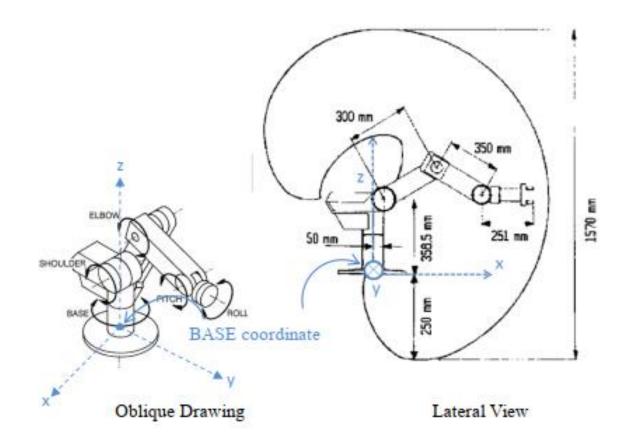
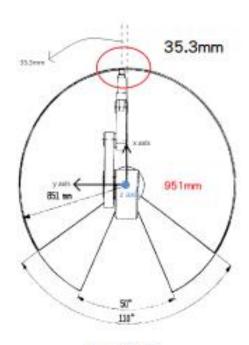
# **Robotics: Assignment II**

## Forward Kinematics and Inverse Kinematics

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# Consider the ER-7 robot arm shown in the following figures:

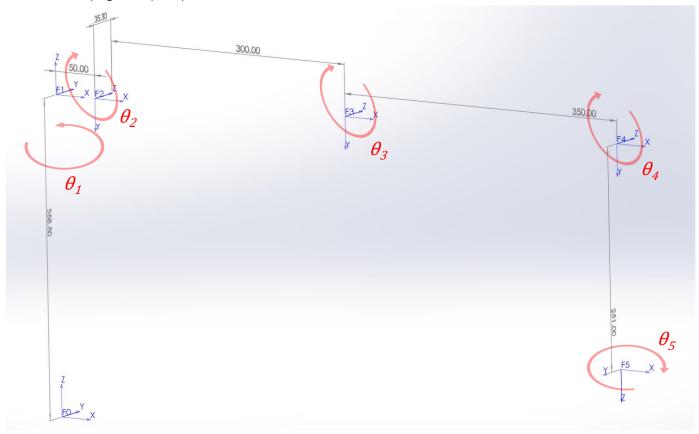




Top View

### Part A (25%)

(1) According to ER-7 arm, draw the link coordinate diagram using D-H convention in Craig version from lecture slides page 34. (10%)



(2) Find the kinematics parameters of ER-7 and fill the table below: (15%)

ER-7				
Joint	$\alpha i-1$	°) <b>ai-1</b> (mm)	<b>di</b> (mm)	θί
1	0	0	358.5	<b>0</b> 1
2	-90	50	0	<b>0</b> 2
3	0	300	35.3	<b>0</b> 3
4	0	350	0	<b>0</b> 4
5	-90	0	251	<b>0</b> 5

#### **PART B (30%)**

(1) Derive transformation matrices for each consecutive link, and also the transformation matrices  $T_5^0$  (from frame 5 to frame 0).

Note: This should be revised to list all the transformation matrix, i.e.  $T_1^{base}$ ,  $T_2^1$ ,  $T_3^2$ ,  $T_4^3$ ,  $T_5^4$ ,  $T_5^{base}$ .

#### Part C (45%)

(1) Derive the inverse kinematics for ER-7. Given the target pose of the gripper tip  $(x, y, z, \varphi, \theta, \psi)$  with respect to the base coordinate, calculate  $(\theta 1, \theta 2, \theta 3, \theta 4, \theta 5)$ . For the transformation from the base to the gripper tip, please refer to Inverse Kinematic slides. Let's assume the target is reachable in elbow-up configuration, and that the gripper tip pose is always vertically downward. (30%)

Because the tip pose is always vertically downward, the x y z is determined only by th1, th2, th3, and the z axis of frame 5 is always negative to the frame 0. So the x4 y4 z4 in T04 = x y z+251, with this correlation we can calculate th1 th2 th3. For elbow up configuration, we choose the [th1 th2 th3] set when th2 < 0 for afterward calculation.

$$\begin{split} 50\cos(th_1) - \frac{353\sin(th_1)}{10} + 300\cos(th_1)\cos(th_2) - 350\cos(th_1)\sin(th_2)\sin(th_3) + 350\cos(th_1)\cos(th_2)\cos(th_3) = &\chi \\ \frac{353\cos(th_1)}{10} + 50\sin(th_1) + 300\cos(th_2)\sin(th_1) - 350\sin(th_1)\sin(th_2)\sin(th_3) + 350\cos(th_2)\cos(th_3)\sin(th_1) = &\chi \\ \frac{717}{2} - 350\cos(th_2)\sin(th_3) - 350\cos(th_3)\sin(th_2) - 300\sin(th_2) = &\chi + 251 \end{split}$$

For th4, if we take some of the elements of T15 and do atan2, we can know  $\theta 2 + \theta 3 + \theta 4$ , as  $\theta 2 \theta 3$  is already known,  $\theta 4$  can be found by subtracting.

$dy$ known, $\theta 4$ can be found by subtracting.	
$V_{12} = -\frac{1}{5} \frac{1}{234}$ $V_{12} = -\frac{1}{5} \frac{1}{234}$ $V_{13} = -\frac{1}{5} \frac{1}{234}$	(0 1 2 52 1000 0 1 0 52 0 600 0 - 2 52 0 519 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
1/24=-85 1/24=-85	12 
1/22 - C9 T15	02+03+04=-4
1/3/=-{23469	6
1832 = 6234 85 (23 - 6423) = - (234 1832 = -1. [C4 = -6423] = - (234 1834 = -3.0062-25(E4 623 + 25)64823	350 (263 - 350)3/2
= -30092 -271 (234 - 77 (23	
tan (-1/33) = 02+03+04	

$$th4_n = atan2(T15_subs(1,3), -T15_subs(3,3)) - S.th2(2,1) - S.th3(2,1);$$

For th5, because the tip is always vertically downward, the desired roll is done only by  $\theta 1$  and  $\theta 5$ ; so we can add  $\theta 1$  and the roll to get  $\theta 5$ . As in my code written.

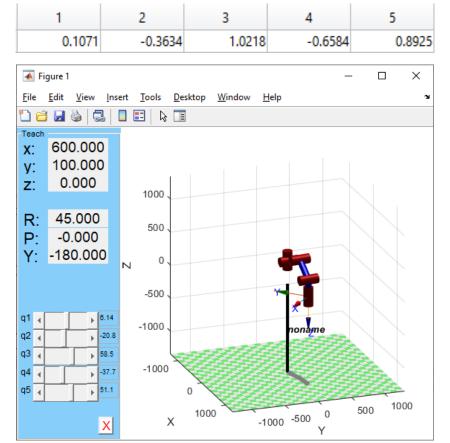
$$th5 = phi + S.th1(2,1);$$

Because the constraint of the question, the  $\theta$ ,  $\psi$  remain the same (0, pi).

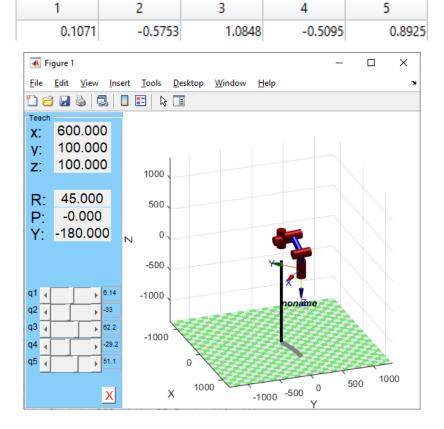
(2) Based on the previous question, please calculate ( $\theta$ 1 ,  $\theta$ 2 ,  $\theta$ 3 ,  $\theta$ 4 ,  $\theta$ 5 ) with the following target poses. The translation parameters (x, y, z) are in millimeter, and the rotation parameters ( $\phi$ ,  $\theta$ ,  $\psi$ ) are in radian. (15%)

For more information please refer my MATLAB code. (Please install Peter Corke's robotics toolbox add-in to get a better experience).

(1)  $(x, y, z, \phi, \theta, \psi) = (600,100,0, \pi/4, 0, \pi)$ 

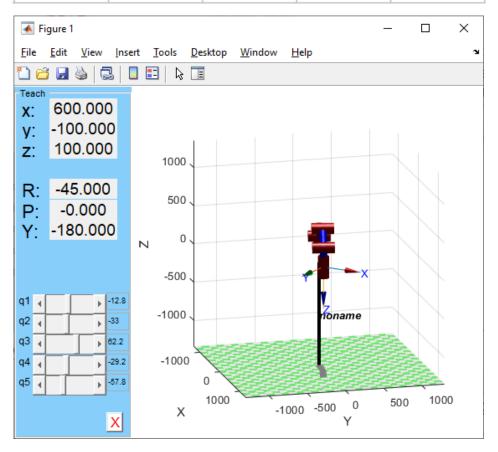


(2)  $(x, y, z, \phi, \theta, \psi) = (600, 100, 100, \pi/4, 0, \pi)$ 



(3)  $(x, y, z, \phi, \theta, \psi) = (600, -100, 100, -\pi/4, 0, \pi)$ 

1	2	3	4	5
-0.2232	-0.5753	1.0848	-0.5095	-1.0086



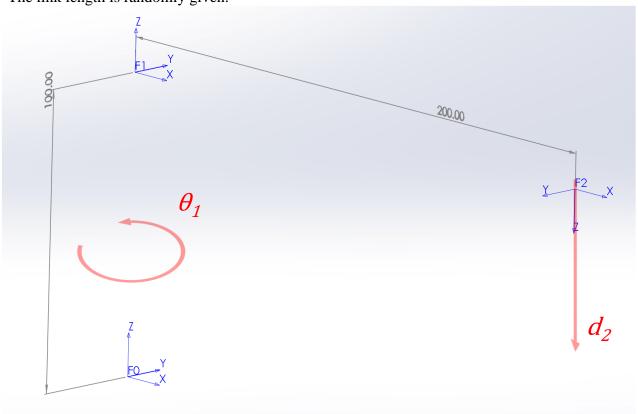
## PART D (10%) bonus

Consider the following robot arm which is consist of a revolute joint and prismatic joint:



(1) Find the DH representation the same as Part A (1) (6%)

The link length is randomly given.



SCARA				
Joint	αi-1 (*)	ai-1 (mm)	di (mm)	$\theta i$
1	0	0	d1	<b>0</b> 1
2	180	a2	d2	0

(2) For all DH parameters ( $\alpha_{i-1}$ ,  $\alpha_{i-1}$ ,  $d_i$ ,  $\theta_i$ ), which two parameters are actuator joint (varying parameters)? (4%)

 $\theta_1$  and  $d_2$  are varying parameters, since joint 1 is a revolute joint, and joint 2 is a prismatic joint.