pi^2}{6}$

Integrate[Sqrt[x] Log[x]/(x + 1)
2
, {x, 0, Infinity}]

结果为 π

第四题

 \mathbf{Q} : Find the solution of the following equation with respect to θ :

$$A\cos\theta + B\sin\theta + C = 0$$

\mathbf{A} :

let $x_1 = \cos \theta$ and $x_2 = \sin \theta$, then the solution is given by the intersection of the circle and the line:

$$x_1^2 + x_2^2 = 1$$

 $Ax_1 + Bx_2 + C = 0$

We reformulate the equations in a parametric form:

$$|\mathbf{x}|^2 = 1$$

 $\mathbf{x}(t) = \mathbf{a} + t\mathbf{b}$

where $\mathbf{x} = (x_1, x_2)$, $\mathbf{a} = (0, -C/B)$, $\mathbf{b} = (-C/A, C/B)$, and t is a parameter. The intersection points satisfy the following equation:

$$|\mathbf{a} + t\mathbf{b}|^2 = 1$$

which can be solved for t to find the intersection points:

$$t_{1,2} = rac{-\mathbf{a}\cdot\mathbf{b}\pm\sqrt{(\mathbf{a}\cdot\mathbf{b})^2-|\mathbf{b}|^2(|\mathbf{a}|^2-1)}}{|\mathbf{b}|^2}$$