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These control how quickly the stepsize is increased or decreased between iterations
function result_rkintegrate, x0temp, x1temp, output, regions, resolution=resolution
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                'Keep takeing R.K. steps until every packet has reached the time of "image taken"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               ************************
                                                                                                                   ******************
                                                                                                                                                                                    Driver routine to run the 5th order RK integrator from Numerical
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               initial guess at best stepsize
                                                                                                                                                                                                                                                                                                                                                                                 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if (n_elements(resolution) EQ 0) then resolution = 1d-6
                                                                                                                                                                                                                                                                                                                                                                            dN/dt = n(r(t)), r(t) = x0 + t*(x1-x0), N(t=0) = integrate from <math>t=0->t=1 or x0->x1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ; -- don't use this right now - may want to change
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ;; yscale = scaling parameter for each variable
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ;Set variables in preparation for iteration count = 0L ;; number of steps taken
                                                                                                                                                                                                                                                                                                                                                                                                                                                                             ;; Function returns integral over path.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if \sim(array\_equal(sz0, sz1)) then stop if (sz0[0] \to 2] then begin
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              sz0 = size(x0) & sz1 = size(x1)
                                                                                                                                                                                                                                                                                  x0,x1 should be nx3 arrays
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          ;; Written by Matthew Burger
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                x0 = x0temp & x1 = x1temp
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        h = replicate(0.1d, npts)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ;; Version 4.0: 3/24/2011
                                                         compile_opt idl2, hidden
                                                                                                                                                                                                                    Recipies, 3rd Ed.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             x0 = transpose(x0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          timeinc = resolution
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             x1 = transpose(x1)
                                                                                                                                                                                                                                                                                                                                                 Solve function:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              sz0 = size(x0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             = -.25
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       npts = sz0[1]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 safety = .95
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           grow = -.2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 shrink
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Now generate sub-arrays containing only the particles that are still being tracked
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ;; Run the rk5 step result_rk5, t_sub, h_sub, x0_sub, v0_sub, N_sub, delta, output, regions
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          ;; Check where difference is very small - adjust step size
                                                                                                                                                                                                                                                                                                            if (regions EQ !null) then regions = results_voronoi(output)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ;Adjust stepsize to be no more than time remaining h\_sub = (h\_sub \ LE \ trem)*h\_sub + (h\_sub \ GT \ trem)*trem
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ;; difference relative to acceptable difference
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           ;; Do the error check ;; scale = a_tol + |y| * r_tol scale = resolution + abs(N_sub)*resolution
                                                                                                                                                                                                                                                                                                                                                                                                     moretogo = where(tremain GT timeinc, ntogo)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              g = where(delta LE 1.0, ng, comp=b)
if (ng GT 0) then beain
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               h_sub[noerr] = h_sub[noerr]*10.
                                                                                                                                                     tend = 1. ;; integrate from 0 to 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if (noerr[0] NE -1) then begin
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         noerr = where(delta LE 1e-7)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            ;; Put the post-step values
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ;print, n_elements(noerr)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   t[moretogo[g]] = t_sub[g]
N[moretogo[g]] = N_sub[g]
                                                                                                                                                                                                                   L_step = dblarr(npts,10000)
N_step = dblarr(npts,10000)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          trem = tremain[moretogo]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      x0_sub = x0[moretogo,*]
v0_sub = v0[moretogo,*]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  delta[noerr] = 1.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         t_sub = t[moretogo]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               h_sub = h[moretogo]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                N_sub = N[moretogo]
                                                                                                                                                                                                                                                                                                                                                                                                                                    done = (ntogo \mathbb{E}_{\mathbb{Q}} 0)
                                                                                                                                                                                                                                                                                                                                                                          tremain = tend - t
                                                                                                                                                                                                                                                                                                                                                                                                                                                               while ~(done) do
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  delta /= scale
                                                              t = dblarr(npts)
                                                                                         N = dblarr(npts)
                                                                                                                          v0 = x1-x0
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moretogo = where(tremain GT timeinc, ntogo) ;; check to see which ones aren't done
count++ ;; step counter
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (count mod 10 EQ 0) then print, 'Step Number: ' + strint(count) +
                                                                                                                                                                                                                                                                                                                                                                                                                                                       qqq = where(h LT 1e-7) & if (qqq[0] NE -1) then stop ;; error test
                                                                                                                                                                                                                                                                                                                               ;; don't let step size drop below 1/10th previous step size
h[moretogo[b]] = max([[htemp], [0.1*h_sub[b]]], dim=2)
                                                                                                                  if (ng NE ntogo) then begin
;; don't adjust the bad values, but do fix the stepsize
htemp = safety * h_sub[b] * delta[b]^shrink
q = where(htemp LT 0.0, nq) & if (nq NE 0) then stop
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                If it goes 100000 steps then it will never stop!
h[moretogo[g]] = safety*h_sub[g]*delta[g]^grow
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 q = where(N LT 0, nq) & if (nq GT 0) then stop
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        done = ((\text{ntogo EQ 0}) \circ \vec{r} (\text{count GT 100000.}))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ', Points Remaining: ' + strint(ntogo)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   tremain = tend - t
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                return, N
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