<u>从程序优化角度,我们的课程安排</u>

- Week 1: Tuning for In-core programming
- Week 2: Tools: Intel compiler and Vtune
- Week 3: Tuning for Parallel programming
- Week 4: Show case

并行程序性能分析与优化

本主题的内容

- •并行程序性能优化
 - •如何来分析并行程序的性能?
 - •并行程序有哪些性能问题?
 - •如何优化并行程序性能?
 - •哪些工具帮助我们诊断并行程序的性能问题?

分析的问题

•如何量度一个程序的性能?

•如何衡量一个并行程序的好坏?

并行程序性能指标和性能模型

通用的性能评价指标

•程序执行时间

是指用户的响应时间(访问磁盘和访问存储器的时间, CPU时间, I/O时间以及操作系统的开销) Linux: gettimeofday(us) / clock_gettime (ns)

- Windows: QueryPerformanceFrequency / QueryPerformanceCounter
- MPI_Wtime/MPI_Wtick
- 获取并行程序时间
 - 1. Barrier
 - 2. Start Timer
 - 3. Run Program
 - 4. End Timer
 - 5. Max(EndTime[i]-StartTime[i])

Speedup

- The speedup of a parallel application is
 Speedup(p) = Time(1)/Time(p)
- Where
 - Time(1) = execution time for a single processor and
 - Time(p) = execution time using p parallel processors
- If Speedup(p) = p we have perfect speedup (also called linear scaling)
- As defined, speedup compares an application with itself on one and on p processors, but it is more useful to compare
 - The execution time of the best serial application on 1 processor

versus

The execution time of best parallel algorithm on p processors

Superlinear Speedup

Question: can we find "superlinear" speedup, that is Speedup(p) > p?

- Choosing a bad "baseline" for T(1)
 - Old serial code has not been updated with optimizations
 - Avoid this, and always specify what your baseline is
- Shrinking the problem size per processor
 - May allow it to fit in small fast memory (cache)
- Application is not deterministic
 - Amount of work varies depending on execution order
 - Search algorithms have this characteristic

Efficiency

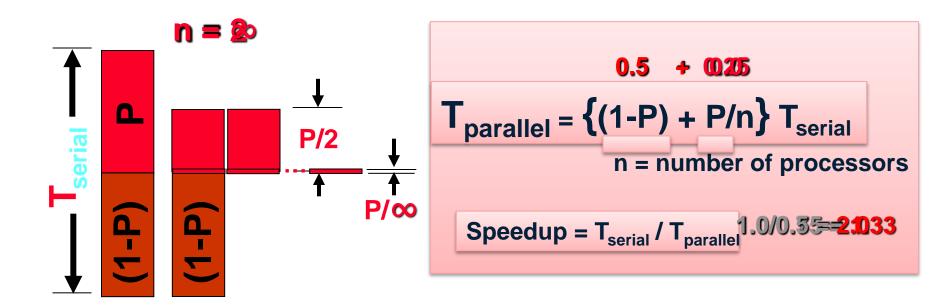
- The parallel efficiency of an application is defined as
 Efficiency(p) = Speedup(p)/p
 - Efficiency(p) ≤ 1
 - For perfect speedup Efficiency (p) = 1
- We will rarely have perfect speedup.
 - Lack of perfect parallelism in the application or algorithm
 - Imperfect load balancing (some processors have more work)
 - Cost of communication
 - Cost of contention for resources, e.g., memory bus, I/O
 - Synchronization time
- Understanding why an application is not scaling linearly will help finding ways improving the applications performance on parallel computers.

并行程序性能分析 - 性能模型

- •加速比定律
 - 并行系统的加速比是指对于一个给定的应用 ,并行算法(或并行程序)的执行速度相对 于串行算法(或串行程序)的执行速度加快 了多少倍。
 - Amdahl 定律
 - Gustafson定律
- 可扩放性评测标准
 - •等效率度量标准

Amdahl's Law

Describes the upper bound of parallel execution speedup

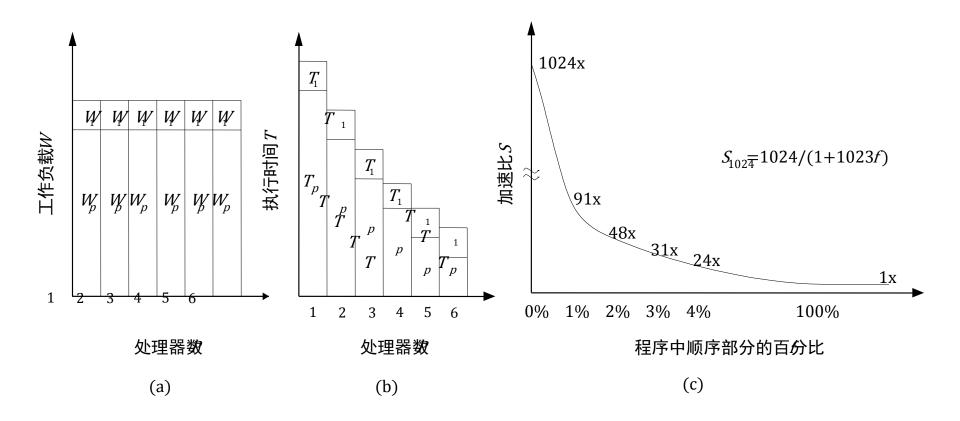


Serial code limits speedup

Amdahl 定律

- P: 处理器数;
- W: 问题规模(计算负载、工作负载, 给定问题的总计算量);
 - W_s : 应用程序中的串行分量,f是串行分量比例($f = W_s/W$, $W_s = W_1$);
 - W_p: 应用程序中可并行化部分, 1-f为并行分量比例;
 - $W_s + W_p = W$;
- $T_s = T_1$: 串行执行时间, T_p : 并行执行时间;
- S: 加速比, E: 效率;
- 出发点:
 - 固定不变的计算负载;
 - 固定的计算负载分布在多个处理器上并可以有效并行
 - 增加处理器加快执行速度,从而达到了加速的目的。

Amdahl定律



Gustafson定律

• 出发点:

- 对于很多大型计算,精度要求很高,即在此类应用中精度是个关键因素,而计算时间是固定不变的。此时为了提高精度,必须加大计算量,相应地亦必须增多处理器数才能维持时间不变
- 除非学术研究,在实际应用中没有必要固定工作负载而计算程序 运行在不同数目的处理器上,增多处理器必须相应地增大问题规模才有实际意义
- Gustafson加速定律: S'=—

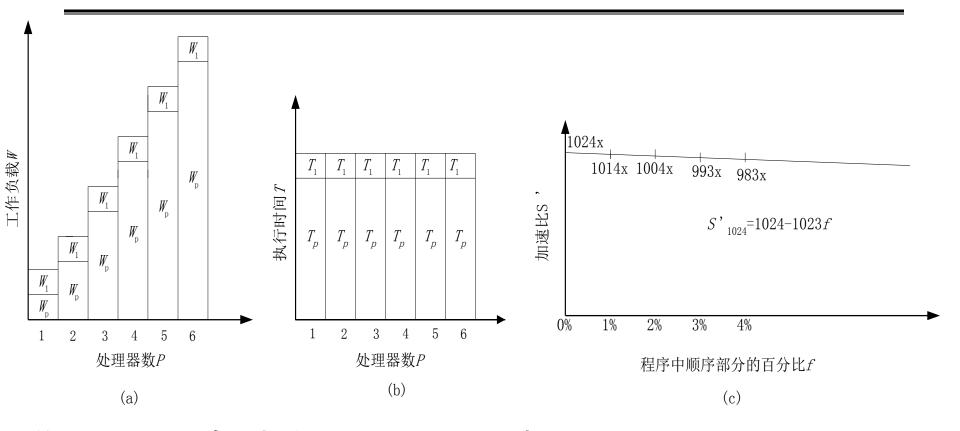
$$S' = \frac{W_S + pWp}{W_S + p \cdot Wp/p} = \frac{W_S + pWp}{W_S + W_P}$$

$$S' = f + p(1-f) = p + f(1-p) = p-f(p-1)$$

•并行开销Wo:

$$S' = \frac{W_S + pW_P}{W_S + W_P + W_O} = \frac{f + p(1 - f)}{1 + W_O / W}$$

Gustafson定律



增加问题的规模有利于提高加速的因素:

较大的问题规模可提供较高的并发度; 额外开销的增加可能慢于有效计算的增加; 算法中的串行分量比例不是固定不变的(串行部分所占的比例 随着问题规模的增大而缩小)。

14

加速比分析

- •影响加速比的因素:处理器数与问题规模
 - 加大的处理器数超过了算法中的并发程度
 - 求解问题中的串行分量
 - 并行处理所引起的额外开销(通信、等待、竞争、冗余操作和同步等)

粗略的串行程序流程



粗略的并行程序流程

启动多进程(线程),载入程序执行

任务划分

附加的流程

多进程(线程)初始数据载入

分进程(线程)计算

多进程(线程)通信与同步

多进程数据输出

结束计算,销毁多进程(线程)

理想的并行在哪里? 开销与性能问题在哪 里?

常见的并行开销有哪些?

- 1. 创建和销毁并行进程、线程的开销
 - 创建和销毁进程本身是高开销的工作
 - PowerPC 700MHz(每个周期 15ns 执行 4flops; 创建一个进程1.4ms,可执行 372,000flops)
 - 创建和销毁多个进程的开销在系统中随进程数增加
 - 启动4096进程可能需要s级时间

常见的并行开销有哪些?

- 通信开销是并行开销的主要部分
 - 多机间的通信开销相对于计算很大
 - Cray T3E
 - FP peak: 900 Mflops → 1.11 nanoseconds/flop
 - Communication using MPI (Message Passing Interface):
 - Latency: 3 microseconds (~ 2702 FPs)
 - Bandwidth: 120 MB/s (~ 60 FPs/double-word)
 - IBM SP Power3
 - FP peak: 1.5 Gflops → 0.67 nanoseconds/flop
 - Communication using MPI:
 - Latency: 8 microseconds (~ 11940 FPs)
 - Bandwidth: 347 MB/s (~ 35 FPs/double-word)
 - Linux Pentium3 cluster (J. Riedy, UC Berkeley)
 - FP peak: 700 Mflops → 1.43 nanoseconds/flop
 - Communication
 - Latency: 80 microseconds (~55944 FPs)
 - Bandwidth: 40 MB/s (~ 140 FPs/double-word)

量度点对点通信开销

- Transfer time $(n) = T_0 + n/B$
 - useful for message passing, memory access
- As *n* increases, bandwidth approaches asymptotic rate
- How quickly it approaches depends on T_{ρ} (latency)

量度群集通信开销

• 典型的群集通信

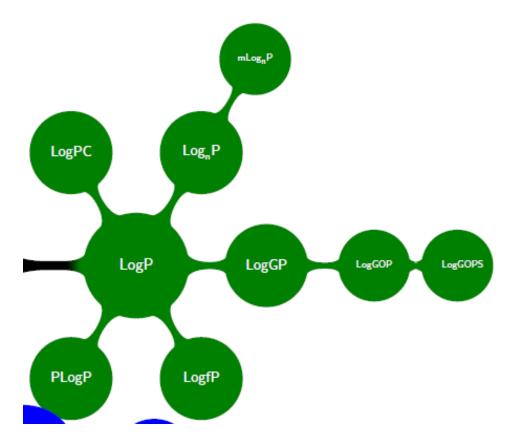
- •广播(Broadcasting):处理器0发送m个字节给所有的n个处理器;
- 收集(Gather): 处理0接收所有n个处理器发来在消息, 所以处理器0最终接收了mn个字节;
- 散射(Scatter):处理器0发送了m个字节的不同消息给所有n个处理器,因此处理器0最终发送了mn个字节;
- •全交换(Total Exchange):每个处理器均彼此相互 发送m个字节的不同消息给对方,所以总通信量为 mn²个字节;
- T (m, n) = t_0 (n) + m/ r_{∞} (n)

通信性能依平台和实现不同而变化,可以参考http://mvapich.cse.ohio-state.edu/benchmarks/或者IMB完成MPI通信测试

It is not so easy......

- 通信模型参数会因很多因素不同而变化
 - 同时通信的进程数
 - 同时发送的消息数
 - 消息的大小
 - 网络的拓扑结构
 - 网络的拥挤程度
 - 不同的MPI实现
 - 群集消息通信算法
 - 之前发送的消息情况

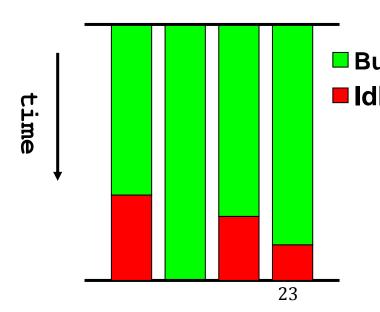
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Threading Issues for performance

- Data Races introduce performance issues
 - Concurrent access of same variable by multiple threads
 - Synchronization
 - Share data access must be coordinated
 - Explicit and implicit Barrier in OMP
 - Be aware of memory model and implicit barrier (parallel/for/single)

(paramer/ for / single)	
Fortran	C/C++
BARRIER END PARALLEL CRITICAL and END CRITICAL END DO END SECTIONS END SINGLE ORDERED and END	barrier parallel - upon entry and exit critical - upon entry and exit ordered - upon entry and exit for - upon exit sections - upon exit single - upon exit

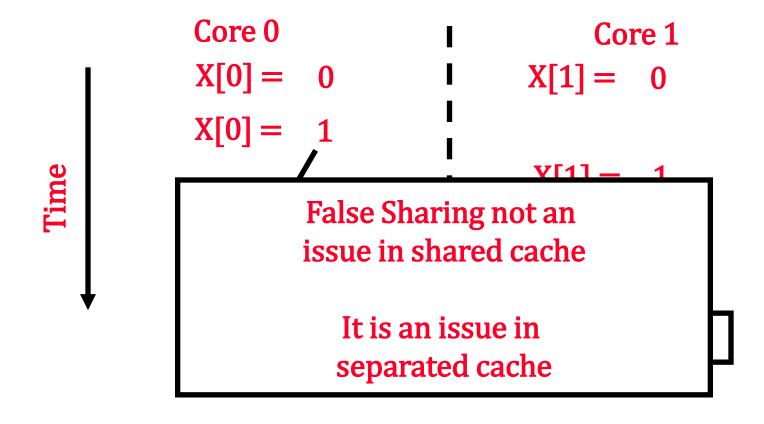


Threading Issues for performance

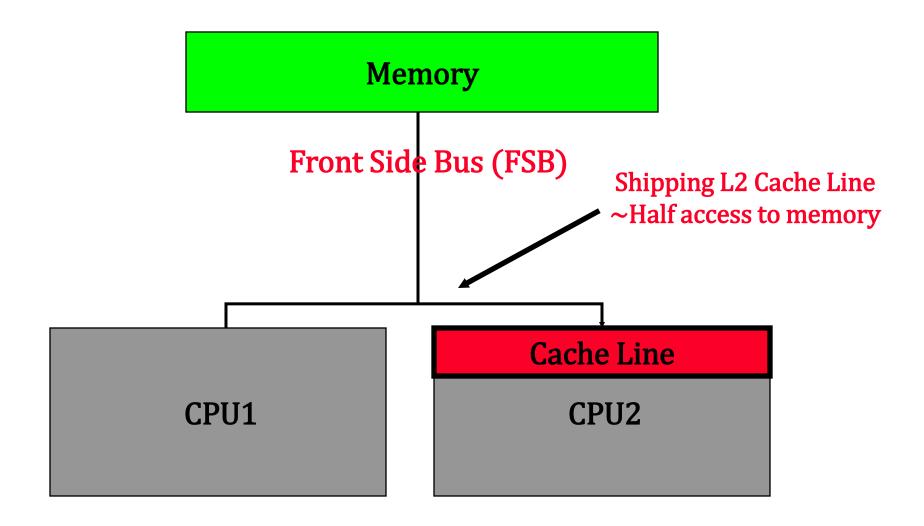
- Data Races introduce performance issues
 - Mutex
 - Atomic /critical /reduction will lead to serial computation
 - 优化策略:减小串行范围,减少同步次数
 - Dead Locks
 - Indefinite wait for resources, caused by locking hierarchy in threads
 - False Sharing
 - Threads writing different data on the same cache line

False Sharing

- Performance issue in programs where cores may write to different memory addresses BUT in the same cache lines
- Known as Ping-Ponging Cache line is shipped between cores

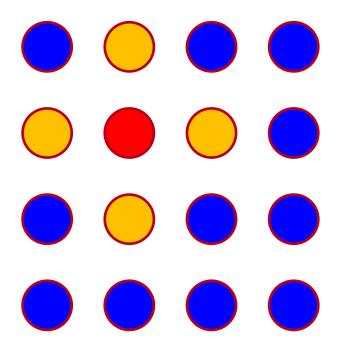


With a separated cache



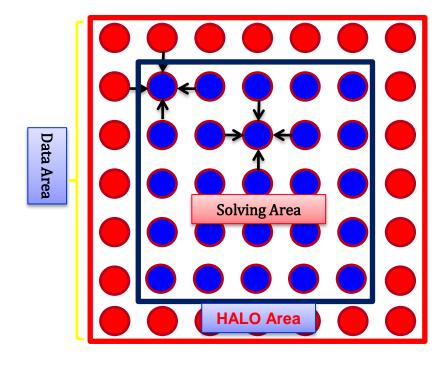
常见的并行开销还有哪些?

•并行化过程中引入的空间和相应的时间开销

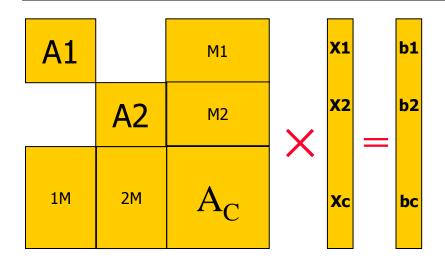


常见的并行开销还有哪些?

- •并行化过程中引入的空间和相应的时间开销
 - •消息缓冲区准备
 - •交叠数据的分配和使用



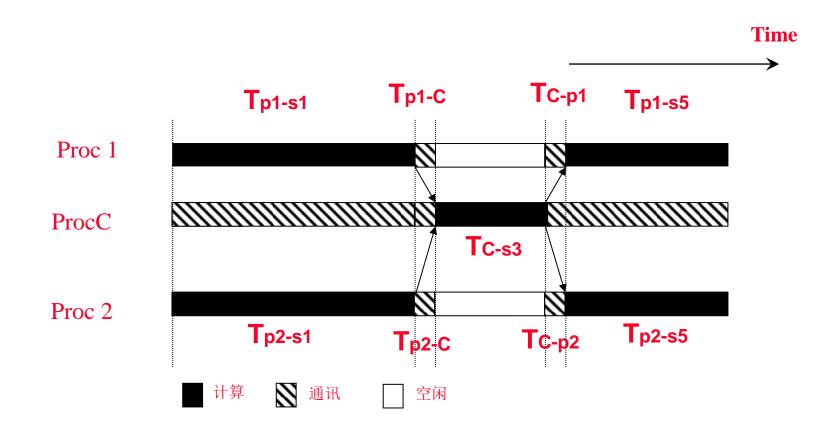
例子



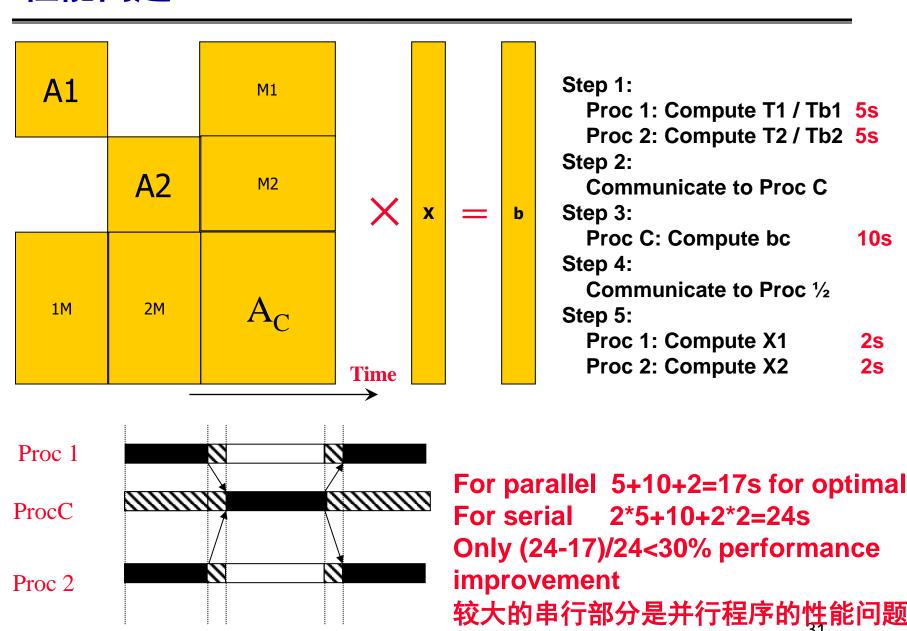
```
Step 1:
  Proc 1: Compute T1=-1M * inv(A1) * M1; Tb1= -1M * inv(A1) * b1 Tp1-s1
  Proc 2: Compute T2=-2M * inv(A2) * M2; Tb2= -2M * inv(A2) * b2 Tp2-s1
Step 2:
                                             Tp1-C / Tp2-C
  Communicate T1/Tb1, T2/Tb2 to Proc C
Step 3:
  Proc C: Compute bc by (AC-T1-T2)*Xc=bc-Tb1-Tb2
Step 4:
                                             Tc-p1 / Tc-p2
  Communicate Xc to Proc 1, Proc2
Step 5:
                                             Tp1-s5
  Proc 1: Compute X1
                                             Tp2-s5
  Proc 2: Compute X2
```

例子

• 从性能角度, 你希望是怎样的并行执行过程?

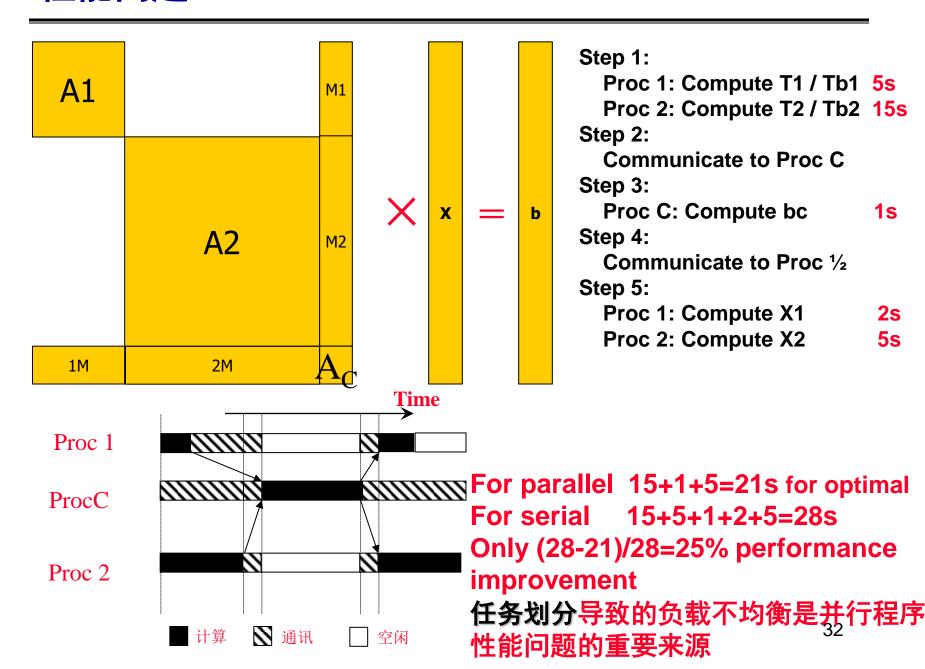


性能问题



通讯

性能问题



Summary: Performance issues in Parallel Applications

The primary sources of inefficiency in parallel codes

- 1. DO NOT have **enough parallelism**
- 2. Too much parallelism overhead
 - Thread creation, synchronization, communication
- 3. Load imbalance inefficient task scheduling
 - Different amounts of work across processors
 - Computation and communication
 - Different speeds (or available resources) for the processors
 - Possibly due to load on the machine

4. Poor single processor performance

• Typically in the memory system

Principles of Parallel Computing

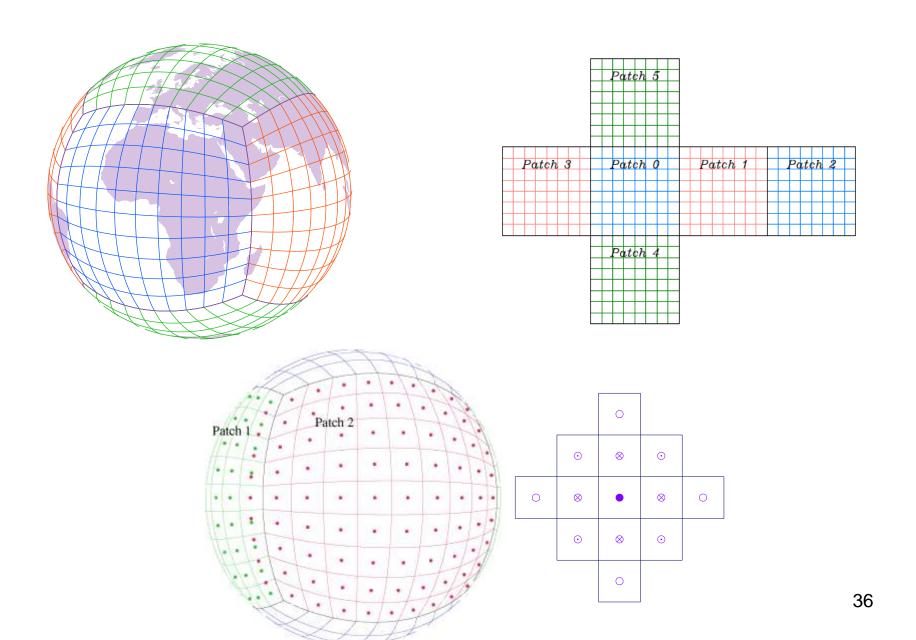
- Speedup, efficiency, and Amdahl's Law
- Finding and exploiting parallelism
- Finding and exploiting data locality
- Load balancing (task scheduling)
- Decrease parallel overhead

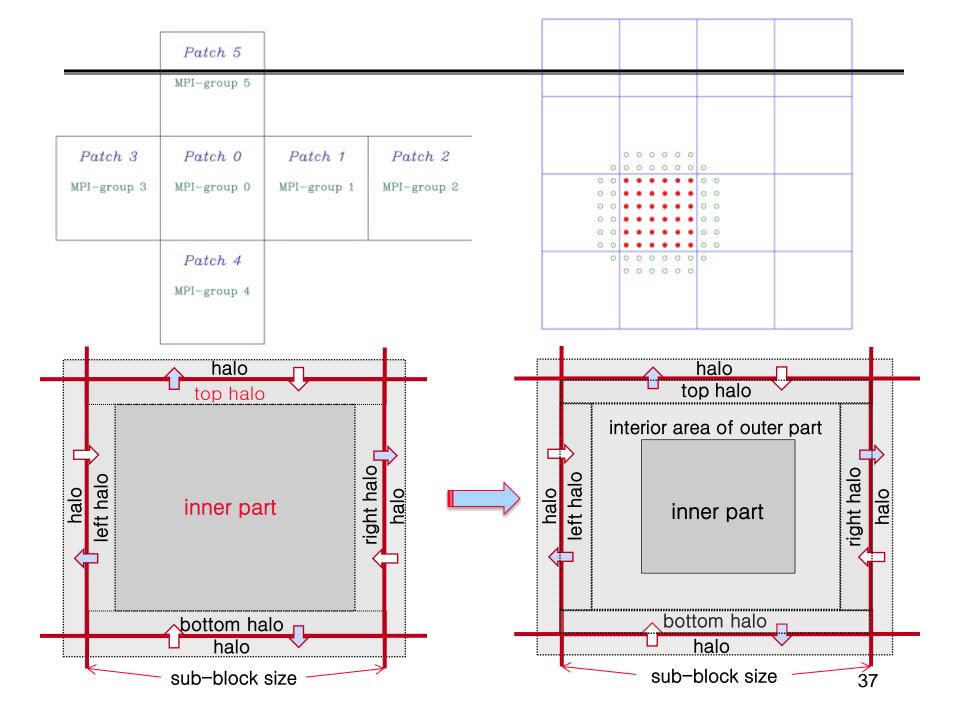
All of these things make parallel programming more difficult than sequential programming.

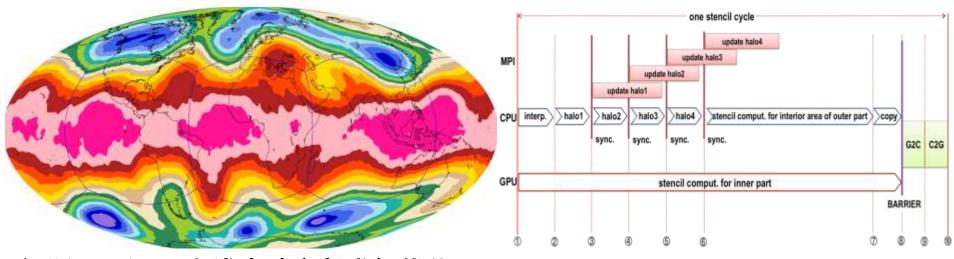
Solving the problem in Parallel Overhead when multiprocessing

- 静态的进程创建对整体性能影响有限
- •核心问题在于解决通信开销问题
 - 通过增加各个进程的计算比重降低通信开销比例
 - 粒度
 - 计算与通信比率
 - Fine-grained:分解成很多小的任务,适合SMP、多核
 - Coarse-grained:分解成不多的大的任务,适合Cluster
 - 粒度选择需要与机器模型的匹配
 - 聚合消息减少通信开销
 - 消息聚合隐藏消息延迟
 - 计算和通信重叠
 - 在高并行度下尽可能减小高开销的群集通信
 - 慎用Scatterv和Gatherv(MPICH) -- 与MPI的实现相关

计算通信重叠

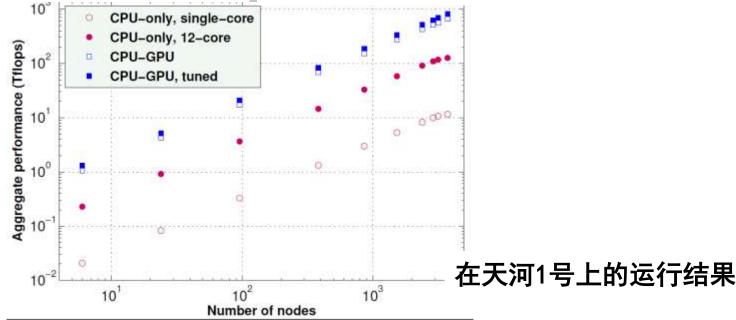






问题:天河1A上浅水波方程求解优化

构造和实现计算与通讯并发执行的算法



Solving the problem in Parallel Overhead when multithreading

Thread Creation overhead

- Overhead increases rapidly as the number of active threads increases
- Solution: Use of re-usable threads and thread pools
 - Amortizes the cost of thread creation
 - Keeps number of active threads relatively constant

Locality

- Allocate on stack or use thread local storage to release Heap contention
- Replicate data copies for use by multi-threads
- False sharing can degrade performance, so organize data efficiently

Data race overhead

- Use as less as syn. (explicit and implicit)
- Keep few active threads to access data area
- Decrease the size of critical sections
- Atomic updates versus critical sections
 - Some global data updates can use atomic operations
 - Use atomic updates whenever possible



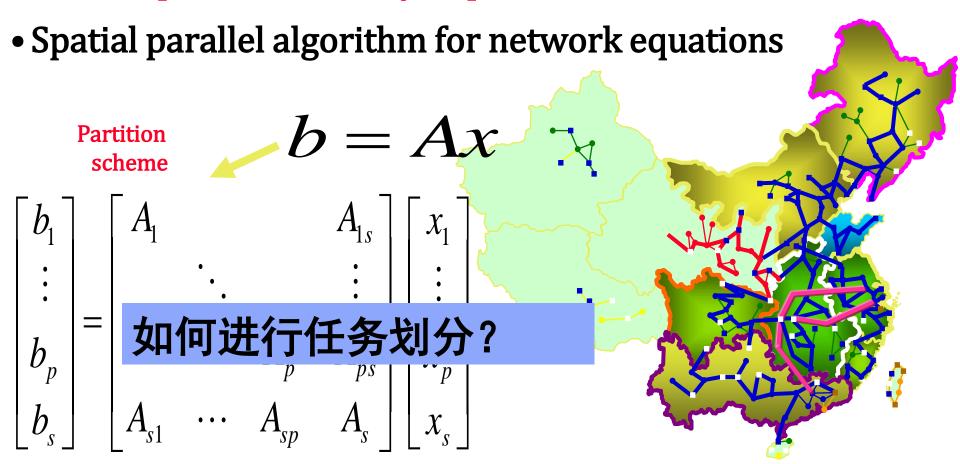
以前的一个例子

Computational Model

- Differential Algebra Equations

$$\dot{X} = f(X,V) = AX + Bu(X,V)$$
$$0 = I - Y(X) * V$$

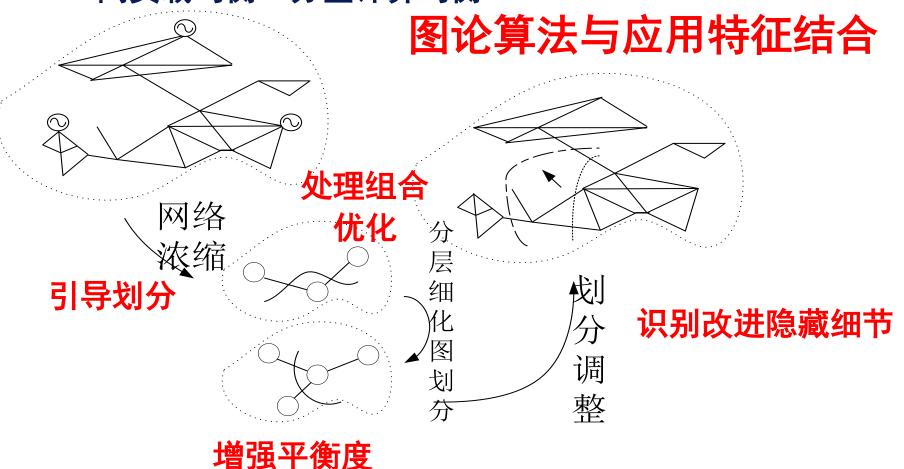
State equations are easy to parallel



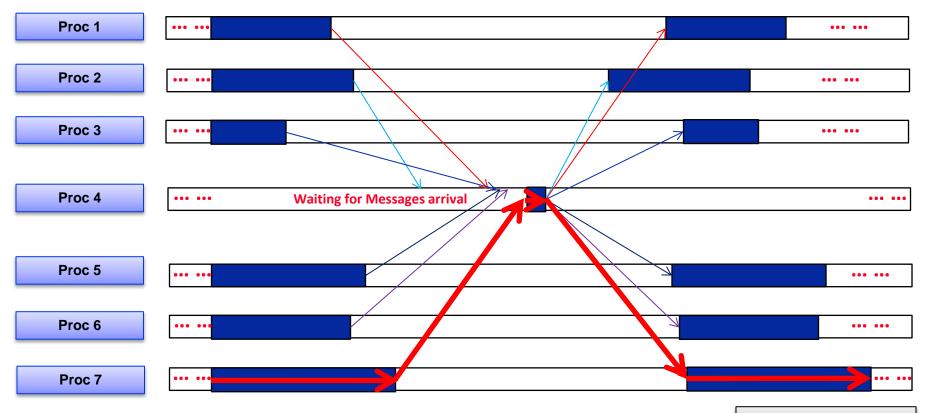
任务划分

・任务划分

- 低通信 一 降低固有串行部分比例
- 高负载均衡一分区计算均衡



Critical Path

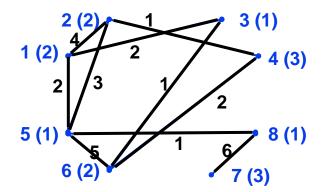


Critical path

The critical path is the longest execution flow

Definition of Graph Partitioning from Berkeley CS267

- Given a graph $G = (N, E, W_N, W_E)$
 - N = nodes (or vertices),
 - $W_N = \text{node weights}$
 - E = edges
 - W_E = edge weights



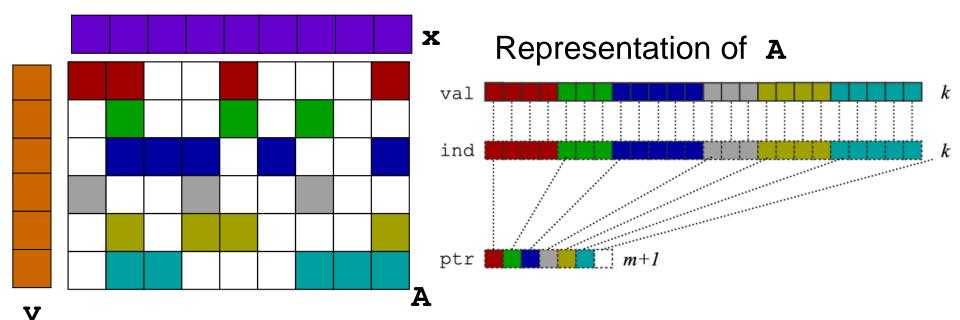
- Ex: $N = \{tasks\}, W_N = \{task costs\}, edge (j,k) in E means task j sends W_E(j,k) words to task k$
- Choose a partition $N = N_1 U N_2 U ... U N_P$ such that
 - The sum of the node weights in each N_j is "about the same"
 - \bullet The sum of all edge weights of edges connecting all different pairs $N_j\,$ and N_k is minimized
- Ex: balance the work load, while minimizing communication
- Special case of $N = N_1 U N_2$: Graph Bisection

Some Applications

- Telephone network design
 - Original application, algorithm due to Kernighan
- Load Balancing while Minimizing Communication
- Sparse Matrix times Vector Multiplication
 - Solving PDEs
 - $N = \{1,...,n\}$, (j,k) in E if A(j,k) nonzero,
 - $W_N(j) = \# nonzeros in row j$, $W_E(j,k) = 1$
- VLSI Layout
 - $N = \{units on chip\}, E = \{wires\}, W_E(j,k) = wire length$
- Sparse Gaussian Elimination
 - Used to reorder rows and columns to increase parallelism, and to decrease "fill-in"
- Data mining and clustering
- Physical Mapping of DNA
- Image Segmentation

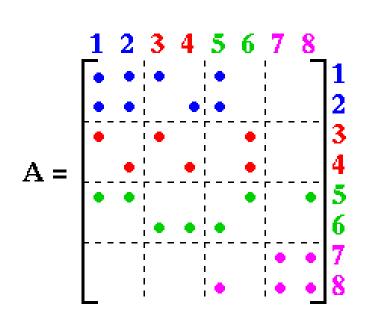
SpMV in Compressed Sparse Row (CSR) Format

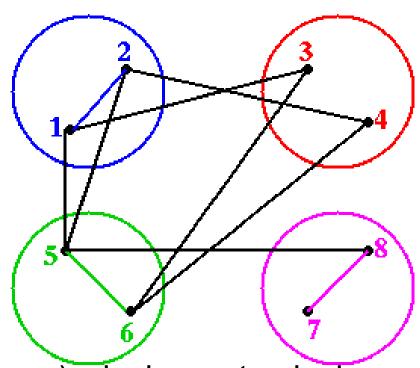
CSR format is one of many possibilities



Matrix-vector multiply kernel: $y(i) \leftarrow y(i) + A(i,j) \times x(j)$

Sparse Matrix Vector Multiplication y = y +A*xPartitioning a Sparse Symmetric Matrix

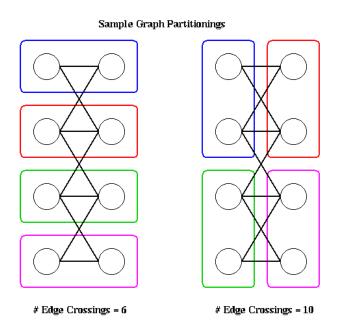




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Cost of Graph Partitioning

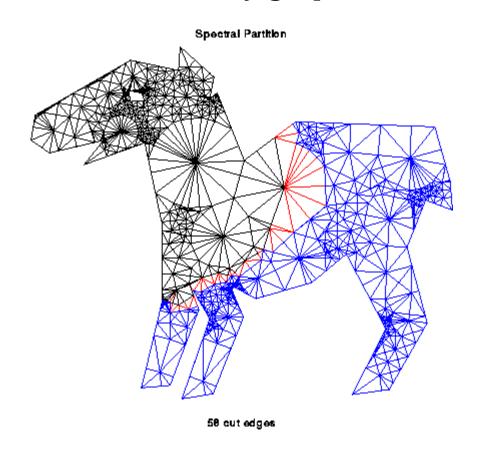
- Many possible partitionings to search
- Just to divide in 2 parts there are: n choose n/2



- Choosing optimal partitioning is NP-complete
 - (NP-complete = we can prove it is a hard as other well-known hard problems in a class Nondeterministic Polynomial time)
 - Only known exact algorithms have cost = exponential(n)
- We need good heuristics

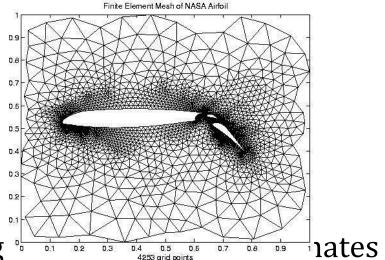
First Heuristic: Repeated Graph Bisection

- To partition N into 2^k parts
 - bisect graph recursively k times
- Henceforth discuss mostly graph bisection



Overview of Bisection Heuristics

- Partitioning with Nodal Coordinates
 - Each node has x,y,z coordinates → partition space



- Partitioning 0 0.1 0.2 0.3 0.4 0.5 0.6 0.7 0.8 0.9
 - E.g., Sparse matrix of Web documents
 - A(j,k) = # times keyword j appears in URL k
- Multilevel acceleration (BIG IDEA)
 - Approximate problem by "coarse graph," do so recursively

02/11/2010 50

Available Implementations

- Multilevel Kernighan/Lin
 - METIS (www.cs.umn.edu/~metis)
 - ParMETIS parallel version
- Multilevel Spectral Bisection
 - S. Barnard and H. Simon, "A fast multilevel implementation of recursive spectral bisection ...", Proc. 6th SIAM Conf. On Parallel Processing, 1993
 - Chaco (www.cs.sandia.gov/CRF/papers_chaco.html)
- Hybrids possible
 - Ex: Using Kernighan/Lin to improve a partition from spectral bisection
- Recent package, collection of techniques
 - Zoltan (www.cs.sandia.gov/Zoltan)

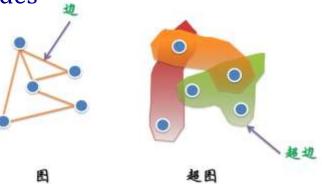
Comparison of methods

- Metrics
 - Speed of partitioning
 - Number of edge cuts
 - Other application dependent metrics
- Summary
 - No one method best
 - Multi-level Kernighan/Lin fastest by far, comparable to Spectral in the number of edge cuts
 - www-users.cs.umn.edu/~karypis/metis/publications/main.html
 - see publications KK95a and KK95b
 - Spectral give much better cuts for some applications
 - Ex: image segmentation
 - See "Normalized Cuts and Image Segmentation" by J. Malik, J. Shi

02/11/2010 52

Beyond Simple Graph Partitioning

- Undirected graphs model symmetric matrices, not unsymmetric ones
- More general graph models include:
 - Hypergraph: nodes are computation, edges are communication, but connected to a set (>= 2) of nodes
 - HMETIS package



- Multi-object, Multi-Constraint model: use when single structure may involve multiple computations with differing costs
- For more see Bruce Hendrickson's web page
 - www.cs.sandia.gov/~bahendr/partitioning.html
 - "Load Balancing Myths, Fictions & Legends"

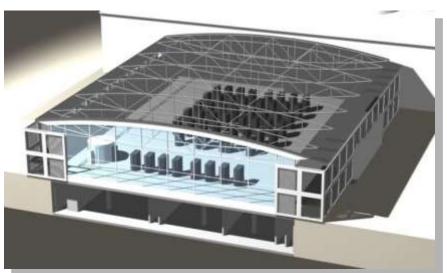
performance tools for parallel programming

Motivation for performance tools [from Berkeley CS267]

- Performance analysis is important
 - For HPC: computer systems are large investments
 - Procurement: O(\$40 Mio)
 - Operational costs: ~\$5 Mio per year
 - Power: 1 MWyear ~\$1 Mio

• Goals:

- Solve **larger** problems (new science)
- Solve problems faster (turnaround time)
- Improve **error** bounds on solutions (confidence)







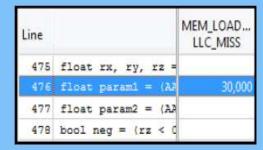
Where is my application...

Spending Time?

Function - Call Stack	CPU Time*
■ algorithm_2	3.560s
do_xform ←	3.560s
∄ algorithm_1	1.412s
⊕ BaseThreadInitThr	0.000s

- Focus tuning on functions taking time
- See call stacks
- See time on source

Wasting Time?



- See cache misses on your source
- See functions sorted by # of cache misses

Waiting Too Long?



- See locks by wait time
- Red/Green for CPU utilization during wait

- Windows & Linux
- Low overhead
- No special recompiles
- ✓ 热点分析
- ✓ 并行度分析
- ✓ 锁和等待分析
- ✓ 对比分析

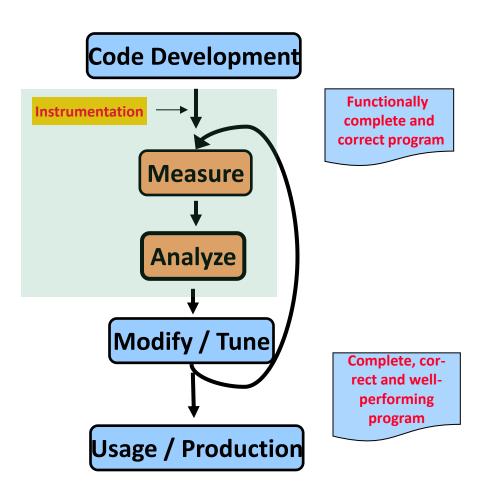
We improved the performance of the latest run 3 fold. We wouldn't have found the problem without something like Intel® VTune™ Amplifier XE.

Claire Cates

Principal Developer, SAS Institute Inc.

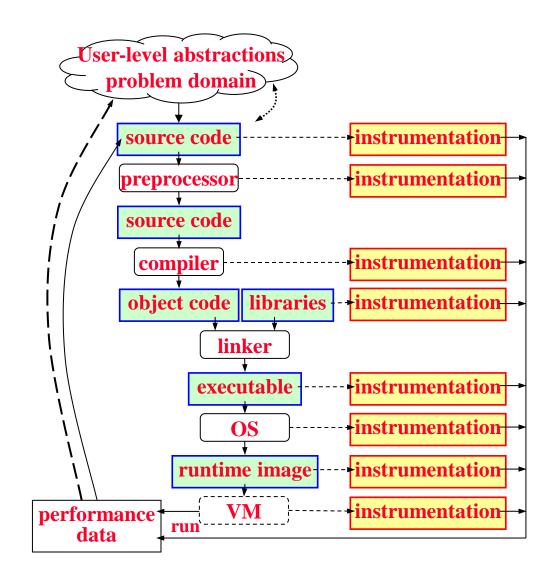
Concepts and Definitions

• The typical performance optimization cycle



Instrumentation

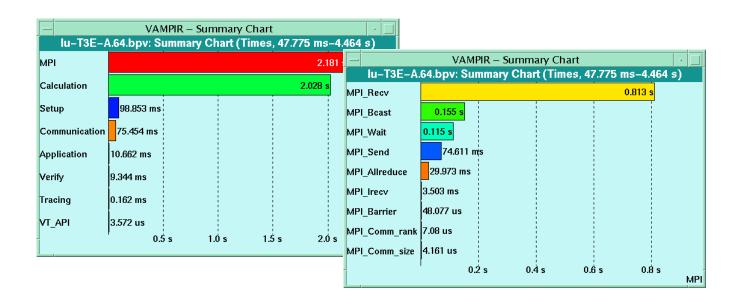
- Instrumentation := adding measurement probes to the code in order to observe its execution
- Can be done on several levels and ddifferent techniques for different levels
- Different overheads and levels of accuracy with each technique
- No application instrumentation needed: run in a simulator. E.g., Valgrind, SIMICS, etc. but simulation speed is an issue



```
Vampir – Trace Visualization (http://www.vampir.eu/)
```

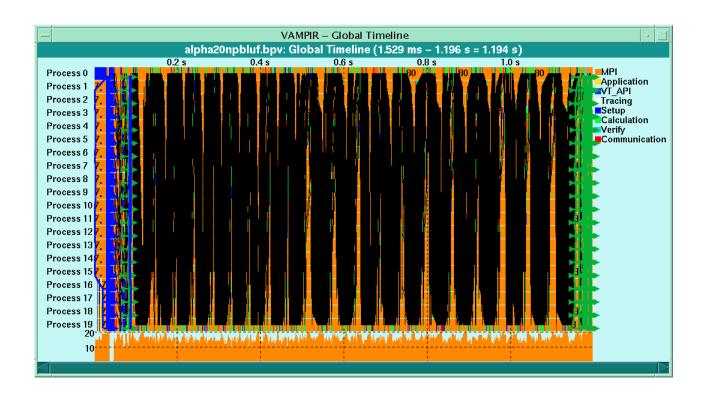
Intel Trace Collector and Analyzer

Vampir overview statistics



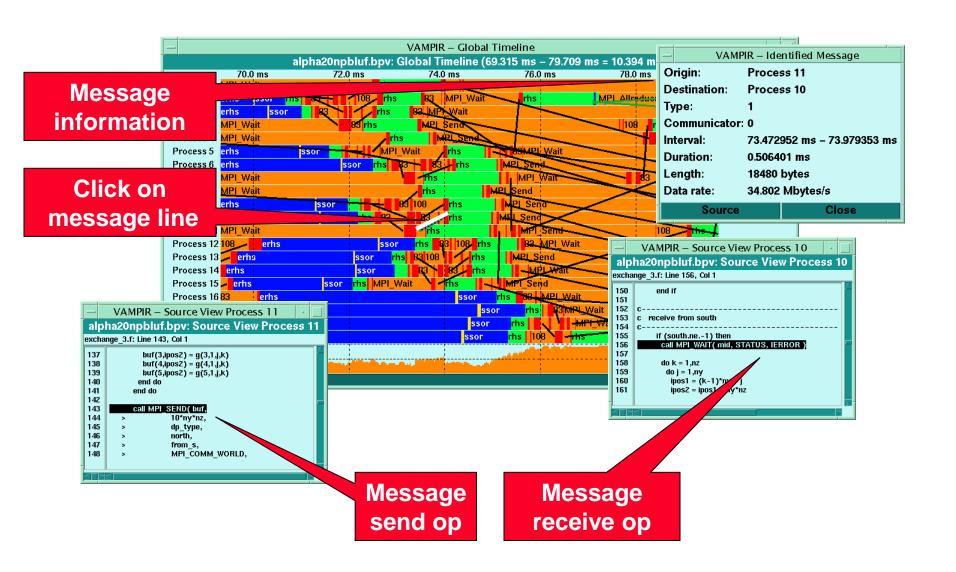
- Aggregated profiling information
 - Execution time
 - Number of calls
- This profiling information is computed from the trace
 - Change the selection in main timeline window
- Inclusive or exclusive of called routines

Timeline display

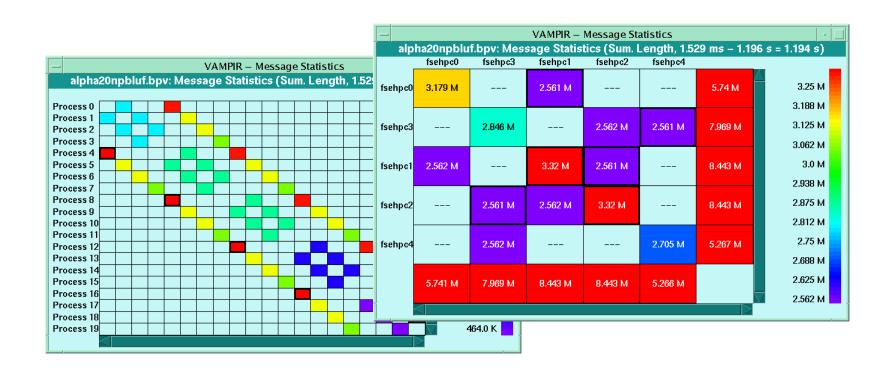


• To zoom, mark region with the mouse

<u>Timeline display – message details</u>

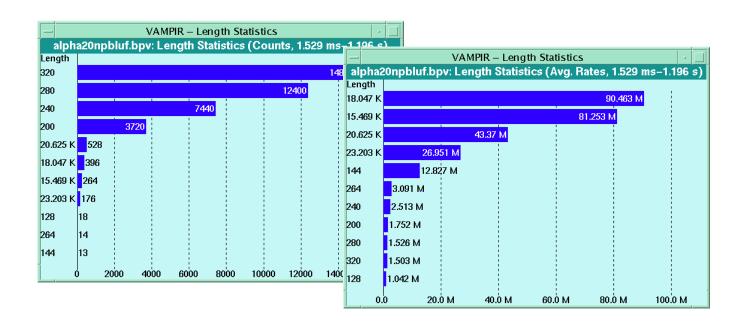


Communication statistics



- Message statistics for each process/node pair:
 - Byte and message count
 - min/max/avg message length, bandwidth

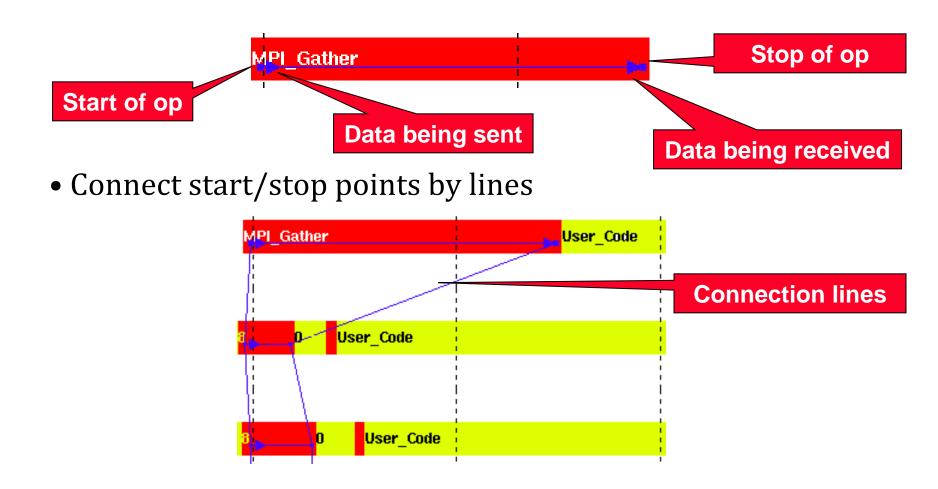
Message histograms



- Message statistics by length, tag or communicator
 - Byte and message count
 - Min/max/avg bandwidth

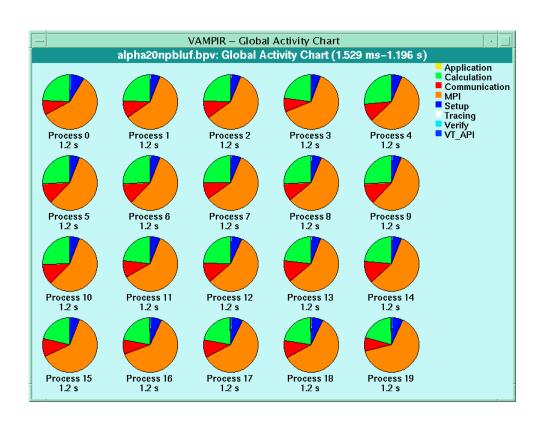
Collective operations

• For each process: mark operation locally



Activity chart

• Profiling information for all processes



Summary

- Performance montioring concepts
 - Instrument, measure, analyze
 - Profiling/tracing, sampling, direct measurment

Tools

- PAPI, ompP, and IPM as examples
- Vendor tools: Cray PAT, Sun Studio, Intel Thread Profiler, Vtune, PTU,...
- Portable tools: TAU, Perfsuite, Paradyn, HPCToolkit, Kojak, Scalasca, Vampir, oprofile, gprof, ...

Documentation, Manuals, User Guides

```
✓ PAPI
```

• http://icl.cs.utk.edu/papi/

√ompP

• http://www.ompp-tool.com

✓IPM

http://ipm-hpc.sourceforge.net/

✓TAU

http://www.cs.uoregon.edu/research/tau/

✓ VAMPIR / INTEL Trace Collector and Analyzor

• http://software.intel.com/en-us/intel-trace-analyzer

✓ Scalasca

• http://www.scalasca.org