

STOR 320 Modeling III

Lecture 17

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Introduction

- Instructions
 - Download Tutorial 13 Zip
 - Unzip Folder
 - Required Packages
 - library(modelr)
 - library(tidyverse)
 - library(purrr)
 - library(broom)
 - Open .Rmd File and Knit



Discussion

- Problems With Current Approach
 - Same Model For All Locations
 - Not All Locations Used in Train
 - Not All Locations Used in Test
 - Residuals Indicate that Model Can Be Improved
 - Not Helpful for Forecasting
 - Ambiguous Results: No Clear Winner



- Previously
 - Split Data in Train and Test
 - Train (28 Rivers)
 - Test (3 Rivers)
 - Purpose
 - Estimate Out-of-Sample Error
 - Pick Best Model Based on This Estimate
 - Combat Overfitting
 - Robustification
 - Goal: Find the Simplest Model that Adequately Predicts



- Current Issues
 - Decision on Final Model Heavily Influenced by the Test Data
 - Loss of Data in Model Fitting
 - Not Appropriate in Small Datasets
- Cross Validation Idea
 - Split Data Into Many Groups
 - Each Group Acts as a Test Set
 - All Data is Used in Both Model Fitting and Model Testing
 - Help: Chapter 5 (ISLR)



- Tidyverse Concepts
 - Chapter 20 (R4DS)
 - List-Columns
 - Columns in Data Frames or Tibbles Can Be Lists
 - What this Means
 - Column of Tables
 - Column of Models
 - Column of Functions
 - Functions
 - nest(): Converts Rows of a Data Frame into a List
 - unnest(): What do You Think It Does?

Part 1: Cross Validation by Location

- Run Chunk 1
 - Observe the Output
 - Column of Tibbles
- Run Chunk 2
 - Imagine We Wanted to Split
 - Test: Data For Location 103
 - Train: All Remaining Data
 - Use of filter() and unnest()
 - First Glimpse -> 365 x 8
 - Second Glimpse -> 10,972 x 8



• Chunk 3

- Run Each Line
- What is Happening?
- Use View() on DATA2 and Scan Through the Data
- What do You Notice?

Chunk 4

- Create a Loop that Repeats this Process for Each Location
- Each Location Is a Test Set
- Predictions Saved are All Out-of-Sample
- Run Chunk 4 to Test Your Code

of NORTH CAROLINA at CHAPEL HILL

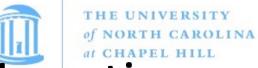
Part 1: Cross Validation by Location

Chunk 4 (Continued)

```
DATA2=DATA
DATA2$linpred=NA
for(k in unique(DATA2$L)){
 TEST = NEST.DATA %>% filter(L==k) %>%
unnest()
 TRAIN = NEST.DATA %>% filter(L!=k) %>%
unnest()
 linmod=lm(W~A, data=TRAIN)
 linmodpred=predict(linmod,newdata=TEST)
 DATA2$linpred[which(DATA2$L==k)]=linmodpred
```

Part 1: Cross Validation by Location

- Chunk 5
 - In Our Data, We Have:
 - Actual Water Temperatures
 - Out-of-Sample Predicted Water Temperatures
 - Create RMSE.func() With Two Arguments
 - actual= vector of actual water temperatures
 - predict=vector of predicted water temperatures
 - Use This Function on the Two Columns in DATA2 for RMSE
 - actual=W
 - predict=linpred



Part 1: Cross Validation by Location

Chunk 5 (Continued)



```
RMSE.func(actual=DATA2$W,predict=DATA2$linpred)
[] 3.147084
```

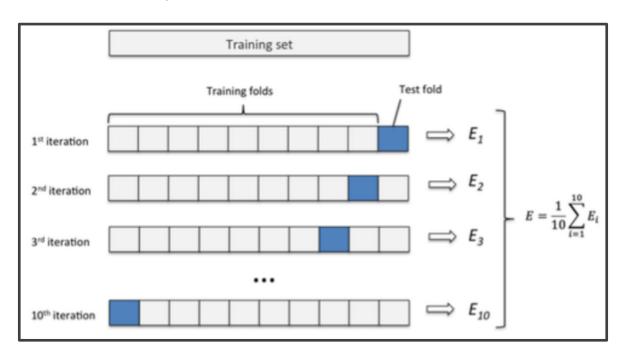


Intermission

- Current
 - Using the Natural Grouping of Data for 31-Fold Cross Validation
 - Only Fit One Linear Model
 - Should Use Cross-Validation for Multiple Different Models and Compare Cross-Validated RMSE
- Next
 - Randomly Assign Observations to K-Folds
 - CV Function: crossv_kfold(K)

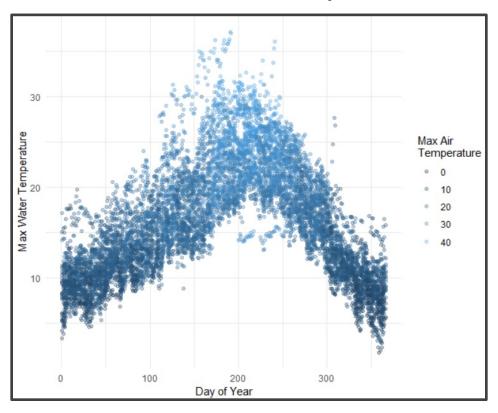


- Overview (*K*=10)
 - Randomly Split Observations Into K Groups
 - Each Fold Acts as a Test Set
 - If Each Fold Contains Approximately the Same # of Observations,





- Run Chunk 1
 - Variables (Julian Day)
 - Clear Non-Linear Relationship





General Polynomial Model

$$W = a + \sum_{i=1}^{I} b_i A^i + \sum_{j=1}^{J} c_j D^j + \varepsilon$$

- Perform K-Fold CV to Estimate Out-of-Sample RMSE for Choices of *I=4* and *J=3*
- Ultimate Goal is To Select Best I and J

- Run Chunk 2
 - Fit Model with I=4 and J=3
 - Functions from broom Package
 - tidy()
 - glance()
 - Used to Preview Models

```
tidy(polymodel)
A tibble: 8 x 5
                       estimate std.error statistic
                                                        p.value
term
<chr>
                          <db7>
                                      <db7>
                                                 \langle db 1 \rangle
                                                           \langle db 1 \rangle
                          16.2
(Intercept)
                                    0.0273
                                               595.
                                                       0.
poly(A, 4)1
                         328.
                                    4.36
                                                75.3
                                                       0.
poly(A, 4)2
                          49.0
                                    2.80
                                                17.5
                                                       1.62e-67
poly(A, 4)3
                                    2.78
                                                 1.02 3.06e- 1
                           2.85
                          -3.62
                                    2.72
poly(A, 4)4
                                                -1.33 1.84e- 1
poly(JULIAN_DAY, 3)1
                          46.0
                                    2.78
                                                16.6
                                                       8.85e-61
poly(JULIAN_DAY, 3)2
                        -226.
                                    4.31
                                               -52.5
                                               -20.5
poly(JULIAN_DAY, 3)3
                         -59.3
                                    2.89
                                                       8.66e-92
```

```
glance(polymodel)
A tibble: 1 x 11
r.squared adj.r.squared sigma statistic p.value
                                                                       logLik
                                                                                    AIC
                                                                                             BIC
     < db 1 >
                       <db1> <db1>
                                            <db7>
                                                      <db1> <int>
                                                                         \langle db 1 \rangle
                                                                                  \langle db 1 \rangle
                                                                                           \langle db 1 \rangle
     0.797
                                            5525.
                       0.797 2.71
                                                                   8 -23804. 47626. 47691.
```



- Run Chunk 3
 - Divide Data into 10 Folds
 - Use crossv_kfold() Function
 - Variables are Lists of Train and Test Sets
 - For Each Row, We Want to Fit on Train and Predict on Test



- Run Chunk 4
 - Create Function to Fit Models
 - Apply Function to All Train Sets Using purrr::map()
 Function

```
DATA4=DATA3 %>%
     mutate(tr.model=map(train,train.model.func,i=i,j=j))
head(DATA4)
A tibble: 6 x 4
                           tr.model
         test
        <1ist>
                       <chr> <chr> <ist>
<S3: resample> <S3: resample> 01
                           <S3: 1m>
<S3: resample> <S3: resample> 04
                           <S3: 1m>
<S3: resample> <S3: resample> 05
                           <S3: 1m>
<S3: resample> <S3: resample> 06
                           <S3: 1m>
```

- Functions from purrr Package
 - map() Loop Over Train
 - map2() Loop Over Fitted Models and Test



- Run Chunk 5
 - purrr::map2() Iterates Function Over Two Arguments
 - For Every Test Set and Trained Model, We Use

augment() to Get Predictions

```
DATA4.PREDICT = DATA4 %>%
          mutate(predict=map2(test,tr.model,~augment(.y,newdata=.x))) %>%
          select(predict) %>%
          unnest()
head(DATA4.PREDICT)
A tibble: 6 x 10
JULIAN DAY YEAR
                                      TIME MONTH
                                                    DAY I.fitted
                                                                 .se.fit
                         < db 7 >
                                     <int> <int>
                                                                   < db 7 >
     <int> <int> <int>
                               <db1>
                                                           < db 1
                          9.8
           2003
                    103
                                 5.1
                                                                  0.138
                                        12
            2003
                    103
                          9.9
                                6.2
                                                                  0.119
                    103
            2003
                                                          10.4
                                                                  0.0744
            2003
                    103
                          9.5
                                        30
                                                           9.14
                                                                  0.0803
                         12.5
                               11.4
            2003
                    103
                                        47
                                                          10.5
                                                                  0.0621
                                        50
        50 2003
                    103 l
                         10.7
                                14
                                                          11.5
                                                                  0.0548
```

Next, Compare Actual With Fitted Using RMSE.func()

```
RMSE.func(actual=DATA4.PREDICT$W,predict=DATA4.PREDICT$.fitted)
2.709727
```



Look Ahead

- What We Have Done
 - Specify I and J
 - Use 10-Fold Cross Validation to Estimate Out-of-Sample RMSE
- How We Should Use This
 - Choose Max I and Max J (Example: 10)
 - Initiate 10 x 10 Matrix of NA
 - Loop Through All i and j to Capture Out-of-Sample RMSE
 - Create a Tile Plot that Visualizes the RMSE for Each Combination of i and j
 - Choose Best i and j