

Lecture 28

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Introduction

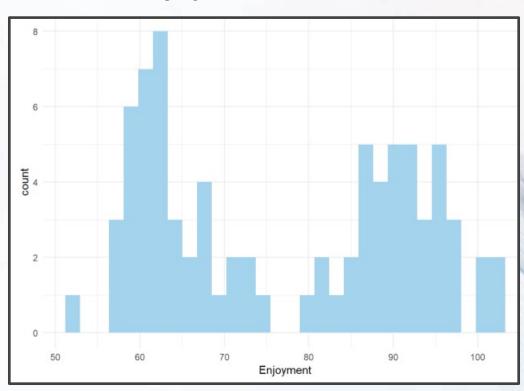
- Read Chapter 23 (R4DS)
- Previously: Numeric Variables
- New Focus
 - Categorical Predictor Variables
 - Interaction Effects
- Understand Using Multiple Datasets and Visualizations

Example 1: Data

- Data Overview
 - Enjoyment (E)
 - Food (F)
 - Condiment (C)
 - 80 Observations

Enjoyment <dbl></dbl>		Condiment <chr></chr>
81.92696	Hot Dog	Mustard
84.93977	Hot Dog	Mustard
90.28648	Hot Dog	Mustard
89.56180	Hot Dog	Mustard
97.67683	Hot Dog	Mustard

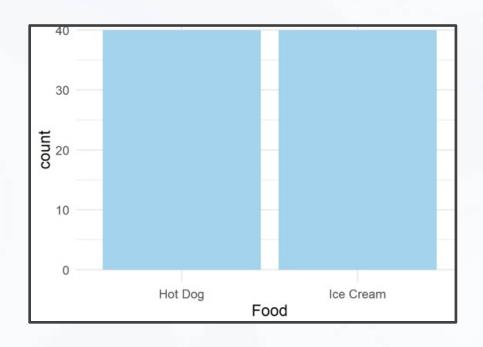
Enjoyment Visualized

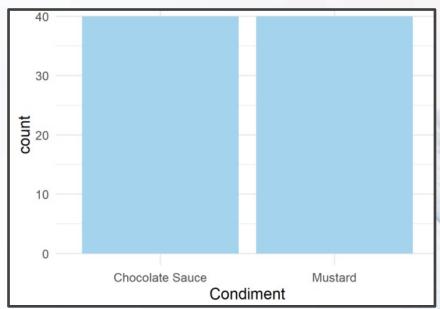


Example 1: Data

Food Visualized







Example 1: Question

Question of Interest

Can We Predict a Person's Culinary Enjoyment if...

We Serve Them a Particular Item:

- Hot Dog
- Ice Cream

With a Particular Condiment

- Mustard
- Chocolate Sauce



Regressing E on F

- $\hat{E} = 77.5 0.283F$
- Questions:
 - What Does 77.5 Represent?
 - What About -0.283?

What is R Doing?

```
CONDIMENT$Food[1:6]
## [1] "Hot Dog" "Hot Dog" "Hot Dog" "Hot Dog
" "Hot Dog" "Hot Dog"
head (model matrix (CONDIMENT, Enjoyment~Food))
## # A tibble: 6 x 2
     `(Intercept) ` `FoodIce Cream`
          <dbl>
                            <dbl>
```

Example 1: Interpretation

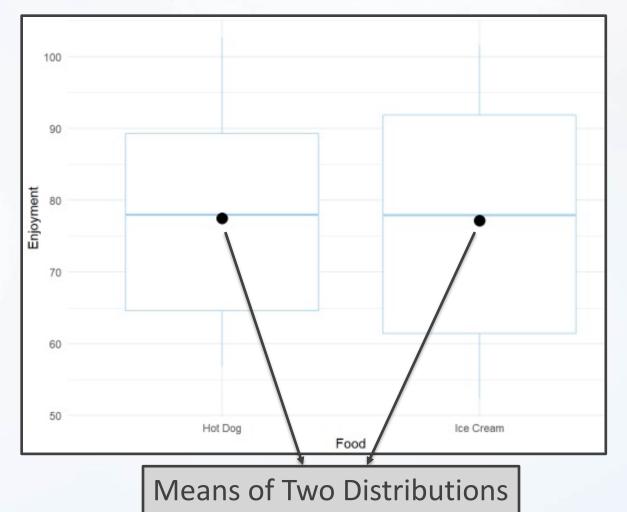
- Regressing E on F
 - $\hat{E} = 77.5 0.283F$

•
$$F = \begin{cases} 0 & if \ Hot \ Dog \\ 1 & if \ Ice \ Cream \end{cases}$$

- If You Eat a Hot Dog, $\hat{E} = 77.5 0.283(0) = 77.5$
- If You Eat Ice Cream, $\hat{E} = 77.5 0.283(1) = 77.217$
- P-value = 0.934 for the Parameter Estimated by 0.283 (Not Statistically Significant)

Example 1: Interpretation

Understanding This Visually



Regressing E on C

Significant: P-value < 0.05

•
$$\hat{E} = 79.2 - 3.73C$$

Not Significant: P-value > 0.05

•
$$C = \begin{cases} 0 & if \ Chocolate \ Sauce \\ 1 & if \ Mustard \end{cases}$$

Regressing E on C + F

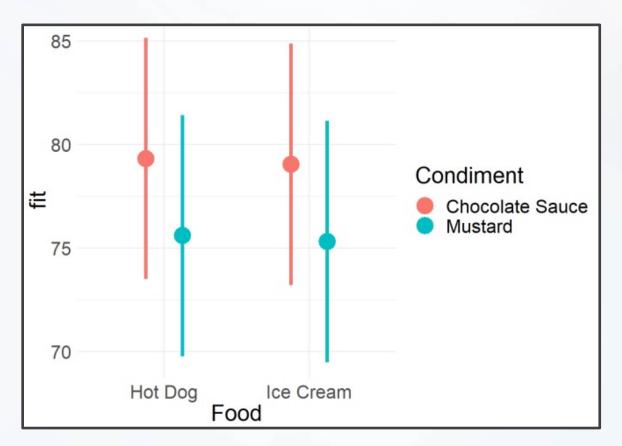
•
$$\hat{E} = 79.3 - 0.283F - 3.73C$$
• $F = \begin{cases} 0 & \text{if Hot Dog} \\ 1 & \text{if Ice Cream} \end{cases}$

•
$$C = \begin{cases} 0 & \text{if Chocolate Sauce} \\ 1 & \text{if Mustard} \end{cases}$$

What does 79.3 Represent?

Obtaining Predicted Values

Prediction Visualization



Interaction Effect

```
EvFC.Full.Model=lm(Enjoyment~Food+Condiment+Food*Condiment, data=CONDIMENT)
tidy (EvFC. Full. Model)
## # A tibble: 4 x 5
                               estimate std.error statistic p.value
  <chr>
                                  <dbl>
                                           <dbl>
                                                 <dbl>
                                                            <dbl>
## 1 (Intercept)
                                           1.12 58.3 7.18e-65
                                 65.3
                            27.7 1.58 17.5 2.11e-28
## 2 FoodIce Cream
## 3 CondimentMustard
                            24.3 1.58 15.3 5.58e-25
                                  -56.0 2.24 -25.0 1.95e-38
## 4 FoodIce Cream:CondimentMustard
```

$$\hat{E} = 65.32 + 27.73F + 24.29C - 56.03FC$$

•
$$F = \begin{cases} 0 & \text{if Hot Dog} \\ 1 & \text{if Ice Cream} \end{cases}$$
• $C = \begin{cases} 0 & \text{if Chocolate Sauce} \\ 1 & \text{if Mustard} \end{cases}$
• $FC = \begin{cases} 0 & \text{otherwise} \\ 1 & \text{if Ice Cream and Mustard} \end{cases}$

Interaction Effect

$$\hat{E} = 65.32 + 27.73F + 24.29C - 56.03FC$$

•
$$F = \begin{cases} 0 & if \ Hot \ Dog \\ 1 & if \ Ice \ Cream \end{cases}$$

•
$$F = \begin{cases} 0 & if \ Hot \ Dog \\ 1 & if \ Ice \ Cream \end{cases}$$
• $C = \begin{cases} 0 & if \ Chocolate \ Sauce \\ 1 & if \ Mustard \end{cases}$

•
$$FC = \begin{cases} 0 & otherwise \\ 1 & if Ice Cream and Mustard \end{cases}$$

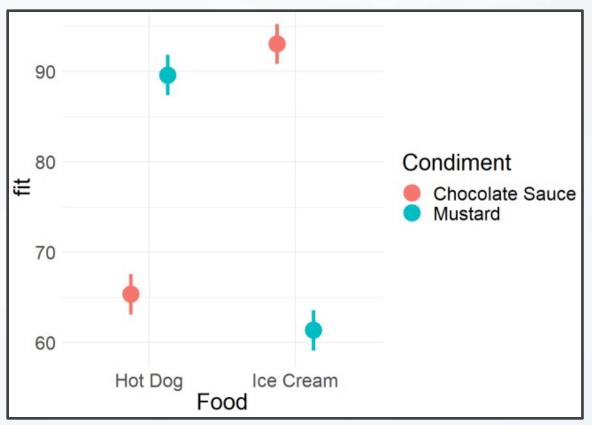
Hot dog with Chocolate = 65.32

Hot dog with Mustard = 65.32 + 24.29

Ice cream with Chocolate = 65.32 + 27.73

Ice cream with Mustard = 65.32 + 27.73 + 24.29 - 56.03

- Understanding This Visually
 - What Is Different?



Example 1: Summary

- Summary
 - Categorical Predictors
 - Purpose:
 - Generalize t-test
 - Estimate Difference in Means Between Groups

Example 2: Data

- Data Overview
 - Popular Built-in Data
 - Sepal.Width (W)
 - Sepal.Length (L)
 - Species (S)
 - 150 Observations

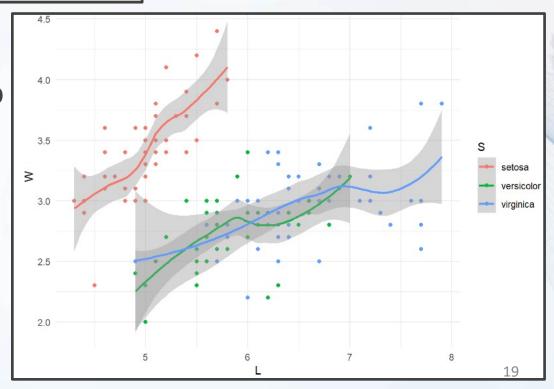
```
IRIS=iris[,c(1,2,5)]
names(IRIS)=c("L", "W", "S")
head (IRIS)
     5.1 3.5 setosa
     4.9 3.0 setosa
     4.7 3.2 setosa
     4.6 3.1 setosa
     5.0 3.6 setosa
## 6 5.4 3.9 setosa
```

Example 2: Question

Question of Interest

Can We Explain the Variation in Sepal Width Using Sepal Length and Species (setosa, versicolor, virginica)?

Visual of Relationship



Multiple Models

```
model1=lm(W~L, IRIS)
tidy (model1)
## # A tibble: 2 x 5
                estimate std.error statistic p.value
     term
                   <dbl>
     <chr>
                             <dbl>
                                       <dbl>
                                                <dbl>
                            0.254
## 1 (Intercept) 3.42
                                       13.5 1.55e-27
                                       -1.44 1.52e- 1
## 2 L
                 -0.0619
                            0.0430
model2=lm(W~L+S, IRIS)
tidy (model2)
## # A tibble: 4 x 5
                estimate std.error statistic p.value
     term
     <chr>
                   <dbl>
                             <dbl>
                                       <dbl>
                                               <dbl>
                                    7.12 4.46e-11
                 1.68
                            0.235
## 1 (Intercept)
                                   7.56 4.19e-12
## 2 L
                  0.350 0.0463
  3 Sversicolor
                 -0.983
                                      -13.6 7.62e-28
                            0.0721
## 4 Svirginica
                  -1.01
                            0.0933
                                      -10.8 2.41e-20
```

Setosa: $\hat{E} = 1.68 + 0.35L$ Versicolor: $\hat{E} = 1.68 + 0.35L - 0.983$ Virginica: $\hat{E} = 1.68 + 0.35L - 1.01$

Full Model Estimated

```
model3=lm(W\sim L+S+L*S, IRIS)
                       tidy (model3)
                   # A tibble: 6 x 5
                                    estimate std.error statistic
                                                                 p.value
                     term
                     <chr>>
                                       <dbl>
                                                 <dbl>
                                                            <dbl>
                                                                     <dbl>
                                      -0.569
                                                            -1.03 3.06e- 1
                ## 1 (Intercept)
                                                 0.554
Adjustment
                ## 2 L
                                                 0.110 7.23 2.55e-11
                                       0.799
In Mean
                   3 Sversicelor
                                                 0.713
                                                            2.02 4.51e- 2
                                       1.44
                                                                              Adjustment
                   4 Svirginica
                                       2.02
                                                 0.686
                                                             2.94 3.85e- 3
                                                                              In Slope
                   5 L:Sversicolor
                                      -0.479
                                                 0.134
                                                            -3.58 4.65e- 4
                   6 L:Svirginica
                                      -0.567
                                                 0.126
                                                            -4.49 1.45e- 5
```

Setosa: $\hat{E} = 0.799L - 0.569$

Versicolor: $\hat{E} = (0.799 - 0.479)L + 1.44 - 0.569$

Virginica: $\hat{E} = (0.799 - 0.567)L + 2.02 - 0.569$

Example 2: Predictions

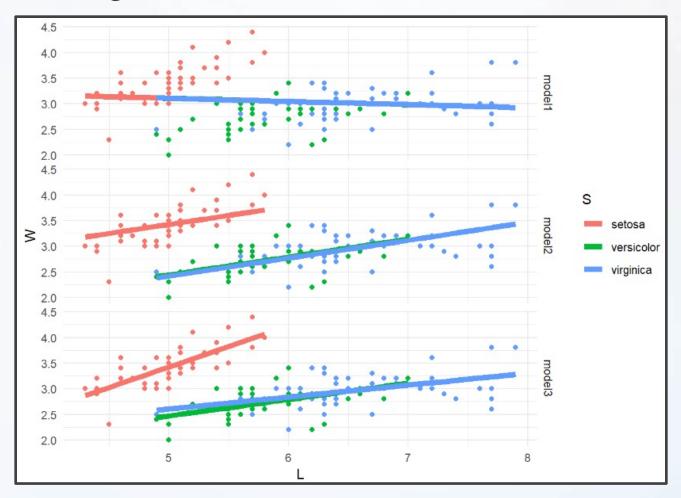
Gathering Predictions

150 Predictions for 3 Models

- Variable Named "model"
- Allows Us To Quickly Create Graphics That Compare Models

Example 2: Visualization

Visualizing Models



Example 2: Summary

- Summary
 - Numerical Response Variable
 - Categorical & Numerical Explanatory Variables