

Project 2

Use Chebyshev spectral method to solve the following Burgers' equation:

$$\begin{aligned}\frac{\partial u}{\partial t} + \frac{\partial}{\partial x} \left(\frac{u^2}{2} \right) &= 0.02 \frac{\partial^2 u}{\partial x^2}, \\ u(-1, t) &= 1, \quad u(1, t) = -1, \\ u(x, 0) &= u_0(x),\end{aligned}$$

where

$$u_0(x) = -\sin\left(\frac{5}{2}\pi x\right).$$

Present the numerical solutions at $t = 0.3k$ for $k = 0, 1, \dots$ until the solution no longer changes (this problem has a “steady state”).

Submit the following to Canvas when finishing your project:

- The source code;
- A simple report including a description of the numerical method and the figures showing the numerical results.

Please complete your submission no later than 23 April, 2023.