# Orbital and Attitude Dynamics Simulation for Nano- and Picosatellites

Murray L Ireland

6th November 2016

## **ABSTRACT**

## **CONTENTS**

List of Figures			3
List of Tables			4
1	Intro	ODUCTION	8
2	Orbital Dynamics		9
	2.1	Kepler Stuff	9
	2.2	Orbital Elements	9
	2.3	Frames of Reference	9
	2.4	More Complex Stuff	9
Bı	BLIOGR	АРНУ	10

## LIST OF FIGURES

### LIST OF TABLES

## LIST OF NOTES

#### **NOMENCLATURE**

#### **UNITS**

All units of measurement throughout this thesis conform to the *Système Internationale*, with deviations from this rule noted where appropriate.

#### **NOTATION**

This section describes the general form of notation for properties such as scalars, vectors and matrices and their derivatives.

#### TIME DERIVATIVES

- $\dot{x}$  first derivative of x with respect to time
- $\ddot{x}$  second derivative of x with respect to time
- $x^{(n)}$  nth derivative of x with respect to time

#### SCALARS, VECTORS AND MATRICES

- x scalar
- x vector or matrix
- $\mathbf{x}^T$  transpose of vector or matrix
- $x_i$  ith element of vector **x**
- f(x) function of scalar x
- $f(\mathbf{x})$  function of vector or matrix  $\mathbf{x}$
- $f_{\mathbf{x}}$  Jacobian of  $f(\mathbf{x})$  with respect to  $\mathbf{x}$

#### **SYMBOLS**

The following symbols are used throughout this thesis. Where a symbol is used only briefly, it is defined at the appropriate point in the text.

#### **LATIN**

 $C_d$  aerodynamic drag coefficient [–]

 $F, \mathbf{F}$  force [N]

g acceleration due to gravity  $[m s^{-2}]$ 

i current [A]

L, M, N rotational forces [N m]

M moment [N m] m mass [kg] R resistance [Ω]

u, v, w surge, sway and heave velocities [m s<sup>-1</sup>]

V magnitude of velocity [m s<sup>-1</sup>]  $V_a$  voltage applied to circuit [V]

X, Y, Z linear forces [N]

x, y, z components of position [m]

#### GREEK

 $\beta$  slip angle [rad]

 $\phi$ ,  $\theta$ ,  $\psi$  roll, pitch and yaw displacements [rad]

 $\rho$  atmospheric density [kg m<sup>-3</sup>]

 $\sigma$  friction coefficient [–]

 $\omega$  rotational speed [rad s<sup>-1</sup>]

 $\omega$  angular velocity vector [rad s<sup>-1</sup>]

#### **SUBSCRIPTS**

*k* iteration of inverse simulation

n iteration of Newton-Raphson method

#### **ABBREVIATIONS**

FDIR fault detection, isolation and reconfiguration

InvSim inverse simulation NED north-east-down

## 1

## **INTRODUCTION**

Put stuff in here at some point, including:

- Previous work
- Taxonomy of rovers
- Inverse simulation

## 2

### **ORBITAL DYNAMICS**

- 2.1 KEPLER STUFF
- 2.2 ORBITAL ELEMENTS
- 2.3 FRAMES OF REFERENCE
- 2.4 MORE COMPLEX STUFF

## **BIBLIOGRAPHY**