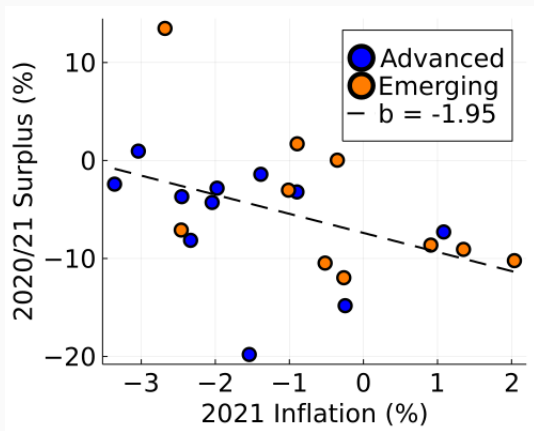


# A Fiscal Decomposition of Unexpected Inflation: Cross-Country Estimates and Theory

Livio Maya

## Fiscal Connection?



COVID Inflation - 21 countries in sample

# Introduction

- Sources of inflation variation
- What drives innovations to the price level?
- Breakdown of **valuation equation of public debt**
- Focus on unexpected inflation  $\Delta E_t \pi_t$ 
  - Campbell and Ammer (1993)
  - Internal consistency of expectations

# Valuation Equation of Public Debt

- Stock market - Campbell and Ammer (1993)

Stock price = Discounted Dividends

$$\Delta E_t [\text{Stock price}] = \Delta E_t [\text{Dividends}] - \Delta E_t [\text{Disc Rates}]$$

- Micro-founded monetary models

$$\frac{\text{Bond Prices} \times \text{Bonds}}{\text{Price Level}} = \sum_t \frac{\text{Surpluses}_t}{\text{Discount}_t}$$

$$\Delta E_t [\text{Bond Price}] - \Delta E_t [\text{Price}] = \Delta E_t [\text{Surplus}] - \Delta E_t [\text{Disc}]$$

# Exercises

## 1. Decomposition estimates

- Bayesian VAR for 21 countries
- Inflation shock  $\Delta E_t \pi_t = 1$
- Discounted surpluses shock:  $\Delta E_t [\text{Disc Surp}] = -1$

## 2. FTPL, New-Keynesian Model

- Volatile surpluses, no contribution to inflation?
- Parametric model of partial debt repayment
- GMM estimate to reproduce decompositions

# Motivation + Results

- Measures not structural
- Stylized facts to be matched by theory
- On average:
  - **Discount rates** → ~80% of total inflation
  - GDP growth → ~20% of total inflation
  - Surplus/GDP → ~0% of total inflation

Inflation has fiscal roots, even if fiscal policy is disconnected from the price level.

# Motivation + Results

- Structural interpretation?
- Volatile surpluses, no inflation?
- **Partial debt repayment** necessary
- Debt repayment in low frequency  $\implies$  hard to estimate!
- On average, 0.78% of 1% GDP deficit is repaid
  - 0.96% in advanced economies
  - 0.59% in developing economies

Discount-driven inflation and realistic surplus process  
preclude partial repayment.

# Why unexpected inflation, not just inflation?

- New Keynesian theory:
  - Fisher: monetary policy sets expected inflation
  - Fiscal policy sets **unexpected** inflation
- Measures do not depend on state of the economy
- Direct connection with impulse response functions



# Literature

- **Monetary-Fiscal Interaction.** Cagan (1956), Sargent and Wallace (1981), Hall and Sargent (1997), Hall and Sargent (2011), Jiang et al. (2019), Corsetti et al. (2019), Sunder-Plassmann (2020), Du et al. (2020), Akhmadieva (2022)
- **Fiscal Theory of the Price Level.** Leeper (1991), Sims (1994), Woodford (1995), Cochrane (1998), Cochrane (2005), Sims (2011), Leeper and Leith (2016), Bassetto and Cui (2018), Cochrane (2022c), Brunnermeier et al. (2022), Cochrane (2022a), Cochrane (2022b)
- **Empirical Finance.** Campbell and Shiller (1988), Cochrane (1992), Campbell and Ammer (1993), Chen and Zhao (2009), Cochrane (2008), Jiang et al. (2019)

# Environment

- 1 period = 1 year
- Consumption good price  $P_t$
- Total output  $Y_t$
- Nominal bonds  $B_{N,t}^n$ , price  $Q_{N,t}^n$ 
  - Pay one unit of currency after  $n$  years
- Real bonds  $B_{R,t}^n$ , price  $P_t Q_{R,t}^n$ 
  - Pay one unit of consumption good after  $n$  years
- Primary Surplus  $P_t S_t$

# Evolution of Public Debt

$$\begin{aligned} & \overbrace{\left[ B_{N,t-1}^1 + P_t B_{R,t-1}^1 \right]}^{\text{Issued Currency}} = \Delta M_t \\ & + \underbrace{\left[ P_t S_t + \sum_{n=1}^{\infty} Q_{N,t}^n \left( B_{N,t}^n - B_{N,t-1}^{n+1} \right) + P_t \sum_{n=1}^{\infty} Q_{R,t}^n \left( B_{R,t}^n - B_{R,t-1}^{n+1} \right) \right]}_{\text{Retired Currency}} \end{aligned}$$

- This is a **budget constraint**
- Assumption 1: households do not value currency  $M_t = 0$

# Evolution of Public Debt

- Assumption 1: households do not value currency  $M_t = 0$
- End-of-period debt  $\mathcal{V}_{N,t}$  and  $\mathcal{V}_{R,t}$

$$(1 + r_t^N)\mathcal{V}_{N,t-1} + (1 + r_t^R)(1 + \pi_t)\mathcal{V}_{R,t-1} = P_t S_t + \mathcal{V}_{N,t} + \mathcal{V}_{R,t}$$

- This is an **equilibrium condition**
- Price level adjusts so that

currency issued = currency retired

# Evolution of Public Debt

- Constant structure of public debt:  $\delta = \mathcal{V}_{N,t} / \mathcal{V}_t$

$$1 + r_t^n = \delta \left[ (1 + r_{N,t}) \right] + (1 - \delta) \left[ (1 + r_{R,t})(1 + \pi_t) \right]$$

- Debt-to-GDP =  $V_t = \mathcal{V}_t / P_t Y_t$
- Surplus-to-GDP =  $s_t = S_t / Y_t$

$$\frac{1 + r_t^n}{(1 + \pi_t)(1 + g_t)} V_{t-1} = s_t + V_t$$

# Evolution of Public Debt

## Linearized equations

$$v_t + \frac{s_t}{V} = \frac{1}{\beta} [v_{t-1} + r_t^n - \pi_t - g_t]$$

$$r_t^n = \delta [r_t^N] + (1 - \delta) [r_t^R + \pi_t]$$

- $v_t$  is log debt-to-GDP
- $r_t^n$  is the nominal return on public debt

# Valuation Equation of Public Debt

- Assumption 2: debt does not spiral  $\lim_{j \rightarrow \infty} \beta^j v_{t+j} = 0$
- Solve flow equation forward:

$$\underbrace{v_{t-1} + r_t^n - \pi_t}_{\text{Real market value of debt}} = \underbrace{\frac{\beta}{V} \sum_{j=0}^{\infty} \beta^j [E_t s_{t+j} + E_t g_{t+j}] - \sum_{j=1}^{\infty} \beta^j [E_t r_{t+j}^n - E_t \pi_{t+j}]}_{\text{Discounted Surpluses}}$$

Now take innovations  $\Delta E_t = E_t - E_{t-1}$

# Marked-to-Market Decomposition

Take innovation on the valuation equation:

$$\epsilon_{r^n,t} - \epsilon_{\pi,t} = \epsilon_{s,t} + \epsilon_{g,t} - \epsilon_{r,t}$$

Terms:

$$\epsilon_{r^n,t} = \Delta E_t r_t^n$$

$$\epsilon_{\pi,t} = \Delta E_t \pi_t \text{ (current inflation)}$$

$$\epsilon_{s,t} = (\beta/V) \sum_{j=0}^{\infty} \beta^j \Delta E_t s_{t+j}$$

$$\epsilon_{g,t} = \sum_{j=0}^{\infty} \beta^j \Delta E_t g_{t+j}$$

$$\epsilon_{r,t} = \sum_{j=1}^{\infty} \beta^j (\Delta E_t r_{t+j}^n - \Delta E_t \pi_{t+j})$$



# Public Finances Model

Why a public finances model?

1. Decompose bond price term
2. No  $r_t^n$  data: use proxy
3. No data on market value of debt (only book value)

# Public Finances Model

## Key Assumptions

- **Assumption:** constant maturity structure
- Decays geometrically at rate  $\omega$ :

$$B_{N,t}^n = \omega_N B_{N,t}^{n-1}$$

$$B_{R,t}^n = \omega_R B_{R,t}^{n-1}$$

- **Assumption:** constant risk premium

$$E_t r_{N,t} = E_t r_{R,t} + E_t \pi_t = i_t$$

# Public Finances Model

- Bond prices:

$$q_{N,t} = (\omega_N \beta) E_t q_{N,t} - [i_t]$$

$$q_{R,t} = (\omega_R \beta) E_t q_{R,t} - [i_t - E_t \pi_{t+1}]$$

- Returns:

$$r_{j,t} = (\omega_j \beta) q_{j,t} - q_{j,t-1} \quad j = N, R$$

# Break down of bond price variation

Proposition: let  $r_t = i_t - E_t \pi_{t+1}$  be the real interest. Then

$$\epsilon_{r^n,t} - \epsilon_{\pi,t} = -\delta \sum_{j=0}^{\infty} (\omega_N \beta)^j \Delta E_t \pi_{t+j} - \sum_{j=1}^{\infty} \beta^j [\delta \omega_N^j + (1 - \delta) \omega_R^j] \Delta E_t r_{t+j}$$

- Discounting affects real and nominal bond prices
- Inflation affects nominal bond prices

# Total Inflation Decomposition

Replace bond return decomp on marked-to-market decomp:

$$-\varepsilon_{\pi,t} = \varepsilon_{s,t} + \varepsilon_{g,t} - \varepsilon_{r,t}$$

Terms:

$$\varepsilon_{\pi,t} = \delta \sum_{j=0}^{\infty} (\omega_N \beta)^j \Delta E_t \pi_{t+j} \text{ (current and future inflation)}$$

$$\varepsilon_{s,t} = \epsilon_{s,t} = (\beta/V) \sum_{j=0}^{\infty} \beta^j \Delta E_t s_{t+j}$$

$$\varepsilon_{g,t} = \epsilon_{g,t} = \sum_{j=0}^{\infty} \beta^j \Delta E_t g_{t+j}$$

$$\varepsilon_{r,t} = \sum_{j=1}^{\infty} \beta^j \left[ 1 - (\delta \omega_N^j + (1 - \delta) \omega_R^j) \right] \Delta E_t r_{t+j}$$

# Comparison of Decompositions

- **Marked-to-market:**  $\epsilon_{r^n,t} - \epsilon_{\pi,t} = \epsilon_{s,t} + \epsilon_{g,t} - \epsilon_{r,t}$ 
  - Current inflation given current bond prices
  - Highlights effect of monetary policy
- **Total inflation:**  $-\epsilon_{\pi,t} = \epsilon_{s,t} + \epsilon_{g,t} - \epsilon_{r,t}$ 
  - Path of inflation given path of discount rates
  - Sensitive to future inflation
  - Nets out effect of discount rates on bond prices

## Build Market Value of Debt

- Converting par to market value of debt
- Dallas Fed, Cox and Hirschhorn (1983) and Cox (1985)

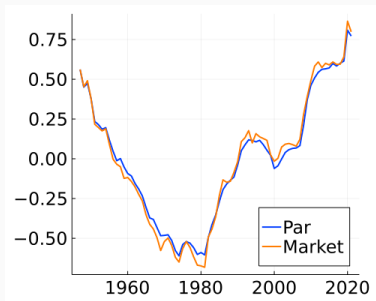
$$\mathcal{V}_{j,t} = \mathcal{V}_{j,t}^b \times \frac{\text{market value of bonds}}{\text{book value of bonds}} = \mathcal{V}_{j,t}^b \frac{Q_{j,t}}{Q_{j,t}^b} \quad \text{for } j = N, R$$

- Book price of bonds evolve according to average interest:

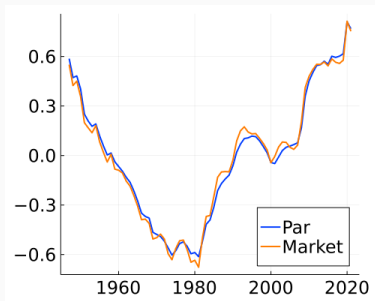
$$i_{N,t}^b = (1 - \omega_N) i_t + \omega_N i_{N,t-1}^b$$

$$i_{R,t}^b = (1 - \omega_R)(i_t - E_t \pi_{t+1}) + \omega_R i_{R,t-1}^b$$

# Comparison with Dallas Fed



(a) Dallas Fed



(b) Model



# Vector Autoregression

- States  $X$

$$X_t = AX_{t-1} + e_t \quad e_t \sim N(0, \Sigma)$$

- Bayesian estimates of 21 countries
- Samples end in 2019 (no COVID!)
- Prior centered around US OLS estimates

$$\begin{bmatrix} i_t & \text{Nominal Interest} \\ \pi_t & \text{Inflation Rate} \\ g_t & \text{GDP Growth} \\ v_t & \text{Market Value Debt} \\ r_t^n & \text{Bond Return (model built)} \\ s_t & \text{Primary Surplus (model built)} \end{bmatrix}$$

# VAR and Decomposition Measures

- VAR uses time series structure to identify revision of expectations

$$\Delta E_t X_{t+j} = A^j X_t$$

$$\sum_{j=0}^{\infty} \beta^j \Delta E_t X_{t+j} = (I - \beta A)^{-1} X_t$$

# The Inflation Shock

- Inflation unexpectedly jumps:  $\Delta E_t \pi_t = 1$
- Other shocks allowed to jump as well

$$\textbf{(Inflation Shock)} \quad e_t = E[e \mid \Delta E_t \pi_t = 1]$$

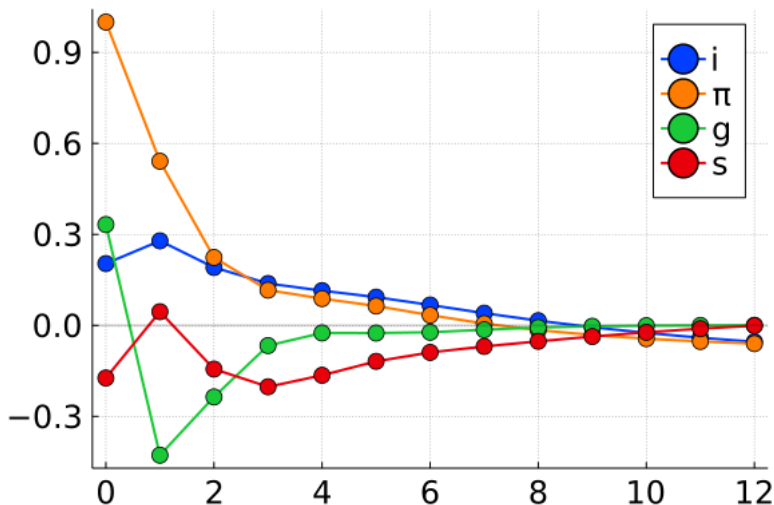
- Proposition: MtM decomposition

$$\epsilon_{r^n,t} - \epsilon_{\pi,t} = \epsilon_{s,t} + \epsilon_{g,t} - \epsilon_{r,t}$$

same as **variance decomposition**

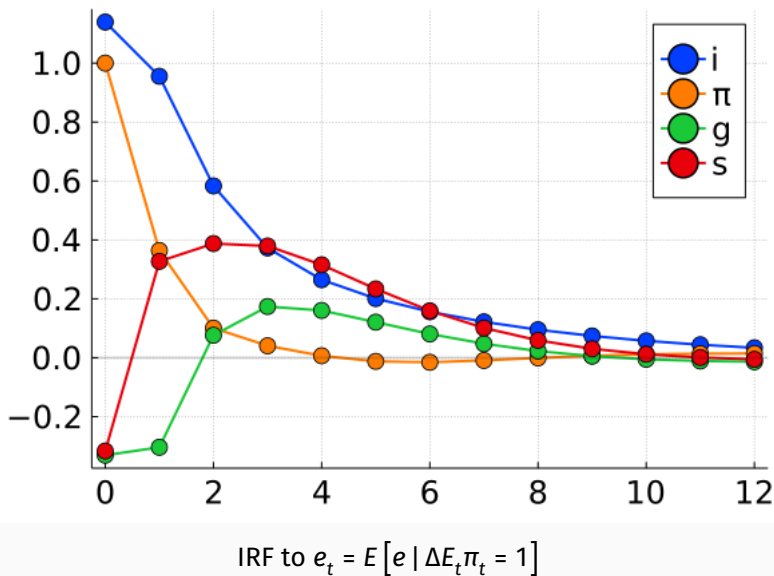
$$\frac{\text{cov}(\epsilon_{r^n,t}, \epsilon_{\pi,t})}{\text{var}(\epsilon_{\pi,t})} - 1 = \frac{\text{cov}(\epsilon_{s,t}, \epsilon_{\pi,t})}{\text{var}(\epsilon_{\pi,t})} + \frac{\text{cov}(\epsilon_{g,t}, \epsilon_{\pi,t})}{\text{var}(\epsilon_{\pi,t})} - \frac{\text{cov}(\epsilon_{r,t}, \epsilon_{\pi,t})}{\text{var}(\epsilon_{\pi,t})}$$

## IRF - United States



IRF to  $e_t = E[e \mid \Delta E_t \pi_t = 1]$

## IRF - Brazil



# Inflation Shock - Marked-to-Market

| Country                       | $\epsilon_{r^n}$ | $-\epsilon_{\pi}$ | = | $\epsilon_s$ | $+\epsilon_g$ | $-\epsilon_r$ |
|-------------------------------|------------------|-------------------|---|--------------|---------------|---------------|
| <i>1947 Sample (Advanced)</i> |                  |                   |   |              |               |               |
| United Kingdom                | ** -0.7          | ** -1             | = | ** -2.2      | ** -0.7       | ** 1.2        |
| United States                 | ** -0.7          | ** -1             | = | -0.3         | ** -0.5       | ** -0.9       |
| <i>1960 Sample (Advanced)</i> |                  |                   |   |              |               |               |
| Canada                        | ** -2.8          | ** -1             | = | 0.3          | * -1.4        | ** -2.8       |
| Denmark                       | ** -0.9          | ** -1             | = | 0.2          | -0.2          | ** -1.9       |
| Japan                         | ** -0.6          | ** -1             | = | ** 2.8       | ** -3.0       | ** -1.4       |
| Norway                        | ** -0.7          | ** -1             | = | 0.7          | * 3.0         | ** -5.4       |
| Sweden                        | ** -0.6          | ** -1             | = | ** 0.9       | ** -0.9       | ** -1.6       |
| <i>1973 Sample (Advanced)</i> |                  |                   |   |              |               |               |
| Australia                     | ** -2.2          | ** -1             | = | 0.2          | 0.1           | ** -3.5       |
| New Zealand                   | ** -1.0          | ** -1             | = | * 1.2        | ** -1.4       | * -1.8        |
| South Korea                   | ** -0.6          | ** -1             | = | ** -2.4      | 0.2           | * 0.7         |
| Switzerland                   | ** -2.0          | ** -1             | = | * -0.8       | 0.1           | ** -2.3       |

Inflation Shock:  $e_t = E[e \mid \Delta E_t \pi_t = 1]$

# Inflation Shock - Marked-to-Market

| Country                       | $\epsilon_{r^n}$ | $-\epsilon_{\pi}$ | = | $\epsilon_s$ | $+\epsilon_g$ | $-\epsilon_r$ |
|-------------------------------|------------------|-------------------|---|--------------|---------------|---------------|
| <i>1997 Sample (Emerging)</i> |                  |                   |   |              |               |               |
| Brazil                        | ** -0.7          | ** -1             | = | ** 2.4       | -0.1          | ** -4.0       |
| Colombia                      | ** -1.4          | ** -1             | = | 0.2          | ** -0.7       | ** -1.9       |
| Czech Republic                | * 0.2            | ** -1             | = | * 0.7        | ** -1.3       | -0.2          |
| Hungary                       | ** -0.8          | ** -1             | = | 0.0          | -0.2          | ** -1.6       |
| India                         | * -0.2           | ** -1             | = | ** -1.0      | -0.1          | -0.1          |
| Israel                        | ** -0.4          | ** -1             | = | ** 0.8       | * -0.4        | ** -1.8       |
| Mexico                        | ** -1.4          | ** -1             | = | * -1.2       | 0.0           | * -1.3        |
| Poland                        | ** -1.4          | ** -1             | = | ** 1.0       | * -0.3        | ** -3.0       |
| South Africa                  | ** -0.6          | ** -1             | = | 0.3          | ** -0.8       | ** -1.1       |
| Ukraine                       | ** -0.5          | ** -1             | = | ** -1.1      | 0.0           | -0.3          |

Inflation Shock:  $e_t = E[e \mid \Delta E_t \pi_t = 1]$

# Inflation Shock - Total Inflation

| Country                       | $-\varepsilon_{\pi}$ | = | $\varepsilon_s$ | $+\varepsilon_g$ | $-\varepsilon_r$ |
|-------------------------------|----------------------|---|-----------------|------------------|------------------|
| <i>1947 Sample (Advanced)</i> |                      |   |                 |                  |                  |
| United Kingdom                | ** -2.8              | = | ** -2.2         | ** -0.7          | 0.1              |
| United States                 | ** -1.5              | = | -0.3            | ** -0.5          | ** -0.7          |
| <i>1960 Sample (Advanced)</i> |                      |   |                 |                  |                  |
| Canada                        | ** -2.6              | = | 0.3             | * -1.4           | ** -1.5          |
| Denmark                       | ** -1.6              | = | 0.2             | -0.2             | ** -1.6          |
| Japan                         | ** -1.5              | = | ** 2.8          | ** -3.0          | ** -1.3          |
| Norway                        | ** -2.0              | = | 0.7             | * 3.0            | ** -5.7          |
| Sweden                        | ** -1.6              | = | ** 0.9          | ** -0.9          | ** -1.5          |
| <i>1973 Sample (Advanced)</i> |                      |   |                 |                  |                  |
| Australia                     | ** -3.1              | = | 0.2             | 0.1              | ** -3.4          |
| New Zealand                   | ** -2.3              | = | * 1.2           | ** -1.4          | ** -2.1          |
| South Korea                   | ** -2.0              | = | ** -2.4         | 0.2              | 0.2              |
| Switzerland                   | ** -2.0              | = | * -0.8          | 0.1              | ** -1.3          |

Inflation Shock:  $e_t = E[e \mid \Delta E_t \pi_t = 1]$



# Inflation Shock - Total Inflation

| Country                       | $-\varepsilon_{\pi}$ | = | $\varepsilon_s$ | $+\varepsilon_g$ | $-\varepsilon_r$ |
|-------------------------------|----------------------|---|-----------------|------------------|------------------|
| <i>1997 Sample (Emerging)</i> |                      |   |                 |                  |                  |
| Brazil                        | ** -0.8              | = | ** 2.4          | -0.1             | ** -3.1          |
| Colombia                      | ** -0.7              | = | 0.2             | ** -0.7          | -0.2             |
| Czech Republic                | ** -0.5              | = | * 0.7           | ** -1.3          | 0.1              |
| Hungary                       | ** -1.4              | = | 0.0             | -0.2             | ** -1.3          |
| India                         | ** -1.4              | = | ** -1.0         | -0.1             | * -0.4           |
| Israel                        | ** -0.6              | = | ** 0.8          | * -0.4           | ** -1.0          |
| Mexico                        | ** -1.4              | = | * -1.2          | 0.0              | -0.3             |
| Poland                        | ** -1.4              | = | ** 1.0          | * -0.3           | ** -2.1          |
| South Africa                  | ** -0.8              | = | 0.3             | ** -0.8          | * -0.3           |
| Ukraine                       | ** -1.2              | = | ** -1.1         | 0.0              | -0.1             |

Inflation Shock:  $e_t = E[e \mid \Delta E_t \pi_t = 1]$

# Inflation Shock - Averages

| Country         | $\epsilon_{r^n}$ | $-\epsilon_{\pi}$ | = | $\epsilon_s$ | $+\epsilon_g$ | $-\epsilon_r$ |
|-----------------|------------------|-------------------|---|--------------|---------------|---------------|
| <i>Averages</i> | ** -1.0          | ** -1             | = | 0.1          | ** -0.4       | ** -1.7       |
| 1947 (Advanced) | ** -0.7          | ** -1             | = | ** -1.2      | ** -0.6       | 0.1           |
| 1960 (Advanced) | ** -1.1          | ** -1             | = | * 1.0        | * -0.5        | ** -2.6       |
| 1973 (Advanced) | ** -1.4          | ** -1             | = | -0.4         | -0.3          | ** -1.7       |
| 1997 (Emerging) | ** -0.7          | ** -1             | = | 0.2          | ** -0.4       | ** -1.5       |

## Marked-to-Market

| Country         | $-\epsilon_{\pi}$ | = | $\epsilon_s$ | $+\epsilon_g$ | $-\epsilon_r$ |
|-----------------|-------------------|---|--------------|---------------|---------------|
| <i>Averages</i> | ** -1.6           | = | 0.1          | ** -0.4       | ** -1.3       |
| 1947 (Advanced) | ** -2.2           | = | ** -1.2      | ** -0.6       | -0.3          |
| 1960 (Advanced) | ** -1.9           | = | * 1.0        | * -0.5        | ** -2.3       |
| 1973 (Advanced) | ** -2.3           | = | -0.4         | -0.3          | ** -1.6       |
| 1997 (Emerging) | ** -1.0           | = | 0.2          | ** -0.4       | ** -0.9       |

## Total Inflation

# Inflation Shock - Takeaways

- Discount rates: 80% of inflation variation (average)
- The rest comes mostly from GDP growth
- Positive contribution of surplus-to-GDP 7/21
- Monetary policy reduces inflation in 20/21

Inflation has fiscal roots, even if fiscal policy is disconnected from the price level.

## Robustness - OLS Estimates

| Country         | $\epsilon_{r^n}$ | $-\epsilon_{\pi}$ | = | $\epsilon_s$ | $+\epsilon_g$ | $-\epsilon_r$ |
|-----------------|------------------|-------------------|---|--------------|---------------|---------------|
| <i>Averages</i> | ** -1.0          | ** -1             | = | 0.2          | ** -0.4       | ** -1.8       |
| 1947 (Advanced) | ** -0.7          | ** -1             | = | ** -1.2      | ** -0.6       | 0.2           |
| 1960 (Advanced) | ** -1.2          | ** -1             | = | * 1.0        | * -0.5        | ** -2.6       |
| 1973 (Advanced) | ** -1.4          | ** -1             | = | -0.4         | -0.3          | ** -1.7       |
| 1997 (Emerging) | ** -0.7          | ** -1             | = | 0.4          | * -0.3        | ** -1.8       |

### Marked-to-Market

| Country         | $-\epsilon_{\pi}$ | = | $\epsilon_s$ | $+\epsilon_g$ | $-\epsilon_r$ |
|-----------------|-------------------|---|--------------|---------------|---------------|
| <i>Averages</i> | ** -1.6           | = | 0.2          | ** -0.4       | ** -1.4       |
| 1947 (Advanced) | ** -2.2           | = | ** -1.2      | ** -0.6       | -0.3          |
| 1960 (Advanced) | ** -1.9           | = | * 1.0        | * -0.5        | ** -2.4       |
| 1973 (Advanced) | ** -2.4           | = | -0.4         | -0.3          | ** -1.6       |
| 1997 (Emerging) | ** -1.0           | = | 0.4          | * -0.3        | ** -1.1       |

### Total Inflation

## Robustness - Minnesota Prior

| Country         | $\epsilon_{r^n}$ | $-\epsilon_{\pi}$ | = | $\epsilon_s$   | $+\epsilon_g$  | $-\epsilon_r$  |
|-----------------|------------------|-------------------|---|----------------|----------------|----------------|
| <i>Averages</i> | <b>** -1.0</b>   | <b>** -1</b>      | = | <b>0.2</b>     | <b>** -0.4</b> | <b>** -1.8</b> |
| 1947 (Advanced) | <b>** -0.7</b>   | <b>** -1</b>      | = | <b>** -1.2</b> | <b>** -0.6</b> | <b>0.2</b>     |
| 1960 (Advanced) | <b>** -1.1</b>   | <b>** -1</b>      | = | <b>* 1.0</b>   | <b>* -0.5</b>  | <b>** -2.6</b> |
| 1973 (Advanced) | <b>** -1.4</b>   | <b>** -1</b>      | = | <b>-0.5</b>    | <b>-0.3</b>    | <b>** -1.7</b> |
| 1997 (Emerging) | <b>** -0.7</b>   | <b>** -1</b>      | = | <b>0.3</b>     | <b>* -0.3</b>  | <b>** -1.8</b> |

### Marked-to-Market

| Country         | $-\epsilon_{\pi}$ | = | $\epsilon_s$   | $+\epsilon_g$  | $-\epsilon_r$  |
|-----------------|-------------------|---|----------------|----------------|----------------|
| <i>Averages</i> | <b>** -1.6</b>    | = | <b>0.2</b>     | <b>** -0.4</b> | <b>** -1.4</b> |
| 1947 (Advanced) | <b>** -2.2</b>    | = | <b>** -1.2</b> | <b>** -0.6</b> | <b>-0.3</b>    |
| 1960 (Advanced) | <b>** -1.9</b>    | = | <b>* 1.0</b>   | <b>* -0.5</b>  | <b>** -2.4</b> |
| 1973 (Advanced) | <b>** -2.3</b>    | = | <b>-0.5</b>    | <b>-0.3</b>    | <b>** -1.6</b> |
| 1997 (Emerging) | <b>** -1.1</b>    | = | <b>0.3</b>     | <b>* -0.3</b>  | <b>** -1.1</b> |

### Total Inflation

## Robustness - 2021 Sample

| Country         | $\epsilon_{r^n}$ | $-\epsilon_{\pi}$ | = | $\epsilon_s$ | $+\epsilon_g$ | $-\epsilon_r$ |
|-----------------|------------------|-------------------|---|--------------|---------------|---------------|
| <i>Averages</i> | ** -1.0          | ** -1             | = | -0.1         | * -0.2        | ** -1.7       |
| 1947 (Advanced) | ** -0.8          | ** -1             | = | ** -1.2      | ** -0.5       | 0.0           |
| 1960 (Advanced) | ** -1.2          | ** -1             | = | * 0.8        | * -0.6        | ** -2.4       |
| 1973 (Advanced) | ** -1.4          | ** -1             | = | -0.6         | -0.2          | ** -1.6       |
| 1997 (Emerging) | ** -0.8          | ** -1             | = | -0.1         | 0.0           | ** -1.7       |

### Marked-to-Market

| Country         | $-\epsilon_{\pi}$ | = | $\epsilon_s$ | $+\epsilon_g$ | $-\epsilon_r$ |
|-----------------|-------------------|---|--------------|---------------|---------------|
| <i>Averages</i> | ** -1.6           | = | -0.1         | * -0.2        | ** -1.3       |
| 1947 (Advanced) | ** -2.2           | = | ** -1.2      | ** -0.5       | * -0.4        |
| 1960 (Advanced) | ** -1.9           | = | * 0.8        | * -0.6        | ** -2.1       |
| 1973 (Advanced) | ** -2.4           | = | -0.6         | -0.2          | ** -1.5       |
| 1997 (Emerging) | ** -1.1           | = | -0.1         | 0.0           | ** -1.0       |

### Total Inflation

# Discounted Surpluses Shock

- Discount rates drive innovations to inflation
- What drives discounted surpluses?
- Put differently: what drives unexpected returns on the **basket** of public bonds?

$$\begin{aligned}e_t &= E[e \mid \Delta E_t(\text{Disc Surpl}) = -1] \\&= E[e \mid \Delta E_t(\epsilon_{s,t} + \epsilon_{g,t} - \epsilon_{r,t}) = -1]\end{aligned}$$

# Discounted Surpluses Shock - Marked-to-Market

| Country                       | $\epsilon_{r^n}$ | $-\epsilon_{\pi}$ | = | $\epsilon_s$ | $+\epsilon_g$ | $-\epsilon_r$ |
|-------------------------------|------------------|-------------------|---|--------------|---------------|---------------|
| <i>1947 Sample (Advanced)</i> |                  |                   |   |              |               |               |
| United Kingdom                | ** -0.8          | ** -0.2           | = | ** -0.5      | -0.1          | * -0.4        |
| United States                 | ** -0.7          | ** -0.3           | = | 0.0          | ** 0.2        | ** -1.2       |
| <i>1960 Sample (Advanced)</i> |                  |                   |   |              |               |               |
| Canada                        | ** -0.8          | ** -0.2           | = | * 0.2        | -0.1          | ** -1.1       |
| Denmark                       | ** -0.8          | ** -0.2           | = | * 0.6        | * 0.5         | ** -2.0       |
| Japan                         | ** -0.6          | ** -0.4           | = | 0.0          | -0.2          | ** -0.8       |
| Norway                        | ** -0.6          | ** -0.4           | = | * 1.0        | * 1.9         | ** -3.9       |
| Sweden                        | ** -0.6          | ** -0.4           | = | ** 0.7       | -0.2          | ** -1.5       |
| <i>1973 Sample (Advanced)</i> |                  |                   |   |              |               |               |
| Australia                     | ** -0.8          | ** -0.2           | = | * 0.5        | * 0.2         | ** -1.7       |
| New Zealand                   | ** -0.6          | ** -0.4           | = | ** 0.8       | ** -0.5       | ** -1.3       |
| South Korea                   | ** -0.6          | ** -0.4           | = | ** -2.4      | ** 1.3        | 0.2           |
| Switzerland                   | ** -0.8          | ** -0.2           | = | -0.1         | * 0.2         | ** -1.1       |

Discounted Surpluses Shock:  $E[e \mid \Delta E_t(\epsilon_{s,t} + \epsilon_{g,t} - \epsilon_{r,t}) = -1]$



# Discounted Surpluses Shock - Marked-to-Market

| Country                       | $\epsilon_{r^n}$ | $-\epsilon_{\pi}$ | = | $\epsilon_s$ | $+\epsilon_g$ | $-\epsilon_r$ |
|-------------------------------|------------------|-------------------|---|--------------|---------------|---------------|
| <i>1997 Sample (Emerging)</i> |                  |                   |   |              |               |               |
| Brazil                        | ** -0.5          | ** -0.5           | = | ** 1.4       | 0.1           | ** -2.6       |
| Colombia                      | ** -0.6          | ** -0.4           | = | 0.0          | ** -0.3       | ** -0.8       |
| Czech Republic                | ** -0.4          | ** -0.6           | = | -0.1         | -0.3          | ** -0.6       |
| Hungary                       | ** -0.6          | ** -0.4           | = | * 0.4        | -0.3          | ** -1.2       |
| India                         | ** -0.5          | ** -0.5           | = | -0.1         | * -0.2        | ** -0.7       |
| Israel                        | ** -0.7          | ** -0.3           | = | ** 0.6       | -0.1          | ** -1.5       |
| Mexico                        | ** -0.6          | ** -0.4           | = | ** -0.6      | 0.1           | * -0.6        |
| Poland                        | ** -0.7          | ** -0.3           | = | ** 0.5       | -0.1          | ** -1.4       |
| South Africa                  | ** -0.7          | ** -0.3           | = | * -0.2       | 0.0           | ** -0.8       |
| Ukraine                       | ** -0.5          | ** -0.5           | = | ** -0.4      | * -0.1        | ** -0.6       |

Discounted Surpluses Shock:  $E[e \mid \Delta E_t(\epsilon_{s,t} + \epsilon_{g,t} - \epsilon_{r,t}) = -1]$

# Discounted Surpluses Shock - Total Inflation

| Country                       | $-\epsilon_{\pi}$ | = | $\epsilon_s$ | $+\epsilon_g$ | $-\epsilon_r$ |
|-------------------------------|-------------------|---|--------------|---------------|---------------|
| <i>1947 Sample (Advanced)</i> |                   |   |              |               |               |
| United Kingdom                | ** -0.9           | = | ** -0.5      | -0.1          | * -0.3        |
| United States                 | ** -0.5           | = | 0.0          | ** 0.2        | ** -0.7       |
| <i>1960 Sample (Advanced)</i> |                   |   |              |               |               |
| Canada                        | ** -0.5           | = | * 0.2        | -0.1          | ** -0.6       |
| Denmark                       | ** -0.6           | = | * 0.6        | * 0.5         | ** -1.6       |
| Japan                         | ** -0.7           | = | 0.0          | -0.2          | ** -0.5       |
| Norway                        | ** -0.9           | = | * 1.0        | * 1.9         | ** -3.8       |
| Sweden                        | ** -0.8           | = | ** 0.7       | -0.2          | ** -1.2       |
| <i>1973 Sample (Advanced)</i> |                   |   |              |               |               |
| Australia                     | ** -0.6           | = | * 0.5        | * 0.2         | ** -1.3       |
| New Zealand                   | ** -0.8           | = | ** 0.8       | ** -0.5       | ** -1.2       |
| South Korea                   | ** -1.2           | = | ** -2.4      | ** 1.3        | 0.0           |
| Switzerland                   | ** -0.5           | = | -0.1         | * 0.2         | ** -0.6       |

Discounted Surpluses Shock:  $E[e \mid \Delta E_t(\epsilon_{s,t} + \epsilon_{g,t} - \epsilon_{r,t}) = -1]$

# Discounted Surpluses Shock - Total Inflation

| Country                       | $-\epsilon_{\pi}$ | = | $\epsilon_s$ | $+\epsilon_g$ | $-\epsilon_r$ |
|-------------------------------|-------------------|---|--------------|---------------|---------------|
| <i>1997 Sample (Emerging)</i> |                   |   |              |               |               |
| Brazil                        | ** -0.3           | = | ** 1.4       | 0.1           | ** -1.9       |
| Colombia                      | ** -0.3           | = | 0.0          | ** -0.3       | -0.1          |
| Czech Republic                | ** -0.5           | = | -0.1         | -0.3          | -0.2          |
| Hungary                       | ** -0.6           | = | * 0.4        | -0.3          | ** -0.8       |
| India                         | ** -0.6           | = | -0.1         | * -0.2        | ** -0.3       |
| Israel                        | ** -0.2           | = | ** 0.6       | -0.1          | ** -0.7       |
| Mexico                        | ** -0.6           | = | ** -0.6      | 0.1           | -0.1          |
| Poland                        | ** -0.5           | = | ** 0.5       | -0.1          | ** -0.9       |
| South Africa                  | ** -0.3           | = | * -0.2       | 0.0           | * -0.1        |
| Ukraine                       | ** -0.6           | = | ** -0.4      | * -0.1        | ** -0.1       |

Discounted Surpluses Shock:  $E[e \mid \Delta E_t(\epsilon_{s,t} + \epsilon_{g,t} - \epsilon_{r,t}) = -1]$

## Discounted Surpluses Shock - Averages

| Country         | $\epsilon_{r^n}$ | $-\epsilon_{\pi}$ | = | $\epsilon_s$ | $+\epsilon_g$ | $-\epsilon_r$ |
|-----------------|------------------|-------------------|---|--------------|---------------|---------------|
| <i>Averages</i> | ** -0.6          | ** -0.4           | = | 0.1          | 0.1           | ** -1.2       |
| 1947 (Advanced) | ** -0.8          | ** -0.2           | = | * -0.2       | 0.1           | ** -0.8       |
| 1960 (Advanced) | ** -0.7          | ** -0.3           | = | * 0.5        | 0.4           | ** -1.9       |
| 1973 (Advanced) | ** -0.7          | ** -0.3           | = | -0.3         | 0.3           | ** -1.0       |
| 1997 (Emerging) | ** -0.6          | ** -0.4           | = | * 0.2        | * -0.1        | ** -1.1       |

### Marked-to-Market

| Country         | $-\epsilon_{\pi}$ | = | $\epsilon_s$ | $+\epsilon_g$ | $-\epsilon_r$ |
|-----------------|-------------------|---|--------------|---------------|---------------|
| <i>Averages</i> | ** -0.6           | = | 0.1          | 0.1           | ** -0.8       |
| 1947 (Advanced) | ** -0.7           | = | * -0.2       | 0.1           | ** -0.5       |
| 1960 (Advanced) | ** -0.7           | = | * 0.5        | 0.4           | ** -1.6       |
| 1973 (Advanced) | ** -0.8           | = | -0.3         | 0.3           | ** -0.8       |
| 1997 (Emerging) | ** -0.4           | = | * 0.2        | * -0.1        | ** -0.5       |

### Total Inflation

# Model Overview

- How hard to reproduce empirical findings? Interpretation?
- Fiscal theory of the price level, New-Keynesian model
- **Partial debt repayment** (but still FTPL!)
- Trend shocks

# Model Equations

- Private sector

$$y_t = E_t y_{t+1} - \gamma(i_t - E_t \pi_{t+1}) + \rho_g u_{g,t}$$

$$\pi_t = \beta E_t \pi_{t+1} + \kappa y_t - \kappa_a a_t$$

$$g_t = y_t - y_{t-1} - u_{g,t}$$

- Central bank

$$i_t = \phi_\pi \pi_t + \phi_g g_t + u_{i,t}$$

## Why trend shocks?

- Otherwise, output stationary  $\implies \epsilon_{g,t} \approx 0$
- Model solution:  $X_t = a(L)e_t$  for finite  $a(1)$
- Growth term of decomposition:

$$\epsilon_{g,t} = \mathbf{1}'_g a(\beta) e_t$$

- In the absence of trend shocks:

$$\begin{aligned} g_t &= \mathbf{1}'_g a(L) e_t = \mathbf{1}'_y (1 - L) a(L) e_t \\ \mathbf{1}'_g a(L) &= \mathbf{1}'_y (1 - L) a(L) \end{aligned}$$

- Therefore  $\epsilon_{g,t} = \mathbf{1}'_g a(\beta) e_t \approx \mathbf{1}'_g a(1) e_t = 0$

# Model Equations

- Flow of debt

$$v_t + \frac{S_t}{V} = \frac{1}{\beta} [v_{t-1} + r_t^n - \pi_t - g_t]$$
$$r_t^n = \delta [r_t^N] + (1 - \delta) [r_t^R + \pi_t]$$

- Bond prices and return

$$q_{N,t} = (\omega_N \beta) E_t q_{N,t} - [i_t]$$
$$q_{R,t} = (\omega_R \beta) E_t q_{R,t} - [i_t - E_t \pi_{t+1}]$$
$$r_{j,t} = (\omega_j \beta) q_{j,t} - q_{j,t-1} \quad j = N, R$$



# Fiscal Policy

- Surplus-to-GDP could follow

$$h_t = \tau(\pi_t + g_t) + u_{s,t}$$

where  $u_{s,t}$  is a standard AR(1)

- No debt repayment
- News about surpluses **always** met by unexpected inflation

# Fiscal Policy

- Surplus-to-GDP process

$$s_t = s_t^* + (1 - v) h_t$$

$$s_t^* = \alpha v_{t-1}^* + v h_t$$

$$v_{t-1}^* = \beta (v_t^* + s_t^*)$$

- $s_t$  and  $s_t^*$  respond to "debt value target"  $v^*$

$$s_t = \alpha v_{t-1}^* + h_t$$

but **not** to actual debt  $v_t$  (or arbitrary  $\Delta E_t \pi_t$ )

# Fiscal Policy

- What is the role of  $v_t^*$ ?

$$s_t = s_t^* + (1 - v) h_t \quad (1)$$

$$s_t^* = \alpha v_{t-1}^* + v h_t \quad (2)$$

$$v_{t-1}^* = \beta (v_t^* + s_t^*) \quad (3)$$

- (2) and (3):  $v^*$  is stationary
- Solve (3) forward:

$$v_{t-1}^* = \beta \sum_{j=0}^{\infty} \beta^j E_t s_{t+j}^* = \beta \sum_{j=0}^{\infty} \beta^j [E_t s_{t+j} - (1 - v) E_t h_{t+j}]$$

# Fiscal Policy

$$v_{t-1}^* = \beta \sum_{j=0}^{\infty} \beta^j \left[ E_t s_{t+j} - (1 - v) E_t h_{t+j} \right]$$

- Take innovations  $\Delta E_t = E_t - E_{t-1}$

$$\beta \sum_{j=0}^{\infty} \beta^j \Delta E_t s_{t+j} = (1 - v) \sum_{j=0}^{\infty} \beta^j \Delta E_t h_{t+j}$$

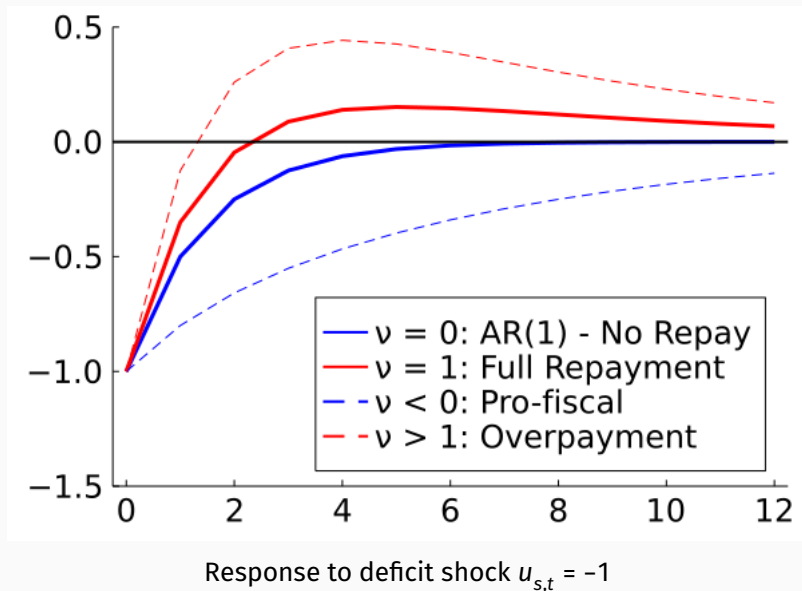
$$\epsilon_{s,t} = (1 - v) \sum_{j=0}^{\infty} \beta^j \Delta E_t h_{t+j}$$

- $v$  governs debt repayment

# Partial debt repayment

- $v = 0$  No debt repayment:  $\epsilon_{s,t} = \sum_{j=0}^{\infty} \beta^j \Delta E_t h_{t+j}$ 
  - $s_t = h_t$  (standard AR(1))
- $v = 1$  Full debt repayment:  $\epsilon_{s,t} = 0$ 
  - $s_t = s_t^* = \alpha v_t^* + h_t$
- $v < 0$  "Pro-fiscal" surplus:  $\epsilon_{s,t} / \sum_{j=0}^{\infty} \beta^j \Delta E_t h_{t+j} > 1$
- $v > 1$  "Overpayment":  $\epsilon_{s,t} / \sum_{j=0}^{\infty} \beta^j \Delta E_t h_{t+j} < 0$

## Partial debt repayment - Cases



# GMM Estimation

- Method of moments:

$$\text{Min}_{\theta} \quad w \left\| \mathcal{D}_{VAR} - \mathcal{D}_{NK}(\theta) \right\| + (1-w) \left\| \mathcal{M} - \mathcal{M}_{NK}(\theta) \right\|$$

- $\mathcal{D}$  contains MtM decomposition for inflation shock
- $\mathcal{M}$  contains second moments
- Estimates for the **United States**

# GMM Estimation

## United States Estimates

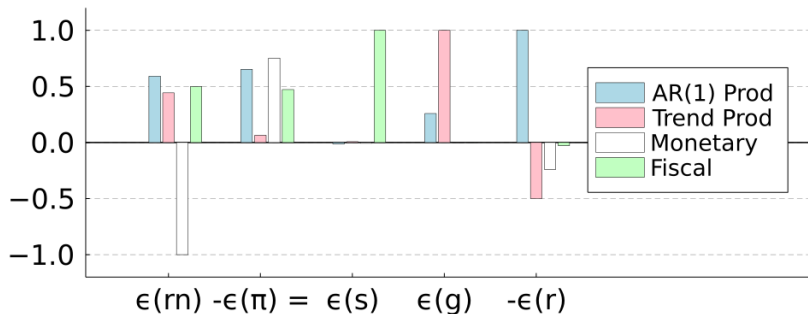
| Fixed          |               | Estimated  |       |
|----------------|---------------|------------|-------|
| Parameter      | Value         | Parameter  | Value |
| $\beta$        | 0.99          | $\rho_a$   | 0.98  |
| $\gamma$       | 0.4           | $\rho_g$   | 0.23  |
| $\varphi$      | 3             | $\rho_i$   | 0.00  |
| $\theta$       | 0.25          | $\rho_s$   | 0.72  |
| $\bar{\omega}$ | $\gamma^{-1}$ | $\phi_\pi$ | 0.68  |
| $\sigma_a$     | 1             | $\phi_g$   | 0.00  |
|                |               | $\tau$     | -0.06 |
|                |               | $\nu$      | 0.89  |
|                |               | $\alpha$   | 0.01  |
|                |               | $\sigma_g$ | 1.21  |
|                |               | $\sigma_g$ | 0.53  |
|                |               | $\sigma_g$ | 1.07  |

US Model Parameters



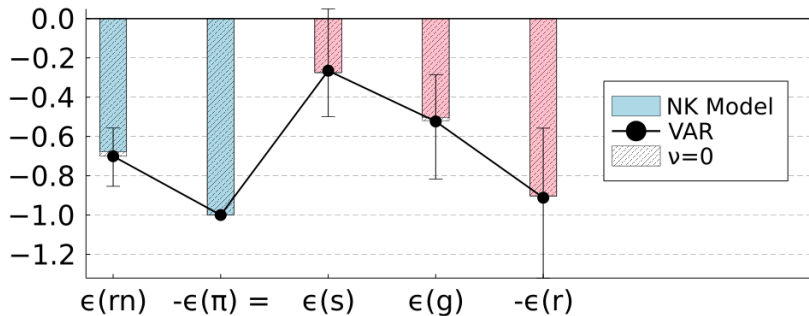
# GMM Estimation

United States Estimates



Fiscal decomposition of structural shocks

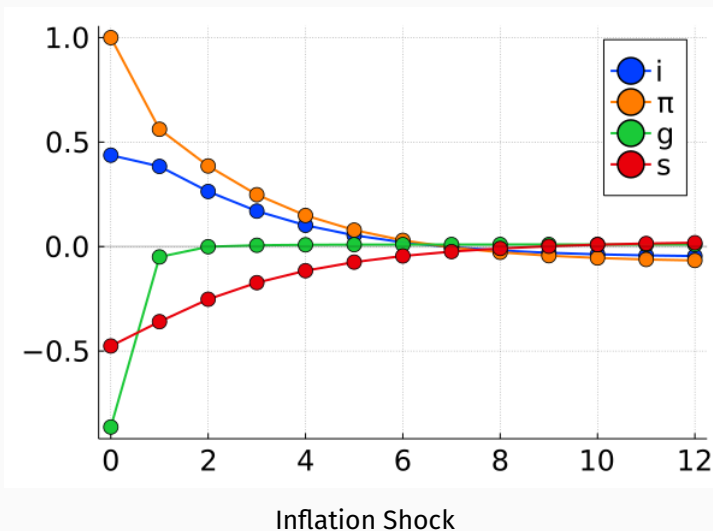
# Is AR(1) surplus a good model?



MtM decomposition of Inflation Shock  $e_t = E[e \mid \Delta E_t \pi_t = 1]$

## Is AR(1) surplus a good model?

Structural shocks:  $\varepsilon_a = -1$ ,  $\varepsilon_g = -0.2$ ,  $\varepsilon_i = -0.3$ ,  $\varepsilon_s = -0.5$



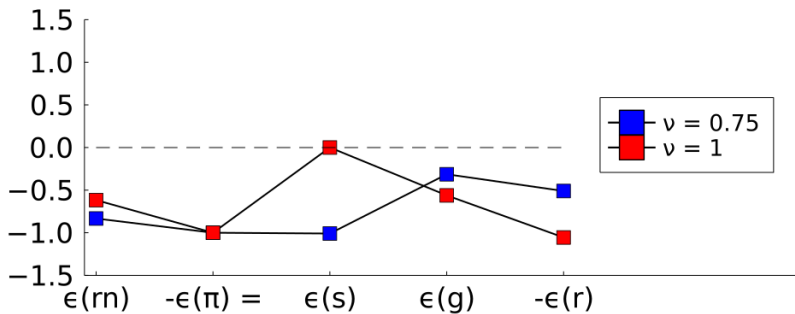
## Is AR(1) surplus a good model?

- $v = 0$  precludes realistic fiscal policy and discount-driven inflation at the same time

|                       | Data | $v = 0.9$ | $v = 0$ |                      | Data  | $v = 0.9$ | $v = 0$ |
|-----------------------|------|-----------|---------|----------------------|-------|-----------|---------|
| $\sigma_i/\sigma_g$   | 1.29 | 0.77      | 1.25    | $\text{cor}(\pi, i)$ | 0.70  | 0.88      | 0.89    |
| $\sigma_\pi/\sigma_g$ | 1.20 | 1.10      | 1.56    | $\text{cor}(\pi, g)$ | -0.11 | -0.35     | -0.40   |
| $\sigma_s/\sigma_g$   | 1.08 | 1.09      | 0.45    | $\text{cor}(g, i)$   | 0.04  | -0.35     | -0.04   |
| $\text{acor}(i)$      | 0.91 | 0.75      | 0.87    | $\text{cor}(i, s)$   | -0.26 | -0.28     | -0.46   |
| $\text{acor}(\pi)$    | 0.69 | 0.72      | 0.81    | $\text{cor}(\pi, s)$ | -0.28 | -0.29     | -0.41   |
| $\text{acor}(g)$      | 0.14 | 0.14      | 0.16    | $\text{cor}(g, s)$   | 0.01  | -0.04     | -0.05   |
| $\text{acor}(s)$      | 0.64 | 0.72      | 0.27    |                      |       |           |         |

Second Moment Fit

## Is AR(1) surplus a good model?



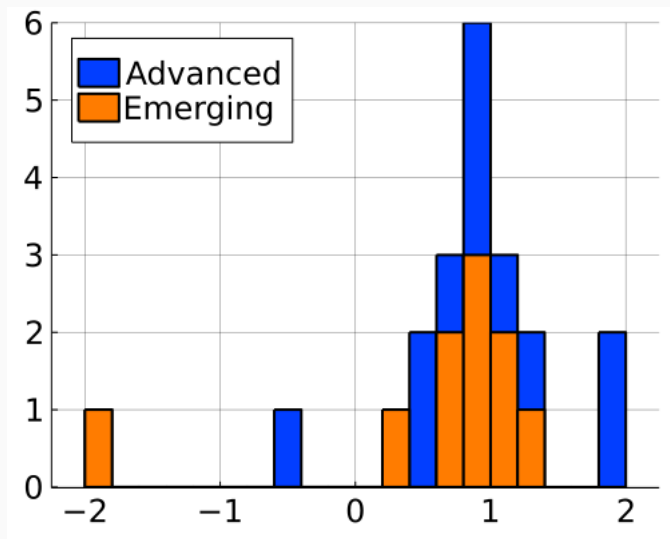
Comparative Statics for  $v$

## Cross-Country Estimates

$$\text{Min}_{\theta} \quad w \left\| \mathcal{D}_{VAR} - \mathcal{D}_{NK}(\theta) \right\| + (1-w) \left\| \mathcal{M} - \mathcal{M}_{NK}(\theta) \right\|$$

- Repeat procedure for each country in the sample
- Use corresponding debt profile  $(\delta, \omega_N, \omega_R)$

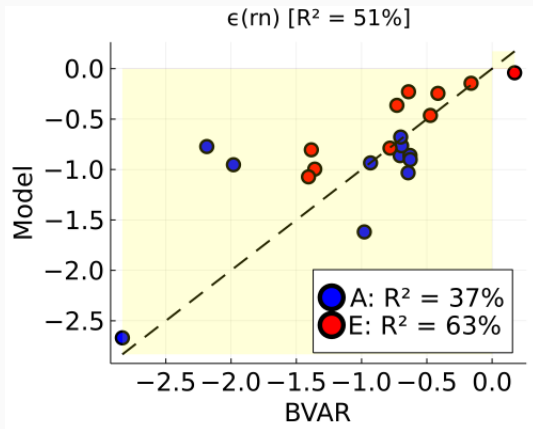
## Cross-Country Estimates of Debt Repayment $v$



Histogram of  $v$  estimates

# Cross-Country Fit of Fiscal Decomposition

$$\epsilon_{r^n,t} - \epsilon_{\pi,t} = \epsilon_{s,t} + \epsilon_{g,t} - \epsilon_{r,t}$$

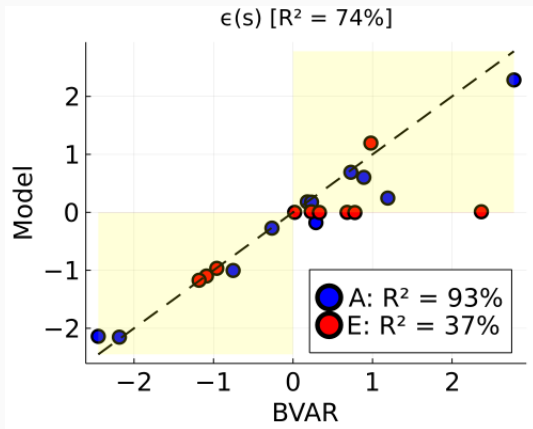


Fit of Bond Price Term  $\epsilon_{r^n,t}$



# Cross-Country Fit of Fiscal Decomposition

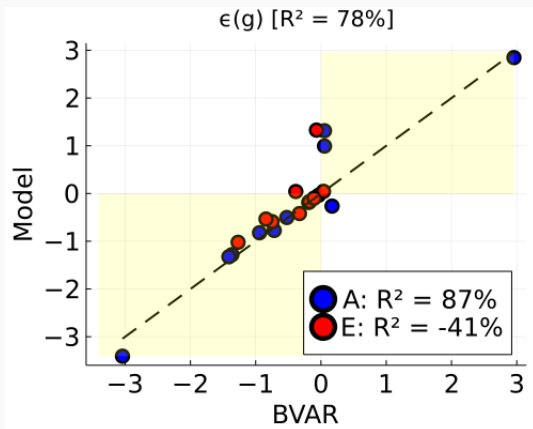
$$\epsilon_{r^n,t} - \epsilon_{\pi,t} = \epsilon_{s,t} + \epsilon_{g,t} - \epsilon_{r,t}$$



Fit of Surplus Term  $\epsilon_{s,t}$

# Cross-Country Fit of Fiscal Decomposition

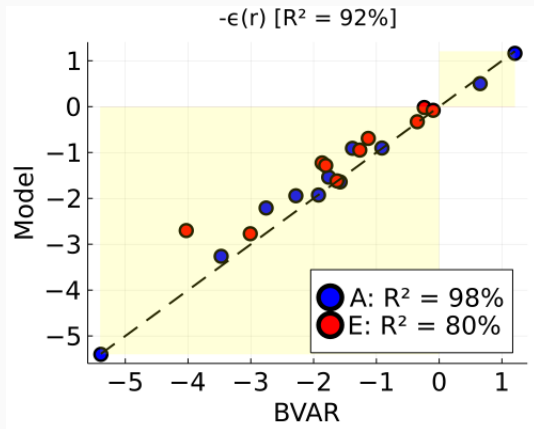
$$\epsilon_{r^n,t} - \epsilon_{\pi,t} = \epsilon_{s,t} + \epsilon_{g,t} - \epsilon_{r,t}$$



Fit of Growth Term  $\epsilon_{g,t}$

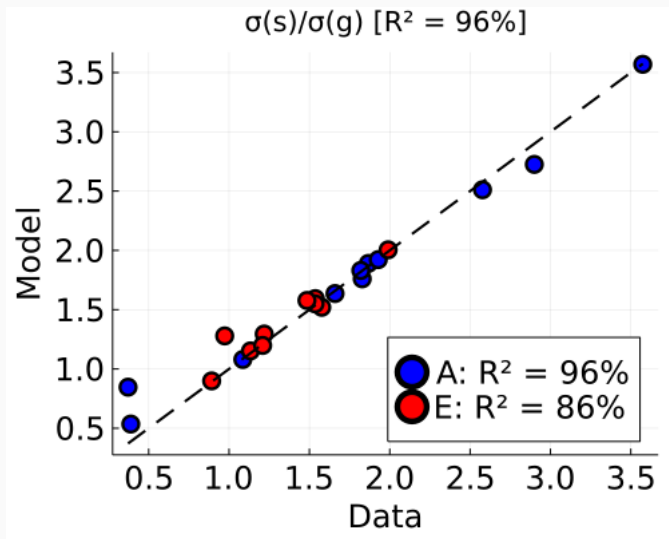
# Cross-Country Fit of Fiscal Decomposition

$$\epsilon_{r^n,t} - \epsilon_{\pi,t} = \epsilon_{s,t} + \epsilon_{g,t} - \epsilon_{r,t}$$



Fit of Discount Term  $\epsilon_{r,t}$

# Cross-Country Fit of Fiscal Policy Volatility



Fit of Fiscal Policy Volatility

# Conclusion

- Innovations to inflation driven mostly by discount rates
- Monetary-fiscal models require partial debt repayment (80-100%)
- Fiscal decomposition as useful moment to identify debt repayment

# Frametitle



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