HW7

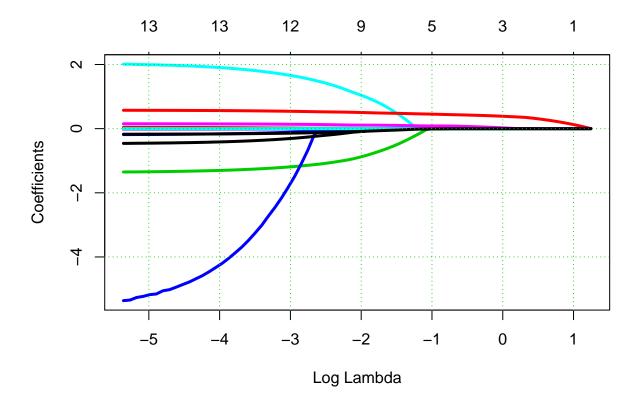
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6.8 - 11

(a)

```
library(MASS)
library(glmnet)
## Warning: package 'glmnet' was built under R version 3.4.3
## Loading required package: Matrix
## Loading required package: foreach
## Warning: package 'foreach' was built under R version 3.4.3
## Loaded glmnet 2.0-13
boston <- Boston
Split <- floor(dim(boston[1])*0.78)</pre>
train <- 1:Split</pre>
## Warning in 1:Split: numerical expression has 2 elements: only the first
## used
test <- (Split+1):dim(boston)[1]</pre>
## Warning in (Split + 1):dim(boston)[1]: numerical expression has 2 elements:
## only the first used
boston.train <- boston[train,]</pre>
boston.test <- boston[test,]</pre>
xtrain.matrix <- model.matrix(crim ~ ., data = boston.train)</pre>
xtest.matrix <- model.matrix(crim ~ ., data = boston.test)</pre>
y <- boston.train$crim
lasso.fit <- glmnet(xtrain.matrix, y, alpha = 1)</pre>
plot(lasso.fit, xvar = "lambda", lwd = 3)
grid(col = 3)
```



(b)

```
lasso.cv <- cv.glmnet(xtrain.matrix, y, alpha = 1)</pre>
best.lambda.lasso <- lasso.cv$lambda.min</pre>
pred.lasso <- predict(lasso.fit, s = best.lambda.lasso, newx = xtest.matrix)</pre>
mean((boston.test$crim - pred.lasso)^2)
## [1] 128.4983
coef(lasso.cv, s = best.lambda.lasso)
## 15 x 1 sparse Matrix of class "dgCMatrix"
##
## (Intercept) -6.922786605
## (Intercept)
## zn
                 0.002797302
## indus
## chas
                -0.826770860
## nox
                 0.970130402
## rm
## age
## dis
                -0.074724415
                 0.498749895
## rad
                 0.001691876
## tax
## ptratio
               -0.019402715
```

```
## black .
## lstat 0.109598343
## medv -0.078744769
```

(c)

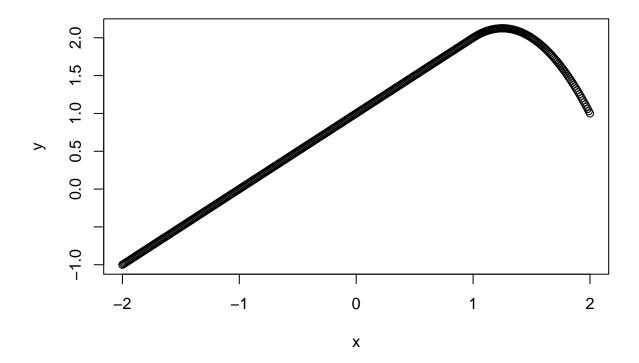
No, not all variables are used in LASSO because it forces some coefficients to be set to zero.

7.9 - 3

```
x \leftarrow seq(-2,2,0.01)

y \leftarrow 1 + x - 2 * (x-1)^2 * I(x>=1)

plot(x,y)
```

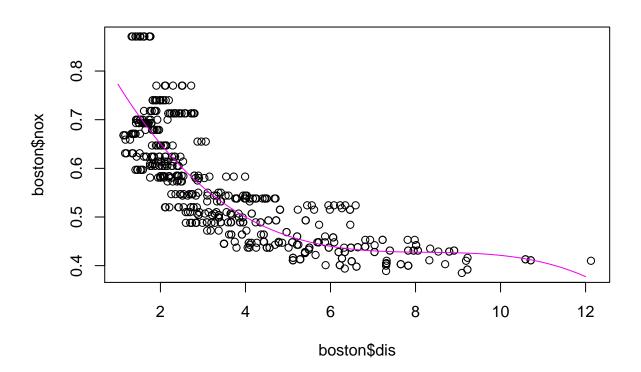


7.9 - 9

(a)

```
model <- lm(nox ~ poly(dis, 3), data = boston)
summary(model)</pre>
```

```
##
## Call:
## lm(formula = nox ~ poly(dis, 3), data = boston)
##
## Residuals:
##
                          Median
         Min
                    1Q
                                        3Q
                                                 Max
## -0.121130 -0.040619 -0.009738 0.023385 0.194904
##
## Coefficients:
##
                  Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                  0.554695
                             0.002759 201.021 < 2e-16 ***
## poly(dis, 3)1 -2.003096
                             0.062071 -32.271 < 2e-16 ***
## poly(dis, 3)2 0.856330
                             0.062071 13.796 < 2e-16 ***
## poly(dis, 3)3 -0.318049
                             0.062071 -5.124 4.27e-07 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.06207 on 502 degrees of freedom
## Multiple R-squared: 0.7148, Adjusted R-squared: 0.7131
## F-statistic: 419.3 on 3 and 502 DF, p-value: < 2.2e-16
plot(boston$dis, boston$nox)
dis <- seq(1,12,0.01)
xdf <- data.frame(dis, dis^2, dis^3)</pre>
y <- predict(model, xdf)</pre>
lines(dis, y, col = "magenta2")
```



(b)

```
for (i in 1:10){
  polyfit <- lm(nox ~ poly(dis, i), data = boston)</pre>
  print(sum(polyfit$residual^2))
## [1] 2.768563
## [1] 2.035262
## [1] 1.934107
## [1] 1.932981
## [1] 1.91529
## [1] 1.878257
## [1] 1.849484
## [1] 1.83563
## [1] 1.833331
## [1] 1.832171
(c)
set.seed(6)
library(boot)
for (i in 1:10){
  polygfit <- glm(nox ~ poly(dis, i), data = boston)</pre>
  loocv <- cv.glm(boston, polygfit)</pre>
  print(loocv$delta)
## [1] 0.005523868 0.005523815
## [1] 0.004079449 0.004079390
## [1] 0.003874762 0.003874708
## [1] 0.003887521 0.003887449
## [1] 0.004164865 0.004164231
## [1] 0.005384278 0.005381096
## [1] 0.01106878 0.01105424
## [1] 0.008121397 0.008112597
## [1] 0.01761636 0.01758879
## [1] 0.004430276 0.004428769
The minimum prediction error is when polynomial degree is 3. Therefore, the optimal degree is 3.
7.9 - 10
(a)
library(ISLR)
## Warning: package 'ISLR' was built under R version 3.4.3
library(leaps)
## Warning: package 'leaps' was built under R version 3.4.3
```

```
college <- College
min.model <- lm(Outstate ~ 1, data = college)</pre>
full.model <- lm(Outstate ~ ., data = college)</pre>
step(min.model, scope = list(lower = min.model, upper = full.model), direction = "forward")
## Start: AIC=12898.87
## Outstate ~ 1
##
##
                 Df Sum of Sq
                                      RSS
                                            AIC
                  1 5684728234 6.8746e+09 12433
## + Expend
## + Room.Board
                  1 5376025290 7.1833e+09 12467
## + Grad.Rate
                  1 4099005307 8.4603e+09 12594
## + perc.alumni 1 4027178047 8.5321e+09 12600
## + Top10perc
                  1 3971446292 8.5879e+09 12606
                  1 3866086440 8.6932e+09 12615
## + S.F.Ratio
## + Private
                  1 3835884599 8.7234e+09 12618
## + Top25perc
                  1 3008031144 9.5513e+09 12688
## + Terminal
                  1 2090498711 1.0469e+10 12759
## + PhD
                  1 1842141521 1.0717e+10 12778
## + Personal
                  1 1123466496 1.1436e+10 12828
## + P.Undergrad 1 807167148 1.1752e+10 12849
## + F.Undergrad 1 584567601 1.1975e+10 12864
## + Enroll
                  1 303598468 1.2256e+10 12882
## <none>
                               1.2559e+10 12899
## + Apps
                      31598296 1.2528e+10 12899
                  1
## + Books
                  1
                      18960781 1.2540e+10 12900
                       8330540 1.2551e+10 12900
## + Accept
                  1
##
## Step: AIC=12432.62
## Outstate ~ Expend
##
                 Df Sum of Sq
##
                                      RSS
                                            AIC
## + Private
                  1 1930753277 4943815915 12178
## + Room.Board
                  1 1683455774 5191113418 12216
## + Grad.Rate
                  1 1411765652 5462803540 12256
## + perc.alumni 1 1237783587 5636785605 12280
                  1 689772774 6184796418 12352
## + Personal
## + F.Undergrad 1 654774545 6219794647 12357
## + S.F.Ratio
                  1 500249678 6374319514 12376
## + Enroll
                  1 497657120 6376912072 12376
## + P.Undergrad 1 492284188 6382285004 12377
## + Top25perc
                  1 314950268 6559618924 12398
## + Top10perc
                  1 308836638 6565732554 12399
                  1 208701510 6665867682 12411
## + Apps
## + Terminal
                  1 197798147 6676771045 12412
## + Accept
                  1 153419952 6721149240 12417
## + PhD
                  1 130314044 6744255148 12420
## <none>
                               6874569192 12433
                      17199346 6857369846 12433
## + Books
##
## Step: AIC=12178.45
## Outstate ~ Expend + Private
##
##
                 Df Sum of Sq
                                     RSS
                                           AIC
```

```
## + Room.Board 1 957521619 3986294296 12013
## + Terminal 1 754304546 4189511369 12052
## + Grad.Rate 1 724055966 4219759949 12057
## + PhD 1 688814006 4255001909 12064
## + perc.alumni 1 447619509 4496196406 12107
## + Top25perc 1 397739454 4546076461 12115
## + Top10perc 1 323275816 4620540099 12128
## + Personal 1 199132763 4744683152 12148
## + Accept
                1 164450738 4779365177 12154
## + Apps
                1 115156477 4828659438 12162
## + Enroll
               1 29686275 4914129640 12176
## + S.F.Ratio 1 22893877 4920922038 12177
## <none>
                            4943815915 12178
## + F.Undergrad 1 11818940 4931996975 12179
## + P.Undergrad 1 8049077 4935766838 12179
## + Books
                 1
                     3883230 4939932685 12180
##
## Step: AIC=12013.18
## Outstate ~ Expend + Private + Room.Board
##
               Df Sum of Sq
                                   RSS
                                         ATC
## + perc.alumni 1 459760795 3526533501 11920
## + Grad.Rate 1 406258441 3580035855 11932
                1 375099014 3611195282 11938
## + PhD
## + Terminal
               1 373461127 3612833169 11939
## + Top25perc 1 279816168 3706478128 11959
## + Top10perc 1 255226620 3731067676 11964
## + Personal
                1 116422238 3869872058 11992
## + Accept 1 44658844 3941635452 12006
## + P.Undergrad 1 37213229 3949081067 12008
                 1 25622787 3960671509 12010
## + Books
                 1 24301498 3961992798 12010
## + S.F.Ratio
## + Apps
                1 17189184 3969105112 12012
## <none>
                            3986294296 12013
                   7189256 3979105040 12014
## + Enroll
                 1
## + F.Undergrad 1
                   204861 3986089435 12015
##
## Step: AIC=11919.97
## Outstate ~ Expend + Private + Room.Board + perc.alumni
##
##
                Df Sum of Sq
                                         AIC
                                   RSS
## + PhD
                1 223766309 3302767192 11871
## + Terminal
                1 215610907 3310922594 11873
## + Grad.Rate 1 185543461 3340990040 11880
## + Top25perc
              1 118673928 3407859573 11895
## + Top10perc
               1 105706952 3420826549 11898
## + Accept
                1 64645426 3461888076 11908
## + Personal
                1 46442640 3480090861 11912
                1 27049039 3499484463 11916
## + Apps
                 1 10686621 3515846880 11920
## + Books
## + P.Undergrad 1 10149425 3516384076 11920
## + Enroll 1 9960934 3516572567 11920
## + S.F.Ratio 1 9765339 3516768162 11920
## <none>
                            3526533501 11920
```

```
## + F.Undergrad 1
                     2355584 3524177917 11921
##
## Step: AIC=11871.03
## Outstate ~ Expend + Private + Room.Board + perc.alumni + PhD
##
                Df Sum of Sq
                                    RSS
                                          ATC
## + Grad.Rate
               1 129273253 3173493939 11842
## + Personal
                 1 48144801 3254622391 11862
## + Top25perc
                 1 33522465 3269244727 11865
                 1 31577086 3271190106 11866
## + Top10perc
## + Accept
                 1 27303953 3275463239 11867
                 1 24459320 3278307873 11867
## + Terminal
## + P.Undergrad 1 20843690 3281923502 11868
## + S.F.Ratio 1 17212529 3285554663 11869
## <none>
                             3302767192 11871
## + Apps
                 1
                    7796385 3294970807 11871
## + Books
                 1 6336668 3296430524 11872
## + F.Undergrad 1 2209904 3300557288 11872
## + Enroll
                      71469 3302695723 11873
                 1
##
## Step: AIC=11842.01
## Outstate ~ Expend + Private + Room.Board + perc.alumni + PhD +
##
      Grad.Rate
##
##
                Df Sum of Sq
                                    RSS
                                          AIC
## + Personal
                1 32007866 3141486073 11836
## + Terminal
                 1 27622869 3145871070 11837
## + S.F.Ratio
                 1 19460763 3154033176 11839
## + Accept
                 1 11686406 3161807533 11841
## + Top25perc
                 1 9214061 3164279878 11842
## + Top10perc
                 1 8384772 3165109167 11842
## <none>
                             3173493939 11842
## + P.Undergrad 1
                   7931779 3165562160 11842
## + F.Undergrad 1 5652800 3167841139 11843
## + Books
                 1
                    4940188 3168553751 11843
## + Enroll
                 1
                    1058307 3172435632 11844
## + Apps
                      218732 3173275207 11844
##
## Step: AIC=11836.13
## Outstate ~ Expend + Private + Room.Board + perc.alumni + PhD +
      Grad.Rate + Personal
##
                Df Sum of Sq
                                    RSS
                                          AIC
## + Terminal
                 1 26960561 3114525512 11831
## + S.F.Ratio
                 1 21488428 3119997645 11833
                 1 16663556 3124822517 11834
## + Accept
                 1 10904040 3130582033 11835
## + Top25perc
## + Top10perc
                 1 10080019 3131406054 11836
## <none>
                             3141486073 11836
## + P.Undergrad 1
                     3056303 3138429770 11837
## + F.Undergrad 1
                    1578173 3139907900 11838
## + Books
                 1
                   1415073 3140071000 11838
## + Apps
                 1
                   1285269 3140200804 11838
## + Enroll
                 1
                        1228 3141484845 11838
```

```
##
## Step: AIC=11831.43
## Outstate ~ Expend + Private + Room.Board + perc.alumni + PhD +
      Grad.Rate + Personal + Terminal
##
##
##
                Df Sum of Sq
                                    RSS
                                           AIC
## + S.F.Ratio
                 1 20590180 3093935332 11828
## + Accept
                 1 14554658 3099970855 11830
## + Top10perc
                 1 10079178 3104446334 11831
## + Top25perc
                 1 8304260 3106221252 11831
## <none>
                              3114525512 11831
## + P.Undergrad 1
                     3795882 3110729631 11832
## + Books
                  1
                     3419067 3111106445 11833
## + F.Undergrad
                    2665838 3111859674 11833
                 1
## + Apps
                      965869 3113559643 11833
                  1
## + Enroll
                  1
                       99749 3114425763 11833
##
## Step: AIC=11828.28
## Outstate ~ Expend + Private + Room.Board + perc.alumni + PhD +
      Grad.Rate + Personal + Terminal + S.F.Ratio
##
##
                Df Sum of Sq
                                    RSS
                 1 18802632 3075132700 11826
## + Accept
## + Top10perc
                     9962656 3083972676 11828
                 1
## + Top25perc
                     8224868 3085710464 11828
                 1
## <none>
                              3093935332 11828
## + P.Undergrad 1
                     2969569 3090965762 11830
                     2926489 3091008843 11830
## + Books
                 1
## + Apps
                  1
                    2330380 3091604952 11830
## + F.Undergrad 1
                    1083561 3092851770 11830
## + Enroll
                  1
                        55569 3093879763 11830
##
## Step: AIC=11825.54
## Outstate ~ Expend + Private + Room.Board + perc.alumni + PhD +
##
       Grad.Rate + Personal + Terminal + S.F.Ratio + Accept
##
                 Df Sum of Sq
                                    RSS
## + F.Undergrad 1 64549767 3010582933 11811
## + Enroll
                  1 52734104 3022398596 11814
## + Apps
                  1 41326268 3033806432 11817
## + P.Undergrad 1
                    9100368 3066032332 11825
## <none>
                              3075132700 11826
## + Top10perc
                     7725972 3067406728 11826
                 1
## + Top25perc
                     5217065 3069915635 11826
                  1
                     3778233 3071354467 11827
## + Books
                  1
##
## Step: AIC=11811.06
## Outstate ~ Expend + Private + Room.Board + perc.alumni + PhD +
##
       Grad.Rate + Personal + Terminal + S.F.Ratio + Accept + F.Undergrad
##
                 Df Sum of Sq
##
                                     RSS
                                           AIC
## + Apps
                 1 43194200 2967388733 11802
## + Top10perc
                  1 17164307 2993418626 11809
## + Top25perc
                  1 11926675 2998656258 11810
```

```
## <none>
                              3010582933 11811
                      2778487 3007804447 11812
## + Books
                  1
                      1816254 3008766679 11813
## + Enroll
                       329602 3010253331 11813
## + P.Undergrad 1
## Step: AIC=11801.83
## Outstate ~ Expend + Private + Room.Board + perc.alumni + PhD +
       Grad.Rate + Personal + Terminal + S.F.Ratio + Accept + F.Undergrad +
##
##
       Apps
##
##
                 Df Sum of Sq
                                      RSS
                                            AIC
                  1 44900435 2922488298 11792
## + Top10perc
## + Top25perc
                  1 24513579 2942875154 11797
## <none>
                              2967388733 11802
## + Enroll
                      4741299 2962647434 11803
                  1
## + Books
                  1
                      1990742 2965397991 11803
## + P.Undergrad 1
                       288766 2967099967 11804
##
## Step: AIC=11791.98
## Outstate ~ Expend + Private + Room.Board + perc.alumni + PhD +
##
       Grad.Rate + Personal + Terminal + S.F.Ratio + Accept + F.Undergrad +
##
       Apps + Top10perc
##
                 Df Sum of Sq
                                      RSS
                      8945433 2913542865 11792
## + Enroll
## <none>
                              2922488298 11792
## + Books
                  1
                      4132382 2918355916 11793
## + Top25perc
                  1
                       361870 2922126428 11794
## + P.Undergrad 1
                       276700 2922211599 11794
##
## Step: AIC=11791.6
## Outstate ~ Expend + Private + Room.Board + perc.alumni + PhD +
##
       Grad.Rate + Personal + Terminal + S.F.Ratio + Accept + F.Undergrad +
##
       Apps + Top10perc + Enroll
##
                 Df Sum of Sq
##
                                     RSS
                                            ATC
## <none>
                              2913542865 11792
## + Books
                      4112173 2909430692 11792
                  1
## + Top25perc
                  1
                       845842 2912697023 11793
## + P.Undergrad 1
                       125055 2913417810 11794
##
## Call:
  lm(formula = Outstate ~ Expend + Private + Room.Board + perc.alumni +
       PhD + Grad.Rate + Personal + Terminal + S.F.Ratio + Accept +
##
       F.Undergrad + Apps + Top1Operc + Enroll, data = college)
##
## Coefficients:
## (Intercept)
                     Expend
                              PrivateYes
                                            Room.Board perc.alumni
##
   -1817.0401
                     0.2004
                               2256.9455
                                                0.8742
                                                            41.9501
##
           PhD
                  Grad.Rate
                                 Personal
                                              Terminal
                                                          S.F.Ratio
##
                    23.8320
                                               22.9730
                                                           -47.0056
       12.6951
                                  -0.2478
               F.Undergrad
##
                                             Top10perc
        Accept
                                     Apps
                                                             Enroll
        0.8024
                    -0.0957
                                               23.6553
##
                                  -0.2999
                                                            -0.5373
```

(b)

```
library(gam)
## Warning: package 'gam' was built under R version 3.4.4
## Loading required package: splines
## Loaded gam 1.15
GAM <- gam(Outstate ~ s(Expend, df = 1) + Private + s(Room.Board, df = 5) + s(perc.alumni, df = 3)
          + s(PhD, df = 1) + s(Grad.Rate, df = 5) + s(Personal, df = 2) + s(Terminal, df = 5)
           + s(S.F.Ratio, df = 4) + s(Accept, df = 1) + s(F.Undergrad, df = 1) + s(Apps, df = 1)
          + s(Top10perc, df = 5) + s(Enroll, df = 1), data = college)
summary(GAM)
## Call: gam(formula = Outstate ~ s(Expend, df = 1) + Private + s(Room.Board,
       df = 5) + s(perc.alumni, df = 3) + s(PhD, df = 1) + s(Grad.Rate,
       df = 5) + s(Personal, df = 2) + s(Terminal, df = 5) + s(S.F.Ratio,
##
##
       df = 4) + s(Accept, df = 1) + s(F.Undergrad, df = 1) + s(Apps,
       df = 1) + s(Top10perc, df = 5) + s(Enroll, df = 1), data = college)
##
## Deviance Residuals:
##
       Min
                  1Q
                       Median
                                    3Q
                                            Max
## -6695.43 -1225.92
                       -32.41 1278.83
                                       9503.91
##
## (Dispersion Parameter for gaussian family taken to be 3547626)
##
       Null Deviance: 12559297426 on 776 degrees of freedom
## Residual Deviance: 2625227130 on 739.9955 degrees of freedom
## AIC: 13961.67
##
## Number of Local Scoring Iterations: 2
## Anova for Parametric Effects
                                  Sum Sq
                                            Mean Sq
                                                      F value
## s(Expend, df = 1)
                            1 5805174796 5805174796 1636.3549 < 2.2e-16 ***
## Private
                            1 1728385723 1728385723 487.1951 < 2.2e-16 ***
## s(Room.Board, df = 5)
                                         921085142 259.6342 < 2.2e-16 ***
                            1 921085142
## s(perc.alumni, df = 3)
                            1 387400810
                                          387400810 109.2000 < 2.2e-16 ***
## s(PhD, df = 1)
                            1 197859484
                                         197859484
                                                      55.7724 2.295e-13 ***
## s(Grad.Rate, df = 5)
                            1 142721584
                                         142721584
                                                      40.2302 3.928e-10 ***
## s(Personal, df = 2)
                                                       8.3617 0.003945 **
                            1
                                29664081
                                           29664081
## s(Terminal, df = 5)
                            1
                                27975896
                                           27975896
                                                       7.8858 0.005114 **
## s(S.F.Ratio, df = 4)
                            1
                                20261176
                                           20261176
                                                       5.7112 0.017106 *
## s(Accept, df = 1)
                                17462856
                                           17462856
                                                       4.9224 0.026813 *
                            1
## s(F.Undergrad, df = 1)
                            1
                                64690780
                                           64690780
                                                      18.2350 2.207e-05 ***
## s(Apps, df = 1)
                                29809487
                                           29809487
                                                       8.4027 0.003858 **
                            1
## s(Top10perc, df = 5)
                            1
                                38635285
                                           38635285
                                                      10.8905 0.001013 **
## s(Enroll, df = 1)
                            1
                                 4234811
                                            4234811
                                                       1.1937 0.274939
## Residuals
                          740 2625227130
                                            3547626
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Anova for Nonparametric Effects
```

```
##
                       Npar Df Npar F
                                      Pr(F)
## (Intercept)
## s(Expend, df = 1)
                             0 48.176 0.0005853 ***
## Private
## s(Room.Board, df = 5)
                            4 2.395 0.0490939 *
## s(perc.alumni, df = 3)
                           2 0.686 0.5037140
## s(PhD, df = 1)
                            0 3.447 2.448e-05 ***
## s(Grad.Rate, df = 5)
                            4 2.400 0.0487172 *
## s(Personal, df = 2)
                            1 5.743 0.0167989 *
                           4 3.061 0.0162070 *
## s(Terminal, df = 5)
## s(S.F.Ratio, df = 4)
                           3 10.435 9.902e-07 ***
## s(Accept, df = 1)
                            0 20.367 0.0012529 **
## s(F.Undergrad, df = 1) 0 4.933 0.0031433 **
## s(Apps, df = 1)
                            0 16.246 0.0029753 **
## s(Top10perc, df = 5)
                           4 1.426 0.2234982
## s(Enroll, df = 1)
                             0 7.091 0.0006335 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```