### Codeforces Round #636 (Div. 3)

### A. Candies

1 second, 256 megabytes

Recently Vova found n candy wrappers. He remembers that he bought x candies during the first day, 2x candies during the second day, 4x candies during the third day,  $\dots$ ,  $2^{k-1}x$  candies during the k-th day. But there is an issue: Vova remembers neither x nor k but he is sure that x and k are positive integers and k>1.

Vova will be satisfied if you tell him **any positive** integer x so there is an integer k>1 that  $x+2x+4x+\cdots+2^{k-1}x=n$ . It is guaranteed that at least one solution exists. **Note that** k>1.

You have to answer t independent test cases.

#### Input

The first line of the input contains one integer t ( $1 \le t \le 10^4$ ) — the number of test cases. Then t test cases follow.

The only line of the test case contains one integer n ( $3 \le n \le 10^9$ ) — the number of candy wrappers Vova found. It is guaranteed that there is some positive integer x and integer k > 1 that  $x + 2x + 4x + \cdots + 2^{k-1}x = n$ .

#### Output

Print one integer — any positive integer value of x so there is an integer k>1 that  $x+2x+4x+\cdots+2^{k-1}x=n$ .

input		
7		
3		
6		
7		
21		
28		
99999999		
999999984		
output		
1		
2		
1		
7		
4		
333333333		
333333328		

In the first test case of the example, one of the possible answers is x=1, k=2. Then  $1\cdot 1+2\cdot 1$  equals n=3.

In the second test case of the example, one of the possible answers is x=2, k=2. Then  $1\cdot 2+2\cdot 2$  equals n=6.

In the third test case of the example, one of the possible answers is x=1,k=3. Then  $1\cdot 1+2\cdot 1+4\cdot 1$  equals n=7.

In the fourth test case of the example, one of the possible answers is x=7, k=2. Then  $1\cdot 7+2\cdot 7$  equals n=21.

In the fifth test case of the example, one of the possible answers is x=4, k=3. Then  $1\cdot 4+2\cdot 4+4\cdot 4$  equals n=28.

# B. Balanced Array

1 second, 256 megabytes

You are given a positive integer n, it is guaranteed that n is even (i.e. divisible by 2).

You want to construct the array a of length n such that:

- The first  $\frac{n}{2}$  elements of a are even (divisible by 2);
- the second  $\frac{n}{2}$  elements of a are odd (not divisible by 2);
- all elements of a are distinct and positive;

• the sum of the first half equals to the sum of the second half (

$$\sum_{i=1}^{rac{n}{2}} a_i = \sum_{i=rac{n}{2}+1}^n a_i$$
).

If there are multiple answers, you can print any. It is **not guaranteed** that the answer exists.

You have to answer t independent test cases.

#### Input

The first line of the input contains one integer t ( $1 \le t \le 10^4$ ) — the number of test cases. Then t test cases follow.

The only line of the test case contains one integer n ( $2 \le n \le 2 \cdot 10^5$ ) — the length of the array. It is guaranteed that that n is even (i.e. divisible by 2).

It is guaranteed that the sum of n over all test cases does not exceed  $2\cdot 10^5$  (  $\sum n \le 2\cdot 10^5$  ).

#### Output

For each test case, print the answer — "N0" (without quotes), if there is no suitable answer for the given test case or "YES" in the first line and **any** suitable array  $a_1, a_2, \ldots, a_n$   $(1 \le a_i \le 10^9)$  satisfying conditions from the problem statement on the second line.

```
input

5
2
4
6
8
10

output

NO
YES
2 4 1 5
NO
YES
2 4 6 8 1 3 5 11
NO
```

## C. Alternating Subsequence

1 second, 256 megabytes

Recall that the sequence b is a a subsequence of the sequence a if b can be derived from a by removing zero or more elements without changing the order of the remaining elements. For example, if a=[1,2,1,3,1,2,1], then possible subsequences are: [1,1,1,1], [3] and [1,2,1,3,1,2,1], but not [3,2,3] and [1,1,1,1,2].

You are given a sequence a consisting of n positive and negative elements (there is no zeros in the sequence).

Your task is to choose **maximum by size** (length) *alternating* subsequence of the given sequence (i.e. the sign of each next element is the opposite from the sign of the current element, like positive-negative-positive and so on or negative-positive-negative and so on). Among all such subsequences, you have to choose one which has the **maximum sum** of elements.

In other words, if the maximum length of *alternating* subsequence is k then your task is to find the **maximum sum** of elements of some *alternating* subsequence of length k.

You have to answer t independent test cases.

### Input

The first line of the input contains one integer t ( $1 \le t \le 10^4$ ) — the number of test cases. Then t test cases follow.

The first line of the test case contains one integer n ( $1 \le n \le 2 \cdot 10^5$ ) — the number of elements in a. The second line of the test case contains n integers  $a_1, a_2, \ldots, a_n$  ( $-10^9 \le a_i \le 10^9, a_i \ne 0$ ), where  $a_i$  is the i-th element of a.

It is guaranteed that the sum of n over all test cases does not exceed  $2\cdot 10^5$  ( $\sum n \le 2\cdot 10^5$ ).

### Output

For each test case, print the answer — the **maximum sum** of the **maximum by size** (length) *alternating* subsequence of a.

```
input

4
5
1 2 3 -1 -2
4
-1 -2 -1 -3
10
-2 8 3 8 -4 -15 5 -2 -3 1
6
1 -1000000000 1 -100000000 1 -100000000

output

2
-1
6
-29999999997
```

In the first test case of the example, one of the possible answers is [1,2,3,-1,-2] .

In the second test case of the example, one of the possible answers is [-1, -2, -1, -3].

In the third test case of the example, one of the possible answers is [-2,8,3,8,-4,-15,5,-2,-3,1].

### D. Constant Palindrome Sum

1 second, 256 megabytes

You are given an array a consisting of n integers (it is guaranteed that n is even, i.e. divisible by a). All a does not exceed some integer a.

Your task is to replace the **minimum** number of elements (replacement is the following operation: choose some index i from 1 to n and replace  $a_i$  with some integer in range [1;k]) to satisfy the following conditions:

- after all replacements, all  $a_i$  are positive integers not greater than k;
- for all i from 1 to  $\frac{n}{2}$  the following equation is true:  $a_i+a_{n-i+1}=x$ , where x should be **the same** for all  $\frac{n}{2}$  pairs of elements.

You have to answer t independent test cases.

### Input

The first line of the input contains one integer t ( $1 \le t \le 10^4$ ) — the number of test cases. Then t test cases follow.

The first line of the test case contains two integers n and k (  $2 \leq n \leq 2 \cdot 10^5, 1 \leq k \leq 2 \cdot 10^5$ ) — the length of a and the maximum possible value of some  $a_i$  correspondingly. It is guratanteed that n is even (i.e. divisible by 2). The second line of the test case contains n integers  $a_1, a_2, \ldots, a_n$  ( $1 \leq a_i \leq k$ ), where  $a_i$  is the i-th element of a.

It is guaranteed that the sum of n (as well as the sum of k) over all test cases does not exceed  $2\cdot 10^5$  ( $\sum n \le 2\cdot 10^5$ ).

### Output

For each test case, print the answer — the  $\min \min$  number of elements you have to replace in a to satisfy the conditions from the problem statement.

```
input

4
4 2
1 2 1 2
4 3
1 2 2 1
8 7
6 1 1 7 6 3 4 6
6 6
5 2 6 1 3 4

output

0
1
4
2
```

# E. Weights Distributing

2 seconds, 256 megabytes

You are given an undirected unweighted graph consisting of n vertices and m edges (which represents the map of Bertown) and the array of prices p of length m. It is guaranteed that there is a path between each pair of vertices (districts).

Mike has planned a trip from the vertex (district) a to the vertex (district) b and then from the vertex (district) b to the vertex (district) c. He can visit the same district twice or more. But there is one issue: authorities of the city want to set a price for using the road so if someone goes along the road then he should pay the price corresponding to this road (he pays each time he goes along the road). The list of prices that will be used p is ready and they just want to distribute it between all roads in the town in such a way that each price from the array corresponds to exactly one

You are a good friend of Mike (and suddenly a mayor of Bertown) and want to help him to make his trip as cheap as possible. So, your task is to distribute prices between roads in such a way that if Mike chooses the optimal path then the price of the trip is the **minimum** possible. **Note that you cannot rearrange prices after the start of the trip**.

You have to answer t independent test cases.

### Input

The first line of the input contains one integer t ( $1 \le t \le 10^4$ ) — the number of test cases. Then t test cases follow.

The first line of the test case contains five integers n,m,a,b and c (  $2 \leq n \leq 2 \cdot 10^5$ ,  $n-1 \leq m \leq min(\frac{n(n-1)}{2}, 2 \cdot 10^5)$ ,  $1 \leq a,b,c \leq n$ ) — the number of vertices, the number of edges and districts in Mike's trip.

The second line of the test case contains m integers  $p_1,p_2,\ldots,p_m$  (  $1\leq p_i\leq 10^9$ ), where  $p_i$  is the i-th price from the array.

The following m lines of the test case denote edges: edge i is represented by a pair of integers  $v_i,\,u_i~(1\leq v_i,u_i\leq n,u_i\neq v_i)$ , which are the indices of vertices connected by the edge. There are no loops or multiple edges in the given graph, i. e. for each pair  $(v_i,u_i)$  there are no other pairs  $(v_i,u_i)$  or  $(u_i,v_i)$  in the array of edges, and for each pair  $(v_i,u_i)$  the condition  $v_i\neq u_i$  is satisfied. It is guaranteed that the given graph is connected.

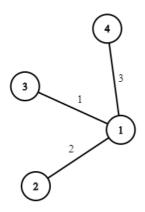
It is guaranteed that the sum of n (as well as the sum of m) does not exceed  $2\cdot 10^5$  ( $\sum n\le 2\cdot 10^5$ ,  $\sum m\le 2\cdot 10^5$ ).

# Output

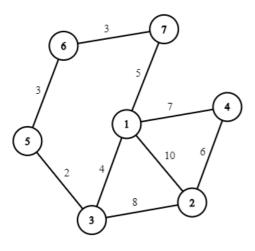
For each test case, print the answer — the **minimum** possible price of Mike's trip if you distribute prices between edges optimally.

```
input
4 3 2 3 4
1 2 3
1 2
1 3
1 4
  9 1 5 7
2 10 4 8 5 6 7 3 3
1 2
1 3
1 4 3 2
3 5
4 2
5 6
1 7
6 7
output
12
```

One of the possible solution to the first test case of the example:



One of the possible solution to the second test case of the example:



### F. Restore the Permutation by Sorted Segments

2 seconds, 256 megabytes

We guessed a permutation p consisting of n integers. The permutation of length n is the array of length n where each element from 1 to n appears exactly once. This permutation is a secret for you.

For each position r from 2 to n we chose some other index l (l < r) and gave you the segment  $p_l, p_{l+1}, \ldots, p_r$  in **sorted** order (i.e. we rearranged the elements of this segment in a way that the elements of this segment are sorted). Thus, you are given exactly n-1 segments of the initial permutation but elements inside each segment are sorted. The segments are given to you in random order.

For example, if the secret permutation is p=[3,1,4,6,2,5] then the possible given set of segments can be:

- [2, 5, 6]
- [4, 6]
- [1, 3, 4]
- [1, 3]
- [1, 2, 4, 6]

Your task is to find **any** suitable permutation (i.e. any permutation corresponding to the given input data). It is guaranteed that the input data corresponds to some permutation (i.e. such permutation exists).

You have to answer t independent test cases.

### Input

The first line of the input contains one integer t ( $1 \le t \le 100$ ) — the number of test cases. Then t test cases follow.

The first line of the test case contains one integer n ( $2 \le n \le 200$ ) — the length of the permutation.

The next n-1 lines describe given segments.

The i-th line contains the description of the i-th segment. The line starts with the integer  $k_i$  ( $2 \le k_i \le n$ ) — the length of the i-th segment. Then  $k_i$  integers follow. All integers in a line are distinct, sorted in ascending order, between 1 and n, inclusive.

It is guaranteed that the required p exists for each test case.

It is also guaranteed that the sum of n over all test cases does not exceed  $200~(\sum n \leq 200)$ .

### Output

For each test case, print the answer: n integers  $p_1,p_2,\ldots,p_n$  (  $1\leq p_i\leq n$ , all  $p_i$  should be distinct) — any suitable permutation (i.e. any permutation corresponding to the test case input).

```
input
5
6
3 2 5 6
2 4 6
3 1 3 4
2 1 3
4 1 2 4 6
5
2
2
2
2
7
  2 3
  1 2
   1 4
   4 5
3 1 2 6
4 1 3 5 6
2 1 2
3 4 5 7
6 1 2 3 4 5 6
3
  1 3 6
2
  1 2
5
2
  2 5
3 2 3 5
4 2 3 4 5
5 1 2 3 4 5
```

```
    output

    3 1 4 6 2 5

    3 2 1 4 5

    2 1 6 3 5 4 7

    1 2

    2 5 3 4 1
```

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