

1 Python correction



```
1 import numpy as np
  import matplotlib.pyplot as plt
3 import scipy
  import scipy.ndimage.filters
5 from scipy import interpolate
```

1.1 Binary image generation

A disk is generated via the meshgrid function.



```
# disk: number of points
2 n = 1024;
# disk: radius
4 R = 300;

6 # construct a binary image of a disk
X, Y = np.meshgrid(np.arange(-n/2,n/2,1) , np.arange(-n/2,n/2,1));
8 I = X**2+Y**2<=R**2;
  I = I.astype('float')
```

1.2 Initial contour

The choice of the initial contour is crucial in this method. The parameters used in this example ensure the convergence of the snake.



```
1 step=.01;
  x = n/2 + 400 * np.cos(np.arange(0,2*np.pi+step,step));
3 y = n/2 + 200 * np.sin(np.arange(0,2*np.pi+step,step));
```

The different parameters are defined by:



```
1 k=.1;
  alpha = .0001;
3 beta = 10;
  gamma= 100;
5 iterations = 1000;
```

1.3 Matrix construction

This is maybe the hardest part of this code, with the use of the `scipy.sparse.diags` function.



```

N = x.size;
2 X = np.array([-beta, alpha+4*beta, -2*alpha-6*beta, alpha+4*beta, -beta,
               ↪ -beta, alpha+4*beta, -beta, alpha+4*beta])
A = scipy.sparse.diags(X, np.array([-2, -1, 0, 1, 2, N-2, N-1, -N+2, -N
               ↪ +1]), shape=(N,N)).toarray();
4 AA = np.identity(N)-gamma*A;
invAA = np.linalg.inv(AA);

```

1.4 External forces

The external forces are computed with the following code. Notice that axis 0 correspond to the vertical axis (y) and the axis 1 corresponds to the horizontal axis (x).



```

1 # external forces computation
G = scipy.ndimage.filters.gaussian_gradient_magnitude(I, 30);
3
# Notice that horizontal axis x is 1, and vertical axis is 0
5 Fy = scipy.ndimage.prewitt(G, axis=0);
Fx = scipy.ndimage.prewitt(G, axis=1);

```

1.5 Display results

To enhance the role of the external forces, the arrows showing the force are displayed (quiver function, see Fig.1).



```

imshow(I,[])
2 hold on
plot([x;x(1)], [y; y(1)], 'g', 'linewidth', 3);
4
%% display arrows for external forces
6 step=20;
subx = 1:step:size(I,1);
8 suby = 1:step:size(I,2);
[Xa, Ya] = meshgrid(subx, suby);
10 quiver(Xa, Ya, Fx(subx, suby), Fy(subx,suby));

```

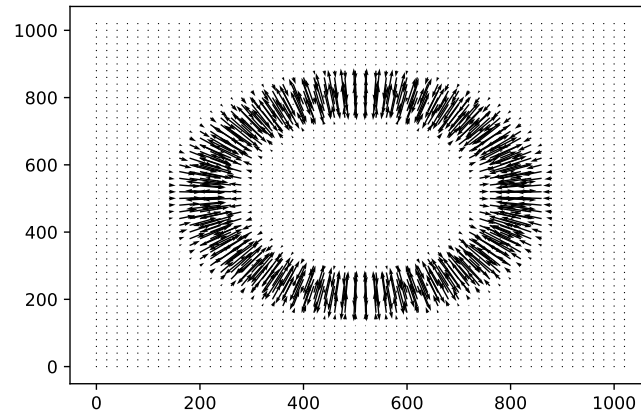


Figure 1: External forces that will be applied to the snake.

1.6 Convergence algorithm



```

# interpolation methods to get values of the external forces at the
2 # coordinates of the snake
sx, sy = I.shape;
4 ix = interpolate.interp2d(np.arange(n), np.arange(n), Fx);
  iy = interpolate.interp2d(np.arange(n), np.arange(n), Fy);
6
# loop for convergence of the snake
8 bar = progressbar.ProgressBar();
  for index in bar(range(iterations)):
10     fex = np.array([float(ix(XX,YY)) for XX,YY in zip(x,y)]);
     fey = np.array([float(iy(XX,YY)) for XX,YY in zip(x,y)]);
12     #print(np.max(fex), np.min(fex))
     x = np.matmul(invAA, x+gamma*fex);
14     y = np.matmul(invAA, y+gamma*fey);

```

The results are displayed in Fig.2.

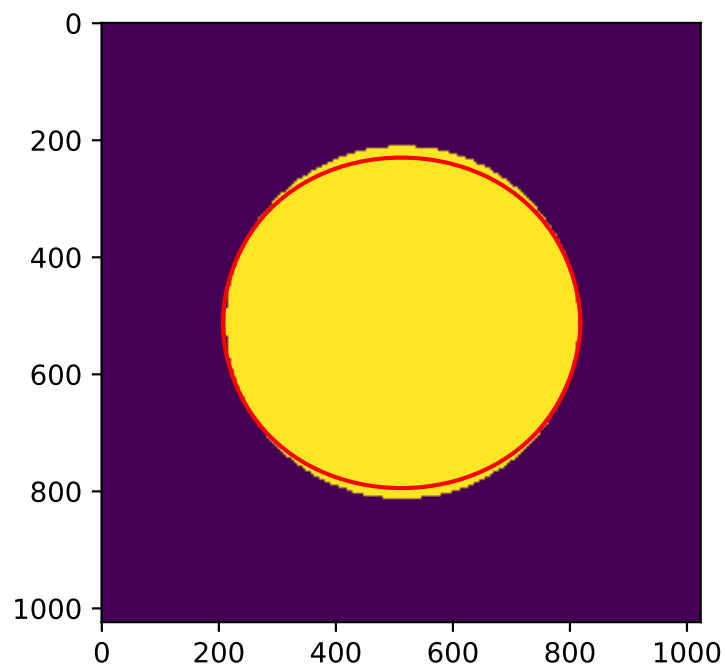


Figure 2: Result of the snake converging toward the disk, after 1000 iterations with the proposed parameters.