

# Algorithmic Trading

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# 1 Fundamentals of Systematic Trading

Based on the book by Rishi K. Narang [2013].

## 1.1 Market Fundamentals

The basic function of a market is to bring buyers and sellers together.

### Process 1.1.1. (*Four Components of a Trade*)

- i. Acquisition of information and quotes
  1. Quality information and transparency are crucial to price discovery
  2. Transparent markets quickly disseminate high-quality information
  3. Opaque markets are those that lack transparency
- ii. Routing of the trade order
  1. Selecting the brokers to handle the trades
  2. Deciding which markets will execute the trades and transmitting the trades to the markets
- iii. Execution. Buys are matched and executed against sells according to the rules of the market
- iv. Confirmation, clearance and settlement
  1. Clearance is the recording and comparison of the trade records
  2. Settlement involves the actual delivery of the security and its payment
  3. Might include trade allocation

Hidden portions of large institutional orders are dark liquidity pools. Orders that are partially revealed are called iceberg or hidden-size orders.

### Remark 1.1.2. (*Risks of Algorithmic Trading*)

- i. Leaks might arise from competitor efforts to reverse engineer them
- ii. Many algorithms lack the capacity to handle or respond to exceptional or rare events.

An auction is a competitive market process involving multiple buyers, multiple sellers, or both. Auctions are useful and cost-effective in pricing a security with an unknown value. On the other hand,

### Definition 1.1.3.

- i. *Market Order*: trade carried out immediately at best price available in market.
- ii. *Limit Order*: only executed at this price or at one more favourable to the trader.
- iii. *Stop/Stop-Loss Order*: order executed at the best price available (become market order) once a bid or ask is made at that particular price or a less-favourable price. Limits loss that can be incurred.
- iv. *Stop-Limit Order*: combination of stop order and limit order. Order becomes limit order as soon as a bid or ask is made at the price equal to or less favourable than stop price. If stop price and limit price is the same, then the order is *stop-and-limit* order.
- v. *Market-if-Touched (MIT)/Board Order*: executed at best available price after trade occurs at a specified price or more favourable. Ensure profit is taken if sufficiently favourable price movements occur.
- vi. *Market-Not-Held/Discretionary Order*: traded as market order, execution may be delayed at broker's discretion for better price.
- vii. *Time-of-Day Order*: Specifies period of time during day when order can be executed.
- viii. *Open/Good-Till-Cancel Order*: in effect until executed or until end of trading in particular contract.
- ix. *Fill-or-Kill Order*: must be executed immediately on receipt or none at all.

**Remark 1.1.4. (*Cornering-the-Market*)** Trader takes huge long futures position and tries to exercise control over supply of underlying commodity. As maturity of futures contract is approaching, position is not closed, number of outstanding contracts exceed commodities available. Holders of short positions desperately try to close positions, leading to rise in both futures and spot prices.

Abuse is dealt with by increasing margin requirements or imposing stricter position limits or prohibiting trades that increase speculator's open position or requiring market participants to close their positions.

## 1.2 Alpha Models

A schematic of a live 'production' trading strategy is shown below, but does not include everything else necessary to create the strategy (i.e., research tools).

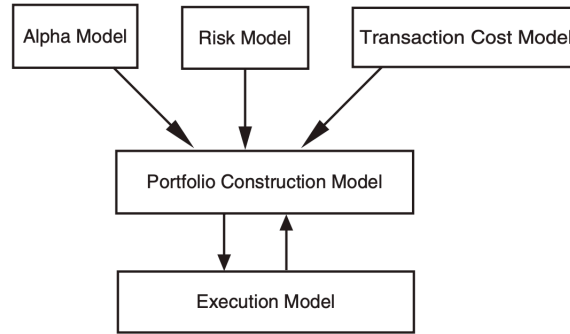


Figure 1: Live 'production' trading strategy

The trading system has three modules:

- i. Alpha model: predicts the future of the instruments considered for trading, i.e. directional alpha
- ii. Risk model: limits amount of exposure to factors that are unlikely to generate returns but could drive losses, i.e. directional exposure limit on an asset class
- iii. Transaction cost model: determine if the cost of the trades needed to migrate from current portfolio to new portfolio is desirable to the portfolio construction model.

These models feed into a portfolio construction model that balances the tradeoffs of profit and risk to determine the best portfolio to hold. The model finds the differences in trades that need to be executed.

The execution model then takes the required trades, and using inputs such as urgency in which the trades need to be executed and dynamics of liquidity in the markets, executes the trades in an efficient and low cost manner.

### 1.2.1 Alpha Models

Theory-driven models test theories of why markets behave in a manner, and see if they can be used to predict the future. Strategies utilising price-related data are trend and mean reversion; strategies utilising fundamental data are value/yield, growth and quality. Usually more than one model is used in combination.

**Definition 1.2.1.** (*Trend Following*) Markets move in given direction long enough that the trend can be identified. As more data support the bull/bear thesis in an uncertain market, more market participants will adopt the same thesis and hence move the asset price to a new equilibrium.

An example of a trend is a moving average crossover indicator. This strategy has less than one point of return for every point of downside risk taken, as market behaviour is unstable and episodic.

**Definition 1.2.2.** (*Mean Reversion*) Markets move in opposite direction to the prevailing trend. Short-term imbalances between buyers and sellers due to liquidity forces prices to move abruptly in one direction, which increases probability of trend reversion as liquidity issue is resolved.

An example of mean reversion strategy is statistical arbitrage, which bets on convergence of prices of similar stocks whose prices have diverged.

Trend and mean reversion strategies are not at odds. Longer-term trends can occur despite smaller oscillations around these trends occurring in the shorter term, hence both strategies may be used in conjunction.

**Definition 1.2.3.** (*Value/Yield*) Value strategies are usually ratios of some fundamental factor against the price of the instrument, inverted to keep the ratio consistent. The higher the yield, the cheaper the instrument.

Markets tend to overestimate risk in risky instruments and underestimate the risk in less risky instruments. When the strategy is executed on a relative basis, i.e., buying the undervalued security and selling the overvalued one against it, this is a *carry trade*. The difference between yield received and yield paid is the *carry*.

*Quant Long Short (QLS)* ranks stocks by attractiveness based on various factors such as value, then buy the higher-ranked stocks while shorting the lower-ranked stocks.

**Definition 1.2.4. (*Growth*)** Make predictions based on asset's expected or historically observed level of economic growth. Forward-looking growth expectations are typically used as a metric.

Growth is trending, and strongest growers are becoming more dominant relative to competitors. Macro growth factors may be used on foreign exchange, while micro growth factors may be used on companies.

**Definition 1.2.5. (*Quality*)** All else being equal, it is better to long high quality and short low quality. Capital safety is important. Factors include earnings quality, equity-to-debt ratios etc.

Data-driven models are more difficult to understand, with more complicated mathematics. Relies on data mining, more technically challenging and far less widely practiced. Typically more used in high-frequency space, as they can discern how market behaves without caring about the economic theory or rational.

### 1.2.2 Strategy Implementation

An implementation approach requires a forecast target, time horizon, bet structure, investment universe, model specification, and run frequency.

*(Forecast Target)* Models may forecast direction, magnitude, duration of move, and may include probability into the forecast. Signal strength is of importance, defined by a larger expected return and/or higher likelihood of return. A higher level of signal strength results in a bigger bet taken on the position.

*(Time Horizon)* Models may have forecast horizons ranging from microseconds to years. There are more variability between short-term and long-term strategies, as short-term strategies are making very large number of trades compared to long-term strategies.

*(Bet Structure)* Models can be made to forecast an instrument relative in itself or to others. For relative forecasts, smaller clusters (pairs) or larger clusters (sectors) may be used. For pairs, few assets can be compared precisely and directly. Large cluster grouping may eliminate impact of general movement of the sector and hence focus on the relative movement of stocks within the sector, allowing for clearer distinction between group behaviour and idiosyncratic behaviour. Clusters may be created either via statistical methods or using heuristics (i.e., fundamentally defined industry groups).

Statistical methods may be fooled by data, leading to bad grouping. Heuristic grouping may be imprecise for conglomerates, and may be too rigid. Relative alpha strategies tend to exhibit smoother returns during normal times than intrinsic alpha strategies, but may face incorrect groupings during stressful periods. This may be mitigated by utilising several grouping techniques in concert.

*(Investment Universe)* Choices made on geography, asset class, instrument class, and exclusions. Generally, liquidity is preferred so estimations of transaction costs are reliable. Large quantities of high quality data is required, which is found in highly liquid and developed markets. Instruments with consistent behaviour is preferred, hence biotech stocks are excluded due to sudden, violent price changes. Hence, the most common asset classes and instruments modelled are common stocks, futures (on bonds and equity indices) and forex.

*(Model Specification)* Focuses on definition of the strategy mathematically, and may be the source of alpha. Specification details in terms of machine learning or data mining techniques are also defined, to assist in fitting models to the data and setting parameter values. Refitting frequency is also defined to refresh the model and make it adapt to current market conditions; may lead to greater risk of overfitting.

*(Run Frequency)* Run frequency of model is defined, from monthly to real time frequency. Increasing frequency of runs lead to greater number of transactions and hence higher transaction costs, and risk of moving portfolio based on noisy data. Less frequency of runs lead to smaller number of larger-sized trades, hence may move the market with block trades; may also miss opportunities to trade at more favourable prices.

### 1.2.3 Blending Models

The three most common approaches are linear models, nonlinear models, and machine learning models. If models are not combined, then several portfolios are constructed based on output from each model, then combined using portfolio construction techniques. The best method depends on the model.

Linear models require independence of factors, and each factor to be additive. To determine the weight of each alpha factor, multiple regression techniques may be used.

Nonlinear models are used when factors are not independent, or the relationship changes over time. Conditional models base the weight of one factor on the reading of another factor. Rotational models assign weights

of factors that fluctuate over time based on updated calculations of the various signal's weights, giving higher weights to factors with better performance recently.

Machine learning models applied to mixing alpha factors are more successful than the approach being used to forecast markets. For rotational models, many approaches to mixing alpha factors periodically update optimal weights based on the changing and growing dataset.

## 1.3 Risk Models

Risk model concerns the intentional selection and sizing of exposures to improve the quality and consistency of returns. By pursuing an alpha, we want to be invested in the movement of the exposure to profit in the long run.

### 1.3.1 Limiting Size of Risk

The quantitative risk models that limit the size of risk varies by the manner in which size is limited, how risk is measured, and what is having its size limited.

Size limits can be limited by hard constraints and penalties. A hard limit may be arbitrary, hence penalty functions may be built to allow a position to increase beyond the limit level, only if the alpha model expects a significantly larger return. The levels of limits and penalties may be determined from either theory or data.

To measure risk, there are two methodologies. The first is longitudinal, and measures risk through the volatility of an instrument. The second is to measure the correlation or covariance between assets (dispersion).

Size limiting may be applied to single positions and groups of positions (sectors, asset classes). It may also be applied to various types of risks and the amount of portfolio leverage.

### 1.3.2 Limiting the Types of Risk

To eliminate unintentional exposure as there is no expectation of being compensated sufficiently for accepting them. This can be achieved through theoretical or empirical risk models.

*(Theory-Driven Risk Models)* Focuses on systematic risk factors, derived from economic theory. Systematic risks cannot be diversified away. Equity may have market risk, sector risk, market capitalisation risk etc. Fixed income may have interest rate risk.

*(Empirical Risk Models)* Uses historical data to determine the unnamed systematic risks that should be measured and mitigated. Uses principal component analysis (PCA) to discern unnamed systematic risks that may correspond to named risk factors. Used by statistical arbitrage traders who are betting on exactly the component of an asset's return not explained by systematic risks.

## 1.4 Transaction Cost Models

Trade is made only if it increases the odds or magnitude of return (from alpha model), or if it decreases the odds or magnitudes of loss (from risk model). However, this improvement should be higher than cost of trading. The transaction cost model is not designed to minimise cost of trading, only to inform portfolio construction engine the cost of making any given trade.

### 1.4.1 Transaction Costs

Transaction costs have three major components: commissions and fees, slippage, market impact.

*(Commissions and Fees)* Paid to brokerages (access to other market participants), exchanges (improved transaction security) and regulators (operational infrastructure) for the services provided. The bank's infrastructure is used by quants, where the brokerage commissions are rather small on a per-trade basis. Brokers also collect clearing and settlement fees. Clearing is the activity involving regulatory reporting and monitoring, tax handling, and handling failure, taken place in advance of settlement. Settlement is the delivery of securities in exchange for payment in full.

*(Slippage)* The change in price between the time the quant system decides to transact and the time when the order is at the exchange for execution. Trend-following strategies suffer most from slippage as assets are already moving in desired direction; mean-reverting strategies suffer the least from slippage. The lower the latency to market, the smaller the slippage. The more volatile an asset, the bigger the slippage.

*(Market Impact)* Measures how much an order moves the market by its demand for liquidity. The impact of the trade on the market is unknown until the trade has already been completed. There may also be interaction between slippage and market impact (i.e., selling when a stock is trending upwards).

### 1.4.2 Types of Models

The four basic types of transaction cost models are flat, linear, piece-wise linear, and quadratic.

*(Flat Model)* Cost of trading is the same, regardless of size of order. Model is reasonable if size traded is nearly always about the same, and liquidity remains sufficiently constant.

*(Linear Model)* Cost of trading increases at a constant rate relative to size of order. Better estimate than flat transaction cost model.

*(Piece-Wise Linear Model)* Using piece-wise linear functions to model costs. Balance between simplicity and accuracy; better accuracy than flat or linear models.

*(Quadratic Model)* Most computationally intensive, but also most accurate.



## 1.5 Portfolio Construction Models

Comes in two major forms: rule-based, optimisers. Rule-based models are based on heuristics, can be exceedingly simple or rather complex, and derived from human experience (trial and error). Optimisers comprises of an objective function and uses algorithms to reach the end goal.

### 1.5.1 Rule-Based Models

Four approaches below are described from simplest to most complex.

*(Equal Position Weighting)* Used if portfolio manager believes that if a position is good enough to own, no other information is needed in determining its size. Strength of signal is not used as input in weighting. Model assumes that there is sufficient statistical strength and power to predict not only direction but also magnitude relative to other forecasts in the portfolio. Portfolio takes few large bets on 'best' forecast, many smaller bets on less dramatic forecasts; may take excess risk in a idiosyncratic event on a seemingly attractive position, resulting in adverse selection bias.

*(Equal Risk Weighting)* Adjust position sizes inversely to volatilities or a measure of risk. More volatile positions given smaller allocations, less volatile positions given larger allocations. When unit of risk is equalised, it is almost always a backward-looking measurement such as volatility. If volatility changes with time, then model will be misled.

*(Alpha-Driven Weighting)* Position size based primarily on alpha model. Alpha signal determines size of position, but usually with size limits. Constraints used also includes limits on size of total bet on a group. May also have a function that relates the magnitude of forecast to size of position. If model used in futures trend following, might suffer sharp drawdowns. Heavy reliance on accuracy of alpha.

*(Decision-Tree Weighting)* Decision path to arrive at the allocation for given instrument, depending on type of alpha model and type of instrument. Constraints may include percentage limits for allocation. Model size grows dramatically if more alpha models or more types of positions are included.

### 1.5.2 Optimisers

Harry Markowitz's mean variance optimisation (MVO) as the pioneer model. Models are based on principles of modern portfolio theory (MPT). Inputs include asset expected return (mean), asset variance, expected correlation matrix. Other inputs include size of portfolio in currency terms, desired risk level (volatility or expected drawdown), and other constraints such as liquidity, universe limits.

Model uses an objective function and an algorithm to seek the goal, usually maximising return of portfolio relative to volatility of portfolio returns.

*(Expected Return)* Alpha models as basis of expected return, which also includes expected direction.

*(Expected Volatility)* Stochastic volatility forecasting methods is commonly used, as volatility may have high and low periods, with occasional jumps. Generalised Autoregressive Conditional Heteroskedasticity (GARCH) is most used.

*(Expected Correlation)* As instrument correlations are not stable over time, it is more appropriate to group assets together before computing correlation within the group.

Optimisation techniques includes the following.

*(Unconstrained Optimisation)* Most basic form with no constraints. Might provide a single-instrument portfolio, where all money will be invested in instrument with highest risk-adjusted return.

*(Constrained optimisation)* Constraints include position limits, limits on various groupings of instruments. Might result in constraints driving the portfolio construction more than the optimiser.

*(Black-Litterman Optimisation)* Blends investor expectations with a degree of confidence about those expectations, and these with historical precedent evident in the data. Adjusts historically observed correlation levels by utilising investor's forecast of return for the various instruments.

*(Grinold and Kahn's Approach)* Builds a portfolio of signals, instead of sizing positions. To build factor portfolios, each of which are usually rule-based portfolios based on a single type of alpha forecast. Each portfolio backtested, then the series of returns are then treated as instruments of a portfolio by the optimiser. Number of factor portfolios is more manageable, usually not more than 20. What is optimised is then a handful of factor portfolios. The model allows for inclusion of risk model, transaction cost model, portfolio size, and risk targets as inputs.

*(Resampled Efficiency)* To improve the inputs to optimisation by addressing oversensitivity to estimation error. To resample data using Monte Carlo simulation to reduce estimation error in inputs to the optimiser.

*(Data-Mining Approaches)* Machine learning techniques such as supervised learning or genetic algorithms used, as MVO involves searching many possible portfolios to find the best.

## 1.6 Execution Model

Two basic ways to execute trade: through electronic, or through human intermediary. For electronic execution, achieved through direct market access (DMA), which allows traders to utilise the infrastructure and exchange connectivity of brokerage firms to trade directly on electronic markets.

Execution algorithms can be acquired through building, using broker's, or a third-party software vendors.

Brokerages offer portfolio bidding, where the 'blind' portfolio for transaction is described by characteristics such as valuation ratios of longs and shorts, sector breakdown, market capitalisation etc. Broker then quote a fee in basis points in terms of the gross market value of portfolio traded. Hence, certainty is provided by the broker to the trader. Once agreement reached, broker receives fee and assumes risk of trading out the portfolio at future market prices, which may be better or worse than prices guaranteed.

### 1.6.1 Order Execution Algorithms

Algorithm determine the way in which systematic execution of portfolio is done. Goal is to minimise cost of trading into and out of portfolio.

*(Aggressive vs Passive)* Algorithm make decision of passive vs aggressive order, depending on how immediately the trader wants to do the trade. Market orders are considered aggressive. Limit order at current best order is fairly aggressive, while limit order below current bid is passive.

Many exchanges pay providers of liquidity for placing passive orders, while charging traders for using liquidity provided. Orders that cross the spread are using liquidity by using a passive order placed by another trader, reducing liquidity available. Paying for liquidity sweetens the deal for passive order, only if order is actually executed; passive trader gets better transaction price and a commission rebate from the exchange.

Momentum strategies uses more aggressive orders; mean reversion uses more passive orders. A stronger, more certain signal will be executed with greater aggressiveness than a weaker or less certain signal. A middle ground will be to put limit orders between best current bid and offer.

*(Large vs Small Order)* A large order may be broken into many smaller orders over a window of time, but risk price moving in adverse direction. Size of chunk depends on transaction cost model estimate, and analysis of correct level of aggressiveness.

*(Hidden vs Visible Order)* A queue as a visible order gives away a bit of information. Hidden order will provide no information to the market, staving off imbalances, but reduces priority of trade in the queue. Algorithmic trading utilising hidden order is 'iceberging', which is taking a single larger order and chopping it into many smaller chunks, most posted to order book as hidden orders.

*(Order Routing)* If there are several pools of liquidity for the same instrument, smart order routing will be used, which determines which pool of liquidity is most suitable for sending a given order. Depth of liquidity on various ECNs and connectivity speeds are also considered in smart order routing.

*(Cancelling and Replacing Orders)* Traders may place larger number of orders with no intention of execution, then rapidly cancelling them and replacing them with other orders. This allows gaining of information on how market responds to the changing depth of the book, providing information on how to profit from the pattern of reaction. If trader wants to buy a large number of shares, he may enter a large number of small orders to sell the shares further away from market and cancel, improving market perception of the overall balance.

### 1.6.2 High Frequency Trading

Alpha driving strategies on extremely near-term bets (seconds or less) are *microstructure alphas*, focusing on liquidity patterns in order book. Larger quants may also use this to guide execution models, improving costs of entering trades. Small differences over a single trade add up significantly in the long run. To trade microstructure alpha as independent high frequency strategies, large investments in infrastructure and research must be done.

A shark strategy is designed to detect large orders that are iceberged, by sending series of very small trades; if each of these small orders get filled quickly, this may be a sign of a large and iceberged order. The shark simply front-run this large, hidden order by placing visible trades in front of the iceberged order. The iceberg strategy must then push prices up to execute trades. When the iceberged order is complete, prices will be pushed up favourably for the shark, which can then exit the position with a quick and relatively riskless profit.

Machine learning techniques may also be used to discern patterns in execution of other player orders. The more inferior the execution models, the easier it is to discern the pattern, allowing the ML strategy to profit from these patterns in the future. Patterns in the shorter timescale are somewhat stable as they are driven by computer algorithms.

### **1.6.3 Trading Infrastructure**

Using a broker that act as trading agent allows the infrastructure requirements to be handled by the broker, instead of dealing with the regulatory and other constraints.

High frequency strategies may use colocation or sponsored access. Colocation setup is where trader attempts to place trading servers as physically close to the exchange as possible.

Financial Information eXchange (FIX) protocol is the choice of real-time electronic communication among users. The software that implements the FIX protocol is free and open source (FIX engine). High frequency traders will likely build their own FIX engines to ensure optimal speeds.

## 1.7 Data Requirements

Upon data reaching the servers, it is processed using data feed handlers.

Price data includes information retrieved or derived from exchanges or transactions. This includes trading volume of stocks, the order book, data derived from levels of various indices etc.

Fundamental data includes financial health, financial performance, financial worth and sentiment. These may be microeconomic or macroeconomic in nature, depending on the nature of asset. A more advanced source of data includes text data requiring Large Language Models to parse, as well as alternative sources of data such as GPS, satellite images etc.

Some examples of primary sources and data types includes:

- i. *Exchanges*: Prices, volumes, timestamps, open interest, short interest, order book data
- ii. *Regulators*: Company financial statements, filings
- iii. *Governments*: Macroeconomic data such as employment, inflation, GDP
- iv. *Corporations*: Announcement of financial results, corporate actions
- v. *News Agencies*: Press releases or news articles
- vi. *Proprietary Data Vendors*: Investment flow data, company reports etc.

On issues regarding missing data, the database and trading systems are required to recognise the difference between zero and blank to prevent estimation errors. Incorrect values can be reduced via ensuring data consistency of units; this can be also detected via spike filters (detects abnormally large, sudden movement in prices). To fix issues regarding corporate actions such as splits and dividends, the price history must be adjusted. For issues from incorrect timestamps, the data timestamp should be tracked against internal timestamps. Macroeconomic and financial earnings data may also produce look-ahead bias, where the data is released data later date, but recorded as a revised data in the past, hence data release date should be tracked.

## 1.8 Research

The scientific method is as follows:

1. Researcher observe a phenomenon in the market and construct a theory.
2. Researcher seeks out information to test the theory.
3. Researcher tests the theory, and with enough confidence, risk some capital on the validity of the theory.

Idea generation comes from four sources:

1. Observing the market, using the scientific method to test the theory
2. Academic literature, requiring significant time to read academic journals, working papers, and conference presentations for ideas. Literature from other fields such as astronomy, physics, or psychology, may provide ideas relevant to quant finance problems.
3. Migration of a researcher or portfolio manager from one quant shop to another.
4. Lessons from activities of discretionary traders

### 1.8.1 Model Testing

*(In-Sample Training)* Train a model by finding optimal parameters over an in-sample period. The sample for fitting the model must be chosen in terms of appropriate length and breadth.

*(Model Quality)* A model can be assessed on the following fronts:

- i. Cumulative profit graph: if profit profile is not smooth, with long periods of inactivity, sharp losses and gains, then the model may have issues
- ii. Average annual rate of return: indicates how well the strategy made on historical data
- iii. Variability of returns: the less variable the level of returns, the better the strategy. May look at lumpiness of returns, which is the portion of strategy's total returns that comes from periods that are significantly above average (measures consistency of returns).
- iv. Worse Peak-to-Valley Drawdowns: measures maximum decline from any cumulative peak in profit curve. The lower the drawdown the better the strategy. Also, to measure recovery period after drawdowns; the shorter the recovery period the better the strategy.
- v. Predictive Power: R-squared statistic may be used, which shows how much of the variability of the predicted asset have been accounted for. A exceedingly high  $R^2$  in would be 0.05 out of sample. Instrument returns may be bucketed by deciles; a model with reliable predictive power is one that appropriately buckets the instruments correctly.
- vi. Percentage Winning Trades, Winning Time Periods: whether the strategy tends to make profits from a small portion of trades that do very well, or from a large number of trades.
- vii. Ratios of Returns vs Risk: Statistics such as risk-adjusted return, Sharpe ratio, information ratio, Sterling ratio, Calmer ratio, Omega ratio.
- viii. Relationship with Other Strategies: value-add of new strategy compared with results of existing strategy with and without the new idea.
- ix. Time decay: understand strategy returns if trades are initiated on lagged basis after receiving a trading signal. Determine strategy sensitivity to timeliness with information received, and crowdedness of strategy.
- x. Sensitivity to specific parameters: high quality strategy has small changes in outcomes from slight changes in parameters. Or else this may be a sign that model may be overfitted.
- xi. Overfitting: plot a graph of parameter value vs function outcome; a good model has a flatter curve with no jumps. Models that are parsimonious (less parameters) uses less assumptions, hence less overfitting.

*(Out-of-Sample Testing)* Tests if model works in real-life.  $R^2$  is typically used to test robustness of model. If out-of-sample  $R^2$  is close to in-sample  $R^2$ , then the strategy is good. Rolling out-of-sample technique may be used to refresh the model over time. Look-ahead bias may be avoided by separating strategy research function from strategy selection function, and withholding a significant portion of database from researchers.

*(Assumptions of Trading)* Overestimation of trading costs may cause portfolio to hold positions for longer than optimal, and underestimation may result in high portfolio turnover and bleed from trading costs. Assumptions on availability of short positions must also be made; hard-to-borrow lists must be taken into consideration.

## 1.9 Quantitative Model Risks

### 1.9.1 Model Risk

Quant models has model risk, the risk that the model does not accurately describe, match, or predict the real-world phenomenon. Each component of the quant model may all have model risk.

*(Inapplicability of Modelling)* Occurs when quant model is mistakenly applied to a problem. May also occur with misapplication of a technique to a given problem.

*(Model Misspecification)* Occurs when the model doesn't fit the real world. Model may work fine most of the time, but fail when an extreme event occurs.

*(Implementation Errors)* Errors in programming or architecting systems. Architectural error may also occur when models are loaded in a wrong sequence.

### 1.9.2 Regime Change Risk

Quant models are based on relationships prevalent in historical data. If there is a regime change, the historical relationships and behaviour may be altered, hence the model may lose effectiveness.

### 1.9.3 Exogenous Shock Risk

Risks driven by information that is not internal to the market, i.e., terrorist attacks, start of wars, bank bailouts, change in regulation such as in shorting rules. May require discretionary overrides.

### 1.9.4 Contagion Risk

Happens when other investors hold the same strategies. First part of risk factor relates to how crowded the quant strategy is. Second part relates to what else is held by other investors that could force them to exit the quant strategy in a panic (ATM effect).

Quant liquidation crisis may be driven by size and popularity of quantitative strategies, subpar returns from operators leading up to the crisis, the practice of funds cross-collateralising many strategies against each other, and risk targeting (risk managers target a specific level of volatility for their funds or strategies).

### 1.9.5 Risk Monitoring

*(Exposure Monitoring Tools)* With current positions held, the positions are grouped for the various exposures (i.e., valuation, momentum level, volatility) to monitor gross and net exposure to various sectors and industries, buckets of market capitalisation, various style factors.

*(Profit and Loss Monitors)* With current portfolio, compare that with previous day closing price. Intraday performance charts are used. May also look at source of profit, hit rate (percentage of time strategy makes money on a given position).

*(Execution Monitors)* Shows progress of executions, i.e., which orders are currently being worked on, which ones are completed, with transaction size and prices. Fill rates for limit orders are used for more passive execution strategies. Slippage and market impact are also monitored.

*(System Performance Monitors)* Checks for software and infrastructure errors. Checks performance of CPUs, speeds of various stages of automated processes, latency in communication of messages to and from exchanges.

## 1.10 Model Evaluation

An evaluator's goal is to understand the strategy (risks, sources of returns), and to judge the fund manager.

Questions that may be asked to evaluate a fund manager's strategy is:

1. Research and strategy development: how new ideas are conceived; how the ideas are tested; what criteria the manager looks for in determining whether a strategy works or not
2. Data sourcing, gathering, cleaning, and management: what data is used; how is the data stored and why that way; how data is cleaned
3. Investment selection and structuring: are the alpha models theory-driven or data-driven; what alpha strategies are used (i.e., trend, reversion, value/yield, growth, or quality); are the bets relative or individual; if bets are relative, what does relative mean exactly; over what time horizon and in what investment universe; how the various alpha models are mixed
4. Portfolio construction: how portfolio construction is performed; what the limits and why is it set that way; what are the inputs to portfolio construction; what is the objective function or goal
5. Execution: what kind of transaction model is used, and why is it chosen; how are the trades executed (manually or algorithmically); are the order execution algorithms hidden or visible, active or passive
6. Risk management and monitoring: what does the risk model account for, and why these things; what are the various risk limits, and why are these set that way; under what circumstances will there be a need to intervene with the model; what is being monitored on an ongoing basis

Types of edge a portfolio manager may have is as follows:

- i. Investment process edge: the quality of processes, of people (how adversity is dealt with)
- ii. Data edge: proprietary access to some sort of data, through superior data gathering, cleaning, storage
- iii. Lack-of-competition edge: not long lasting. More competitive means more cyclical trading space.
- iv. Structural edge: market structure related, caused and removed by regulation

Also, to check the ethics and integrity of fund managers. This may be done via background checks, education verifications, reference checks.

To see how a quant manager fits with rest of portfolio, the key is to build a diversified portfolio that considers three important elements:

- i. Various types of alpha exposures
- ii. Various bet structures
- iii. Various time horizons



## 2 Equities Trading

### 3 Fixed Income Trading

## 4 Derivatives Trading

Based on the classic by John C. Hull [2021]

### 4.1 Fundamentals of the Market

The derivatives market is much larger than the stock market in terms of underlying assets. Derivatives may be used for hedging, speculation, or arbitrage; and also transfer a wide range of risks from one entity to another.

**Definition 4.1.1.** A *derivative* involves two parties agreeing to a future transaction, with value depending on the values of other underlying variables.

A derivatives exchange is a market where individuals and companies trade standardised contracts as defined by the exchange. Once two traders have agreed to trade a product offered by the exchange, it is handled by the exchange clearing house, which takes care of the credit risk by requiring each trade to deposit margin.

If the trade is taken over-the-counter (OTC), participants may present it to a central counterparty (CCP) or clear the trade bilaterally. With the 2008 financial crisis, OTC market is forced to become more like the exchange-traded market, with changes as follows:

- i. Standardised OTC derivatives between two financial institutions in US must, whenever possible, be traded on a swap execution facility (SEF), where market participants can post bid and ask quotes, and can trade by accepting the quotes of other market participants.
- ii. Require that a CCP be used for most standardised derivatives transactions between financial institutions.
- iii. All trades must be reported to a central repository.

#### 4.1.1 Forward, Futures, and Options

**Definition 4.1.2.** A *spot contract* is an agreement to buy or sell an asset almost immediately. A *forward contract* is an agreement to buy or sell an asset at a certain future time for a certain price.

Let  $S_T$  be the spot price of asset at maturity,  $K$  is delivery price.

The payoff from a long position in a forward contract is  $S_T - K$ .

The payoff from a short position in a forward contract is  $K - S_T$ .

Futures contract are traded on an exchange, unlike forwards which are traded OTC. Majority of futures contract do not lead to delivery, as positions are closed prior to delivery period by entering an opposite trade to the original one.

Party in short position may file notice of intention to deliver with the exchange when they are ready to deliver. If the asset is a commodity, the grade of commodity are specified. The contract size specifies the amount of asset that has to be delivered. The place for delivery must also be specified, as commodities may involve significant transportation costs. The delivery month of the commodity may also be specified, and are chosen by the exchange to meet the needs of market participants. Trading typically ceases a few days before the last day on which delivery can be made. Daily price movement limits are also specified by exchange to prevent speculative excess causing large price movements; in this case trading ceases for the day.

As the delivery price for a futures contract is approached, the futures price converges to the spot price of the underlying asset.

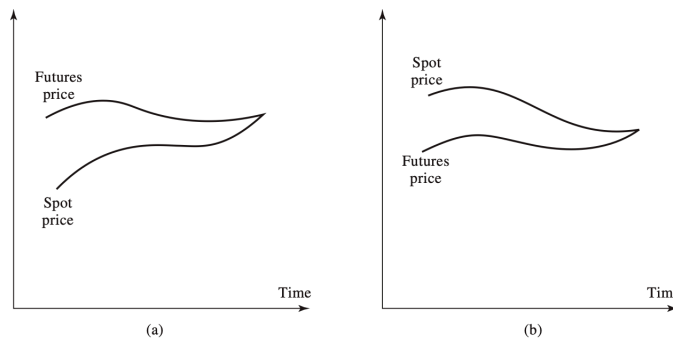


Figure 2: Convergence of futures price to spot price.

Suppose futures price is above spot price during delivery period. Traders have clear arbitrage opportunity: short futures, long asset, make delivery. The futures price will then fall. If futures price is below spot price during delivery period, traders will long futures, wait for delivery, and the futures price will then rise.

Options are traded both on exchanges and OTC.

**Definition 4.1.3.** A *call option* (*put option*) gives the holder the right to sell (buy) the underlying asset by a certain date for a certain price.

**Definition 4.1.4.** An *American option* can be exercised at any time up to expiration date. An *European option* can only be exercised on expiration date itself.

#### 4.1.2 Clearing House

Margin accounts are used by exchanges to organise trading so that contract defaults are avoided. Trader has to keep funds in a margin account; the amount to be deposited at the time the contract is entered into is the *initial margin*. At each of trading day, margin account is adjusted to reflect trader's P&L (*daily settlement, marking to market*). Daily settlement leads to funds flowing daily between traders with long positions and traders with short positions; this daily flow of funds to reflect P&L is the *variation margin*. Trading via brokers requires a *maintenance margin*, which is lower than initial margin; if balance in margin account falls below maintenance margin, trader receives *margin call* and is required to top up to initial margin level within short period of time, or else broker closes out the position. Trader is also entitled to withdraw any balance in margin account that is in excess of the initial margin. Brokers pay interest on balance in margin account. A forward contract is settled at end of life, while futures contract is settled daily. Minimum levels for initial and maintenance margins are set by exchange clearing house. Minimum margin levels are determined by variability of the price of underlying asset, revised when necessary.

The clearing house acts as intermediary in futures transactions, and keep track of all daily transactions for calculating net positions of each of its members. Members must provide initial margin reflecting the total number of contracts cleared. The maintenance margin is set equal to initial margin. In determining margin requirements, the number of contracts outstanding is calculated on a net basis rather than a gross basis. Members are required to contribute to a guaranty fund, which is used in the event that a member defaults, and the member's margin is insufficient to cover losses.

#### 4.1.3 OTC Markets

OTC markets use central counterparties (CCPs), which perform the same role as exchange clearing houses. Members of CCP provide both initial margin and daily variation margin, and contribute to a guaranty fund. If an OTC derivative transaction has been agreed upon between parties A and B, and CCP accepts the transaction, they become the counterparty to both A and B. CCP hence takes on credit risk of both A and B. Transactions are valued daily, and there are daily variation margin payments between members.

For bilaterally cleared OTC, two companies enter a master agreement covering all their trades (ISDA). The agreement includes a credit support annex (CSA), requiring both parties to provide collateral. Collateral agreements in CSAs usually require transactions to be valued daily. Since 2016, regulations require both initial margin and variation margin between financial institutions.

## 4.2 Forwards and Futures

### 4.2.1 Hedging with Futures

The fundamentals of hedging with futures are *hedge-and-forget* strategies, where no changes is made to adjust the hedge once it has been put in place.

**Definition 4.2.1.** (*Basic Principles of Futures Hedging*)

The objective is to take a position that neutralises the risk as far as possible.

- i. *Short Hedge*: short position on futures.  
Used when hedger already owns an asset and will sell the asset at some time in the future; or when asset is not owned right now but will be owned and ready for sale sometime in the future.
- ii. *Long Hedge*: long position on futures.  
Used when hedger will purchase an asset in the future and wants to lock in the price now.

	Short Hedge	Long Hedge
May 15	Spot: 50 Futures: 49	Spot: 50 Futures: 49
August 15 Scenario 1	Spot: 45 Gain from hedge: 4	Spot: 45 Loss from hedge: 4
August 15 Scenario 2	Spot: 55 Loss from hedge: 6	Spot: 55 Gain from hedge: 6

In practice, hedging is not perfect due to factors as follows:

1. Asset being hedged is not exactly the same as the asset underlying the futures contract.
2. Uncertainty as to exact date in which the asset will be bought or sold.
3. Hedge may require the futures contract to be closed out before its delivery month.

These lead to *basis risk*.

**Definition 4.2.2.** The *basis* in a hedging situation is defined as

$$\text{Basis} = \text{Spot Price} - \text{Futures Price}$$

An increase/decrease in basis is a strengthening/weakening of the basis.

**Definition 4.2.3.** Let  $S_i$  be spot price at time  $t_i$ ,  $F_i$  be futures price at time  $t_i$ ,  $b_i$  be basis price at time  $t_i$ . Assume hedge is placed at time  $t_1$ , closed at time  $t_2$ . Price realised for asset is  $S_2$ , profit from futures position is  $F_1 - F_2$ . Effective price obtained for asset hedging is therefore  $S_2 + F_1 - F_2 = F_1 + b_2$ . If  $b_2$  is known, perfect hedge will result. The *basis risk* is the hedging risk from uncertainty associated with  $b_2$ .

**Definition 4.2.4.** *Cross Hedging* occurs when the asset underlying the futures contract is not the same as the asset whose price is being hedged.

Cross hedging is often used when futures of the original asset being hedged are not actively traded on the market, and the hedger seeks an alternative asset to hedge the original asset.

**Definition 4.2.5.** *Hedge Ratio* is the ratio of size of position taken in futures contract to the size of exposure.

Assuming no daily settlement of futures contracts, hedger seeks a hedge ratio that minimises variance of hedged position value. Let  $\Delta S$  be change in spot price,  $\Delta F$  change in futures price. Assuming linear relationship,

$$\Delta S = a + b\Delta F + \epsilon$$

where  $a, b$  are constants,  $\epsilon$  is an error term. Suppose hedge ratio is  $h$ . Change in value of position per unit of exposure to  $S$  is:

$$\Delta S - h\Delta F = a + (b - h)\Delta F + \epsilon$$

Standard deviation is minimised by setting  $h = b$ . Let minimum variance hedge ratio be  $h^*$ . Then

$$h^* = \rho \frac{\sigma_S}{\sigma_F}$$

where  $\sigma_S, \sigma_F$  is standard deviation of  $\Delta S, \Delta F$  respectively,  $\rho$  is coefficient of correlation.

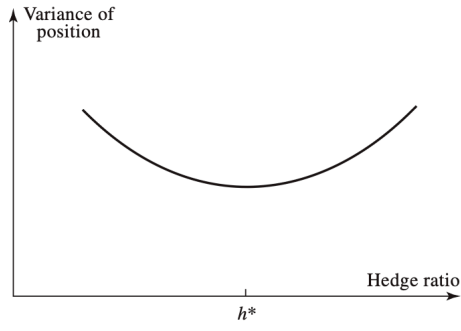


Figure 3: Dependence of variance of position on hedge ratio.

*Hedge effectiveness* is the proportion of variance eliminated by hedging. This is  $R^2$  from regression of  $\Delta S$  against  $\Delta F$ , and equals  $\rho^2$ . Parameters  $\rho$ ,  $\sigma_S$ ,  $\sigma_F$  are estimated from historical data on  $\Delta S$  and  $\Delta F$ .

The optimal number of futures to be used in hedging is

$$N^* = \frac{h^* Q_A}{Q_F}$$

where  $Q_A$  is size of portion being hedged (units),  $Q_F$  is size of one futures contract (units). The futures contract should be on  $h^* Q_A$  units of the asset.

## 5 Currency Trading

## 6 Commodities Trading



## References

John C. Hull. *Options, Futures, and Other Derivatives*. Pearson, 2021.

Rishi K. Narang. *Inside the Black Box: The Simple Truth About Quantitative Trading*. Wiley Finance Series. Wiley, 2013.