

CS 103 Unit 15

Doubly-Linked Lists and Deques

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Singly-Linked List Review

- Used structures/classes and pointers to make 'linked' data structures
- Singly-Linked Lists dynamically allocates each item when the user decides to add it.
- Each item includes a 'next' pointer holding the address of the following Item object
- Traversal and iteration is only easily achieved in one direction

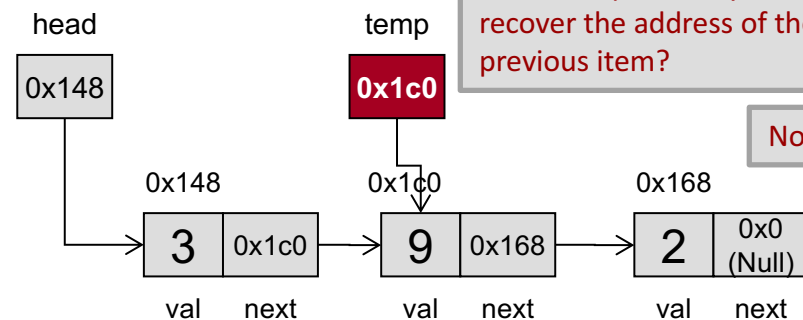
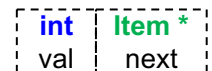
```
#include<iostream>

using namespace std;

struct Item {
    int val;
    Item* next;
};

class List
{
public:
    List();
    ~List();
    void push_back(int v); ...
private:
    Item* head;
};
```

struct Item blueprint:



Given temp...could you ever recover the address of the previous item?

No!!!

Doubly-Linked Lists

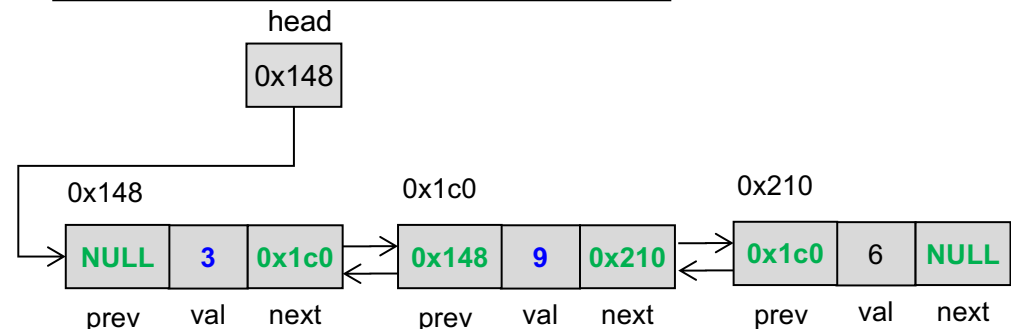
- Includes a previous pointer in each item so that we can traverse/iterate backwards or forward
- First item's previous field should be NULL
- Last item's next field should be NULL

```
#include<iostream>

using namespace std;
struct DListItem {
    int val;
    DListItem* prev;
    DListItem* next;
};

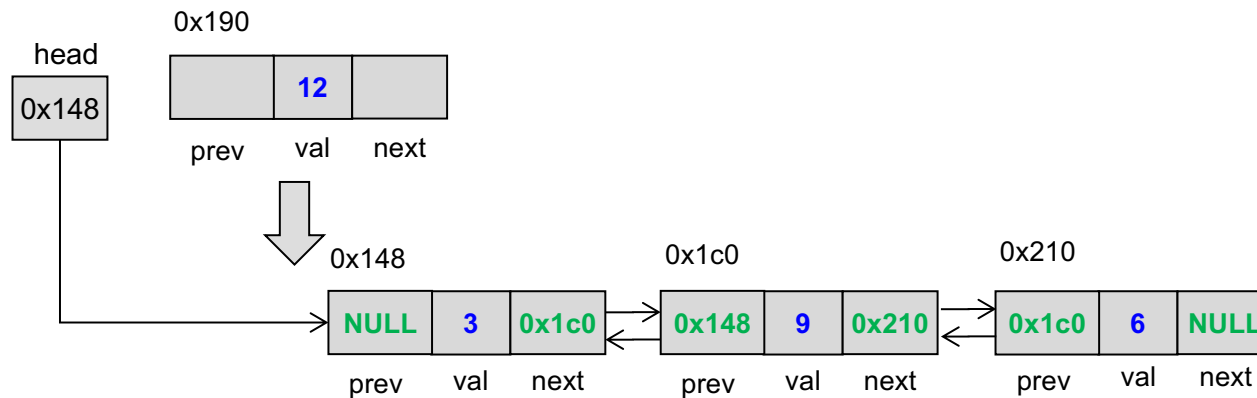
class DLList
{
public:
    DLList();
    ~DLList();
    void push_back(int v); ...
private:
    DListItem* head;
};
```

struct Item blueprint:



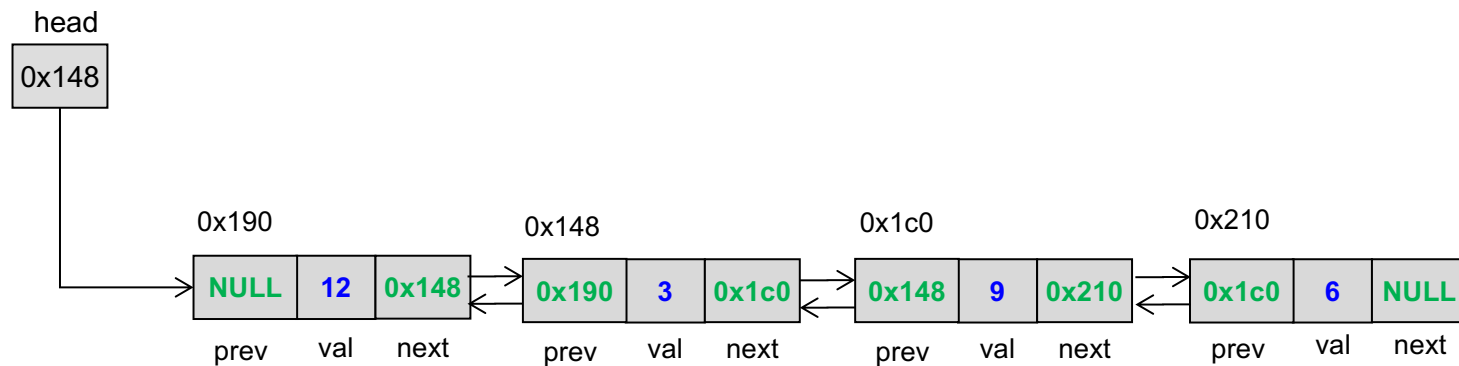
Doubly-Linked List Add Front

- Adding to the front requires you to update...
- ...Answer
 - Head
 - New front's next & previous
 - Old front's previous



Doubly-Linked List Add Front

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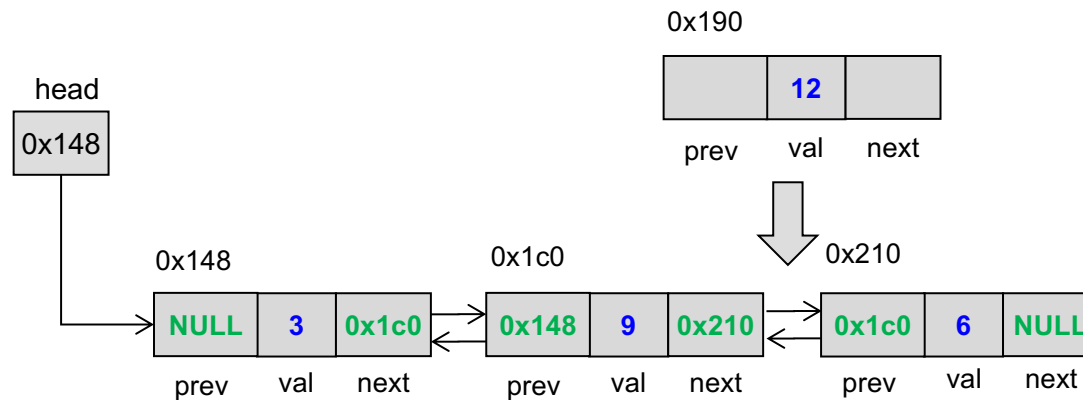


Doubly-Linked List Add Middle

- Adding to the middle requires you to update...

- Previous item's next field
- Next item's previous field
- New item's next field
- New item's previous field

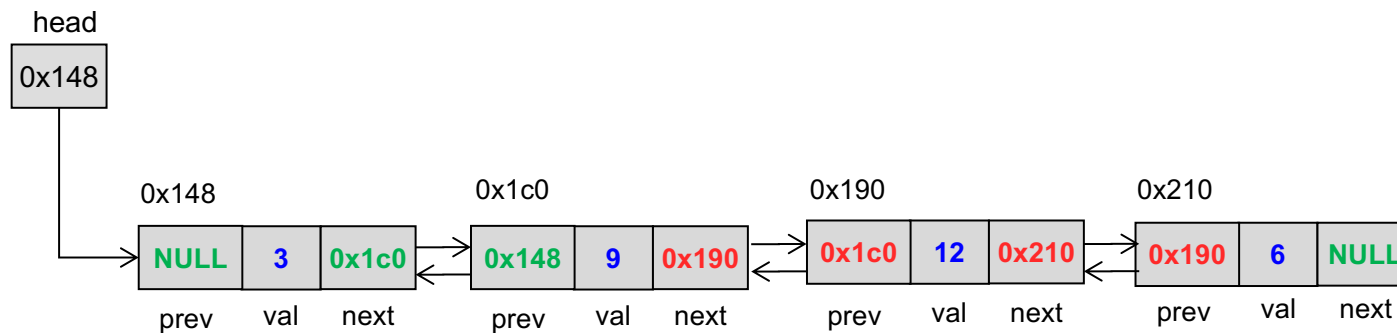
```
curr->prev = temp;  
curr->next = temp->next;  
if (temp) {  
    temp->next = curr;  
}  
if (curr->next) {  
    curr->next->prev =  
curr;  
}
```



Doubly-Linked List Add Middle

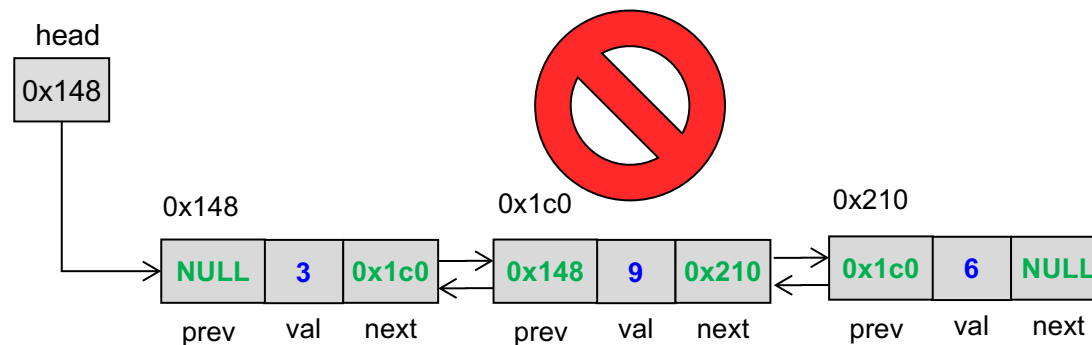
- Adding to the middle requires you to update...
 - Previous item's next field
 - Next item's previous field
 - New item's next field
 - New item's previous field

```
if (curr->prev) {  
    curr->prev->next = curr->next;  
}  
if (curr->next) {  
    curr->next->prev = curr->prev;  
}  
delete curr;
```



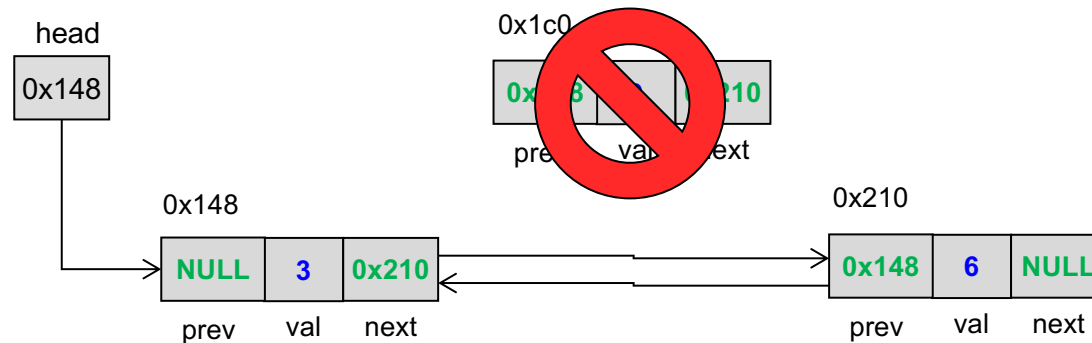
Doubly-Linked List Remove Middle

- Removing from the middle requires you to update...
 - Previous item's next field
 - Next item's previous field
 - Delete the item object



Doubly-Linked List Remove Middle

- Removing from the middle requires you to update...
 - Previous item's next field
 - Next item's previous field
 - Delete the item object

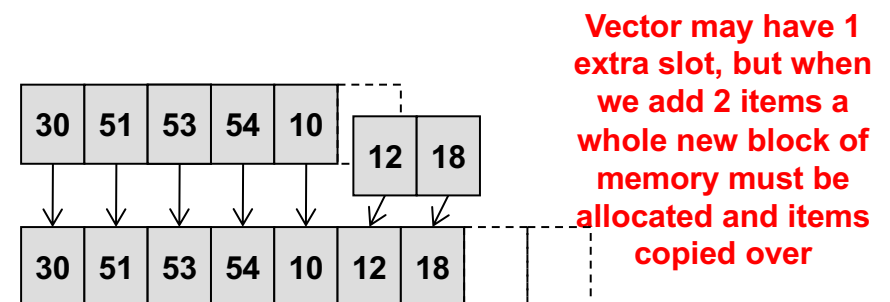
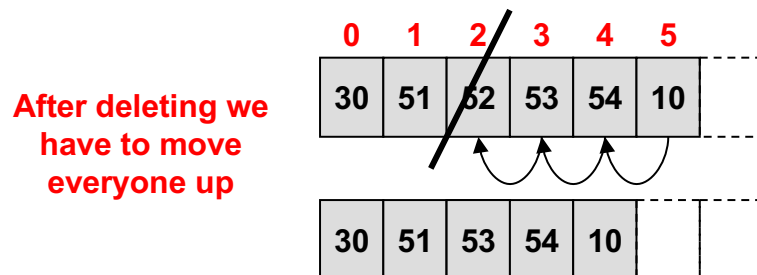


Using a Doubly-Linked List to Implement a Deque

DEQUES AND THEIR IMPLEMENTATION

Understanding Performance

- Recall vectors are good at some things and worse at others in terms of performance
- The Good:
 - Fast access for random access (i.e. indexed access such as `myvec[6]`)
 - Allows for 'fast' addition or removal of items at the **back** of the vector
- The Bad:
 - Erasing / removing item at the front or in the middle (it will have to copy all items behind the removed item to the previous slot)
 - Adding too many items (vector allocates more memory than needed to be used for additional `push_back()`'s...but when you exceed that size it will be forced to allocate a whole new block of memory and copy over every item)

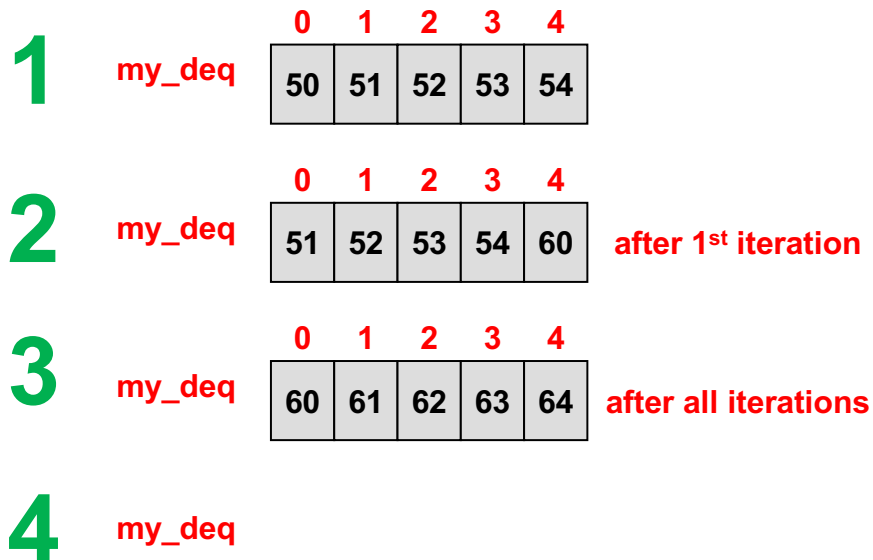


Deque Class

- Double-ended queues (like their name sounds) allow for efficient (fast) additions and removals from either 'end' (*front or back*) of the list/queue
- Performance:
 - Slightly slower at random access (i.e. array style indexing access such as: `data[3]`) than vector
 - Fast at adding or removing items at *front* or *back*

Deque Class

- Similar to vector but allows for `push_front()` and `pop_front()` options
- Useful when we want to put things in one end of the list and take them out of the other



```
#include <iostream>
#include <deque>

using namespace std;

int main()
{
    deque<int> my_deq;
    for(int i=0; i < 5; i++){
        my_deq.push_back(i+50);
    }
    cout << "At index 2 is: " << my_deq[2] ;
    cout << endl;

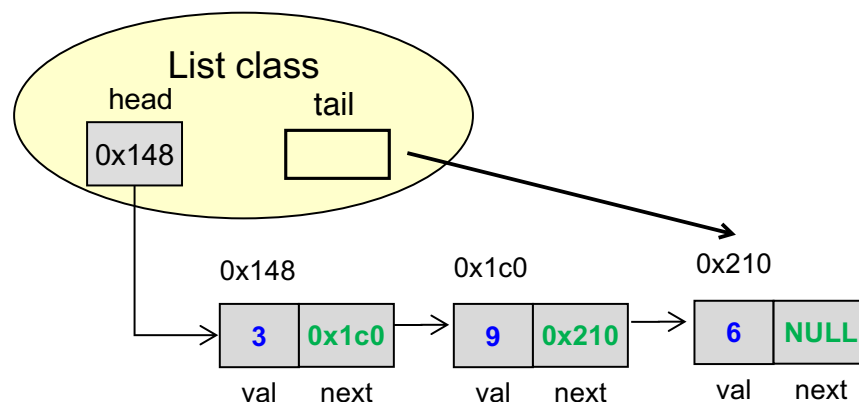
    for(int i=0; i < 5; i++){
        int x = my_deq.front();
        my_deq.push_back(x+10);
        my_deq.pop_front();
    }
    while( ! my_deq.empty()){
        cout << my_deq.front() << " ";
        my_deq.pop_front();
    }
    cout << endl;
}
```

Deque Implementation

- Let's consider how we can implement a deque
- Could we use a singly-linked list and still get fast [i.e. $O(1)$] insertion/removal from both front and back?

Singly-Linked List Deque

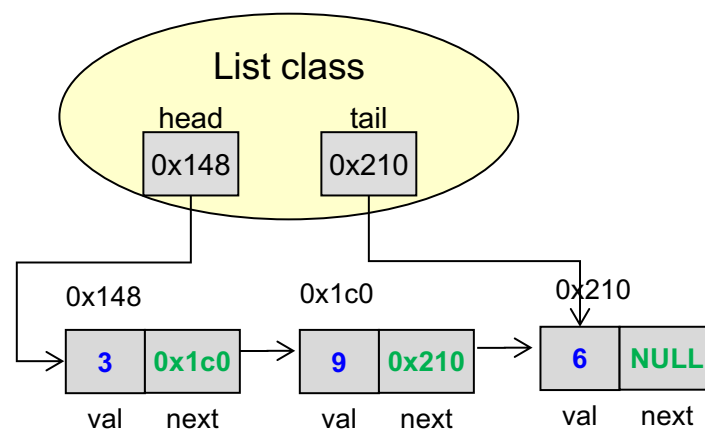
- Recall a deque should allow for fast [i.e. $O(1)$] addition and removal from front or back
- In our current singly-linked list we only know where the front is and would have to traverse the list to find the end (tail)



easy to push front and pop front;
but hard to push back and pop
back; therefore to create a new
tail item to which last item
points; so that four actions only
require $O(n)$.

Option 1: Singly-Linked List + Tail Pointer

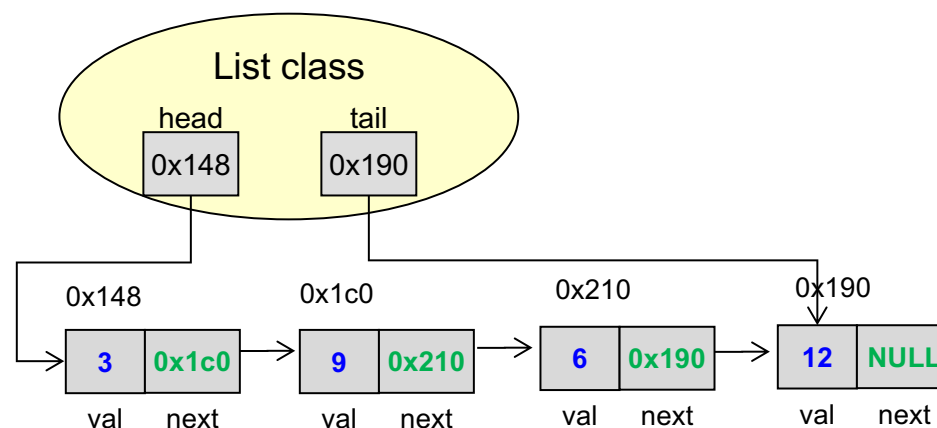
- We might think of adding a tail pointer data member to our list class
 - How fast could we add an item to the end?



*remove from back cannot be done quickly in the singly-linked list but can be done quickly in doubly-linked list.

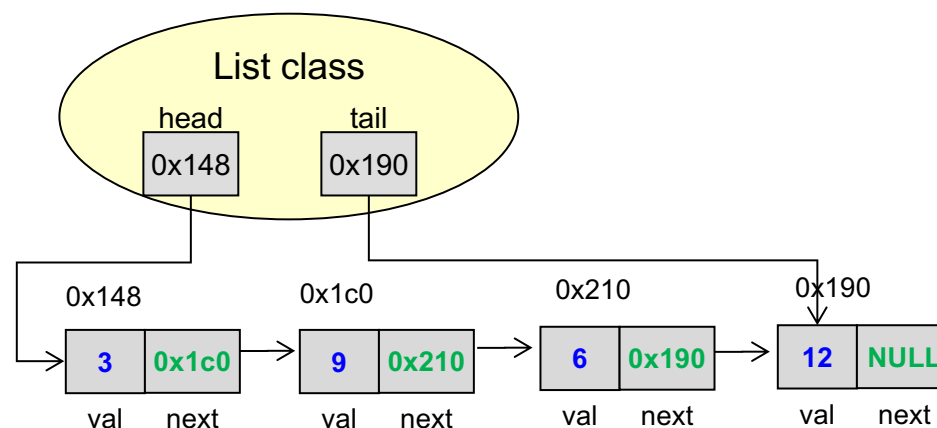
Option 1: Singly-Linked List + Tail Pointer

- We might think of adding a tail pointer data member to our list class
 - How fast could we add an item to the end? $O(1)$
 - How fast could we remove the tail item?



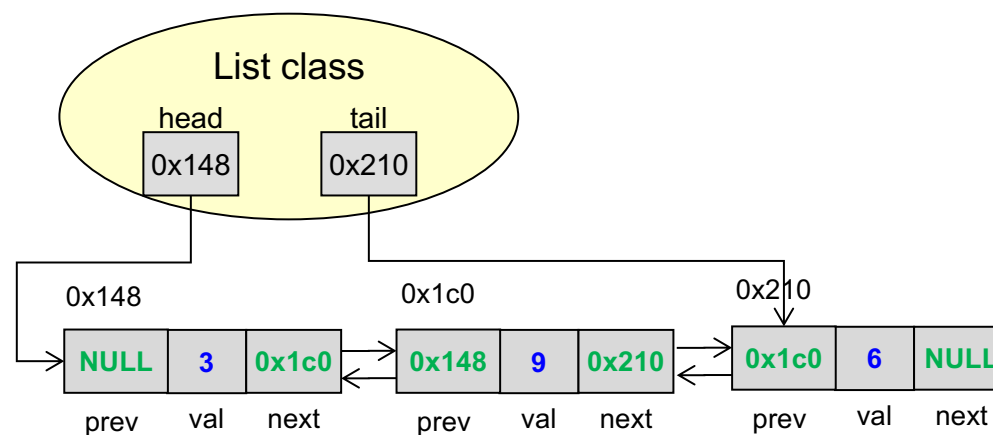
Option 1: Singly-Linked List + Tail Pointer

- We might think of adding a tail pointer data member to our list class
 - How fast could we add an item to the end? $O(1)$
 - How fast could we remove the tail item? $O(n)$
 - Would have to walk to the 2nd to last item



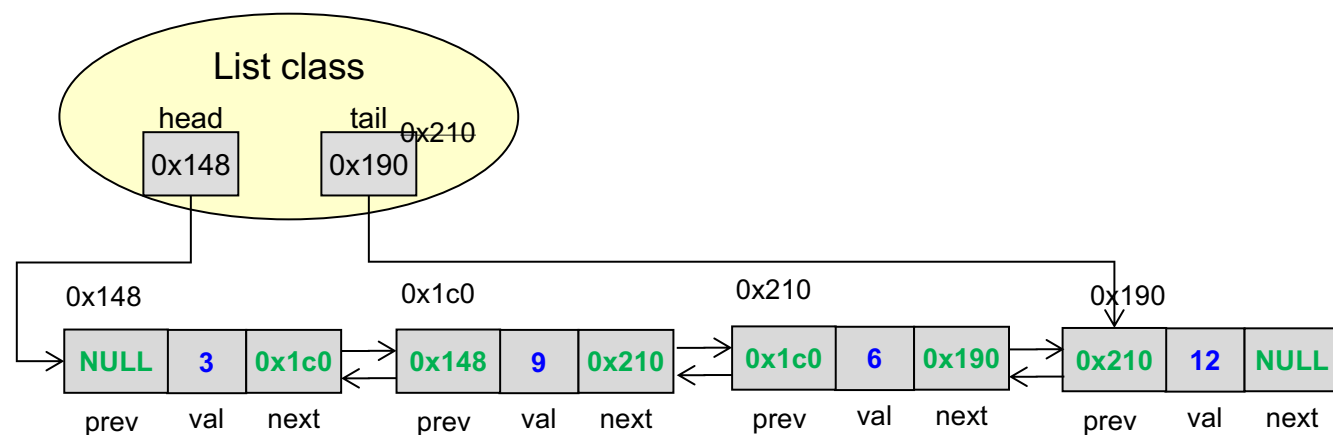
Option 2: Tail Pointer + Double-Linked List

- We might think of adding a tail pointer data member to our list class
 - How fast could we add an item to the end?



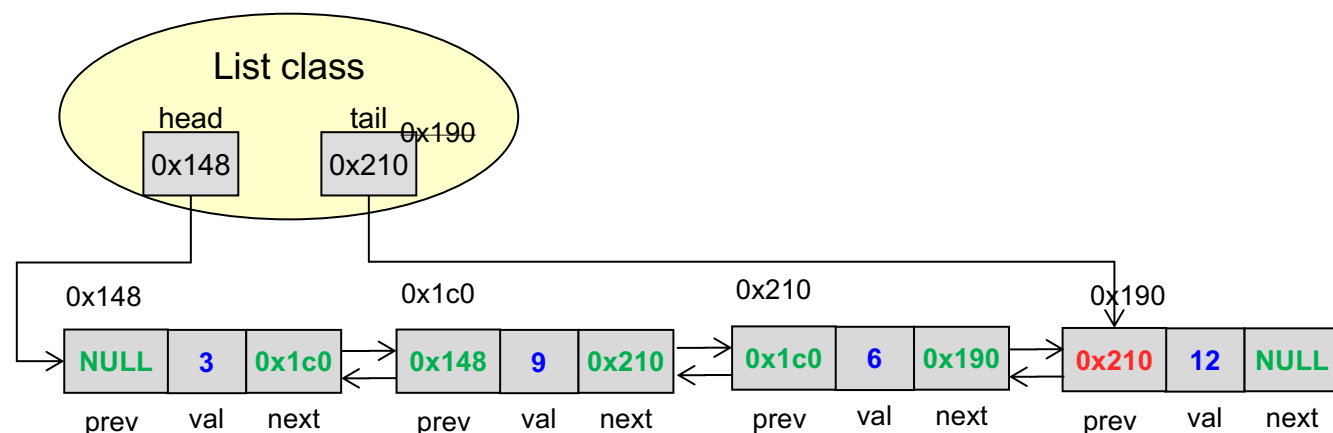
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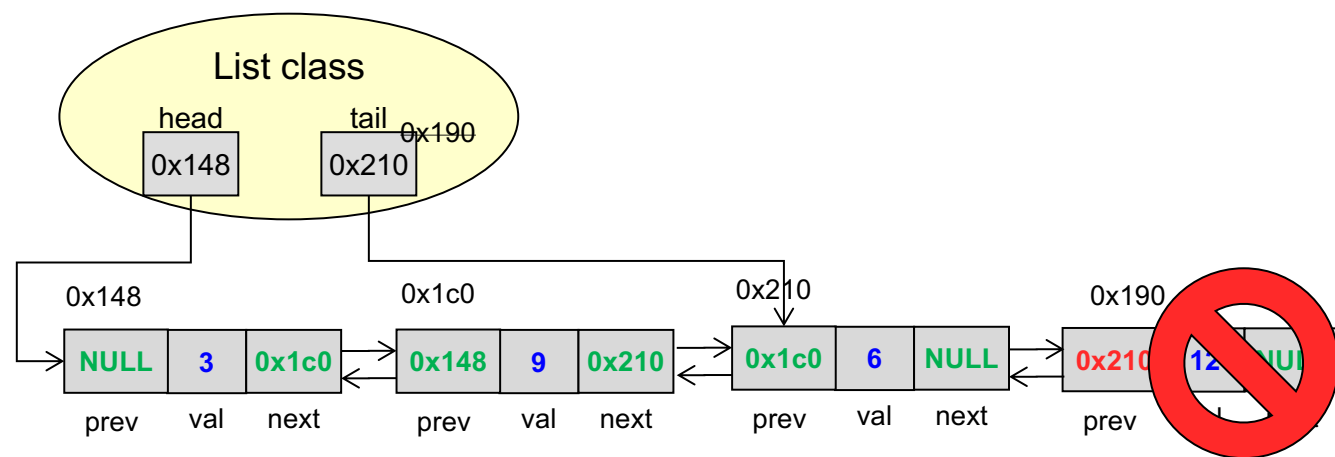
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- We might think of adding a tail pointer data member to our list class
 - How fast could we add an item to the end? $O(1)$
 - How fast could we remove the tail item? $O(1)$
 - We use the PREVIOUS pointer to update tail



Option 2: Tail Pointer + Double-Linked List

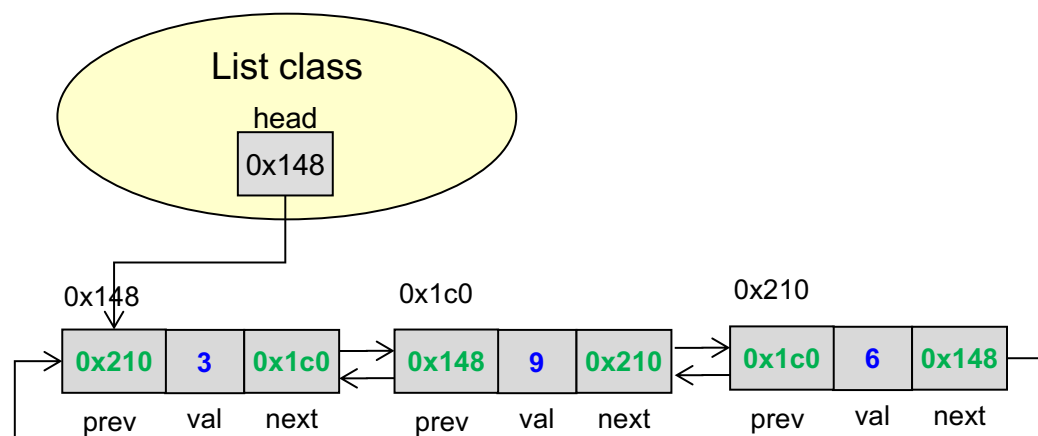
- We might think of adding a tail pointer data member to our list class
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Option 3: Circular Double-Linked List

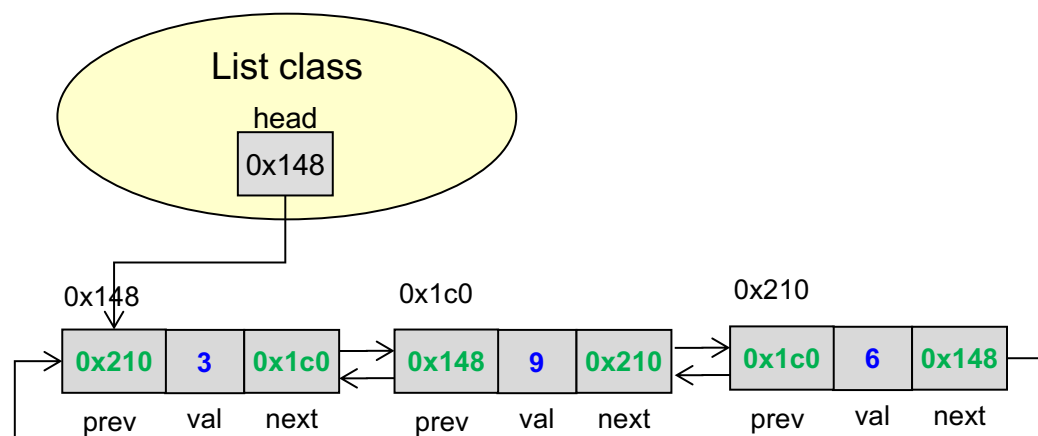
- Make first and last item point at each other to form a circular list
 - We know which one is first via the 'head' pointer

access both sides equally fast,
push back and push front equally fast



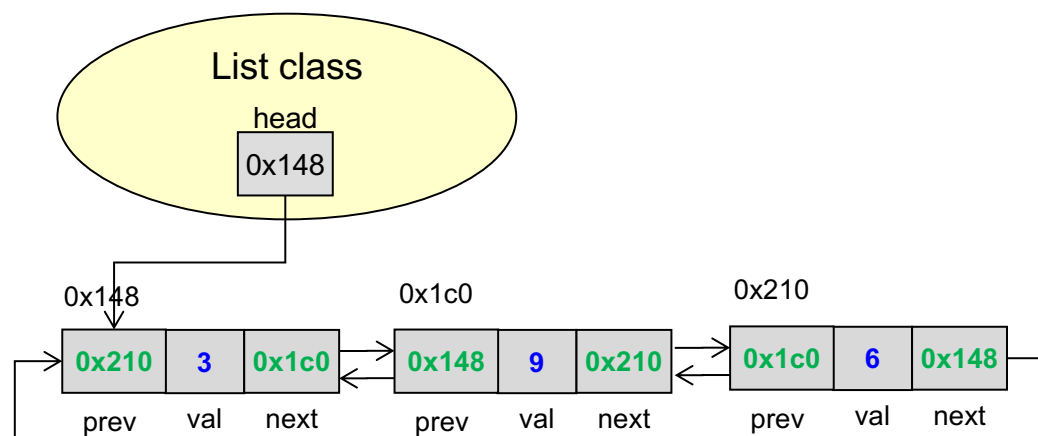
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- Make first and last item point at each other to form a circular list
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 - What expression would yield the tail item?



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- Make first and last item point at each other to form a circular list
 - We know which one is first via the 'head' pointer
 - What expression would yield the tail item?
 - `head->prev`



One Last Point

- Can this kind of deque implementation support $O(1)$ access to element i ?
 - i.e. Can you access `list[i]` quickly for any i ?
- No!!! Still need to traverse the list
- You can use a "circular" array based deque implementation to get fast random access
 - This is similar to what the actual C++ `deque<T>` class does
 - More to come in CS 104!

Activity: Write a 'delist' class

- Write a 'double-ended list' class to store integers that mimics a deque
- Support the following methods
 - size()
 - empty()
 - push_back() and pop_back()
 - push_front() and pop_front()
 - back() and front() [returns back or front integer]