A Fiscal Decomposition of Unexpected Inflation: Cross-Country Estimates and Theory

Livio C. Maya

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Introduction: The Fiscal Sources of Unexpected Inflation

- The Valuation Equation of Public Debt

$$\frac{\text{Market Value of Debt } (\textbf{Bond Prices})}{\textbf{Price Level}} = \text{Intrinsic Value } (\textbf{Discounting}, \textbf{Surpluses}).$$

- Unexpected inflation $\Delta E_t \Pi_t$ must accompany news about:
  - Bond prices Q_t
  - Real surpluses $\{s_{t+k}\}$
  - Real discounting $\{R_{t+k}\}$

$$\Delta E_t \Pi_t = \Delta E_t \left[Q_t - \{s_{t+k}\} + \{R_{t+k}\} \right]$$

- If unexpected inflation exists, it must nowcast/forecast some of these variables
- What are these forecasts? How do they change across countries? How can theory explain them?

- **This paper.**
  1. Estimate a Bayesian-VAR to measure the decomposition for 25 countries
     - Variance decomposition: $\text{var}\left[\Delta E\,\Pi\right] = \text{cov}\left[\Delta E\,\Pi, \quad Q + \{-s\} + \{R\}\right]$
     - ”Aggregate demand” shock: recession + low inflation
  2. Estimate a New-Keynesian model to reproduce B-VAR decompositions
- **Motivation.** How do you read Debt/Price = Discounted Surpluses?
  - Active fiscal: *”How does inflation react to changes in discounted surpluses?”*
    - Surpluses x Inflation in a given economy
    - Surpluses x Inflation across countries
    - Role of monetary policy?
    - Theory: which shocks cause inflation surprises?
  - Active monetary: *”How should discounted surpluses adjust to unexpected inflation?”*

Introduction: Exercises, Motivation, Results

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Introduction: Preview of Key Results

- The variance of unexpected inflation is accounted for by discounted surpluses (all coutries)

$$\underbrace{\text{var}\left[\Delta E\pi\right]}_{>0} = \underbrace{\text{cov}\left[\Delta E\pi, Q\right]}_{<0} + \underbrace{\text{cov}\left[\Delta E\pi, \{-s\} + \{R\}\right]}_{>0}$$

  - Most relevant terms (Surplus-to-GDP, GDP growth and Real discounting) vary
  - Monetary policy trades current for future unexpected inflation
- Lower inflation in recessions: low discounting + higher subsequent surpluses
- Productivity shocks reproduce findings in NK model
  - Policy shocks do not
- Different policy rules explain differences in variance decomposition across countries

Introduction: Related Literature

- **Fiscal Theory of the Price Level.** Cochrane (2022a) and Cochrane (2022b).
  - Analysis of multiple countries + more general debt instruments
  - NK model estimated to reproduce decompositions + Productivity shocks

  Leeper (1991), Sims (1994), Cochrane (1998), Cochrane (2005), Sims (2011), Leeper and Leith (2016), Bassetto and Cui (2018), Cochrane (2022c), Brunnermeier et al. (2022).

- **Monetary-Fiscal Interaction.**
  Cagan (1956), Sargent and Wallace (1981), Hall and Sargent (1997), Hall and Sargent (2011), Jiang et al. (2019), Corsetti et al. (2019), Sunder-Plassmann (2020), Du et al. (2020), Akhmadieva (2022)

- **Empirical Finance** (Decomposition of Returns)
  Campbell and Shiller (1988), Cochrane (1992), Campbell and Ammer (1993), Chen and Zhao (2009).

Fiscal Decomposition: The Valuation Equation

- Environment with discrete time + single good (price P_t) + households and government
- One-period nominal public bonds (price Q_t)
- **In the morning**, the government:
  - redeems bonds B_{t-1} for currency
  - announces real taxes s_t (payable in currency)
  - announces sale of B_t new bonds (payable in currency)
- **In the afternoon**, households trade goods, purchase bonds, pay taxes
- Market clearing + No Money Holding $M = 0$:

$$\boxed{B_{t-1} = P_t s_t + Q_t B_t}$$

Fiscal Decomposition: The Valuation Equation

$$B_{t-1} = P_t s_t + Q_t B_t$$

- *Ex-post* real discounting $\beta_t = Q_t(P_{t+1}/P_t)$ $\beta_{t,t+k} = \prod_{\tau=t}^{t+k} \beta_\tau$
- Iterate law of motion forward:

$$\frac{B_{t-1}}{P_t} = \sum_{k=0}^{p} \beta_{t,t+k-1} s_{t+k} + \beta_{t,t+p} \frac{B_{t+p}}{P_{t+p+1}}$$

- **Key Assumption**: $\lim_{\tau\to\infty} \beta_{t,\tau} \frac{B_\tau}{P_{\tau+1}} = 0$ almost surely (No bubbles)
  - In Macro models: transversality conditions + no Ponzi
- The valuation equation of public debt

$$\frac{B_{t-1}}{P_t} = \sum_{k=0}^{\infty} E_t \left[\beta_{t,t+k-1} s_{t+k}\right]$$

Fiscal Decomposition: In the Simplest Environment

- Nominal rate $1 + i_t = 1/Q_t$ and real interest $r_t = i_t - E_t\pi_{t+1}$
- End-of-period real debt v_t

$$\underbrace{\frac{1}{\beta}v_{t-1} + \frac{v}{\beta}\left(i_{t-1} - \pi_t\right)}_{B_{t-1}/P_t} = s_t + v_t = \sum_{k=0}^{\infty}\beta^k E_t s_{t+k} - \frac{v}{\beta}\sum_{k=1}\beta^k E_t r_{t+k}$$

Linearized valuation equation (all variable in deviations from their mean)

- Innovations $\Delta E_t = E_t - E_{t-1}$ decomposition:

$$\boxed{\Delta E_t \pi_t = -\frac{\beta}{v}\sum_{k=0}^{\infty}\beta^k \Delta E_t s_{t+k} + \sum_{k=0}^{\infty}\beta^k \Delta E_t r_{t+k}}$$

- Variance decomposition:

$$\mathrm{var}\left[\Delta E_t \pi_t\right] = -\mathrm{cov}_\pi\left[\frac{\beta}{v}\sum_{k=0}^{\infty}\beta^k \Delta E_t s_{t+k}\right] + \mathrm{cov}_\pi\left[\sum_{k=0}^{\infty}\beta^k \Delta E_t r_{t+k}\right]$$

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Fiscal Decomposition: Currency and Term Structures + Growth

- Real **market value** debt-to-GDP v_t, surplus-to-GDP s_t and GDP growth g_t (stationarity!)
- Bonds (j, n) promisses one unit of currency j after n periods Currencies
  - Nominal bonds
  - Real bonds (currency denomination = final goods)
  - US Dollar bonds

  Constant structure $\{\delta_j\}$, $\{\omega_j^n\}$

- Bond price $Q_{j,t}^n$, excess return $rx_{j,t}$ $\qquad 1 + \text{return}_{j,t} = 1 + rx_{j,t} + i_{j,t-1} = \frac{\sum_n Q_{j,t}^{n-1} B_{j,t-1}^n}{\sum_n Q_{j,t-1}^n B_{j,t-1}^n}$

  (one-period bonds $\implies rx = 0$)
- Debt law of motion:

$$\frac{v_{t-1}}{\beta} + \frac{v}{\beta}\left[-g_t + \sum_j \delta_j \left(rx_{j,t} + i_{j,t-1} + \Delta h_{j,t} - \pi_{j,t}\right)\right] = v_t + s_t$$

Fiscal Decomposition of Unexpected Inflation

- *Ex-post* real return $r_{j,t} = rx_{j,t} + i_{j,t-1} + \Delta h_{j,t} - \pi_{j,t}$

$$\Delta E_t \pi_t = \underbrace{\left[\Delta E_t rx_t + \sum_{j \neq N} \frac{\delta_j}{\delta} \Delta E_t r_{j,t}\right]}_{\text{Innovation to Bond Prices}} - \frac{\beta}{\delta v} \underbrace{\left[\sum_{k=0}^{\infty} \beta^k \Delta E_t s_{t+k} + \frac{v}{\beta} \sum_{k=0}^{\infty} \beta^k \Delta E_t g_{t+k} - \frac{v}{\beta} \sum_{k=1}^{\infty} \sum_{j} \delta_j \beta^k \Delta E_t r_{j,t+k}\right]}_{\text{Innovation to the Intrinsic Value of Debt}}$$

$$\equiv d_1(rx) + d_1(r_0) - d_1(s) - d_1(g) + d_1(r)$$

- Variance decomposition.

$$\text{var}\left[\Delta E_t \pi_t\right] = \text{cov}_\pi \left[d_1(rx)\right] + \text{cov}_\pi \left[d_1(r_0)\right] - \text{cov}_\pi \left[d_1(s)\right] - \text{cov}_\pi \left[d_1(g)\right] + \text{cov}_\pi \left[d_1(r)\right]$$

Bayesian-VAR: Data and Model

- Annual data on observables $\tilde{x}_t$

$$x_t^{OBS} = \begin{bmatrix} i_t & \text{(Nominal Interest)} \\ \pi_t & \text{(CPI Inflation)} \\ v_t^b & \text{(Par-Value Debt-to-GDP)} \\ g_t & \text{(GDP growth)} \\ \Delta h_t & \text{(Chg. Real Exchange Rate)} \end{bmatrix}$$

- 25 countries (samples starting at 1945, 1960, 1975, 1998)
- General VAR

$$X_t = AX_{t-1} + Ke_t$$

- Decompose $X_t' = [x_t^{OBS'} \;\; x_t^{NOT'}]$

$$X_t = \begin{bmatrix} x_t^{OBS} \\ x_t^{NOT} \end{bmatrix} = \begin{bmatrix} a & 0 \\ b & c \end{bmatrix} \begin{bmatrix} x_{t-1}^{OBS} \\ x_{t-1}^{NOT} \end{bmatrix} + \begin{bmatrix} I \\ k \end{bmatrix} e_t$$

Bayesian-VAR: Empirical Challenges and Solutions

1. Explosive debt dynamics in 1960-2020 implies unstable OLS VARs

$$x_t^{OBS} = a\, x_{t-1}^{OBS} + e_t$$

   - **United States**: Estimate model by OLS (stable!)
   - **Others**: Estimate model with a Bayesian-Regression

$$a^{BAY} = (X'X + \lambda^{-1})^{-1}(X'X\, a^{OLS} + \lambda^{-1}\, a^{PRIOR})$$

   λ maximizes the marginal distribution $p(\text{data})$ and ensures stability

2. Public finance data do not respect law of motion of public debt
   - Define surplus from the law of motion: $s_t = \frac{v_{t-1}}{\beta} - v_t + \frac{v}{\beta}\left[-g_t + \sum_j \delta_j \left(rx_{j,t} + i_{j,t-1} + \Delta h_{j,t} - \pi_{j,t}\right)\right]$
3. No data on the market value of debt, only its par value (v_t^b) Public Finances Model
   - Model for market vs par value (Cox (1985)): $v_t = v_t^b + \frac{v}{\beta} \sum_j \delta_j \left(rx_{j,t} + i_{j,t-1} - i_{j,t-1}^b\right)$
4. No data on bond returns Geometric Term Structure
   - Geometric maturity structure: $rx_{j,t} + i_{j,t-1} = (\omega_j \beta) q_{j,t} - q_{j,t-1}$

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Bayesian-VAR: Variance Decomposition

- **Proposition.** The variance decomposition

$$1 = \frac{\text{cov}_\pi\left[d_1(rx)\right]}{\text{var}\left[\Delta E_t \pi_t\right]} + \frac{\text{cov}_\pi\left[d_1(r_0)\right]}{\text{var}\left[\Delta E_t \pi_t\right]} - \frac{\text{cov}_\pi\left[d_1(s)\right]}{\text{var}\left[\Delta E_t \pi_t\right]} - \frac{\text{cov}_\pi\left[d_1(g)\right]}{\text{var}\left[\Delta E_t \pi_t\right]} + \frac{\text{cov}_\pi\left[d_1(r)\right]}{\text{var}\left[\Delta E_t \pi_t\right]}$$

  is equivalent to the innovations decomposition applied to VAR shock $\text{Proj}(e \mid \Delta E_t \pi_t = 1)$

$$1 = \Delta E_t \pi_t \equiv d_1(rx) + d_1(r_0) - d_1(s) - d_1(g) + d_1(r)$$

- *"Given 1% unexpected inflation, how do we change our nowcast/forecast of the surplus, discounting and bond prices?"*

Bayesian-VAR: Variance Decomposition

Country	$\Delta E_t \pi_t =$	ΔE_t(Bond Prices)		$-\Delta E_t$(Intrinsic Value of Debt)		
		$d_1(r_0)$	$d_1(rx)$	-$d_1(s)$	-$d_1(g)$	$d_1(r)$
United States	1	***0.03**	***-0.78**	**0.57**	0.23	**0.96**
Advanced - 1960 Sample						
Canada	1	***-0.11**	***-1.59**	0.62	***1.22**	0.86
Denmark	1	***-0.29**	**-0.30**	0.42	-0.04	**1.21**
Japan	1	0	***-0.52**	***1.60**	-0.38	0.30
Norway	1	***-0.01**	***-0.36**	**0.60**	**0.47**	0.30
Sweden	1	**-0.15**	***-0.93**	-0.34	***0.98**	***1.42**
United Kingdom	1	***0.52**	***-0.73**	***2.89**	***0.97**	***-2.65**
Advanced - 1973 Sample						
Australia	1	***0.07**	***-0.76**	***2.09**	**0.66**	**-1.06**
New Zealand	1	**-0.10**	***-0.86**	0.40	***0.87**	0.68
South Korea	1	-0.01	***-0.45**	***1.91**	0.17	**-0.62**
Switzerland	1	0	***-0.69**	**0.90**	***0.91**	-0.12

(a) Advanced Economies

Country	$\Delta E_t \pi_t =$	ΔE_t(Bond Prices)		$-\Delta E_t$(Intrinsic Value of Debt)		
		$d_1(r_0)$	$d_1(rx)$	-$d_1(s)$	-$d_1(g)$	$d_1(r)$
Emerging - 1998 Sample						
Brazil	1	**-0.26**	***-0.22**	**-1.46**	**1.05**	**1.89**
Chile	1	-3.80	**-1.33**	8.95	-5.71	2.88
Colombia	1	**1.51**	***-0.96**	1.39	-1.09	0.15
Czech Republic	1	***-0.16**	***-0.37**	-2.31	**2.42**	**1.42**
Hungary	1	***-0.57**	***-0.93**	-0.98	1.60	1.88
India	1	***0.17**	***-0.46**	**1.54**	0.05	-0.30
Indonesia	1	***-2.59**	***-1.07**	1.69	***2.61**	0.35
Israel	1	-0.06	***-0.78**	-0.55	***1.51**	0.88
Mexico	1	-0.02	***-0.74**	**1.41**	0.03	0.32
Poland	1	***-0.45**	***-1.15**	0.87	-0.39	***2.11**
Romania	1	-0.40	***-0.96**	2.24	0.42	-0.31
South Africa	1	**0.36**	***-0.51**	1.58	0.25	-0.68
Turkey	1	**0.37**	***-0.37**	-1.18	-0.15	***2.33**
Ukraine	1	0	***-0.77**	**0.65**	**0.41**	***0.70**

(b) Emerging Economies

Decomposition 2

Bayesian-VAR: Variance Decomposition - Takeaways

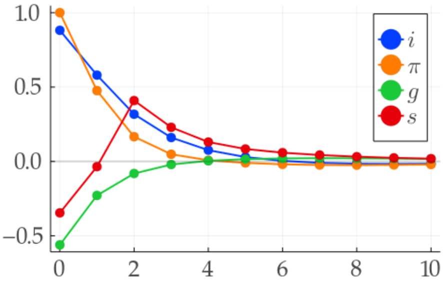

Figure: IRF - Brazil

- Unexpected inflation accounted for by variation in the intrinsic value of debt
- Surplus-to-GDP, GDP growth and real discounting...
  - ...account for unexpected inflation alone in 0/25
  - ...have a positive contribution in 18+/25
- Fiscal roots of inflation do not imply connection between fiscal policy and unexpected inflation
- Nominal bond price dynamics reduce unexpected inflation variance 25/25
  - Effects of monetary policy!

Bayesian-VAR: ”Aggregate Demand” Recession

- ”Aggregate demand” recessions (Great Recession in 2008) feature:
  - Low inflation
  - Low growth
  - Fiscal deficits (often)
- Does that deny the fiscal sources of inflation?
- Where does unexpected (dis)inflation come from?
- Scenario:

$$\Delta E_t g_t = -1 \qquad \Delta E_t \pi_t = -0.5$$

VAR Shock: $\text{Proj}(e \mid \Delta E_t g_t = -1,\ \Delta E_t \pi_t = -0.5)$

Bayesian-VAR: ”Aggregate Demand” Recession

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Advanced - 1960 Sample						
Canada	-0.50	***0.14**	***2.21**	-0.45	0.30	***-2.70**
Denmark	-0.50	***0.20**	***0.86**	**-2.64**	***2.75**	**-1.67**
Japan	-0.50	0	***0.83**	***-1.51**	***1.64**	***-1.46**
Norway	-0.50	0	***0.63**	**-1.36**	***1.72**	**-1.49**
Sweden	-0.50	***0.41**	***1.22**	-0.65	**0.87**	***-2.35**
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Chile	-0.50	***15.78**	***2.94**	-30.50	**30.54**	-19.26
Colombia	-0.50	**1.86**	***0.67**	**-10.90**	***7.57**	0.31
Czech Republic	-0.50	***0.37**	***0.61**	-0.07	**0.25**	**-1.65**
Hungary	-0.50	***0.99**	***0.60**	10.82	-5.29	**-7.63**
India	-0.50	-0.03	0.13	**-1.16**	**0.71**	-0.15
Indonesia	-0.50	***8.23**	**-0.55**	***-11.24**	**1.42**	1.64
Israel	-0.50	***1.79**	**0.37**	**-3.18**	**1.17**	-0.65
Mexico	-0.50	***1.69**	***0.81**	***-4.56**	***1.94**	-0.38
Poland	-0.50	***0.87**	***1.00**	-0.14	**1.30**	***-3.53**
Romania	-0.50	***2.08**	**0.21**	***-8.16**	**2.05**	**3.31**
South Africa	-0.50	-0.10	0.35	***-30.02**	***11.15**	***18.13**
Turkey	-0.50	***0.99**	***0.23**	0.64	**0.52**	***-2.88**
Ukraine	-0.50	0	**-0.68**	**-3.22**	***1.92**	**1.48**

(b) Emerging Economies

Bayesian-VAR: "Aggregate Demand" Recession - Takeaways

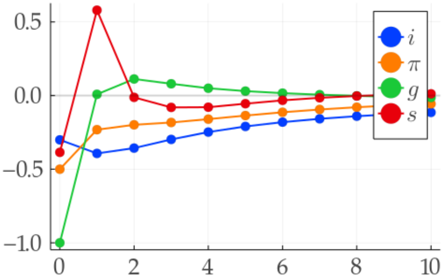

Figure: IRF - United States

- Lower inflation follows from...
  - lower discounting (monetary policy) in 19/25
  - larger surplus-GDP **ratios**, current or in the future in 22/25
- COVID: what if governments reacted to a recession by credibly reducing $\{s\}$ permanently?
- Direction of causality?

The New-Keynesian Model: Setup

- B-VAR decompositions not structural: all shocks are reduced-form
- Theory: How far do we need to go? Not much!
- Two-country NK model:
  - Home economy with $n \to 0$ households and firms (small and open)
  - Foreign economy with $1 - n \to 1$ households and firms (large and "closed")
- **The Standard.** Intertemporal substitution + Calvo rigidity
- **The New.** Production function $\mathcal{A}_t N = \mathcal{T}_t A_t N$ (Home), $\mathcal{A}_t^* N = \mathcal{T}_t A_t^* N$ (Foreign)

(Trend component) $\log \mathcal{T}_t = \log \mathcal{T}_{t-1} + u_{g,t}$

(AR(1) component) $a_t = \rho_a a_{t-1} + \varepsilon_{a,t}$

$a_t^* = \rho_a a_{t-1}^* + \varepsilon_{a,t}^*$

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$$
\begin{aligned}
&\text{(Trend component)} \quad & \log \mathcal{T}_t &= \log \mathcal{T}_{t-1} + u_{g,t} \\
&\text{(AR(1) component)} \quad & a_t &= \rho_a a_{t-1} + \varepsilon_{a,t} \\
& & a_t^* &= \rho_a a_{t-1}^* + \varepsilon_{a,t}^*
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$$

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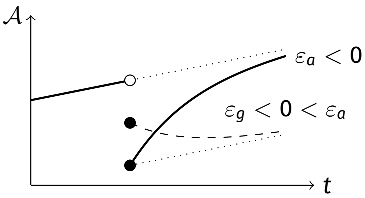
$$



The New-Keynesian Model: The Foreign, Closed Economy

- Private Sector

$$
\begin{aligned}
y_t^* &= E_t y_{t+1}^* - \gamma \; [i_t^* - E_t \pi_{t+1}^*] + E_t u_{g,t+1} \\
\pi_t^* &= \beta \; E_t \pi_{t+1}^* + \kappa \; y_t^* - \kappa_a \; a_t^* \\
g_t^* &= y_t^* - y_{t-1}^* + u_{g,t}
\end{aligned}
$$

Why Trend? Growth

- Unexpected inflation indeterminacy? FTPL.
- Monetary and Fiscal Policy

$$
\begin{aligned}
i_t^* &= \phi_\pi \; \pi_t^* + \phi_g \; g_t^* + \varepsilon_{i,t}^* \\
s_t^* &= \rho_s \; s_{t-1}^* + \tau_\pi \; \pi_t^* + \tau_g \; g_t^* + \varepsilon_{s,t}^*
\end{aligned}
$$

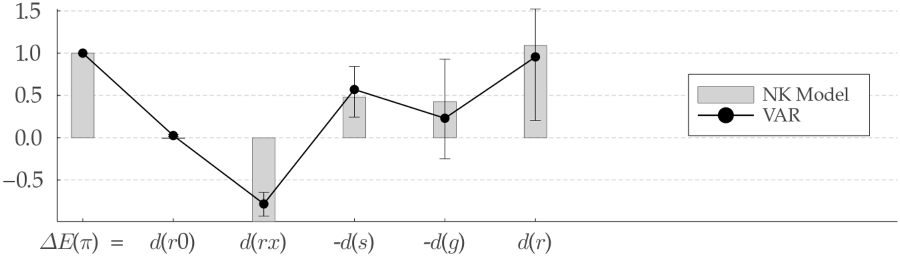
- GMM for US moments

$$
\text{Min}_\Psi \quad \alpha_1 \, \|\mathcal{D}_{VAR} - \mathcal{D}_{NK}(\Psi)\| + \alpha_2 \, \|\mathcal{M} - \mathcal{M}_{NK}(\Psi)\| \qquad \text{s.t. } \Psi \in \Theta
$$

Parameters

The New-Keynesian Model: Reproducing the Variance Decomposition

- **Result.** AR(1) productivity shocks $\varepsilon_{a,t}$ alone reproduce the **variance decomposition** with positive contributions from surplus-to-output, growth and real interest terms



Target: United States. Only AR(1) productivity shocks.

Moments

The New-Keynesian Model: Reproducing the Variance Decomposition

$$\boxed{1 = \Delta E_t \pi_t = d(rx) - d(s) - d(g) + d(r)}$$

- Key Ingredients
  - Persistent shock: $\rho_a = 0.98$
  - Countercyclical deficits: $\tau_g = 0.7$
  - Strong Taylor: $\phi_\pi = 0.8$
- What is the story?
  - Low productivity leads to a recession
    $$d(g) < 0$$
  - Government raises deficit to fight recession
    $$d(s) < 0$$
  - Monetary policy raises nominal interest
    $$d(rx) < 0$$
    $$d(r) > 0$$

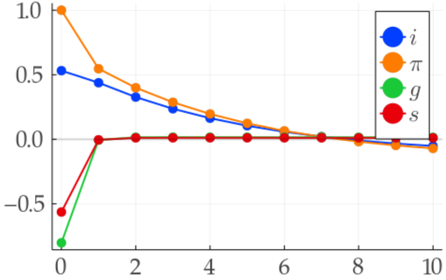


Figure: IRF to $\Delta E_t \pi_t = 1$ ($\varepsilon_{a,t} = -1.15$)

Marginal Costs
vs B-VAR IRF

The New-Keynesian Model: Reproducing the Variance Decomposition

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Marginal Costs | vs B-VAR IRF

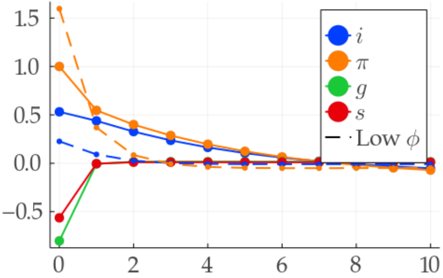
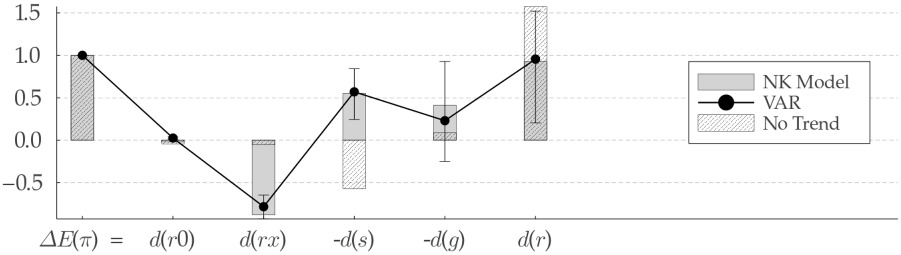


Figure: IRF to $\Delta E_t \pi_t = 1$ ($\varepsilon_{a,t} = -1.15$)

The New-Keynesian Model: Reproducing the Recession Decomposition

$\Delta E_t g_t = -1 \qquad \Delta E_t \pi_t = -0.5$

- **Result.** In the absence of trend shocks, NK model fails to replicate the variance and recession decompositions. Policy shocks do not help.
- **Result.** The model with trend shocks reproduces the **recession decomposition** without policy shocks.



Target: United States Structural Shocks

Moments

The New-Keynesian Model: Reproducing the Recession Decomposition

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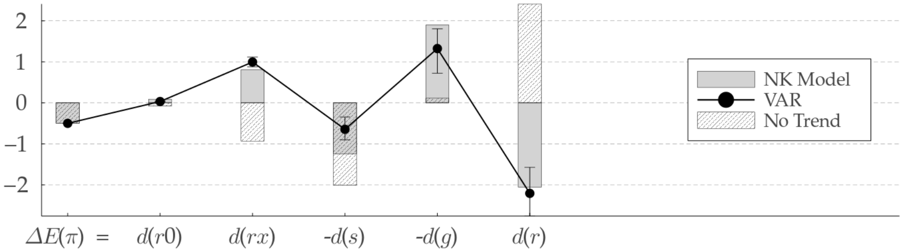

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Moments

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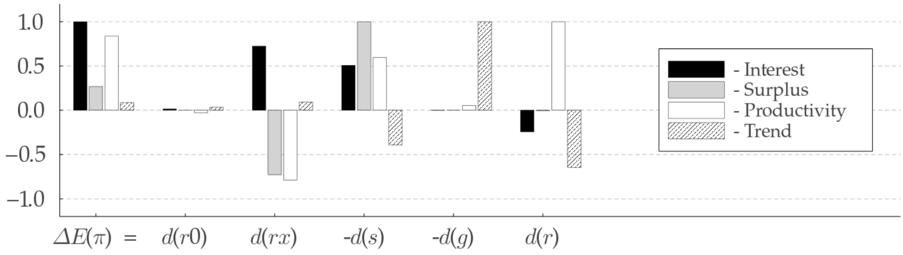

Target: United States Structural Shocks

Moments

$$\boxed{-0.5 = \Delta E_t \pi_t = d(rx) - d(s) - d(g) + d(r)}$$

- Key Ingredients
  - Quiet monetary shocks: $\sigma_i = 0.05$
  - Trend + AR(1) shocks: $\sigma_g = 2.6$, $\sigma_a = 1.4$
  - Strong Taylor: $\phi_\pi = 0.93$
- Intuition
  - AR(1) shocks reproduce variance decomposition
  - Monetary policy shocks generate wrong $d(rx)$
- Recession ($\varepsilon_a = 0.5$, $\varepsilon_g = -1.3$)
  - Recession and lower interest

$$d(g) > 0 \qquad d(rx) > 0$$

  - Low detrended marginal costs: $\pi_t < E_t \pi_{t+1}$
  - Low/increasing inflation + Taylor guarantee low real interest

$$r_t = i_t - E_t \pi_{t+1} \approx \pi_t - E_t \pi_{t+1} < 0$$

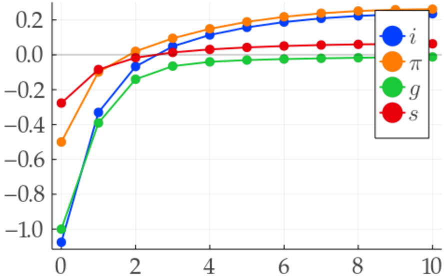

Figure: IRF to $\Delta E_t g_t = -1$, $\Delta E_t \pi_t = -0.5$

Marginal Costs   vs B-VAR IRF

$$y_t = E_t y_{t+1} - \gamma \; [i_t - E_t \pi_{t+1} + \alpha\bar{\omega} \; E_t \Delta z_{t+1}] + E_t u_{g,t+1}$$

$$\pi_{H,t} = \beta \; E_t \pi_{H,t+1} + \kappa \; y_t - \kappa_a \; a_t - \kappa_z \; z_t$$

$$y_t = y_t^* + \gamma_\alpha \; z_t$$

$$h_t = (1 - \alpha) \; z_t$$

$$\pi_t = \pi_{H,t} + \alpha \; \Delta z_t$$

- **Home**: Open trade; Complete markets
- Same parameters of the US estimation
- Same combination of Home productivity shocks:
  - Variance decomposition ✓
  - Recession decomposition ✓

Foreign Policy Shocks | New Zealand Decomp

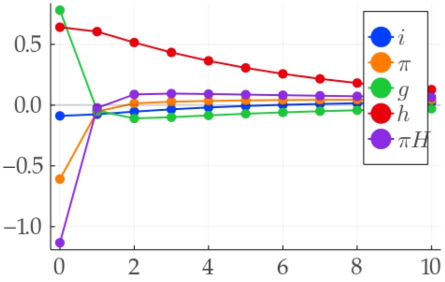

Figure: Productivity Shock in Home Foreign

The New-Keynesian Model: The Open Economy

$$
\begin{aligned}
y_t &= E_t y_{t+1} - \gamma\ [i_t - E_t\pi_{t+1} + \alpha\bar{\omega}\ E_t\Delta z_{t+1}] + E_t u_{g,t+1} \\
\pi_{H,t} &= \beta\ E_t\pi_{H,t+1} + \kappa\ y_t - \kappa_a\ a_t - \kappa_z\ z_t \\
y_t &= y_t^* + \gamma_\alpha\ z_t \\
h_t &= (1-\alpha)\ z_t \\
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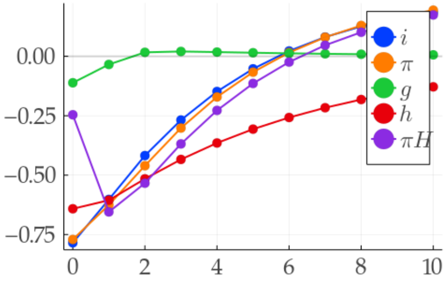

Figure: Productivity Shock in Home Foreign

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Foreign Policy Shocks | New Zealand Decomp

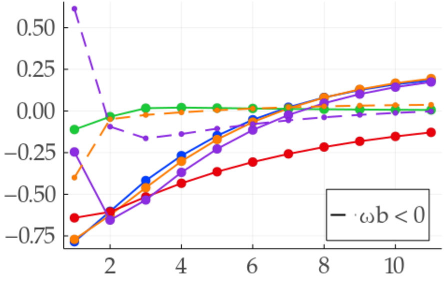

Figure: Productivity Shock in Home Foreign

The New-Keynesian Model: Variance Decomposition and Policy Rules

$$\boxed{1 = \Delta E_t \pi_t = d(\mathrm{BP}) - d(s) - d(g) + d(r)}$$

- Can we match variance decomposition of different countries?
- Vary policy parameters
- Keep other structural parameters constant

$$i_t = \phi_\pi \; \pi_t + \phi_g \; g_t + \varepsilon_{i,t}$$

$$s_t = \rho_s \; s_{t-1} + \tau_\pi \; \pi_t + \tau_g \; g_t + \varepsilon_{s,t}$$

Parameters	New Zealand	Sweden	Denmark	Australia
A. Variance Decomposition - Value of Debt Contribution				
$-d(s)$	0.40 (0.66)	**-0.34 (0.04)**	0.42 (0.48)	2.09 (2.04)
$-d(g)$	0.87 (0.63)	0.98 (1.03)	**-0.04 (-0.02)**	0.66 (0.97)
$d(r)$	0.68 (0.90)	1.42 (1.10)	1.21 (1.17)	**-1.06 (-0.52)**
B. Estimated Parameters				
ρ_a	0.84			
ρ_g	0.27			
ϕ_π	0.93	0.99	0.96	0.91
ϕ_g	0.61	0.63	0.71	1
ρ_s	0	0.26	0.61	0.05
τ_π	0.25	0.01	-0.02	-0.03
τ_g	0.15	-0.10	-0.13	0.25
σ_i	0.05	0	0	0.51
σ_s	0.08	0	0.12	0.50
σ_a	1.41			
σ_g	2.62			
C. Productivity Shocks Projected by $\Delta E_t \pi_t = 1$				
$\varepsilon_{g,t}$	-0.35	-0.48	0.12	-0.74
$\varepsilon^*_{a,t}$	-0.77	-0.82	-0.06	-0.08
$\varepsilon_{a,t}$	-0.61	-0.76	-1.49	-0.16

Variance Decomps and Policy Rules

Conclusion

- Valuation equation of public debt $\Longrightarrow$ decomposition of unexpected inflation
- B-VAR based estimation of two versions of the decomposition
- In most countries:
  - **Variance** of unexpected inflation stems from discounted surpluses (all of its components)
  - **Recessions**: low inflation follow from low discounting and "not so expansionary" fiscal policy
- Stylized New-Keynesian models reproduce VAR decompositions
  - Relevance of productivity shocks
  - Relevance of policy rules

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Appendix: Public Debt Currency Denomination

Return

Symbol	Description	Nominal Debt	Real Debt	Dollar Debt
j	Index Symbol Notation	N δ, ω	R δ_R, ω_R	D δ_D, ω_D
P_j	Price per Good	P	1	P_t^{US}
$\mathcal{E}_j$	Nominal Exchange Rate	1	P	Dollar NER
H_j	Real Exchange Rate	1	1	Dollar RER
π_j	Log Variation in Price	π	0	π_t^{US}
Δh_j	Log Real Depreciation	0	0	Δh_t

Table: Public Debt Denomination

Appendix: Public Finances Model

Return

Appendix: Geometric Term Structure

Return | Decomposition 2

- To each currency portfolio j, fixed geometric maturity structure:

$$B^{n}_{j,t} = \omega_j B^{n-1}_{j,t}$$

- Total return on currency-j portfolio:

$$1 + rx_{j,t} + i_{j,t-1} = \frac{1 + \omega_j Q_{j,t}}{Q_{j,t-1}} \quad \Longrightarrow \quad \boxed{rx_{j,t} + i_{j,t-1} = (\omega_j \beta) q_{j,t} - q_{j,t-1}}$$

- Assume **constant risk premia** $E_t rx_{j,t+1} = 0$

$$\boxed{q_{j,t} = (\omega_j \beta) E_t q_{j,t+1} - i_{j,t}} = -\sum_{k=0}^{\infty} (\omega_j \beta)^k E_t i_{j,t+k}$$

Appendix: Second Decomposition

Return

- From geometric maturity structure Geometric Term Structure

$$\Delta E_t rx_{j,t} = -\sum_{k=1}^{\infty} (\omega_j \beta)^k \left[\Delta E_t r_{j,t+k} + \Delta E_t \pi_{j,t+k} - \Delta E_t \Delta h_{j,t+k}\right]$$

- Replace on the original fiscal decomposition

$$\Delta E_t \pi_t = \overbrace{\left[-\sum_{k=1}(\omega\beta)^k \Delta E_t \pi_{t+k} - \frac{\delta_D}{\delta}\sum_{k=0}^{\infty}(\omega_D \beta)^k \Delta E_t \pi^{US}_{t+k}\right]}^{\text{Innovation to Nominal Variables}}$$

$$\underbrace{-\frac{\beta}{\delta v}\left[\sum_{k=0}^{\infty}\beta^k \Delta E_t s_{t+k} + \frac{v}{\beta}\sum_{k=0}^{\infty}\beta^k \Delta E_t g_{t+k} - \frac{v}{\beta}\sum_{k=1}^{\infty}\sum_{j}\delta_j \beta^k (1-\omega^k)\Delta E_t r_{j,t+k} - \frac{\delta_D v}{\beta}\sum_{k=0}^{\infty}(\omega_D\beta)^k \Delta E_t \Delta h_{t+k}\right]}_{\text{Innovation to Real Variables}}$$

$$\equiv -d_2(\pi) - d_2(\pi^{US}) - d_2(s) - d_2(g) + d_2(r) + d_2(\Delta h)$$

Appendix: Second Decomposition

Return

Country	$\Delta E_t \pi_t =$	$-\Delta E_t$(Future Inflation)		$\pm \Delta E_t$(Real Variables)			
		$-d_2(\pi)$	$-d_2(\pi^{US})$	$-d_2(s)$	$-d_2(g)$	$d_2(r)$	$d_2(\Delta h)$
United States	1	***-1.12**	-	**0.57**	0.23	***1.32**	0
Advanced - 1960 Sample							
Canada	1	***-1.53**	***-0.07**	0.62	***1.22**	**0.78**	**-0.03**
Denmark	1	***-0.49**	***-0.20**	0.42	-0.04	**1.23**	0.08
Japan	1	***-1.14**	0	***1.60**	-0.38	***0.91**	0
Norway	1	***-0.70**	0	**0.60**	**0.47**	**0.64**	0
Sweden	1	***-1.02**	**-0.10**	-0.34	***0.98**	***1.54**	-0.07
United Kingdom	1	***-2.34**	0	***2.89**	***0.97**	**-0.52**	0
Advanced - 1973 Sample							
Australia	1	***-1.47**	0	***2.09**	***0.66**	-0.27	0
New Zealand	1	***-1.02**	***-0.08**	0.40	***0.87**	**1.04**	**-0.21**
South Korea	1	***-0.74**	***-0.03**	***1.91**	0.17	-0.33	**0.01**
Switzerland	1	***-0.79**	0	**0.90**	***0.91**	-0.02	0

(a) Advanced Economies

Country	$\Delta E_t \pi_t =$	$-\Delta E_t$(Future Inflation)		$\pm \Delta E_t$(Real Variables)			
		$-d_2(\pi)$	$-d_2(\pi^{US})$	$-d_2(s)$	$-d_2(g)$	$d_2(r)$	$d_2(\Delta h)$
Emerging - 1998 Sample							
Brazil	1	***-0.11**	0	**-1.46**	**1.05**	**1.46**	0.07
Chile	1	-0.76	**-2.75**	8.95	-5.71	-0.35	1.62
Colombia	1	***-0.61**	-0.04	1.39	-1.09	0.02	**1.34**
Czech Republic	1	-0.02	**-0.05**	-2.31	**2.42**	0.98	-0.03
Hungary	1	***-0.69**	***-0.15**	-0.98	1.60	1.83	***-0.61**
India	1	***-1.05**	***0.09**	**1.54**	0.05	0.41	-0.04
Indonesia	1	***-0.79**	***-1.33**	1.69	***2.61**	0.26	**-1.45**
Israel	1	***-0.54**	0.10	-0.55	***1.51**	0.61	-0.12
Mexico	1	***-0.60**	**0.17**	**1.41**	0.03	0.52	**-0.52**
Poland	1	***-0.59**	***-0.21**	0.87	-0.39	***1.43**	-0.11
Romania	1	***-1.14**	***-0.53**	2.24	0.42	-0.54	0.55
South Africa	1	0.05	-0.01	1.58	0.25	-0.79	-0.07
Turkey	1	***-0.76**	***-0.40**	-1.18	-0.15	***3.35**	0.14
Ukraine	1	**-0.29**	0	**0.65**	***0.41**	**0.23**	0

(b) Emerging Economies

Appendix: NK Model Parameters

Return

Appendix: Why Trend Shocks? The Growth Component

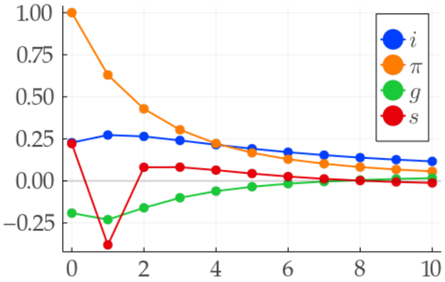
Return

Appendix: Estimated Moments

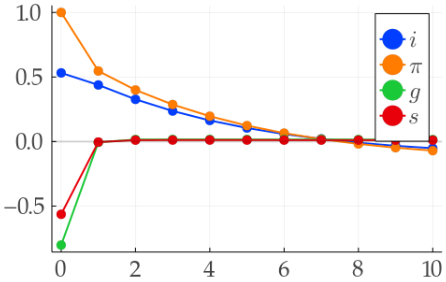
NK Simple NK Full

Appendix: Simple Model - US Data vs Model

NK Simple



(a) B-VAR



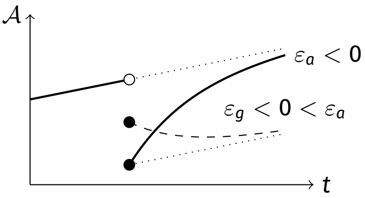
(b) NK Model (Only Prod. Shocks)

Appendix: Marginal Costs

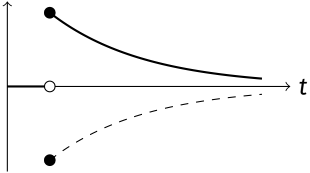
NK Simple

- AR(1) Productivity Shock
  - High marginal costs + strong Taylor rule ($\phi_\pi \approx 1$):

$$i_t \approx \underbrace{\pi_t > E_t\pi_{t+1}}_{mc_t > 0} \implies r_t = i_t - E_t\pi_{t+1} > 0$$



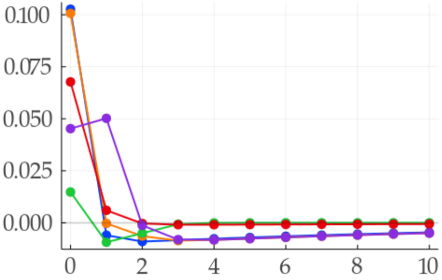
(a) Productivity Path $\mathcal{A}_t$



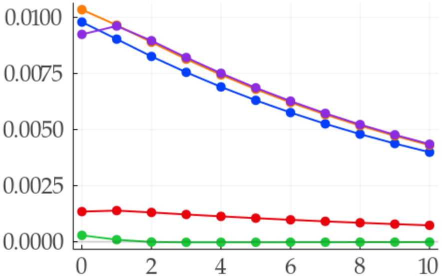
(b) $-a_t$ or Mg. Cost at fixed wages

Appendix: NK Open - Foreign Policy Shocks

Return



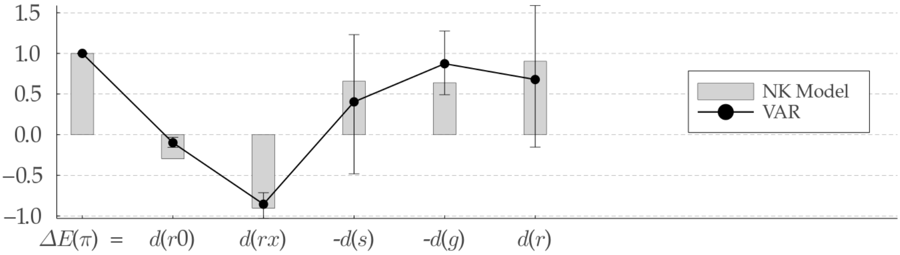
(a) Monetary $\varepsilon^*_{i,t} = 1$



(b) Fiscal $\varepsilon^*_{s,t} = 1$

Appendix: NK Open - New Zealand Decomposition

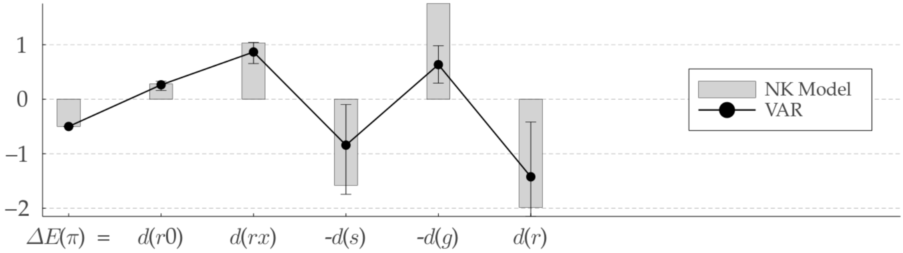
Return



Data: New Zealand - Variance Recession

Appendix: NK Open - New Zealand Decomposition

Return



Data: New Zealand - Variance Recession