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# Modern Electrical & Electronic Technologies

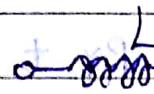
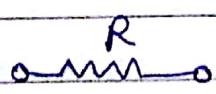
Google group: MEET\_2017

- Topics :-
- (i) Electrical Measuring Instruments
  - (ii) Transformers
  - (iii) Induction Motors
  - (iv) Special motors
  - (v) Electrical drives
  - (vi) Electrical heating
  - (vii) Digital Electronics + Intro to Mechatronics

mid-term

\* Electrical engineering: Quantities to be measured

- (i) Voltage (Volts)
- (ii) Current (Ampere)
- (iii) Power (Watts)
- (iv) Energy (Joules)
- (v) Resistance (ohm ( $\Omega$ ))
- (vi) Reactance
- (vii) Inductance (Henry ( $H$ )))
- (viii) Capacitance ( $F$ )
- (ix) Frequency (Hz) or (cls)
- (x) Angular frequency [ $\omega = 2\pi f$ ]



$$X_L = 2\pi f L \quad \text{--- (1)}$$

$$X_C = \frac{1}{2\pi f C} \quad \text{--- (2)}$$

$$\omega = 2\pi f \quad \text{--- (3)}$$

$$X_L = \omega L \quad \text{--- (4)} \quad X_C = \frac{1}{\omega C} \quad \text{--- (5)}$$

$$f = \frac{1}{T} \quad \text{--- (6)}$$

$$\omega = \frac{2\pi}{T} \quad \text{--- (7)}$$

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$$R.P.M. = 1000$$

$$R.P.S. = \frac{1000}{60}$$

## Electrical Parameters

↓  
Direct Current  
(D.C.) Type

↓  
Alternating Current  
(A.C.) Type

↓  
No time dependence

↓  
Time dependence

Q1. A 220 V D.C. supply is connected across a water-heater (geyser) and draws 4.4 A current. Calculate the resistance of heating element inside the heater.

Ans  $R = \frac{220}{4.4} = 50 \Omega$

Q2. For the heater in Prob 1, calculate the amount of power dissipated in the element. Also, calculate energy consumed in 1 hour

Ans  $P = VI = 220 \times 4.4 = \text{Watts}$

$$E = P \times t \\ = 220 \times 4.4 \times 3600$$

$$= 3484.8 \text{ KJoules} \\ = \text{Kwh}$$

Note:- Energy we pay for is measured in Kwh (kilo watt-hour)

\* \*

$$1 \text{ KWh} = 1000 \text{ Watt} \times 3600 \text{ sec.}$$

$$= 3.6 \times 10^6 \text{ Watt-sec.}$$

$$\therefore 1 \text{ KWh} = 3.6 \times 10^6 \text{ Joule}$$

$$[\because 1 \text{ Watt-sec} = 1 \text{ Joule}]$$

$$\frac{1}{1} \text{ Joule} = \frac{1}{3.6 \times 10^6} \text{ KWh}$$

$$\approx 2.77778 \times 10^{-7} \text{ KWh}$$

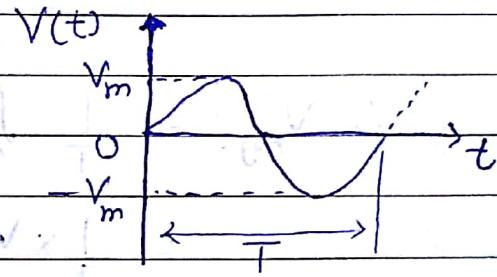
\* A.C. signals:-

(i)

$T$  = Time-period (sec).

$V_m$  = Maximum or Peak

Value of Voltage

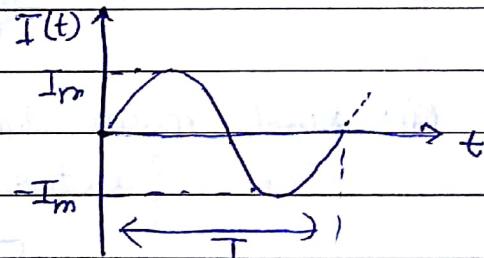


$$\text{Frequency } (f) = \frac{1}{T} \quad \Rightarrow \quad T = \frac{1}{f} \quad \text{--- (2)}$$

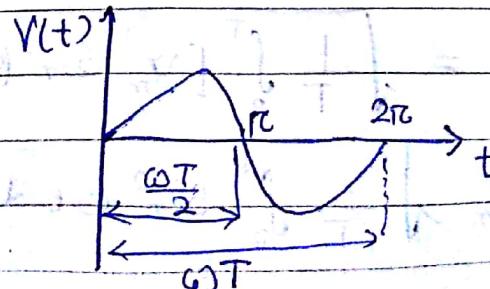
(ii)  $I_m$  = Peak Value for Current

$$\text{Angular frequency } (\omega) \\ = 2\pi f \quad \text{--- (3)}$$

$$\omega = \frac{2\pi}{T} \quad \text{--- (4)}$$



$$\Rightarrow \omega T = 2\pi f$$



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(i) Average Value ( $V_{Avg}$ . or.  $V_{DC}$ ) :-

$$V_{DC} = V_{Avg} = \frac{1}{T} \int_0^T v(t) dt \quad - \textcircled{1}$$

$$v(t) = V_m \sin \omega t \quad - \textcircled{2} \quad (\text{from first graph with phase diff.} = 0)$$

$$\begin{aligned} \cancel{V_m} \cdot \omega T &= 2\pi \\ \Rightarrow \omega &= \frac{2\pi}{T} \quad - \textcircled{3} \\ &= 2\pi f \quad - \textcircled{4} \end{aligned}$$

$$\begin{aligned} \therefore V_{Avg.} &= \frac{1}{T} \int_0^T V_m \sin(\omega t) dt \\ &= \frac{1}{T} \times V_m \left[ -\frac{\cos \omega t}{\omega} \right]_0^T \\ &= -\frac{V_m}{T} [\cos \omega T - \cos 0] \\ &= -\frac{V_m}{T} \times 0 = 0 \quad - \textcircled{5} \end{aligned}$$

(ii) Root-mean square (RMS) Value  
or Effective value :-

$$V_{RMS} \triangleq \sqrt{\frac{1}{T} \int_0^T [v(t)]^2 dt} \quad - \textcircled{6}$$

For the same graph,

$$V_{RMS} = \sqrt{\frac{1}{T} \int_0^T [V_m^2 \sin^2(\omega t)] dt} \quad - \textcircled{7}$$

$$= V_m \sqrt{\frac{1}{T} \int_0^T \sin^2 \omega t dt} \quad - \textcircled{8}$$

Notes: Make sure that you mention units of all calculated values.

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$$= V_m \cdot \sqrt{1 + E \int_0^T \left[ \frac{1}{2} (1 - \cos 2\omega t) \right] dt} \quad \text{--- (1)}$$

$$= V_m \sqrt{\left[ \frac{1}{2} - \frac{1}{2T} \left[ \frac{\sin 2\omega t}{2\omega} \right]_0^T \right]^T} \quad \text{--- (2)}$$

$$V_{RMS} = \frac{V_m}{\sqrt{2}} \quad \text{--- (1)}$$

Similarly,

For an A.C. current  $I(t) = I_m \sin \omega t$

It can be shown that  $\overline{I_{AC}} = 0$   $\text{--- (3)}$

$$I_{avg} = \overline{I_{AC}} = 0 \quad \text{--- (3)}$$

$$\therefore I_{RMS} = \frac{I_m}{\sqrt{2}} \quad \text{--- (4)}$$

Q For A.C. Voltage waveform shown below, calculate the numerical values of the following:

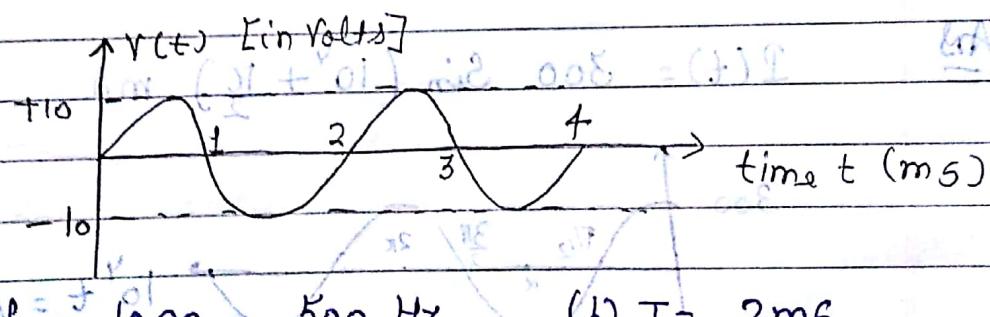
(a) Frequency

(b) Time-period (c) Angular freq.

(d) Peak-Value

(e) Peak-to-peak Value

(f) RMS value and, (g) Average Value



$$\text{Ans} \quad (a) f = \frac{1000}{2} = 500 \text{ Hz}$$

$$(b) T = 2 \text{ ms}$$

$$(c) \omega = 2\pi f = 1000\pi \approx 3140 \text{ rad/s}$$

(d) Peak Value = 10 Volts

(e) Peak-to-peak Value = 10 + 10 = 20 Volts

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(f)  $V_c = \frac{V_m}{\sqrt{2}} \approx \frac{10}{\sqrt{2}} \approx 7.07 V$

(g)  $V_{avg} = 0 V$

Q Repeat problem 1, for an A.C. current given by the following equation.

$$I(t) = 300 \sin(10^4 t) \text{ mA}$$

where  $t$  is time in seconds.

Ans

$$I_p = 300 \text{ mA}$$

$$\omega = 10^4 \text{ rad/sec.}$$

$$f = \frac{10^4}{2\pi} \approx 1591.55 \text{ c/s.}$$

$$T = \boxed{6.28 \times 10^{-4}} \text{ sec.}$$

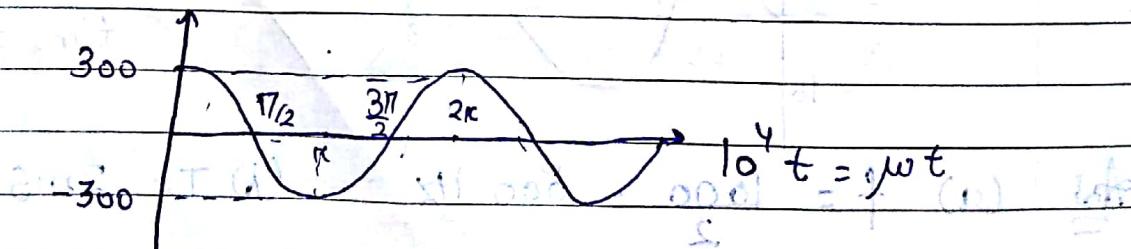
$$I_{rms} = \frac{300}{\sqrt{2}} \text{ mA}$$

$$I_{p-p} = 600 \text{ mA}$$

Q Repeat prob. 2 for  $I(t) = 300 \cos(10^4 t) \text{ mA}$

Ans

$$I(t) = 300 \sin\left(10^4 + \frac{\pi}{2}\right) \text{ mA}$$



$$300 \text{ mA} + (-300 \text{ mA}) = 0 \text{ mA} \quad (a)$$

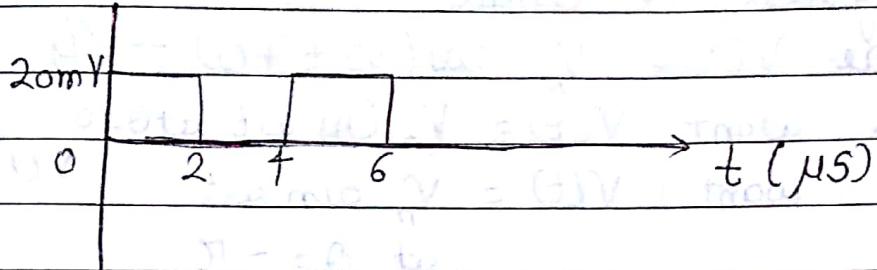
$$I_{avg} = 0$$

$$I_{rms} = \frac{300}{\sqrt{2}} \text{ mA}$$

$$I_p = 300 \text{ mA} \quad \text{and} \quad I_{p-p} = 600 \text{ mA}$$

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Q Repeat problem 1 for the Voltage wave form shown below:



Ans  $T = 4 \mu s$   $\Rightarrow V_p = 20 mV$

$$V_{DC} = \frac{1}{T} \int_0^T v(t) dt$$

$$= \frac{1}{T} \left[ \int_0^{T/2} (20 \times 10^{-3}) dt + 0 \right]$$

$$\therefore \frac{1}{T} \times 10^{-2} \times T = 10^{-2} = 10 mV$$

$$V_{rms} = \sqrt{\frac{1}{T} \int_0^{T/2} [v(t)]^2 dt}$$

$$= \sqrt{\frac{1}{T} \times \frac{1}{2} \times 400 \times 10^{-6}}$$

$$= \sqrt{2} \times 10^{-2} V = 10\sqrt{2} mV$$

$$\oplus = (+) \oplus (-) \oplus \oplus \oplus$$

$$\oplus = (0 + 10) \oplus (0) \oplus 10 \oplus =$$

$$(0 - [10(2+1)]) \sin(\omega t) + 10 \cos(\omega t) = 10 \sin(\omega t)$$

$$\therefore P = 100 mW = 10 \times 10^3$$

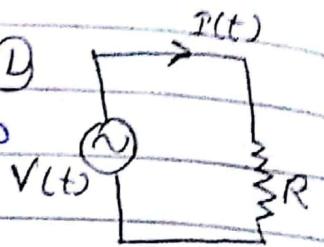
## \* Power in A.C. circuits:-

1. Purely resistive load:-

Assume  $V(t) = V_m \cos(\omega t + \theta) - (1)$

If we want  $V(t) = V_m \cos \omega t \text{ at } \theta = 0$

If we want  $V(t) = V_m \sin \omega t$  at  $\theta = -\frac{\pi}{2}$



$\theta$  is known as the phase-shift or phase-angle and can be measured either in radians or in degrees.

$$I(t) = \frac{V(t)}{R} - (2)$$

$$= \frac{V_m}{R} \cos(\omega t + \theta) - (3)$$

$$I(t) = I_m \cos(\omega t + \theta) - (4)$$

$$\text{where } I_m \triangleq \frac{V_m}{R} - (5)$$

Time dependent power can be written as-

$$P(t) \triangleq V(t) I(t) - (6)$$

$$= V_m I_m \cos^2(\omega t + \theta) - (7)$$

$$= \frac{V_m I_m}{2} [1 + \cos\{2(\omega t + \theta)\}] - (8)$$

$$[\because V_{rms} = \frac{V_m}{\sqrt{2}}, I_{rms} = \frac{I_m}{\sqrt{2}}]$$

$$= I_{rms} V_{rms} + V_{rms} I_{rms} \cos\{2(\omega t + \theta)\} - (9)$$

↓  
Real Power

↓  
Reactive Power

Average Power -

$$\begin{aligned}
 \text{(Consumed power)} \quad P_{\text{Avg}} &= P_{\text{DC}} = \frac{1}{T} \int_0^T p(t) dt \quad \text{--- (16)} \\
 &= V_{\text{rms}} I_{\text{rms}} + \frac{1}{T} \left[ \frac{\sin 2\omega t + 0}{2\omega} \right]_0^T \\
 &= V_{\text{rms}} I_{\text{rms}} + \frac{1}{2T\omega} \left[ \sin 2\theta - \sin 0 \right] \\
 &= V_{\text{rms}} I_{\text{rms}}
 \end{aligned}$$

Problem 1 :- An A.C. water heater operates at 220V (r.m.s.), 50 Hz input & consumes 1 kW. Calculate the resistance of heating element.

$$\underline{\underline{\text{Ans}}} \quad V_{\text{rms}} I_{\text{rms}} = 1000$$

$$\therefore I_{\text{rms}} = \frac{1000}{V_{\text{rms}}} = \frac{1000}{220} \text{ Amperes}$$

$$R = \frac{V_{\text{rms}}}{I_{\text{rms}}} = \frac{220 \times 220}{1000} \Omega = 48.4 \Omega$$

$$P = V_{\text{rms}} I_{\text{rms}}$$

$$= I_{\text{rms}}^2 R = \frac{V_{\text{rms}}^2}{R}$$

Power factor :-

The "Power-factor Angle" is defined as the phase-difference between  $V(t)$  &  $I(t)$

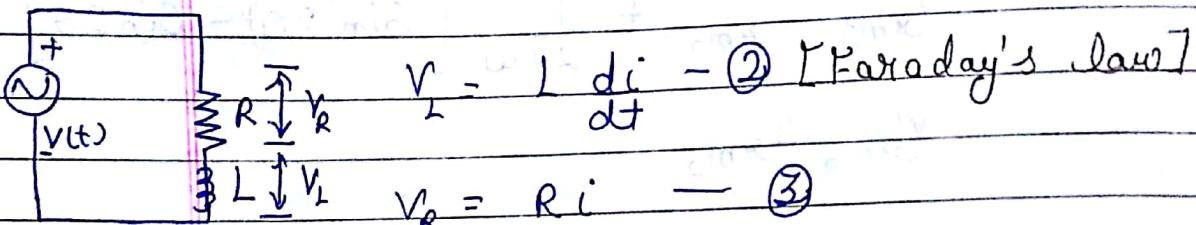
Power factor is defined to be  $\cos \phi$

Note:- Power factor of purely-resistive circuit =  $\cos \phi$   
Teacher's Signature =  $\cos \phi = 1$

Problem 2:- Load containing

2. Load containing a resistor & an indicator.

$$V(t) = V_m \cos(\omega t + \theta_v) \quad \text{--- (1)}$$



$$V_L = L \frac{di}{dt} \quad \text{--- (2) [Faraday's Law]}$$

$$V_R = R i \quad \text{--- (3)}$$

$$V = V_L + V_R \quad \text{--- (4) [Using Kirchoff's Voltage Law]}$$

$$L \frac{di}{dt} + R i = V \quad \text{--- (5)}$$

Impedance -

$$Z = R + j \omega L$$

Simplified case -  $R = 0$

$$V_R = 0 \quad \text{--- (6)}$$

$$L \frac{di}{dt} = V = V_m \cos(\omega t + \theta_v)$$

$$i = \frac{1}{L} \int v dt \quad \text{--- (7)}$$

$$i = \frac{1}{L} \left[ V_m \sin(\omega t + \theta_v) \right]$$

Note:- Clearly,  $i$  &  $V$  of purely indicative circuit have  $\frac{\pi}{2}$  phase-difference, hence power-factor  $= 0$  i.e. power consumed - 0

$$P = V_{\text{rms}} I_{\text{rms}} \cos \phi$$

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$$i = \frac{V_m}{\omega L} \sin(\omega t + \theta_v) - \textcircled{8}$$

We define the reactance of the Inductor -

$$X_L = \omega L - \textcircled{9}$$

$$= 2\pi f L - \textcircled{10}$$

$$i = I_m \sin(\omega t + \theta_v) - \textcircled{11}$$

$$\Rightarrow i = I_m \cos(\omega t + \theta_v - \frac{\pi}{2})$$

$$\text{where, } I_m = \frac{V_m}{\omega L} - \textcircled{12}$$

$$i = I_m \cos(\omega t + \theta_p) - \textcircled{13}$$

$$\text{For } \theta_p = \theta_v - \frac{\pi}{2} - \textcircled{14}$$

Power Factor Angle

$$\phi = \theta_v - \theta_p - \textcircled{15}$$

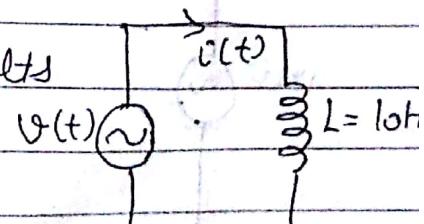
$$= \frac{\pi}{2}$$

$$\therefore P.F. = \cos \phi = 0 - \textcircled{16}$$

Q Consider a purely-inductive load connected to an A.C. Voltage source, as shown below:

$$V(t) = 314 \cos(314t + 45^\circ) \text{ Volts}$$

(given)



Calculate the r.m.s. value of current flowing in the load.

Also write mathematical expression depicting the dependence of load current on time.

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Sol.  $V_{\text{rms}} = \frac{311}{\sqrt{2}}$ ,  $\omega = 314$

$$V = L \frac{di}{dt}$$

$$\begin{aligned} i &= \frac{1}{L} \int V dt \\ &= \frac{1}{10} \int 311 \cos(314t + 45^\circ) dt \\ &= \frac{1}{10} \left[ \frac{311}{314} \sin(314t + 45^\circ) \right] \end{aligned}$$

$$\begin{aligned} X_L &= 2\pi f L = \omega L \\ &= 314 \times 10 = 3140 \Omega \end{aligned}$$

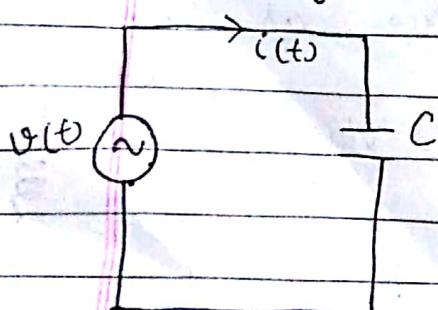
$$i = \frac{311}{3140} \sin(314t + 45^\circ) A \approx 0.1 \cos(314t - 45^\circ) A$$

$$I_{\text{rms}} = \frac{311}{3140 \times \sqrt{2}} \approx 0.07 A$$

~~P.F.~~

$$\begin{aligned} \text{P.F. angle} \rightarrow \phi &= \theta_V - \theta_I \\ &= \frac{\pi}{4} - (-\frac{\pi}{4}) = \frac{\pi}{2} \quad \therefore \text{P.F.} = \cos \phi = 0 \end{aligned}$$

Case 3: Purely-Capacitive load :-



$$v(t) = V_m \cos(\omega t + \theta_v) \quad \text{--- (1)}$$

$$i = C \frac{dv}{dt} \quad \text{--- (2)}$$

$$= -C V_m \omega \sin(\omega t + \theta_v) \quad \text{--- (3)}$$

The reactance of capacitor is defined as-

$$X_C = \frac{1}{\omega C} = \frac{1}{2\pi f C} \quad \text{--- (4)}$$

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$$i(t) = -\frac{V_m}{X_C} \sin(\omega t + \theta_v)$$

$$= -\frac{V_m}{X_C} \cos(\omega t + \theta_v + \frac{\pi}{2})$$

$$\theta_I = \frac{\pi}{2} + \theta_v$$

$$\Rightarrow \phi = \theta_v - \theta_I = -\frac{\pi}{2} = 0$$

Power factor  $\rightarrow \cos(-\frac{\pi}{2}) = 0$

Case 4: Load has  $R, L \& C$

$$v(t) = V_m \cos(\omega t + \theta_v) - ①$$

$$i(t) = I_m \cos(\omega t + \theta_I) - ②$$

$$I_m = \frac{V_m}{\sqrt{R^2 + (X_L - X_C)^2}} - ③$$

where,

$$X_L = 2\pi f L = \omega L - ④$$

$$X_C = \frac{1}{2\pi f C} = \frac{1}{\omega C} - ⑤$$

$$P.F. \text{ Angle: } \phi = \theta_v - \theta_I - ⑥$$

$$\phi = \tan^{-1} \left( \frac{X_L - X_C}{R} \right) - ⑦$$

$$P.F. = \cos \phi - ⑧$$

Average Power [True Power] :-

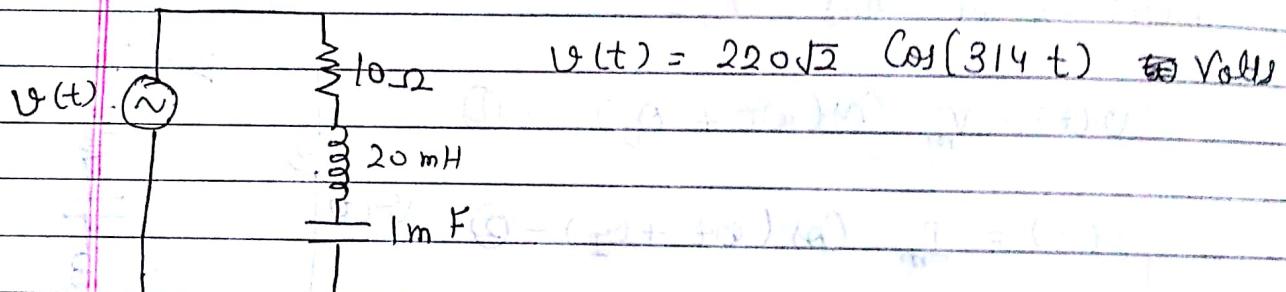
$$P = P_{\text{rms}} V_{\text{rms}} \cos \phi \quad [\text{Unit: Watts}]$$

Reactive Power [Phantom Power]:-

$$Q = V_{rms} \cdot I_{rms} \sin \phi \quad [\text{Unit: VAR}]$$

Voltage Ampere.

Q Calculate the power factor, the consumed power & reactive power in the load below:-



$$\phi = \tan^{-1} \left( \frac{x_1 - x_C}{R} \right)$$

$$X_1 = \frac{314 \times 20 \times 10^{-3}}{2} \Omega$$

$$= 6.28 \Omega$$

$$X_C = -\frac{1}{2\pi f C} = -\frac{1}{\omega C}$$

$$= \frac{1}{3.14 \times 1 \times 10^{-3}} \approx 3.19 - 2$$

$$\phi \approx \tan^{-1} \left( \frac{6.28 - 3.19}{10} \right)$$

$$\approx \tan^{-1}(0.309) \approx 17.17^\circ$$

$$P.F. \rightarrow \cos \phi \approx \cos(17.17^\circ) \approx 0.955$$

Consumed power  $\rightarrow P = \frac{220^2}{10^2 + 3.09^2} \approx 10.47$

$$P = 220 \times \frac{220}{10^2 + 3.09^2} \times \cos \phi$$

$$\approx \frac{220^2}{10.47} \times 0.955$$

$$\approx 4416 \text{ Watt}$$

Reactive Power  $\rightarrow Q = V_{\text{rms}} I_{\text{rms}} \sin \phi$   
 $= 1371.6 \text{ VAR}$   
 $= 1.3716 \text{ kVAR}$

### \* Power Triangle:-

(i) We define the true power (also known as consumed power, average power, real power, actual power, power dissipated etc.) as -

[ $P \rightarrow \text{watts}$ ]

$$P = V_{\text{rms}} I_{\text{rms}} \cos \phi \quad \text{--- (1)}$$

where  $\phi$  is the "power-factor angle" and  $\cos \phi$  is Power-factor

(ii) we also define the reactive power (also known as, imaginary power, phantom power etc.) as -

$$Q = V_{\text{rms}} I_{\text{rms}} \sin \phi \quad \text{--- (2)}$$

[ $'Q'$  is measured in VAR]

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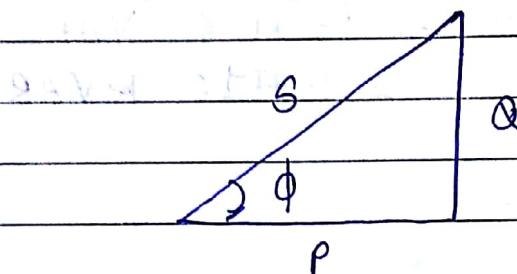
(iii) In addition "Apparent power" is defined as

$$S = V_{\text{rms}} I_{\text{rms}} \quad - \textcircled{3}$$

Note:- 'S' is measured in ~~VA~~ VA.

$$\therefore P = S \cos \phi \quad - \textcircled{4}$$

$$Q = S \sin \phi \quad - \textcircled{5}$$



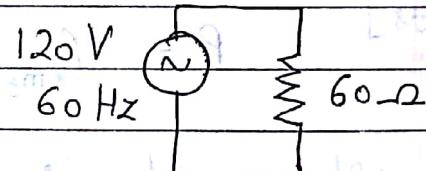
$$S = \sqrt{P^2 + Q^2} \quad - \textcircled{6}$$

$$\phi = \tan^{-1}\left(\frac{Q}{P}\right)$$

Now sketch the Power-Triangle for other circuit shown below:

Ans

$$P = V_{\text{rms}} I_{\text{rms}} \cos \phi$$



$$V_{\text{rms}} = 120 \text{ V} \quad (\text{given})$$

$$I_{\text{rms}} = \frac{120}{60} = 2 \text{ A}$$

$$\phi = 0^\circ$$

$$\therefore P = 120 \times 2 = 240 \text{ Watts}$$

$$\text{Now, } Q = 120 \times 2 \times 0 = 0 \text{ VAR}$$

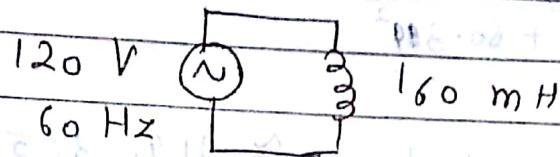
$$S = 240 \text{ VA}$$

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$$Q = 0, \phi = 0$$

$$S = P = 240$$

Q2. Repeat the problem 1 for the circuit shown below:



$$\text{Ans} \quad \phi = \frac{\pi}{2}, V_{\text{rms}} = 120$$

$$X_L = 2\pi f L = 2 \times 3.14 \times 60 \times 160 \times 10^{-3}$$

$$= \frac{60.288}{2} \approx 60.319 \Omega$$

$$I_{\text{rms.}} = \frac{120}{60} \approx 2 \text{ A}$$

$$\text{Here, } P = 0$$

$$Q \approx 120 \times 2 = 238.73 \text{ VAR}$$

$$S = 238.73 \text{ VA}$$

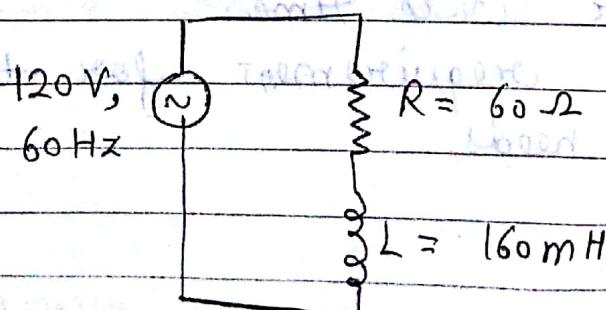
Inbetwile addt. to

$$Q = S = 238.75$$

because  $\phi = \frac{\pi}{2}$  addt. in leading

$$\phi = \frac{\pi}{2} \text{ addt. in leading}$$

Q Repeat problem 1 for the circuit shown below:



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$$\phi = \tan^{-1} \left( \frac{X_L - X_C}{R} \right) = \tan^{-1} \left( \frac{X_L}{R} \right) =$$

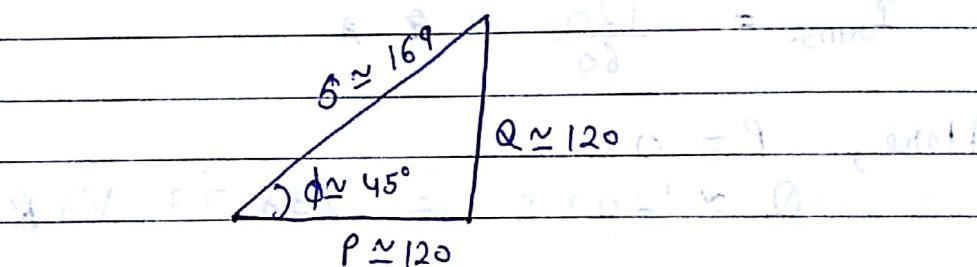
$$\approx 45^\circ : 15^\circ$$

$$P_{\text{rms}} = \frac{120}{\sqrt{60^2 + 60 \cdot 30^2}} \approx 1.41$$

$$P \approx 120 \times 1.41 \times \frac{1}{\sqrt{2}} \approx 119.365 \text{ Watts}$$

$$Q \approx 119.998 \text{ VAR}$$

$$S = \sqrt{P^2 + Q^2} \\ \approx 169.256 \text{ VA}$$

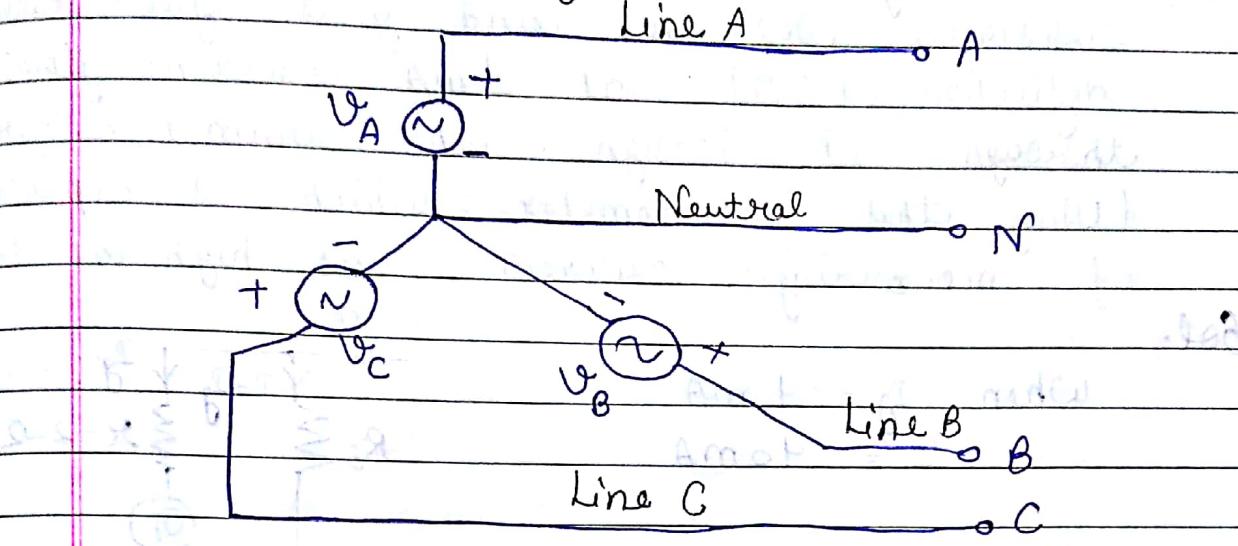


### \* Three-Phase systems:-

Most of the electrical power in Today's world is generated using three-phase systems. Advantage of a three-phase system over a single-phase system are:

- (i) Constant-power with time
- (ii) Less material requirement for the same power needs.

(a) Star - Connected generators :-

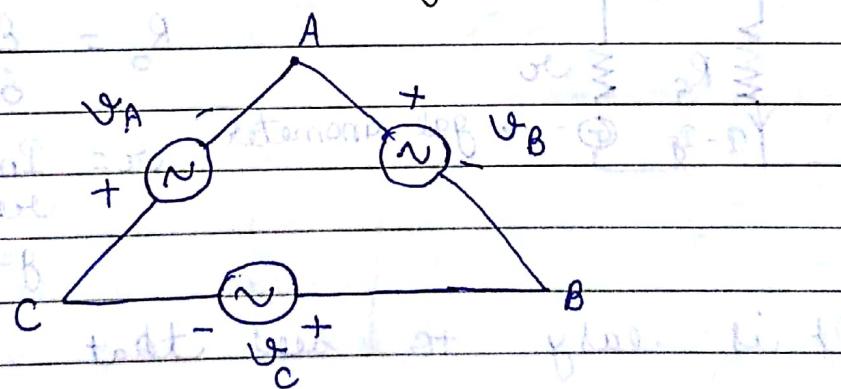


$$V_A = V_m \cos(\omega t) \text{ Volts}$$

$$V_B = V_m \cos(\omega t + 120^\circ) \text{ Volts}$$

$$V_C = V_m \cos(\omega t + 240^\circ) \text{ Volts}$$

(b) Delta - Connected systems



Load can also be A type or Star type

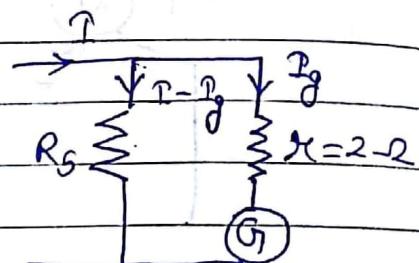
Teacher's Signature

Q A moving-coil Galvanometer has internal resistance ( $r_g$ ) =  $2\Omega$  and gives full-scale deflection (F.S.D) at  $1\text{ mA}$  current flowing through it. Design the ammeter circuit (using this galvanometer) which is capable of measuring current as high as  $10\text{ mA}$ .

Sol.

When  $I_g = 1\text{ mA}$

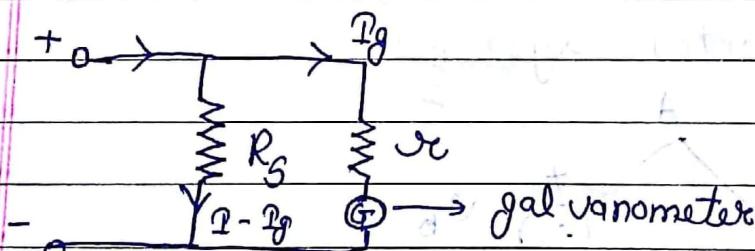
$\therefore I = 10\text{ mA}$



$$(I - I_g) R_s = r_g \times I_g$$

$$\Rightarrow R_s = \frac{r_g I_g}{I - I_g} = \frac{2 \times 1}{9} = \frac{2}{9} \Omega$$

\* Equations for analyzing/designing an ammeter (Ammeter-meters)



$R_s$  = External shunt resistance

$r_g$  = Internal resistance of galvanometer G

It is easy to see that

$$R_s \cdot (I - I_g) = r_g I_g \quad \text{--- (1)}$$

$$\therefore R_s I = I_g (r_g + R_s)$$

$$\therefore \frac{I_g}{I} = \frac{R_s}{R_s + R_g} \quad \text{--- (2)}$$

Q You are given the ammeter circuit shown below. It is given that  $R_g = 2\Omega$  and  $R_s = 10\Omega$ . It is also known that the galvanometer shows full-scale deflection (F.S.D) when the galvanometer current =  $100\mu A$ . Over what range can this ammeter measure current?

Ans

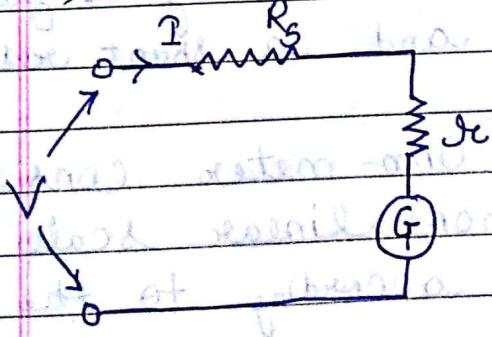
$$R_{FSD} = 100 \quad I_g = 100\mu A$$

(Galvanometer - mid)

$$R_{FSD} = \frac{I_g \times (R_s + R_g)}{R_s}$$

$$= 100 \times \frac{12}{10} = 120\mu A$$

\* Equations for Analysing/Designing a Voltmeter:-



$$V_g = I \cdot R_g \quad \text{(F.S.D)} \quad \text{--- (1)}$$

$$I = \frac{V}{R_s + R_g} = \frac{V}{R_s + R_g} \quad \text{--- (2)}$$

$$V_g = \frac{R_g}{R_s + R_g} V \quad \text{--- (3)}$$

By KVL,

$$\begin{aligned} V &= I R_s + V_g \\ &= \frac{V R_s}{R_s + R_g} + V_g \end{aligned}$$

$$\Rightarrow V \left[ 1 - \frac{R_g}{R_s + R_g} \right] = V_g$$

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Q. Using a galvanometer with internal resistance =  $1\ \Omega$  and FSD current =  $1\text{mA}$ . Design a Voltmeter capable of measuring voltages as high as  $50\text{V}$ .

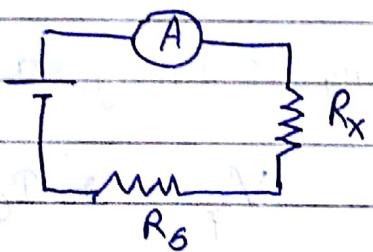
Ans  $V_G = 1\ \Omega \times 1\text{mA} = 1\text{mV}$

$$V_{FSD} = \left( \frac{R_s + R}{R_s} \right) V_G = 50$$

$$\Rightarrow R_s \approx 50\text{ k}\Omega$$

\* Ohm-meter:-

== A simple Ohm-meter consists of a battery, an ammeter, and a safety resistance  $R_s$ , all connected in series with the resistance being measured.



The ammeter itself consists of a galvanometer and a shunt resistance.

The display of an Ohm-meter consists of an inverted non-linear scale calibrated in Ohms, according to the following equation:

$$I = \frac{V}{R_s + R_x} \quad \text{--- (1)}$$

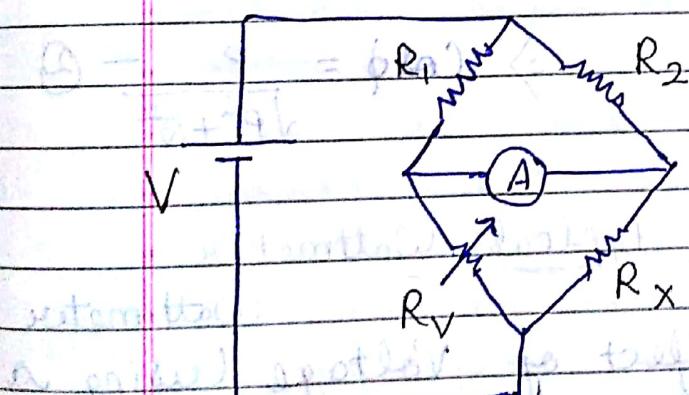
$$\text{i.e. } R_x = \frac{V}{I} - R_s \quad \text{--- (2)}$$

## ★ Measuring Small resistance Values using Wheatstone Bridge:

For small resistances, typically less than  $6\Omega$ , moving-coil based Ohm meter display poor accuracy, since they do not separate the resistance to be measured ( $R_x$ ) from the resistance of the wires used for making the circuit, internal resistance of the battery, errors in obtaining precise values of the safety resistance ( $R_g$ ), etc.

In such cases, we use Wheat-stone Bridge which is Null-Type Instrument

(not a DEFLECTION-Type instrument)



The ammeter in this circuit should be able to handle currents in both directions. It does not have to be highly accurate for non-zero current values.

The ammeter must, however, be able to reliably indicate which way the current is flowing through it, and also when the current fully vanishes when

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Null-condition is obtained by varying  $R_V$ , the unknown resistance ' $R_X$ ' can be calculated using -

$$R_X = \left( \frac{R_2}{R_1} \right) R_V \quad \text{--- (1)}$$

- ~~Watt-meters :-~~
- ~~(i)~~ Watt-meters :- (i) is used to measure Average Power 'P'.
  - (ii) VAR-meters are used to measure Reactive Power 'Q'.
  - (iii) Power factor can be measured using Power triangle.

$$\cos \phi = \text{P.F.}$$

$$\frac{P}{S} = \text{P.F.} \quad \text{--- (1)}$$

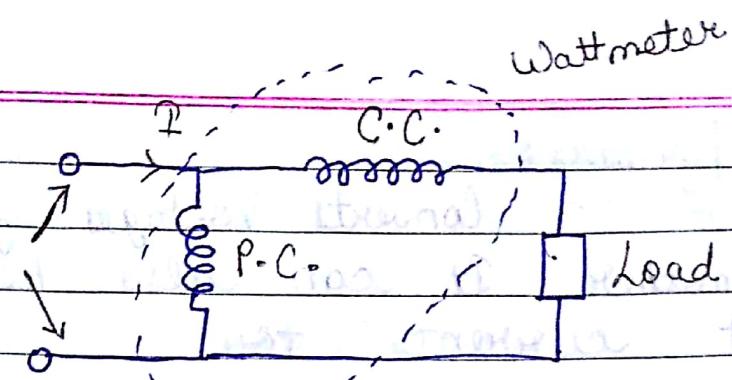
$$\Rightarrow \cos \phi = \frac{P}{\sqrt{P^2 + Q^2}} \quad \text{--- (2)}$$

### Construction of a Typical Wattmeter

Combines the effect of Voltage (using a "Voltage Coil" which is known as "pressure coil") and current (using a "Current coil")

P.C.  $\Rightarrow$  Pressure coil

C.C.  $\Rightarrow$  Current coil



Schematic

Wattmeter Types:-

- (i) Dynamometer type → Commonly used for DC power (Using two coils)
- (ii) Induction Type → Commonly used for AC power
- (iii) Electrostatic Type → Not much used because Torque/weight ratio is small

(i) Induction Type Wattmeter - (a) works on the principle of torque produced induced production by induced currents in a short-circuited coil which is under the influence of other current-carrying coils.

(b) Induction Type Wattmeters are used only for AC measurements.

(c) The few decisive advantages of the induction type Wattmeter are sturdy construction, very long circular scale, reasonably-low torque/weight ratio; almost maintenance-free operation etc.

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