Handed out: 2 Oct 2019 Due: 13 Nov 2019 (start of lecture)

In this project, you will implement the hidden Markov model's Viterbi algorithm and forward-backward algorithm, and apply them both to Twitter tweets and intraday stock prices. Email your submission to Lim Suang (e0319343@u.nus.edu; prefix your email's subject with [BT3102 Project]). Make sure to answer all the questions, and to attach your code, generated files, and answers.

Question 1. Group Formation (5 points)

This project is to be done in a group of three. Form your group and email Lim Suang with your group members' names by 9 Oct 2019.

1 POS Tagging of Tweets

Twitter (www.twitter.com) is a popular microblogging site that contains a large amount of user-generated posts, each called a tweet. By analyzing the sentiment embedded in tweets, we gain precious insights into commercial interests such as the popularity of a brand or the general belief in the viability of a stock¹. (Many companies earn revenue from providing such tweet sentiment analysis.) In such sentiment analysis, a typical upstream step is the part-of-speech (POS) tagging of tweets, which generates POS tags that are essential for other natural language processing steps downstream.

You are required to build a POS tagging system using the hidden Markov model (HMM). (Please implement your code generically so that it can be easily reused for the next task on intraday stock prices. It would be a really bad (time-consuming, gut-wrenching) idea to implement another HMM for the next task. The files you require are:

- (i) twitter_train.txt,
- (ii) twitter_train_no_tag.txt,
- (iii) twitter_dev_no_tag.txt,
- (iv) twitter_dev_ans.txt,
- (v) twitter_tags.txt, and
- (vi) hmm.py.

twitter_train.txt is a labelled training set. Each non-empty line of the labeled data contains one token and its associated POS tag separated by a tab. An empty line separates sentences (tweets). Below is an example with two tweets (there is an empty line after "??,").

 $^{^{1}}$ https://ieeexplore.ieee.org/document/8455771

```
rt ~
@USER_123d5421 @
I O
like V
IPhones N
@USER_2346f3f51 @
wat O
wearin V
4 P
the D
party N
??,
```

Both twitter_dev_no_tag.txt and twitter_dev_ans.txt have the same format as twitter_train.txt, except that the former does not contain tags and the latter does not contain tokens. twitter_dev_ans.txt contains the tags of the corresponding tokens in twitter_dev_no_tag.txt. Both files are used to evaluate your code. (We will evaluate your code with more data from the same domain.) twitter_train_no_tag.txt contains the same data as twitter_train.txt, but without any tags. twitter_train*.txt and twitter_dev*.txt contain 1101 and 99 tweets respectively.

twitter_tags.txt contains the full set of 25 possible tags. hmm.py contains skeleton code, and you have to write your code in this file.

Recall that the joint likelihood of the observed data x_1, x_2, \ldots, x_n and its associated tags y_1, y_2, \ldots, y_n is given by an HMM as:

$$P(x_1, x_2, \dots, x_n, y_1, y_2, \dots, y_n) = \prod_{t=0}^{n+1} a_{y_t, y_{t+1}} \prod_{t=1}^n b_{y_t}(x_t)$$

where y_0 and y_{n+1} are the START (*) and STOP states respectively, $a_{i,j} = P(y_t = j | y_{t-1} = i)$ is the transition probability, and $b_j(w) = P(x_t = w | y_t = j)$ is the output probability.

Question 2. Naive Approach (5 points)

(a) Write a function to estimate the output probabilities from the training data twitter_train.txt using maximum likelihood estimation (MLE), i.e.,

$$P(x = w | y = j) = b_j(w) = \frac{count(y = j \to x = w)}{count(y = j)}$$

where the numerator is the number of times token w is associated with tag j in the training data, and the denominator is the number of times tag j appears. Save these output probabilities into a file named naive_output_probs.txt.

A problem you may encounter is that the training data twitter_train.txt does not contain some tokens (words) that appear in the test data. You can handle this "unseen token" problem by smoothing the output probability as

$$b_j(w) = \frac{count(y = j \to x = w) + \delta}{count(y = j) + \delta \times (num_words + 1)},$$

where num_words is the number of unique words in the training data, δ is a real number, and the +1 in the denominator accounts for unseen tokens (all unseen tokens "collapse" into a single token). Typical values of δ to try are: 0.01, 0.1, 1, 10. Pick one that works best for you. (This smoothing applies to the other questions too.)

(b) Using these output probabilities, we can naively obtain the best tag j^* for a given token w with the following equation.

$$j^* = \underset{j}{\operatorname{argmax}} b_j(w) = \underset{j}{\operatorname{argmax}} P(x = w | y = j)$$

Write a function naive_predict() (see hmm.py) that uses the output probabilities in naive_output_probs.txt to predict the tags of the tweets in twitter_dev_no_tags.txt with this naive approach. Write your predictions into a file named naive_predictions.txt in the same format as twitter_dev_ans.txt.

(c) What is the accuracy of your predictions (number of correctly predicted tags / number of predictions)? (Use the evaluate function in hmm.py.)

(Remember to submit your output files naive_output_probs.txt and naive_predictions.txt.)

Question 3. Better But Still Naive Approach (5 points)

A better approach is to estimate j^* using

$$j^* = \operatorname*{argmax}_{j} P(y = j | x = w).$$

- (a) How do you compute the right-hand side of this equation?
- (b) Implement this approach in a method naive_predict2() (see hmm.py) that uses the output probabilities in naive_output_probs.txt to predict the tags of the tweets in twitter_dev_no_tags.txt. You can also make use of other information in twitter_train.txt. Write your predictions into a file named naive_predictions2.txt in the same format as twitter_dev_ans.txt.
- (c) What is the accuracy of your predictions? (Use the evaluate function in hmm.py.)

(Please remember to submit naive_predictions2.txt.)

Question 4. Viterbi algorithm (20 points)

(a) Write a function to compute the output probabilities and transition probabilities from the training data twitter_train.txt using the MLE approach, saving the output probabilities to output_probs.txt, and the transition probabilities to trans_probs.txt. (You may reuse the function you have defined earlier to compute the output probabilities.) Recall that the transition probability is defined as

$$a_{i,j} = P(y_t = j | y_{t-1} = i) = \frac{count(y_{t-1} = i, y_t = j)}{count(y_{t-1} = i)},$$

where $count(y_{t-1} = i, y_t = j)$ is the number of times tag i transitions to tag j in the training data, and $count(y_{t-1} = i)$ is the number of times tag i appears in the training data. You may wish to "smooth" the transition probability in a similar manner as for the output probability.

(b) Write a function viterbi_predict that implements the Viterbi algorithm. This function uses the output probabilities and transition probabilities (stored in output_probs.txt and trans_probs.txt respectively) to predict the tags for tweets in twitter_dev_no_tag.txt, and writes the predictions to viterbi_predictions.txt. This function also accepts twitter_tags.txt so that it knows the full set of tags. Recall that the Viterbi algorithm computes the best tag sequence $y_1^*, y_2^*, \ldots, y_n^*$ for an observed token sequence x_1, x_2, \ldots, x_n in this manner:

$$y_1^*, y_2^*, \dots, y_n^* = \underset{y_1, y_2, \dots, y_n}{\operatorname{argmax}} P(x_1, x_2, \dots, x_n, y_1, y_2, \dots, y_n).$$

(c) What is the accuracy of your Viterbi algorithm on twitter_dev_no_tag.txt? (Use the evaluate function in hmm.py.)

(Remember to submit output_probs.txt, trans_probs.txt and viterbi_predictions.txt.)

Question 5. Improvements (10 points)

- (a) How can you improve your POS tagger further? Describe your ideas to improve your system. You are not allowed to use any external resources or packages, and must design your new POS tagger within the framework of HMMs. However, you are free to perform any automatic (i.e., not manual) preprocessing of the data. Hints: Could you better handle unseen words? Could you better model transition probabilities? Could you take advantage of linguistic patterns present in tweets? Could the words be clustered into meaningful groups?
- (b) Write a function viterbi_predict2 that implements your improved system. This function takes the same input as viterbi_predict. If your changes affect the output probabilities and transition probabilities, write those new probabilities into output_probs2.txt and trans_probs2.txt respectively. If those probabilities are not affected, simply copy your previous files to output_probs2.txt and trans_probs2.txt. Write your predictions to viterbi_predictions2.txt
- (c) What is the accuracy of your improved system? (Use the evaluate function in hmm.py.)

(Remember to submit output_probs2.txt, trans_probs2.txt and viterbi_predictions2.txt.)

Question 6. Forward-Backward Algorithm (20 points)

Till now, we have assumed that the tags are provided in the training data. However, in reality, tags are not available in tweets. We have learned that the forward-backward algorithm can be used to learn the transition and output probabilities when tags are not provided in the training data.

(a) Write a function forward_backward to implement the forward-backward algorithm. This function accepts twitter_train_no_tag.txt as training data. It also accepts twitter_tags.txt. Because the forward-backward algorithm is an iterative algorithm, this function accepts a max_iter to control the maximum number of iterations that can be executed. Recall that with each iteration of the algorithm, it updates its output probabilities and transition probabilities so as to increase the likelihood of the observed data, i.e., $\prod_{k=1}^{N} P(x_1^{(k)}, x_2^{(k)}, \dots, x_n^{(k)})$ where N is the number of training examples. Hence another way to terminate the algorithm is when the fractional change of the (log)likelihoods between consecutive iterations falls below some threshold. Thus, this function accepts such a threshold thresh to determine when

the iterations can be terminated. This function also accepts a seed so that you can replicate the initial random initialization of your output probabilities and transition probabilities. Because the performance of the forward-backward algorithm is highly dependent on the initialization of the output probabilities and transition probabilities, and it may take a long time to converge, you are only required to run the algorithm for 10 iterations (i.e., $max_iter=10$; you could set thresh to a small value such as 10^{-4} .)

If you find that your implementation contains multiply nested for-loops, think carefully how you could reduce the level of nesting to speed up your code. A little thought could save you an immense amount of time. Also note that it is not a good idea to initialize the output probabilities and transition probabilities as uniform distributions.

- (b) Save your output probabilities and transition probabilities right after initialization in output_probs3.txt and trans_probs3.txt, and use these to run your improved POS tagging system viterbi_predict2 on twitter_dev_no_tag.txt. Save the predicted tags in fb_predictions3.txt. What is the accuracy? (Use the evaluate function in hmm.py.)
- (c) Save your output probabilities and transition probabilities right after 10 iterations in output_probs4.txt and trans_probs4.txt, and use these to run your improved POS tagging system viterbi_predict2 on twitter_dev_no_tag.txt. Save the predicted tags in fb_predictions4.txt. What is the accuracy? (Do not be too alarmed if the accuracy did not improve. Note that you have only run the algorithm for a measly 10 iterations and for a single random initialization. We will test the forward-backward more thoroughly in the next application.)
- (d) Write the log-likelihoods of the observed data for each of the 10 iterations. What do you observe about the log-likelihoods?

(Remember to submit output_probs3.txt, trans_probs3.txt, viterbi_predictions3.txt, output_probs4.txt, trans_probs4.txt and viterbi_predictions4.txt.)

2 Modeling and Prediction of Intraday Stock Price Movements

Intraday stock price analysis refer to the study of how stock prices change within a day of trading. The short-term intraday behavior of a stock differs greatly from its long-term interday behavior. Accurately modeling intraday behavior is an important task in high-frequency trading (HFT)² because it confers HFT traders an advantage in forecasting stock movements.

You will reuse the HMM you have developed for tweet POS tagging for modeling intraday trades and predicting stock price movements. (In BT4013, we will learn more sophisticated Bayesian networks for modeling intraday trades.)

The relevant files are:

- (i) cat_price_changes_train.txt
- $(ii) \ {\tt cat_price_changes_dev.txt}$
- (iii) cat_price_changes_dev_ans.txt
- (iv) cat_states.txt
- (v) hmm.py

²https://www.investopedia.com/terms/h/high-frequency-trading.asp

cat_price_changes_train.txt contains the difference in Caterpillar's³ stock prices between consecutive trades on Jan 4, 2010. Each line contains the change in stock price (in cents) between consecutive trades (i.e., $Price_{i+1} - Price_i$ where $Price_i$ is price of the i^{th} trade). Consecutive non-empty lines give a sequence of consecutive price changes. An empty line separates sequences. Below is an example with two sequences of price changes (there's an empty line after the last 2).

-1 1 3 4 -6

0

cat_price_changes_dev.txt and cat_price_changes_dev_ans.txt are used to evaluate your code. cat_price_changes_dev.txt is in the same format as cat_price_changes_train.txt. Each line in cat_price_changes_dev_ans.txt contains the price change that occurs after the last change in its associated sequence in cat_price_changes_dev.txt. For example, if cat_price_changes_dev.txt contains the two sequences above and cat_price_changes_dev_ans.txt contains the two integers below, then -5 occurs after -6 of the first sequence, and -4 occurs after 2 in the second sequence.

-5 -4

You may assume that a price change is always an integer between -6 and 6 (inclusive).

cat_price_changes_train.txt contains 1981 sequences. cat_price_changes_dev*.txt contains 981 sequences.

cat_states.txt contains the set of possible states $\{s0, s1, s2\}$ (excluding the START (*) and STOP states), i.e., the possible values for each y_t . hmm.py is where you write your code.

Question 7. Applying Forward-Backward Algorithm on Intraday Data (25 points)

(i) Reuse the forward-backward function you have implemented for tweets POS tagging to learn the output probabilities and transition probabilities for the training data in cat_price_changes_train.txt. This function also accepts cat_states.txt. Set the maximum iteration of the forward-backward algorithm to a large value (e.g., max_iter = 100000) and the convergence threshold to a small value (e.g., thresh = 1e-4). This allows the forward-backward algorithm to run to convergence to get reasonable values of the output probabilities and transition probabilities. Write the output probabilities and transition probabilities to cat_output_probs.txt and cat_trans_probs.txt respectively. (The data and set of possible states should be small enough for you to run the algorithm to convergence if you have implemented it efficiently.)

³https://www.caterpillar.com/

- (ii) Examine the output probabilities. For each state s (s0, s1, s2), provide the probabilities that it generates positive integers, zero, and negative integers, i.e., $P(0 < x \le 6|y = s), P(x = 0|y = s), P(-6 \le x < 0|y = s)$. What semantics has your HMM learned for each state (s0, s1, s2), i.e., what does each state represent?
- (iii) Examine the transition probabilities. Using the semantics in your answer to the previous question, what has your HMM learned about the transitions from state to state?
- (iv) After you have learned the output probabilities and transition probabilities, you are given a sequence of consecutive intraday stock price changes x_1, x_2, \ldots, x_n . How can you use these probabilities to predict the next stock price change x_{n+1} ?
- (v) Write a function cat_predict that implements your answer to the previous question. This function takes the probabilites in cat_output_probs.txt and cat_trans_probs.txt, and predicts the next price change for each sequence in cat_price_changes_dev.txt. This function also accepts cat_states.txt. Write your predictions to cat_predictions.txt with one prediction per line.
- (vi) What is the average squared error of your predictions, i.e., $\frac{1}{N}\sum_{i=1}^{N}(x_{i}^{predicted}-x_{i}^{truth})^{2}, \text{ where } x_{i}^{predicted} \text{ is your prediction for sequence } i, x_{i}^{truth} \text{ is the correct next price change for sequence } i, \text{ and } N \text{ is the number of sequences? (Use the evaluate_ave_squared_error function in hmm.py.)}$ Naively predicting the next price change to be equal to the previous price change gives an average squared error of 3.94. Can you do better?

(Remember to submit cat_output_probs.txt, cat_trans_probs.txt, and cat_predictions.txt.)