

1 Python correction

1.1 Pyramidal decomposition and reconstruction

1.1.1 Decomposition

The following function makes the decomposition of the Laplacian and Gaussian pyramids at the same time. The Laplacian pyramid can be reconstructed without any additional information. This is illustrated in Fig. 1.



```

1 def LaplacianPyramidDecomposition(Image, levels, interp='bilinear'):
2     """
3     Laplacian / Gaussian Pyramid
4     The last image of the laplacian pyramid allows a full reconstruction
5     ↪ of the original image.
6     Image: original image, float32
7     levels: number of levels of decomposition
8     interp: interpolation mode for downsizing the image
9
10    returns: pyrL, pyrG: Laplacian and Gaussian pyramids, respectively,
11    ↪ as a list of arrays
12    """
13
14    pyrL = [];
15    pyrG = [];
16
17    sigma = 3.;
18    for l in range(levels):
19        prevImage = Image.copy();
20        g = ndimage.gaussian_filter(Image, sigma);
21        print(g.dtype)
22
23        Image = misc.imresize(g, .5, interp=interp, mode='F');
24        primeImage= misc.imresize(Image, prevImage.shape, interp=interp,
25        ↪ mode='F');
26
27        pyrL.append(prevImage - primeImage);
28        pyrG.append(prevImage);
29
30    pyrL.append(Image);
31    pyrG.append(Image);
32    return pyrL, pyrG;

```



Informations

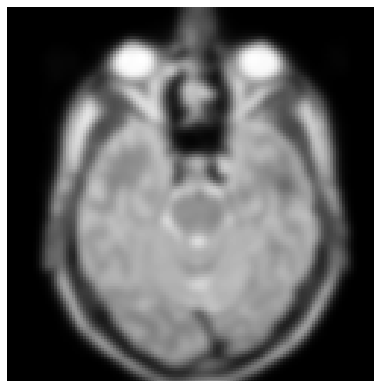
Notice that with the `misc.imresize` function, the float mode of the operation has to be specified.



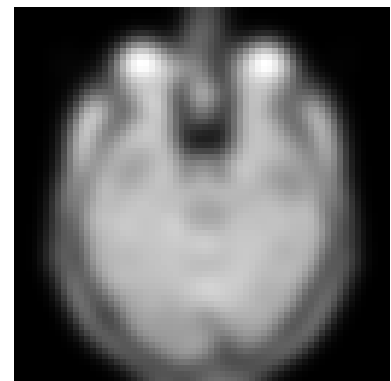
(a) Original image.



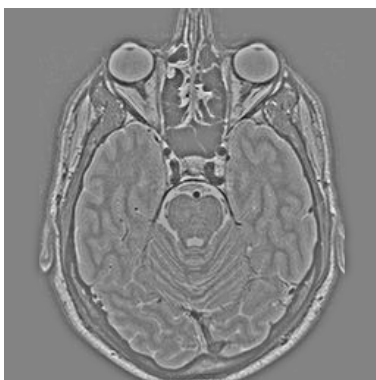
(b) Gaussian pyramid level 1.



(c) Level 2.



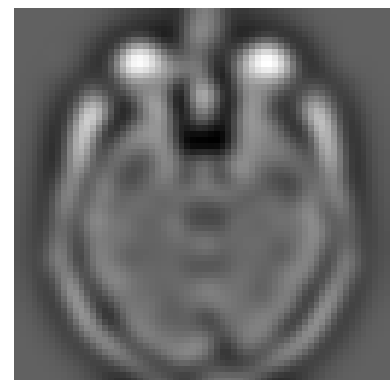
(d) Level 3.



(e) Laplacian pyramid level 1.



(f) Level 2.



(g) Level 3.

Figure 1: Gaussian and Laplacian pyramids, for 3 levels of decomposition. The Laplacian pyramid in addition to the last level of the Gaussian pyramid is required to exactly reconstruct the original image.

1.1.2 Reconstruction

The reconstruction is straightforward and exact because of the construction of the residue. The details can be filtered (removed for example), thus giving the following result Fig. 2.



```

def LaplacianPyramidReconstruction(pyr, interp='bilinear'):
    """
    Reconstruction of the Laplacian pyramid, starting from the last image
    pyr: pyramid of images (list of arrays)
    interp: interpolation mode, for upsizing the image
    returns: Image, reconstructed image
    """
    Image = pyr[-1];
    for i in range(len(pyr)-2, -1, -1):
        Image = pyr[i] + misc.imresize(Image, pyr[i].shape, interp=interp
                                       ↪ , mode='F');
    return Image;

```



(a) Reconstruction of the pyramid without any detail.



(b) Reconstruction of the pyramid with all the details.

Figure 2: Reconstruction of the Laplacian pyramid.

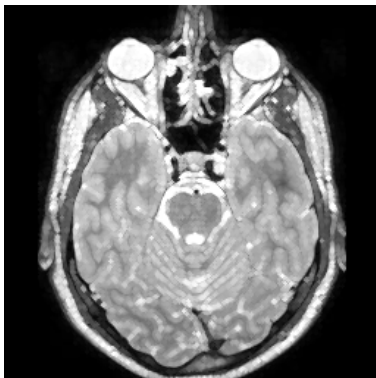
1.2 Scale-space decomposition and multiscale filtering



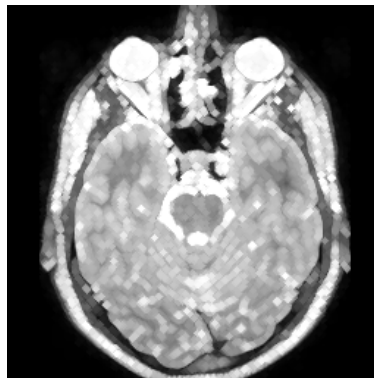
```

1 def morphoMultiscale(I, levels):
2     """
3     Morphological multiscale decomposition
4     I: original image, float32
5     levels: number of levels, int
6
7     returns: pyrD, pyrE: pyramid of Dilations/Erosions, respectively
8     """
9     pyrD=[];
10    pyrE=[];
11    for r in np.arange(1,levels):
12        print(r)
13        se = morphology.disk(r);
14        pyrD.append(morphology.dilation(I, selem=se));
15        pyrE.append(morphology.erosion(I, selem=se));
16    return pyrD, pyrE;

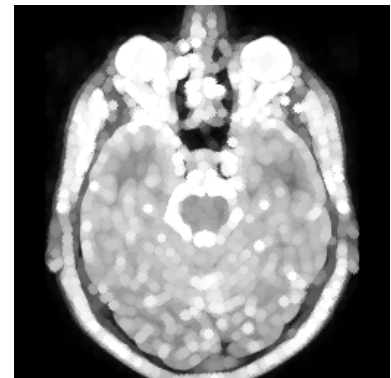
```



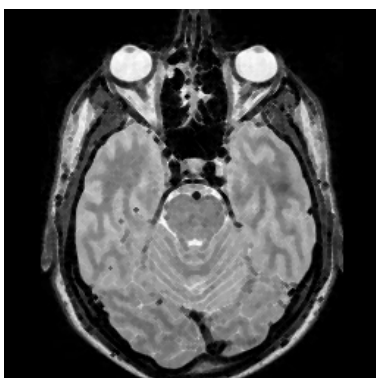
(a) Dilation scale 1.



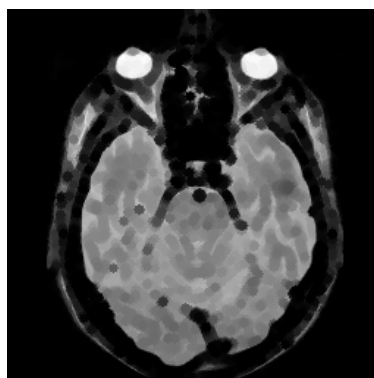
(b) Dilation scale 2.



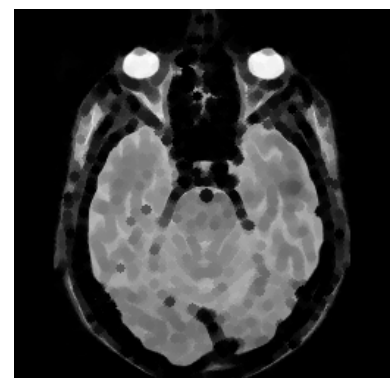
(c) Dilation scale 3.



(d) Erosion scale 1.



(e) Erosion scale 2.



(f) Erosion scale 3.

Figure 3: Morphological multiscale decomposition by dilation and erosion.

1.3 Kramer and Bruckner multiscale decomposition

The results are illustrated in Fig.4.



Figure 4: Kramer and Bruckner multiscale decomposition, with $r = 5$.



```
def kb(I, r):
    """
    Elementary Kramer/Brckner filter. Also called toggle filter.
    I: image
    r: radius of structuring element (disk), for max/min evaluation
    """
    se = morphology.disk(r);
    D=morphology.dilation(I, selem=se);
    E=morphology.erosion(I, selem=se);
    difbool = D-I < I-E;
    k = D*difbool + E * (~difbool);
    return k;
```



```
def KBmultiscale(I, levels, r=1):  
    """  
    2      Kramer and Bruckner multiscale decomposition  
    4  
    I: original image, float32  
    6    pyrD: pyramid of Dilations  
    pyrE: pyramid of Erosions  
    8  
    returns: MKB: Kramer/Bruckner filters  
    10    """  
    MKB = [];  
    12    MKB.append(I);  
    for i in range(levels):  
    14        MKB.append(kb(MKB[i-1], r));  
    return MKB
```