



UNIVERSIDAD DE CÓRDOBA

comprometida con el desarrollo regional

TEORIA DE GRAFOS



UNIVERSIDAD DE CÓRDOBA

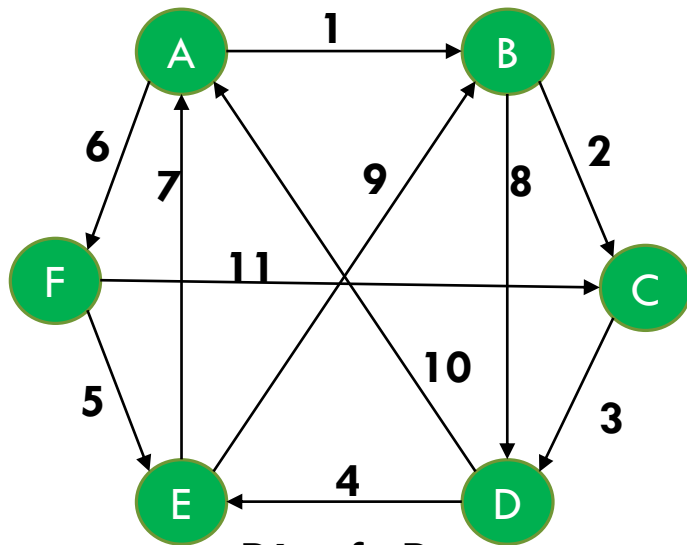
comprometida con el desarrollo regional

UNIDAD 4. SUBDIGRAFO

SUBDIGRAFOS

Definición: Se dice que un dígrafo simple D_1 es un **subdígrafo** de un dígrafo D si y sólo si, cada vértice en D_1 es también un vértice en D , asigna a cada arista de D_1 un par ordenado de vértices de D_1 .

Ejemplo:



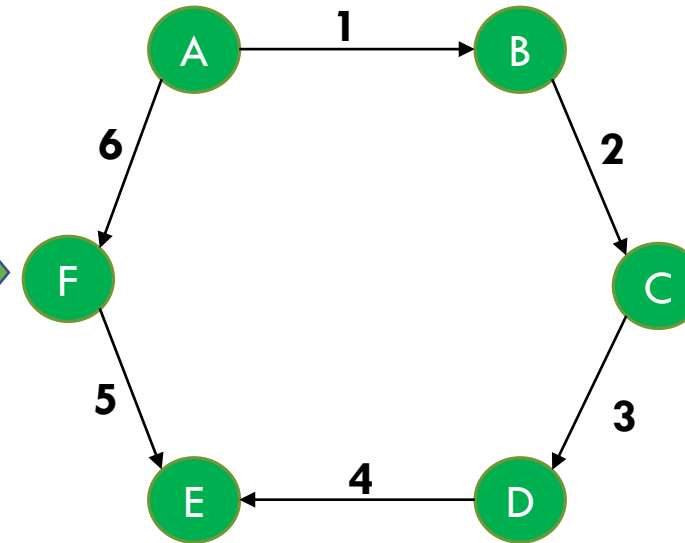
Dígrafo D

$$D = (V, A, f)$$

$$D(V) = \{A, B, C, D, E, F\}$$

$$D(A) = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11\}$$

$$F_D = \begin{cases} f_D(1) = (A, B), f_D(2) = (B, C), \\ f_D(3) = (C, D), f_D(4) = (D, E), \\ f_D(5) = (E, F), f_D(6) = (F, A), \\ f_D(7) = (A, E), f_D(8) = (B, D), \\ f_D(9) = (C, A), f_D(10) = (D, B), \\ f_D(11) = (F, C) \end{cases}$$



Subdígrafo D1

$$D = (V, A, f)$$

$$D(V) = \{A, B, C, D, E, F\}$$

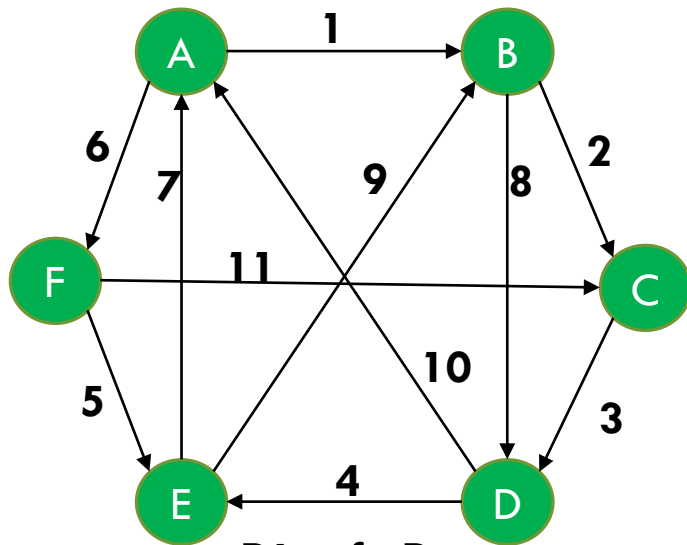
$$D(A) = \{1, 2, 3, 4, 5, 6\}$$

$$F_{D_1} = \begin{cases} f_{D_1}(1) = (A, B), f_{D_1}(2) = (B, C), \\ f_{D_1}(3) = (C, D), f_{D_1}(4) = (D, E), \\ f_{D_1}(5) = (E, F), f_{D_1}(6) = (F, A) \end{cases}$$

SUBDIGRAFO COBERTOR

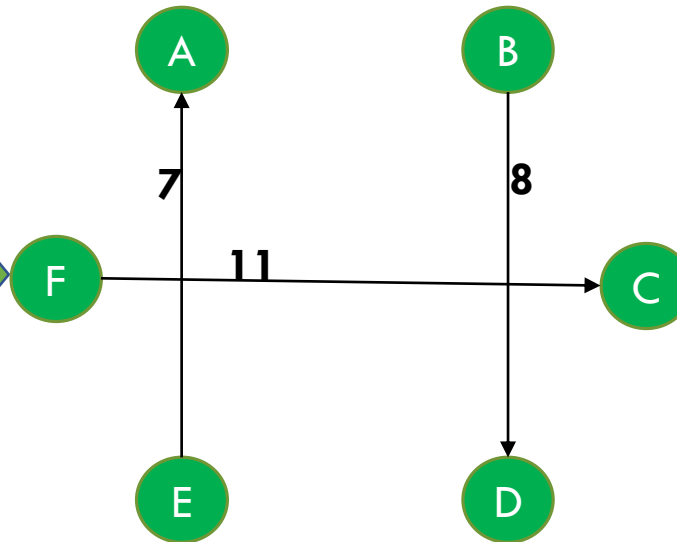
Definición: Un subdigrafo $D1$ de un dígrafo D se llama **cobertor** si contiene a todos los vértices de D ($V(D1) = V(D)$).

Ejemplo:



Dígrafo D

$$\begin{aligned}
 D &= (V, A, f) \\
 D(V) &= \{A, B, C, D, E, F\} \\
 D(A) &= \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11\} \\
 F_D &= \begin{cases} f_D(1) = (A, B), f_D(2) = (B, C), \\ f_D(3) = (C, D), f_D(4) = (D, E), \\ f_D(5) = (E, F), f_D(6) = (A, F), \\ f_D(7) = (E, A), f_D(8) = (B, D), \\ f_D(9) = (E, B), f_D(10) = (D, A), \\ f_D(11) = (F, C) \end{cases}
 \end{aligned}$$

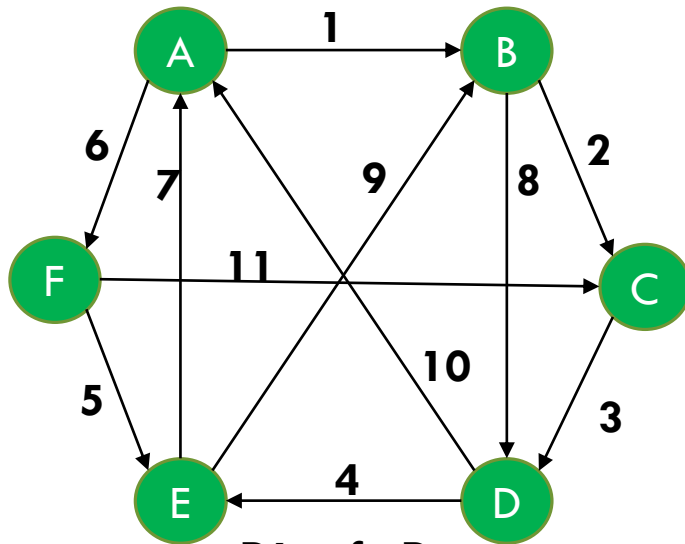


Subdígrafo Cobertor D2

$$\begin{aligned}
 D &= (V, A, f) \\
 D(V) &= \{A, B, C, D, E, F\} \\
 D(A) &= \{7, 8, 10, 11\} \\
 F_D &= \begin{cases} f_D(7) = (E, A), f_D(8) = (B, D), \\ f_D(10) = (D, A), f_D(11) = (F, C) \end{cases}
 \end{aligned}$$

VÉRTICES-DISYUNTOS

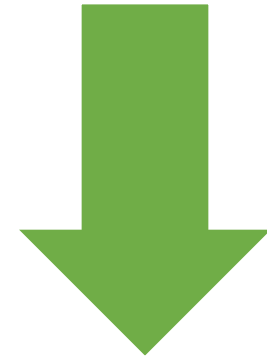
Definición: Dos subdígrafos D_1 y D_2 de un dígrafo D son **VÉRTICES-DISYUNTOS**, si no poseen vértices comunes ($V(D_1) \cap V(D_2) = \emptyset$).



Dígrafo D

$D = (V, A, f)$
 $D(V) = \{A, B, C, D, E, F\}$
 $D(A) = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11\}$

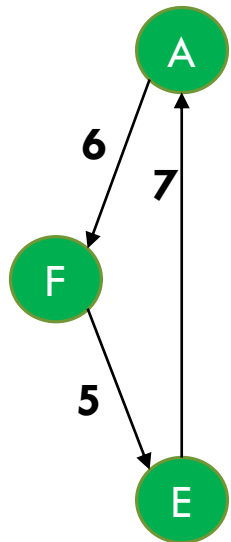
$F_D = \left\{ \begin{array}{l} f_D(1) = (A, B), f_D(2) = (B, C), \\ f_D(3) = (C, D), f_D(4) = (D, E), \\ f_D(5) = (E, F), f_D(6) = (A, F), \\ f_D(7) = (E, A), f_D(8) = (B, D), \\ f_D(9) = (E, B), f_D(10) = (D, A), \\ f_D(11) = (F, C) \end{array} \right.$





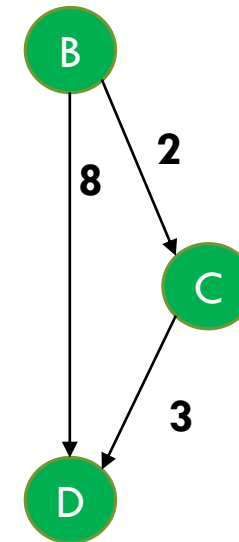
VÉRTICES-DISYUNTOS

Ejemplo: El subdígrafo D4 es vértice-disyunto del subdígrafo D5



D4

$$\begin{aligned} D &= (V, A, f) \\ D(V) &= \{A, F, E\} \\ D(A) &= \{5, 6, 7\} \\ F_D &= \begin{cases} f_D(5) = (F, E), f_D(6) = (A, F), \\ f_D(7) = (E, A) \end{cases} \end{aligned}$$

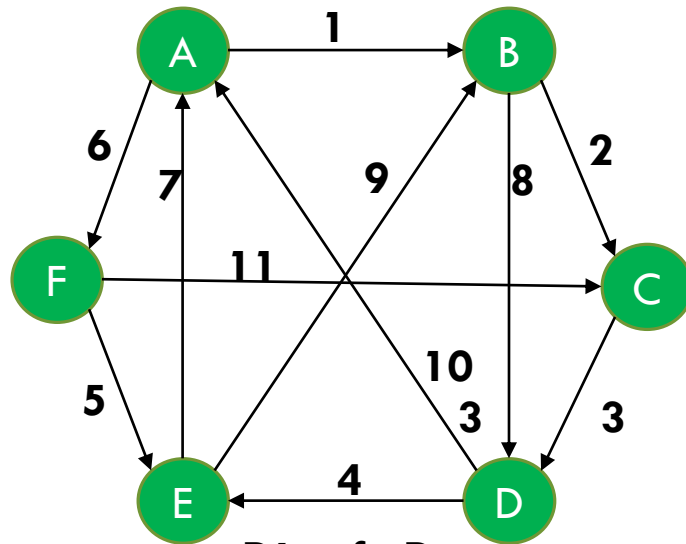


D5

$$\begin{aligned} D &= (V, A, f) \\ D(V) &= \{B, C, D\} \\ D(A) &= \{2, 3, 8\} \\ F_D &= \begin{cases} f_D(2) = (B, C), f_D(3) = (C, D), \\ f_D(8) = (B, D) \end{cases} \end{aligned}$$

ARISTAS-DISYUNTOS

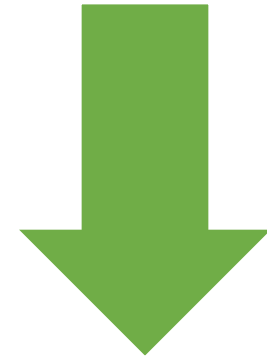
Definición: Dos subdígrafos D_1 y D_2 de un dígrafo D son **ARISTAS-DISYUNTOS**, si no poseen aristas en común ($A(D_1) \cap A(D_2) = \emptyset$).



Dígrafo D

$D = (V, A, f)$
 $D(V) = \{A, B, C, D, E, F\}$
 $D(A) = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11\}$

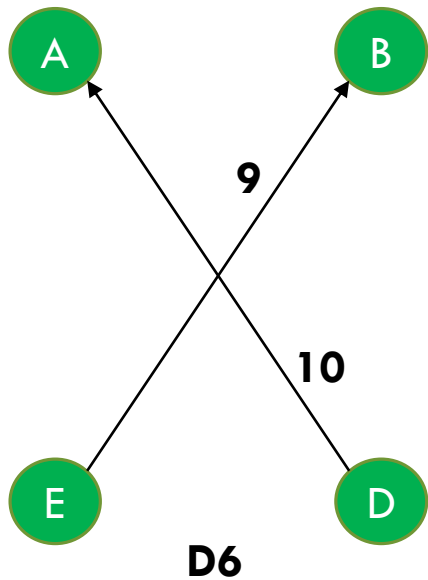
$F_D = \left\{ \begin{array}{l} f_D(1) = (A, B), f_D(2) = (B, C), \\ f_D(3) = (C, D), f_D(4) = (D, E), \\ f_D(5) = (E, F), f_D(6) = (A, F), \\ f_D(7) = (E, A), f_D(8) = (B, D), \\ f_D(9) = (E, B), f_D(10) = (D, A), \\ f_D(11) = (F, C) \end{array} \right.$





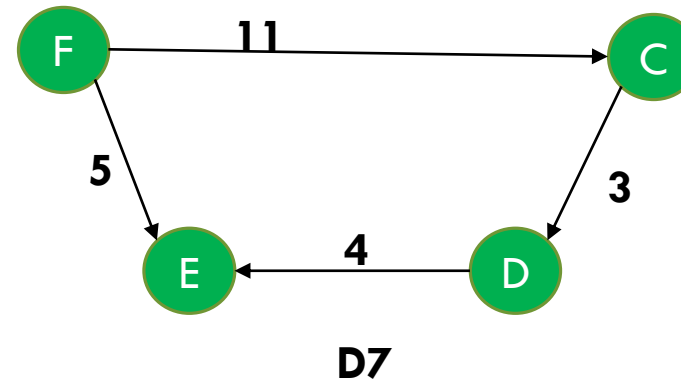
ARISTAS-DISYUNTOS

Ejemplo: Los subdígrafos D6 y D7 son aristas-disyuntas ya que no tienen aristas en comunes



$D = (V, A, f)$
 $D(V) = \{A, B, D, E\}$
 $D(A) = \{9, 10\}$

$F_D = \left[\begin{array}{l} f_D(9) = (E, B), f_D(10) = (D, A) \end{array} \right.$



$D = (V, A, f)$
 $D(V) = \{F, C, D, E\}$
 $D(A) = \{11, 3, 4, 5\}$

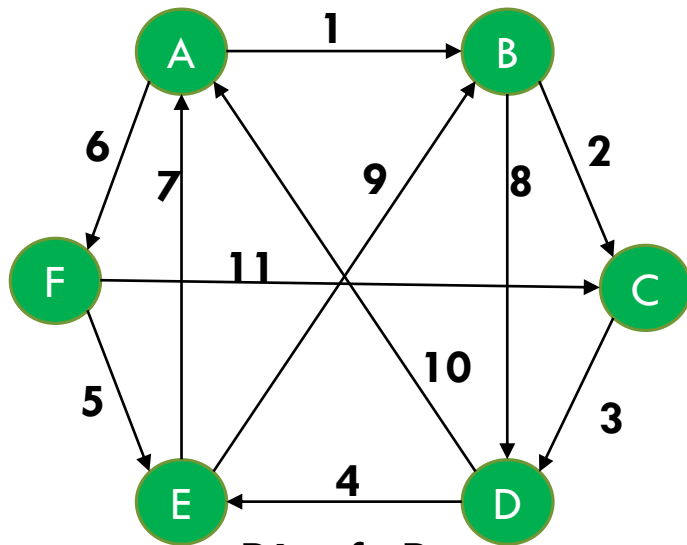
$F_D = \left[\begin{array}{l} f_D(11) = (F, C), f_D(3) = (C, D) \\ f_D(4) = (D, E), f_D(5) = (F, E) \end{array} \right.$



RESTANTE AL SUPRIMIR UN CONJUNTO DE VÉRTICES

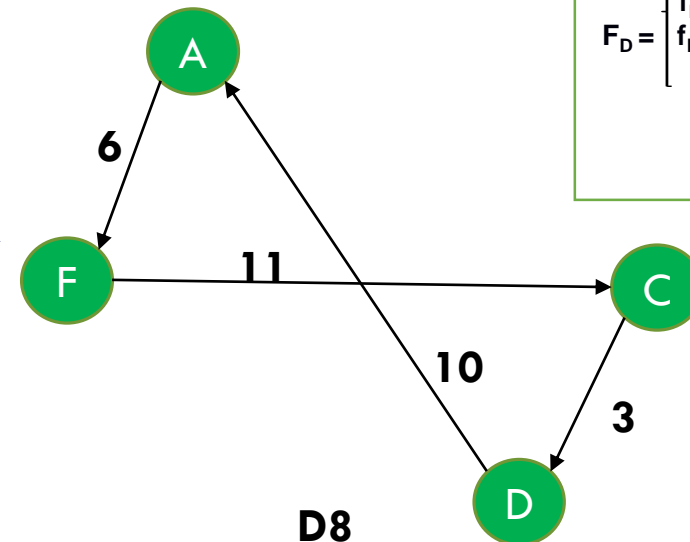
Definición: Sea D un dígrafo con $|V| \geq 2$ y sea $v' \in V$, la operación supresión de V' consiste en suprimir de D los vértices de V' y las aristas incidentes en ellos. Se denota $D - \{V'\}$.

Ejemplo: $D - \{B, E\}$



Dígrafo D

$$\begin{aligned} D &= (V, A, f) \\ D(V) &= \{A, B, C, D, E, F\} \\ D(A) &= \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11\} \\ F_D &= \begin{cases} f_D(1) = (A, B), f_D(2) = (B, C), \\ f_D(3) = (C, D), f_D(4) = (D, E), \\ f_D(5) = (F, E), f_D(6) = (A, F), \\ f_D(7) = (E, A), f_D(8) = (B, D), \\ f_D(9) = (E, B), f_D(10) = (D, A), \\ f_D(11) = (F, C) \end{cases} \end{aligned}$$



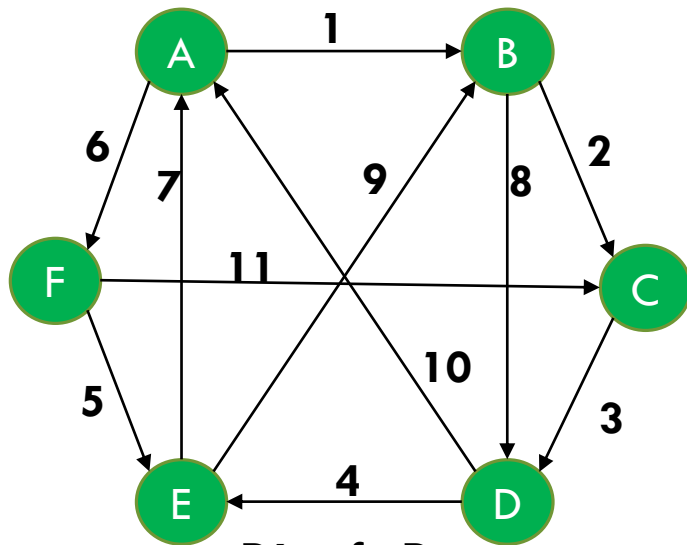
D8

$$\begin{aligned} D &= (V, A, f) \\ D(V) &= \{A, C, D, F\} \\ D(A) &= \{6, 11, 10, 3\} \\ F_D &= \begin{cases} f_D(6) = (A, F), f_D(11) = (F, C) \\ f_D(10) = (D, A), f_D(3) = (C, D) \end{cases} \end{aligned}$$

RESTANTE AL SUPRIMIR UN CONJUNTO DE ARISTAS

Definición: Sea D un dígrafo, sea $A1 \neq 0$ Y $A1 \leq A$. se llama subdígrafo restante al suprimir $A1$, al subdígrafo obtenido al suprimir de A las aristas de $A1$. se denota por $D - \{A1\}$

Ejemplo: $D - \{7, 8, 11\}$



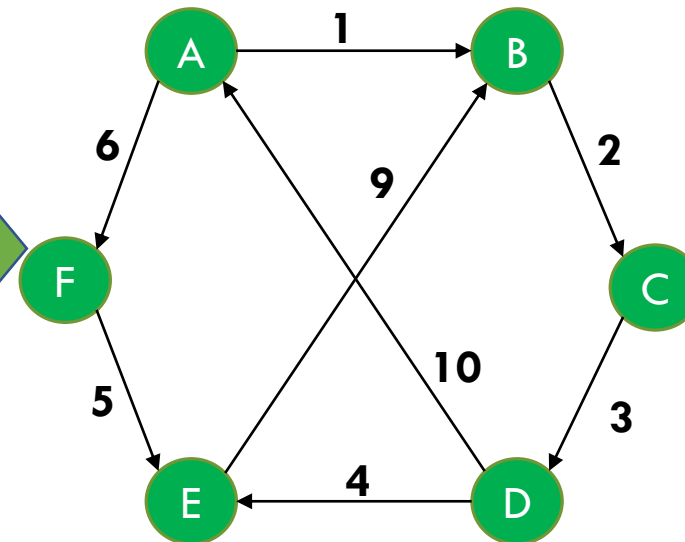
Dígrafo D

$$D = (V, A, f)$$

$$D(V) = \{A, B, C, D, E, F\}$$

$$D(A) = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11\}$$

$$F_D = \begin{cases} f_D(1) = (A, B), f_D(2) = (B, C), \\ f_D(3) = (C, D), f_D(4) = (D, E), \\ f_D(5) = (F, E), f_D(6) = (A, F), \\ f_D(7) = (E, A), f_D(8) = (B, D), \\ f_D(9) = (E, B), f_D(10) = (D, A), \\ f_D(11) = (F, C) \end{cases}$$



D9

$$D = (V, A, f)$$

$$D(V) = \{A, B, C, D, E, F\}$$

$$D(A) = \{1, 2, 3, 4, 5, 6, 9, 10\}$$

$$F_D = \begin{cases} f_D(1) = (A, B), f_D(2) = (B, C), \\ f_D(3) = (C, D), f_D(4) = (D, E), \\ f_D(5) = (F, E), f_D(6) = (A, F), \\ f_D(9) = (E, B), f_D(10) = (D, A), \end{cases}$$