

MOS

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$$\sigma = \frac{P}{A} \quad G = \frac{Sl}{J} \quad \text{lateral} \quad \epsilon = \frac{\delta d}{d}$$

Hooke's law $\sigma = E\epsilon$ $E \rightarrow$ young's modulus

$\mu = \frac{\text{lateral strain}}{\text{linear strain}}$

elongation % $> 5\%$ \rightarrow ductile
 $< 5\%$ Brittle

$$\frac{Sl}{AE}, \quad \frac{\sigma_1}{\sigma_2} = \frac{E_1}{E_2} \rightarrow \text{Modular ratio (Composite bar)}$$

$$\Delta L = L\alpha\Delta t, \quad \delta = E\alpha\Delta t$$

$$\sigma_{th} = \left(\frac{\Delta L - \delta}{L} \right) E \quad E = \frac{AL}{L} \rightarrow \frac{AL - \delta}{L}$$

$$E_1 + E_2 = (\alpha_2 - \alpha_1) A \Delta t$$

$$\text{strain energy } U = \frac{\sigma^2}{2E} AL$$

$$\sigma_\theta = \frac{\sigma_x + \sigma_y}{2} + \left(\frac{\sigma_x - \sigma_y}{2} \right) \cos 2\theta + \tau \sin 2\theta$$

$$\tau_\theta = - \left(\frac{\sigma_x - \sigma_y}{2} \right) \sin 2\theta + \tau \cos 2\theta$$

$$\tan 2\theta_p = \frac{2\tau}{\sigma_x - \sigma_y}$$

$$\sigma_\theta = \sigma_x \cos^2 \theta + \sigma_y \sin^2 \theta \quad (\text{when } \tau = 0 \text{ i.e. } \sigma_x \text{ \& } \sigma_y)$$

$$\sigma_{1,2} = \frac{\sigma_x + \sigma_y}{2} \pm \sqrt{\left(\frac{\sigma_x - \sigma_y}{2} \right)^2 + \tau^2}$$


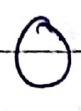

$$\tau_{max} = \frac{\sigma_1 - \sigma_2}{2}$$

$$= \sigma_x + \sigma_y$$

$$\theta_s' = \theta_p + 45^\circ$$

* Stresses in beams:




$$\frac{M}{I} = \frac{E}{R} = \frac{\sigma}{y}$$

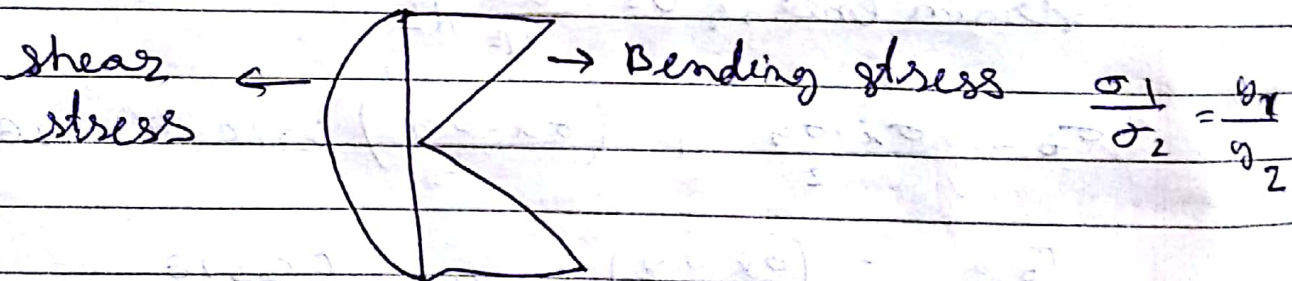
 $\frac{BD^3}{12}$
  $\frac{\pi}{64} D^4$
  $\frac{BD^3}{36}$

Section modulus: $Z = \frac{I}{y_{max}}$

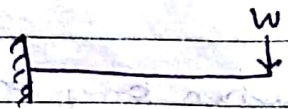
Beam of uniform strength: having same M along the longitudinal axis.

$$T = \frac{E}{2I} A \bar{y}$$

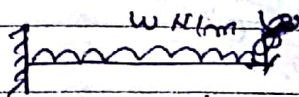
 $T_{max} = 1.5 T_{avg}$
  $T_{max} = (1/3) T_{avg}$
 $T_{max} = 3/8 T_{avg}$



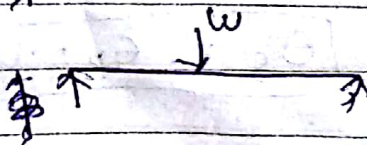
* Slope and deflection: $E I \psi'' = M$



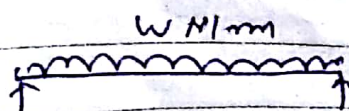
$$y = \frac{W l^3}{3 E I}, \quad y' = \frac{W l^2}{2 E I}$$



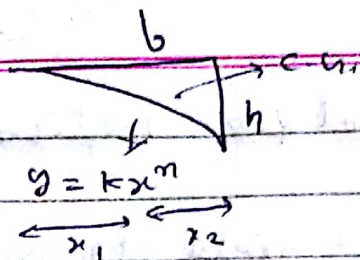
$$y = \frac{W l^4}{8 E I}, \quad y' = \frac{W l^3}{6 E I}$$



$$y = \frac{W l^3}{48 E I}, \quad y' = \frac{W l^2}{16 E I}$$



$$y = \frac{5 W l^4}{384 E I}, \quad y' = \frac{W l^3}{24 E I}$$



$$x_1 = \left(\frac{n+1}{n+2} \right) b, \quad x_2 = \frac{b}{(n+2)}$$

$$\text{Area} = \frac{bh}{n+1}$$

* Torsion:

$$\frac{T}{J} = \frac{\tau}{R} = \frac{C\theta}{L}$$

$$\frac{T}{J} = \frac{\tau}{R} \rightarrow \text{Strength}$$

$$\frac{T}{J} = \frac{C\theta}{L} \rightarrow \text{stiffness, rigidity}$$

~~strong~~

Rigidity: $EF \rightarrow$ flexure rigidity

$CT \rightarrow$ Torsional rigidity

Polar modulus $Z_p = \frac{J}{R}$ (strength of shaft)

$$\text{Power} = TW, \quad \omega = \frac{2\pi N}{60}$$

o

$$\text{Strain energy } U = \frac{1}{2} T\theta = \frac{T^2}{4C} \times \text{Volume (Solid shaft)}$$

* Columns:

slenderness ratio $\rightarrow \frac{L}{K}$ here $K = \sqrt{\frac{I}{A}}$ (length of equivalent)

$$32 < \frac{L}{K} < 120 \quad (\text{short, medium \& long})$$

$$P_{C2} = \frac{\pi^2 EI}{L_e^2}$$

$$\left(L_e = L \right)$$

$$\sum_{i=1}^n L_e = \frac{L}{2}$$

$$= \frac{\pi^2 EI}{(L_e/K)^2}$$

$$\left(L_e = 2L \right)$$

$$\left(L_e = \frac{L}{\sqrt{2}} \right)$$

Teacher's Signature

Euler's formula: Correct for medium & larger columns,
when critical value = yield stress.

Rankine's Empirical formula:

$$\frac{1}{P_R} = \frac{1}{P_C} + \frac{1}{P_e}$$

$P_R \rightarrow$ Critical load

$P_C \rightarrow$ direct load ($\sigma_y \cdot A$)

$P_e =$ Euler's load

Short Column $\Rightarrow P_R = P_C$

long Column $\Rightarrow P_R = P_e$

$$P_R = \frac{\sigma_y \cdot A}{1 + a(1/k)^2}$$

$a \rightarrow$ Rankin Constant

$$\frac{\sigma_y}{\pi^2 E}$$

\Rightarrow Eccentric load: $\sigma_{max} = \frac{e S e c \alpha}{2}$ (secant formula)

$$\sigma_{max} = \frac{P}{A} \pm \frac{M y_c}{I}$$

$\alpha^2 = \frac{P}{E I}$

$M = P y_{max}$

Perry's formula:

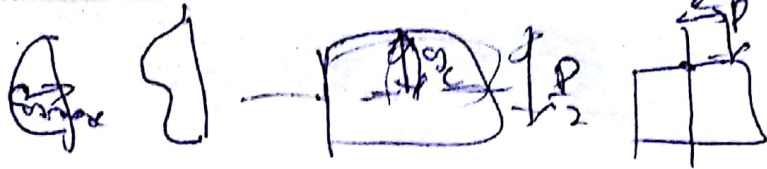
$$\left(\frac{\sigma_{max}}{\sigma_0} - 1 \right) \left(1 - \frac{\sigma_0}{\sigma_y} \right) = \frac{1.2 e y_c}{k^2}$$

For min $\frac{1}{k} \Rightarrow P_e = P_C$

\Rightarrow Initial curve:

$$D.M = P y_{max} = \frac{P C P_e}{P_e - P}$$

$$\sigma_{max} = \frac{P}{A} \pm \frac{M y_c}{I}$$



$$\left(\frac{\sigma_{max}}{\sigma_0} - 1 \right) \left(1 - \frac{\sigma_0}{\sigma_c} \right) = \frac{C \gamma_c}{k^2}$$

* Pressure vessels:

$\frac{t}{d} < \frac{1}{20}$ thin, $\frac{t}{d} > \frac{1}{20}$ thick

$$F_v = P_i d t \quad \sigma_c = \frac{P_i d}{2t}, \quad \sigma_l = \frac{P_i d}{4t}$$

→ For cylindrical.

$$\text{Max shear stress} = \frac{\sigma_c - \sigma_l}{2} = \frac{P_i d}{8t}$$

$$\frac{\delta d}{d} \Leftarrow \text{hoop strain } \epsilon_h = \frac{\sigma_h}{E} - \mu \frac{\sigma_l}{E} = \frac{P_i d}{2tE} \left(1 - \frac{\mu}{2} \right)$$

$$\frac{\delta l}{l} \Leftarrow \text{longitudinal strain } \epsilon_l = \frac{\sigma_l}{E} - \mu \frac{\sigma_h}{E} = \frac{P_i d}{2tE} \left(\frac{1}{2} - \mu \right)$$

$$\frac{\delta v}{v} \Leftarrow \text{Volumetric strain} \quad \left[\begin{array}{l} \epsilon_v = 2\epsilon_h + \epsilon_l \\ \frac{\delta v}{v} = 2 \frac{\delta d}{d} + \frac{\delta l}{l} \end{array} \right] = \frac{P_i d}{4tE} (5 - 4\mu)$$

$$\sigma_{\text{spherical}} = \frac{P_i}{4t} = \sigma_h = \sigma_l$$

$$\epsilon_v = 3\epsilon = \frac{3P_i d}{4tE} (1 - \mu)$$

$$\left[\begin{array}{l} \epsilon_h = \epsilon_l = \frac{P_i d}{4tE} (1 - \mu) \\ \epsilon_h = \sigma_h - \mu \sigma \end{array} \right]$$

Thin cylinder shell with hemispherical ends:

$$\frac{P_i d}{2t_c} = \frac{P_i d}{4t_s} \quad \Rightarrow \quad \boxed{t_c = 2t_s}$$

To avoid distortion:

$$\frac{P_i d}{2t_c E} \left(1 - \frac{\mu}{2} \right) = \frac{P_i d}{4t_s E} (1 - \mu) \quad \Rightarrow \quad \boxed{\frac{t_c}{t_s} = \frac{2 - \mu}{1 - \mu}}$$