

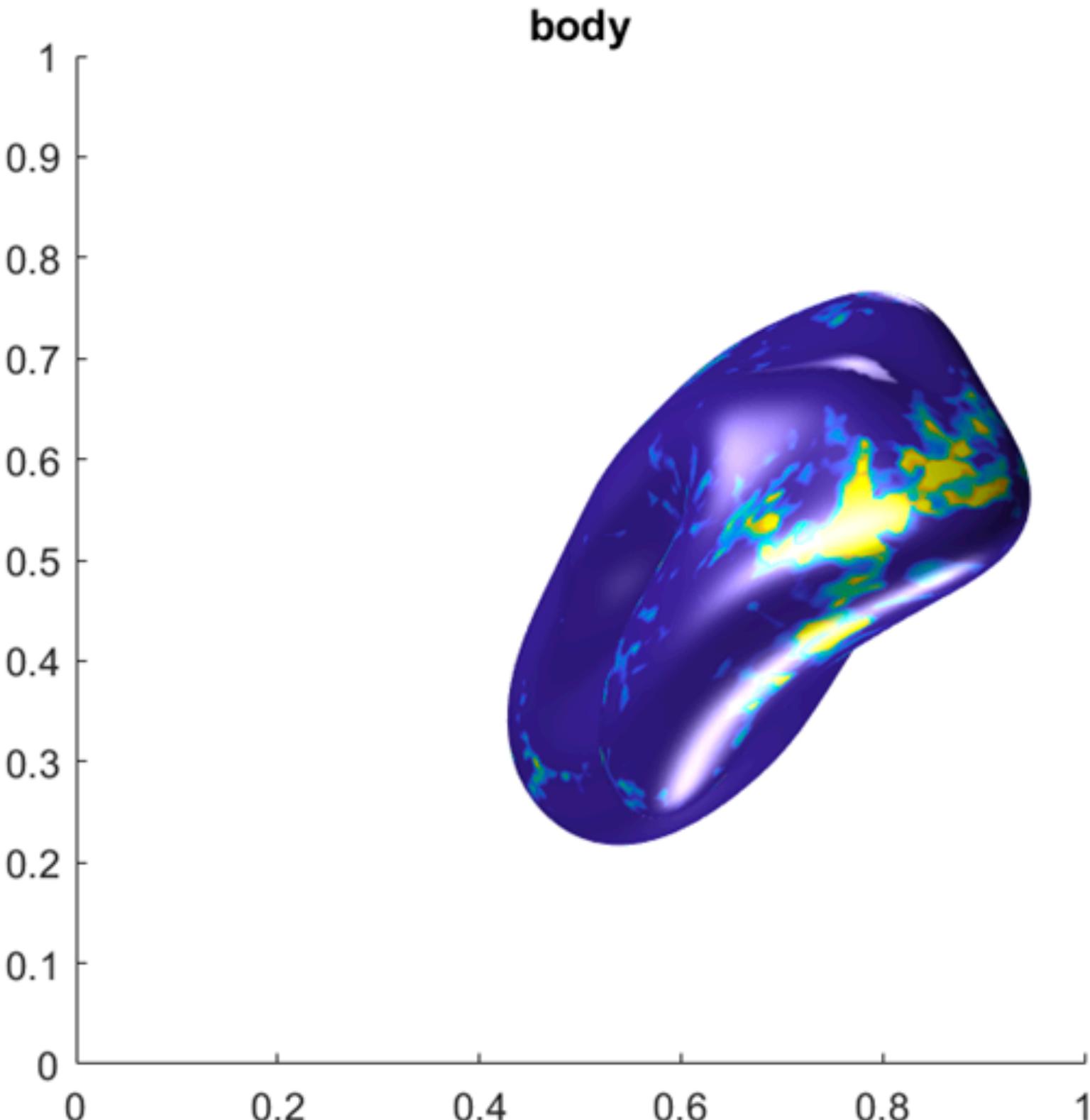
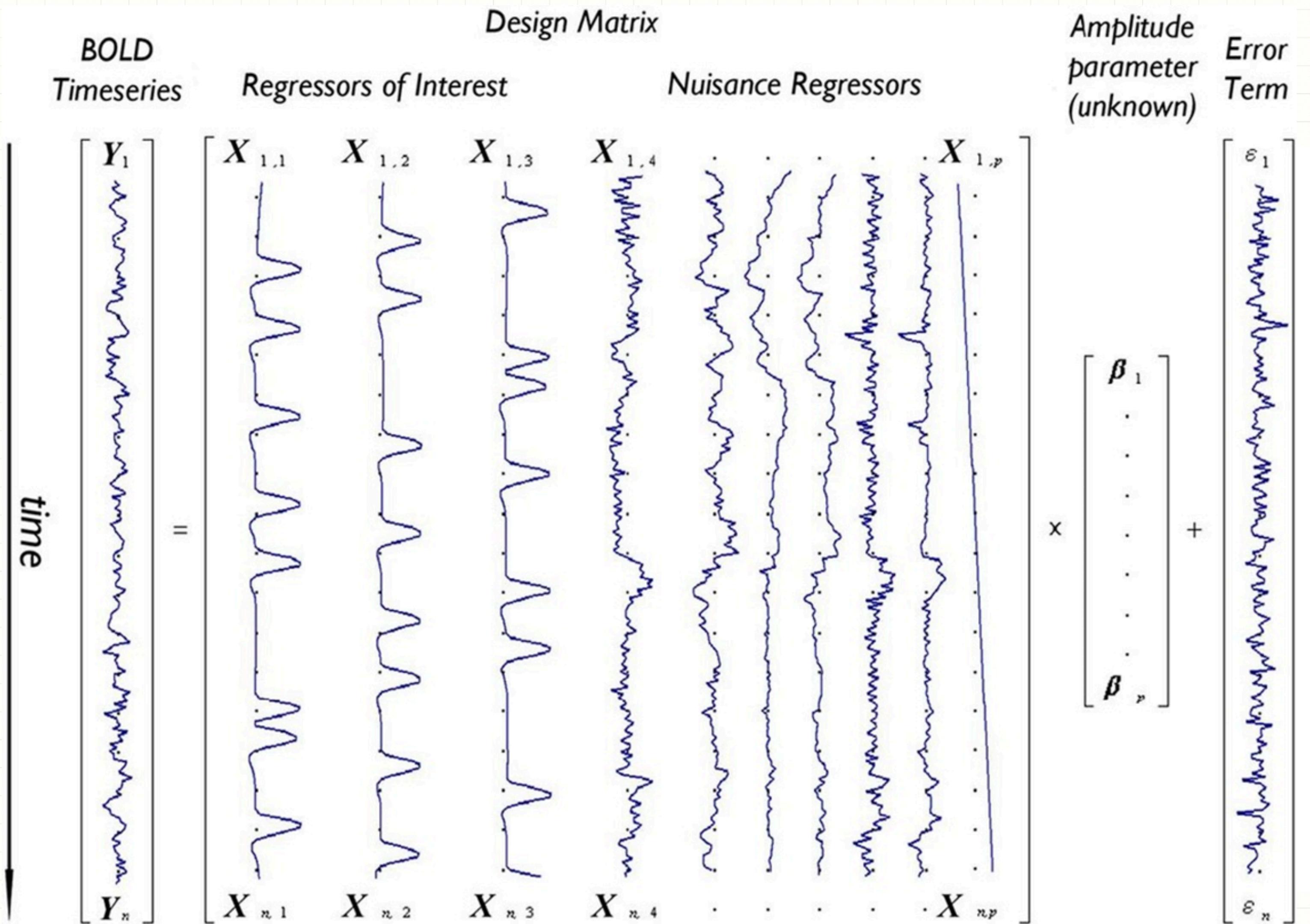
# Multivariate Analysis in fMRI 功能性磁共振成像中的多变量分析

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# 复习：一般线性模型



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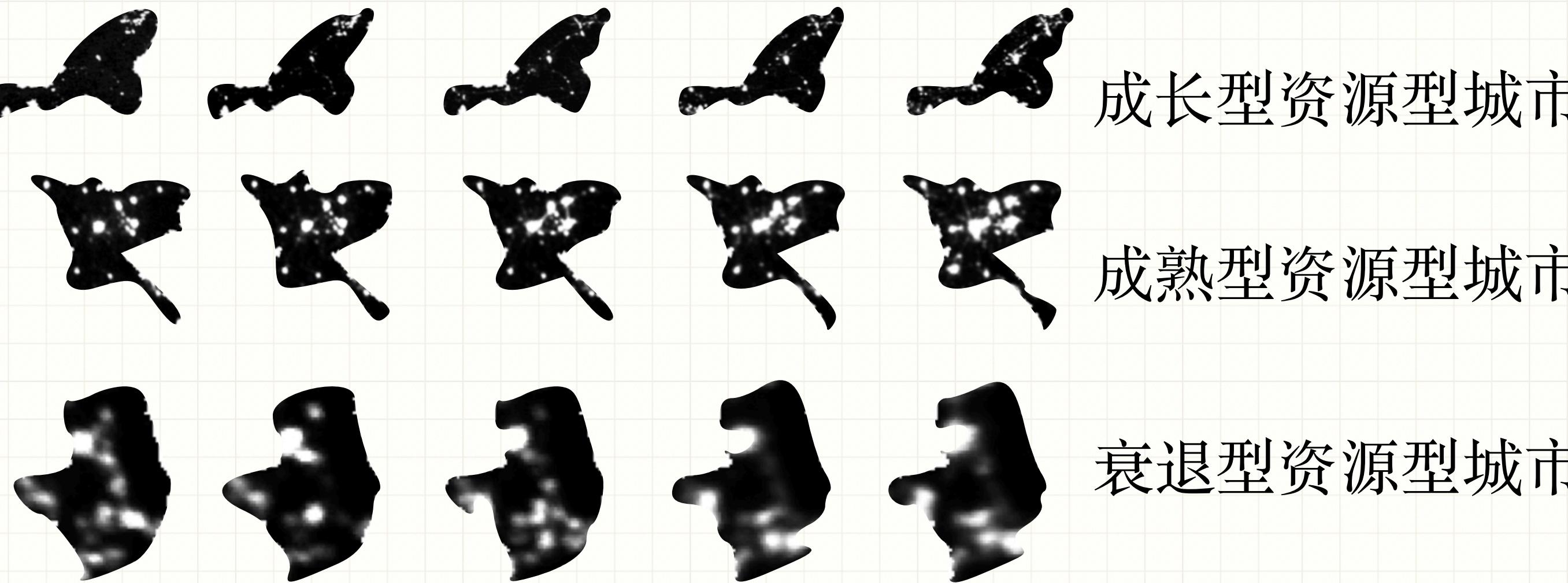


# Multivariate Analysis Concept



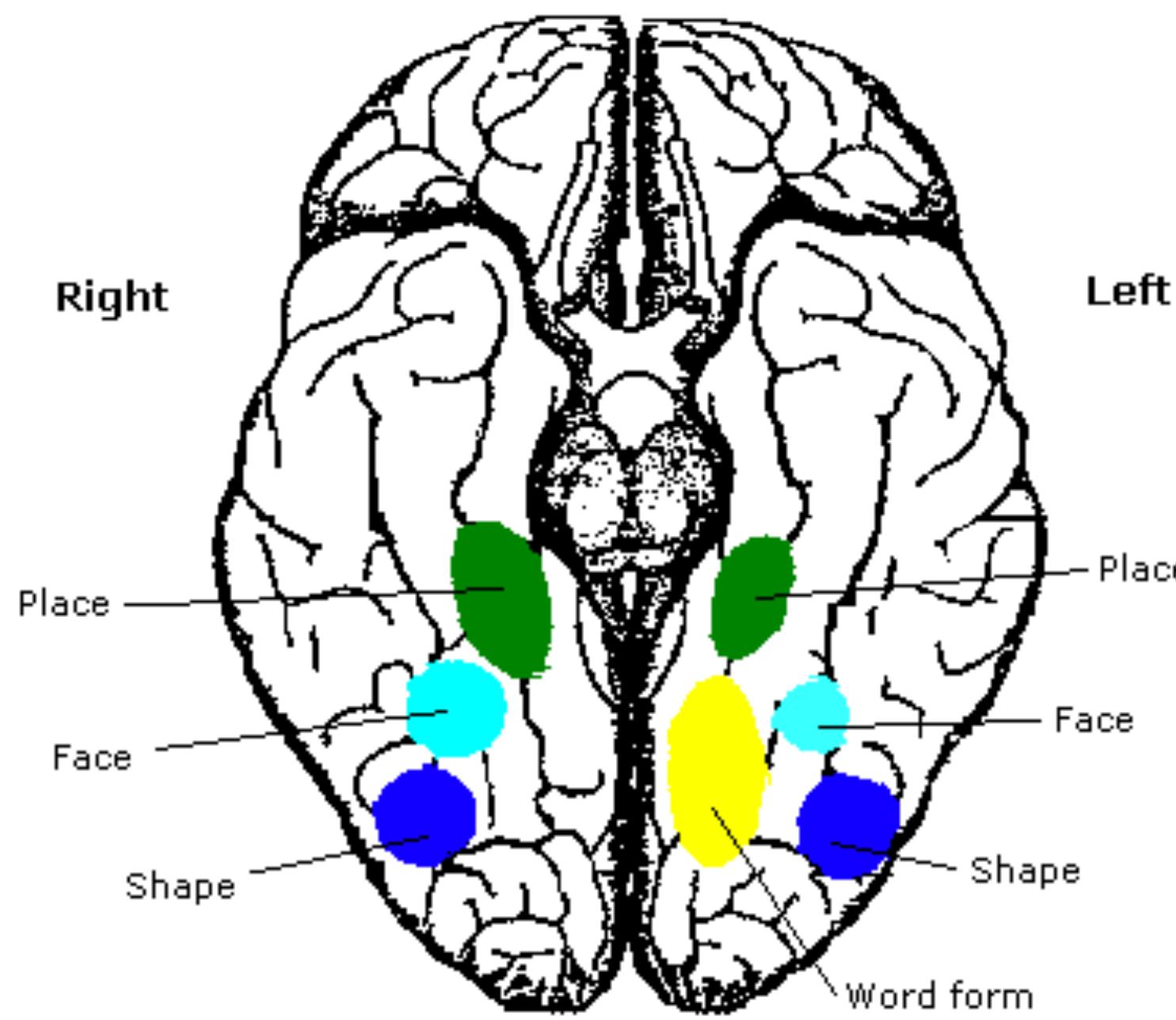
Univariate Analysis  
**Where** is the area?  
**How** strong the light is?

基于 OLS 夜间灯光的全国资源型城市空间结构时空演化研究



Multivariate Analysis  
The **Structure** of the light.  
The **Information** represented in a region!

# Multivariate Analysis Concept

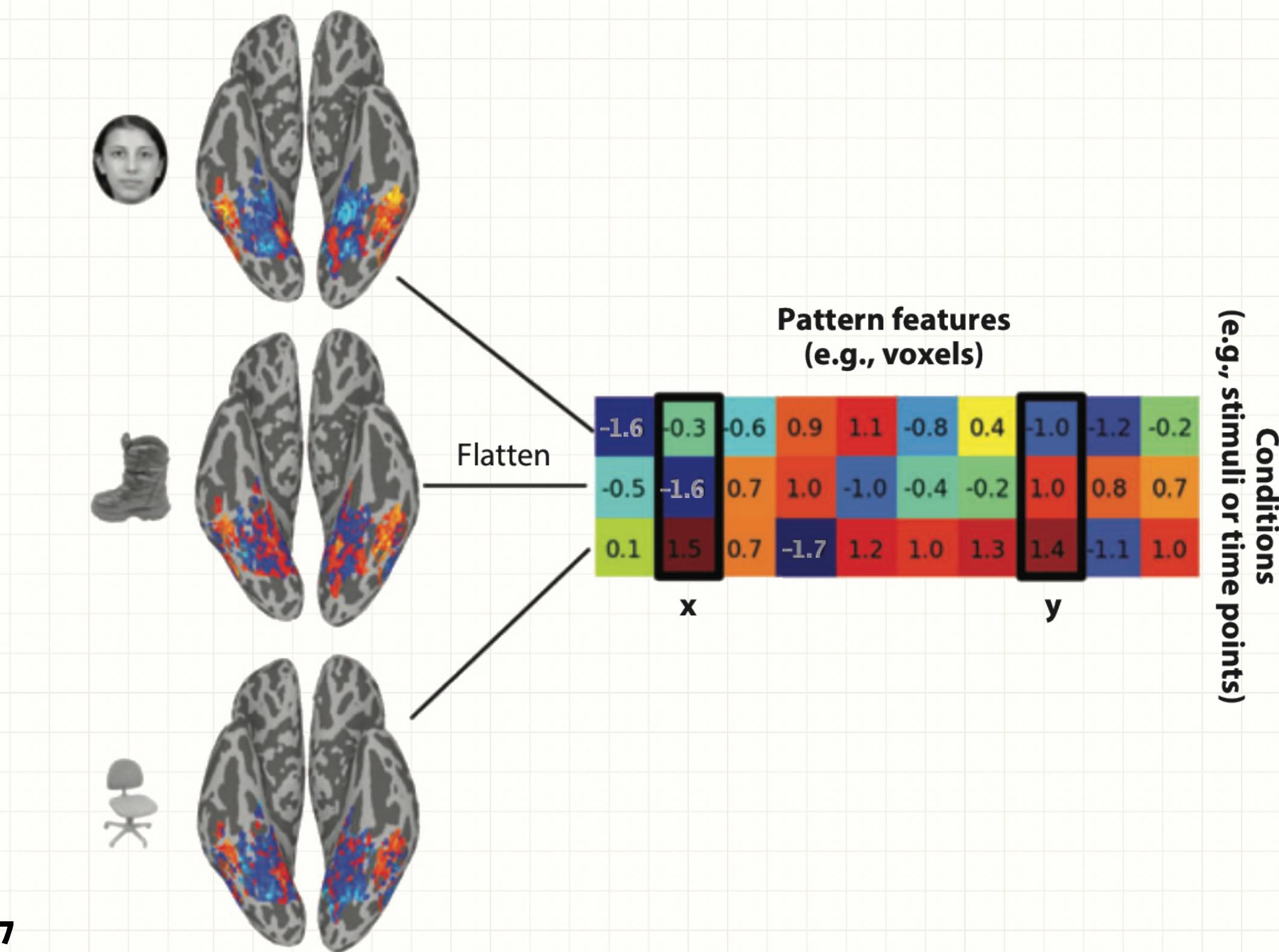


相同的步骤在每一个体素重复一次

# Univariate fMRI

# Where is the area?

# How strong its response is?



# Multivariate Analysis in fMRI

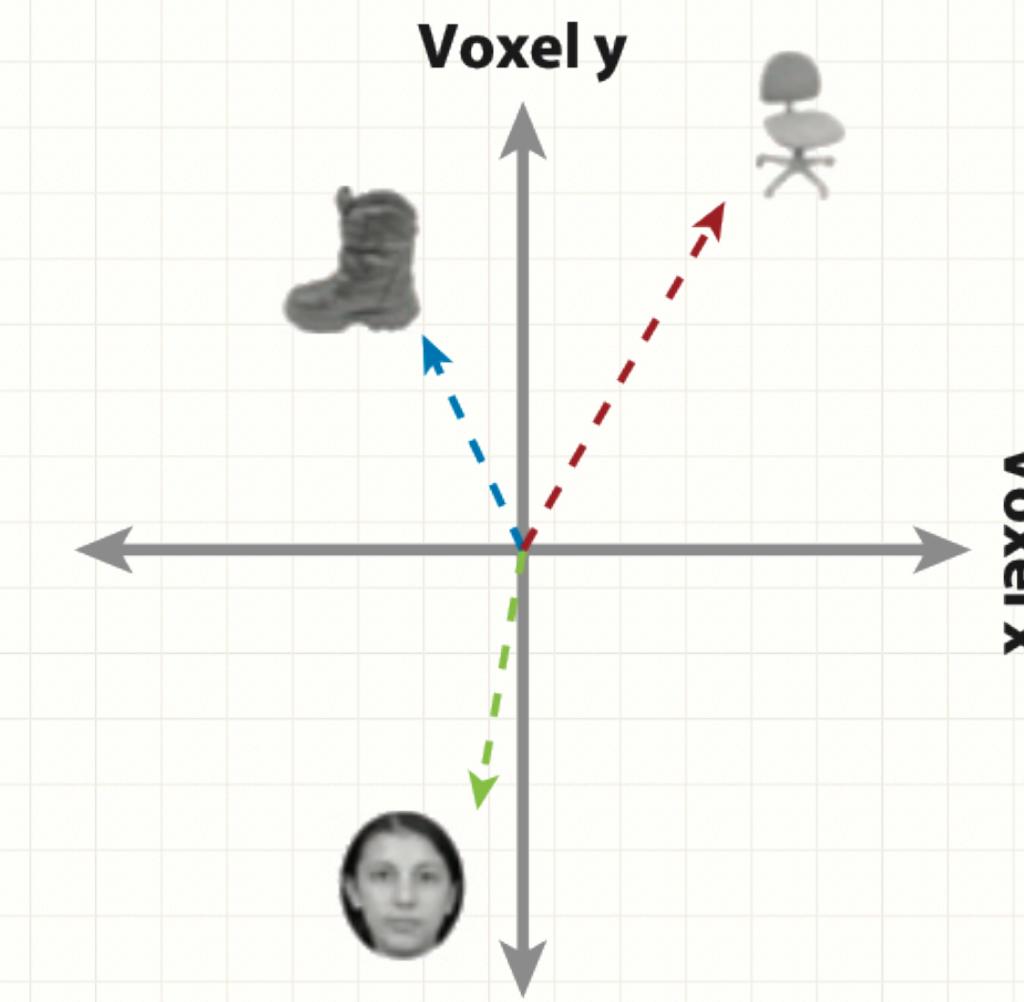
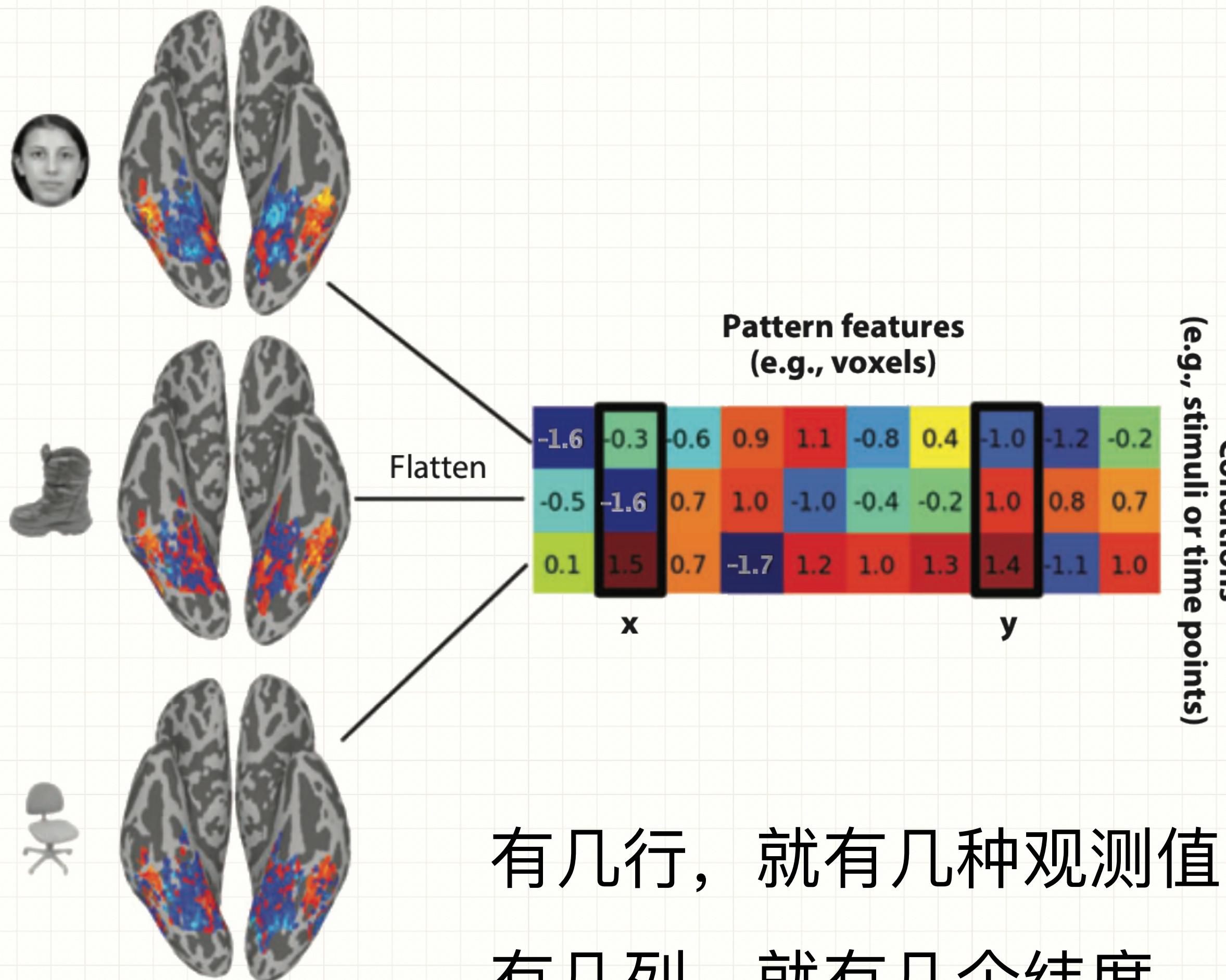
# The **Structure** of the response! 激活模式

# The **Information** represented in a region!

# Multivariate Analysis Concept



## REPRESENTATIONAL SPACES



有几行，就有几种观测值，在这里是三张图片的Beta

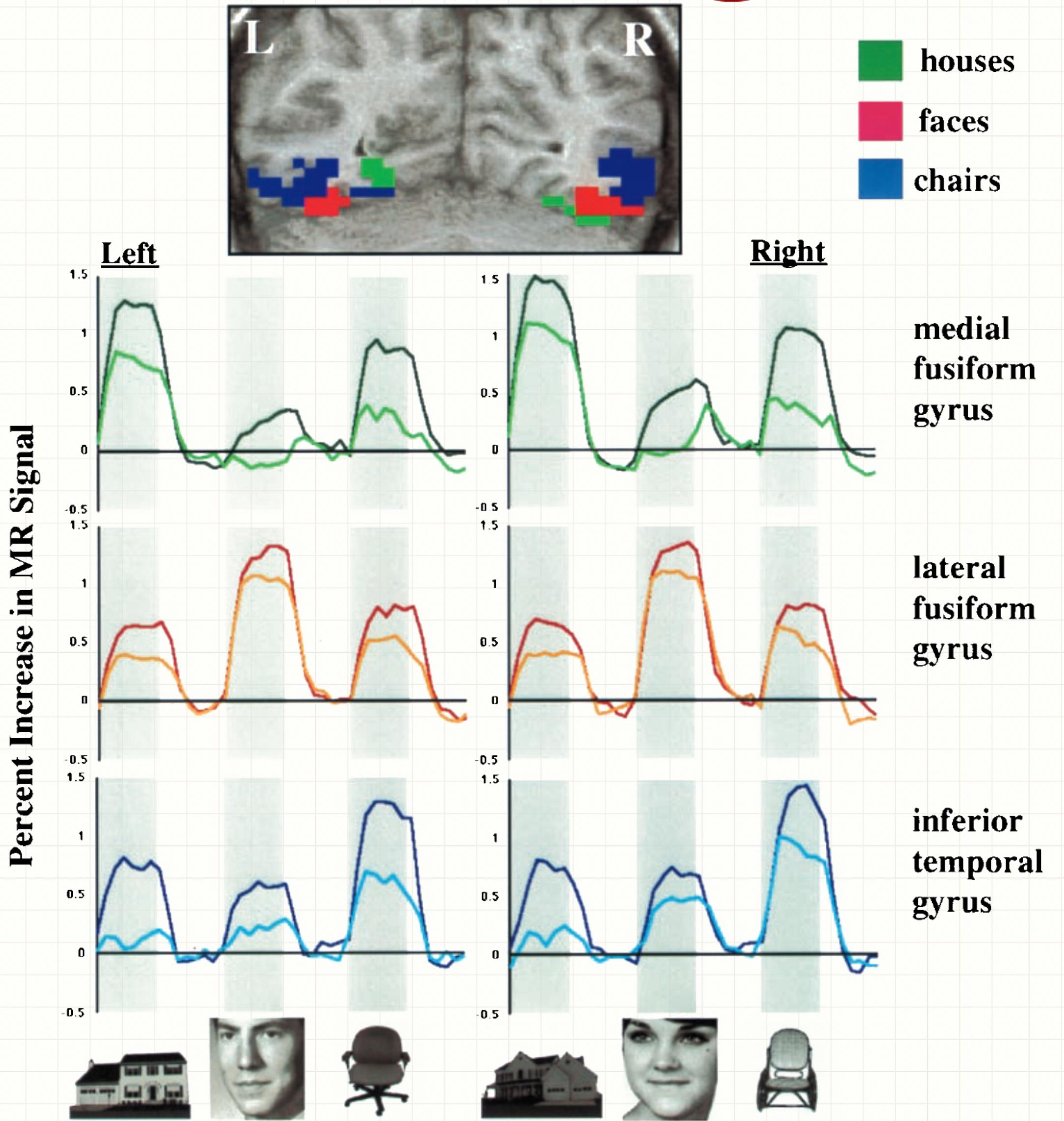
有几列，就有几个纬度，在这里是皮层的体素数

# Why Multivariate Analysis?



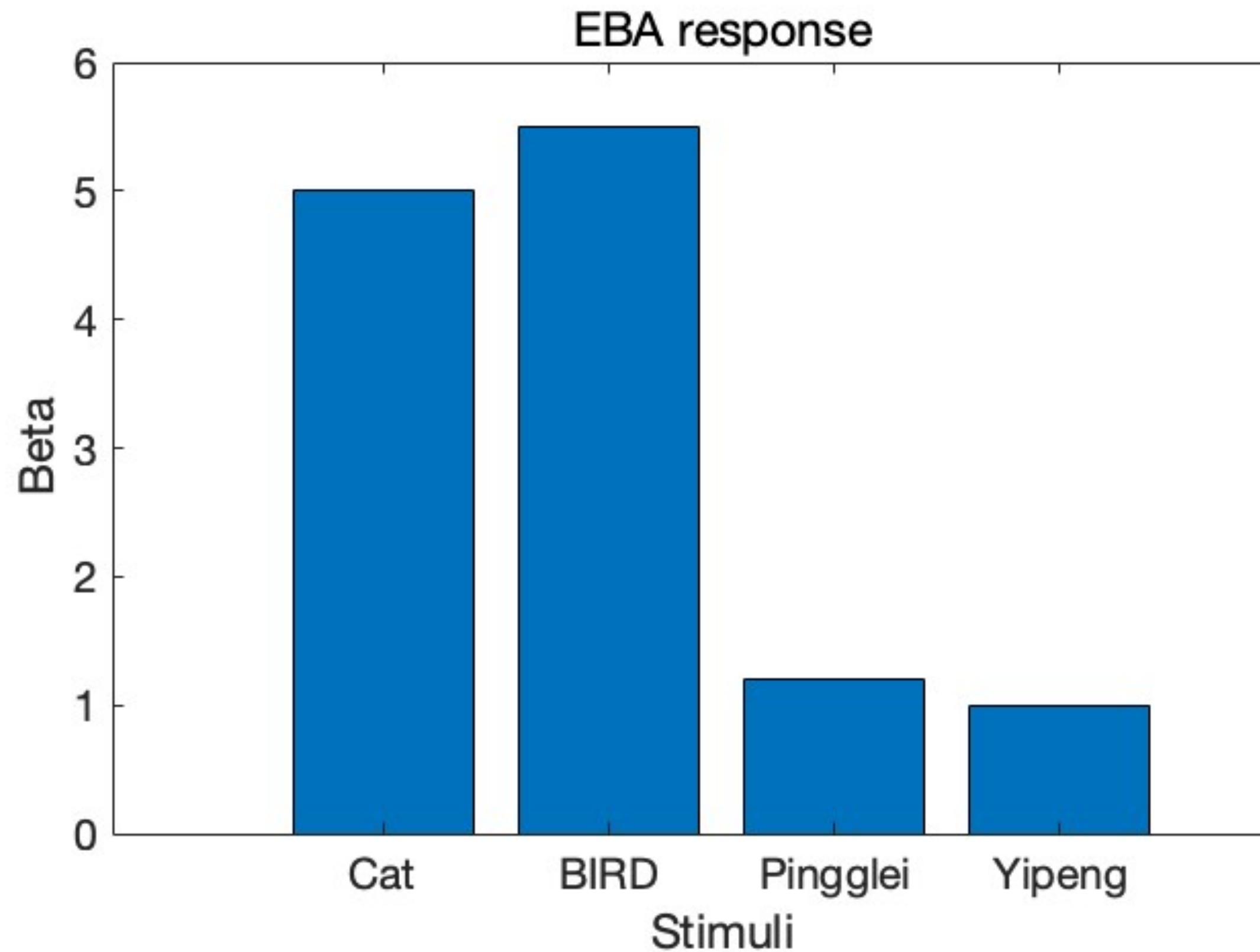
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The representation of an object is not restricted to a region that responds maximally to that object, but rather is **distributed** across a broader expanse of cortex.

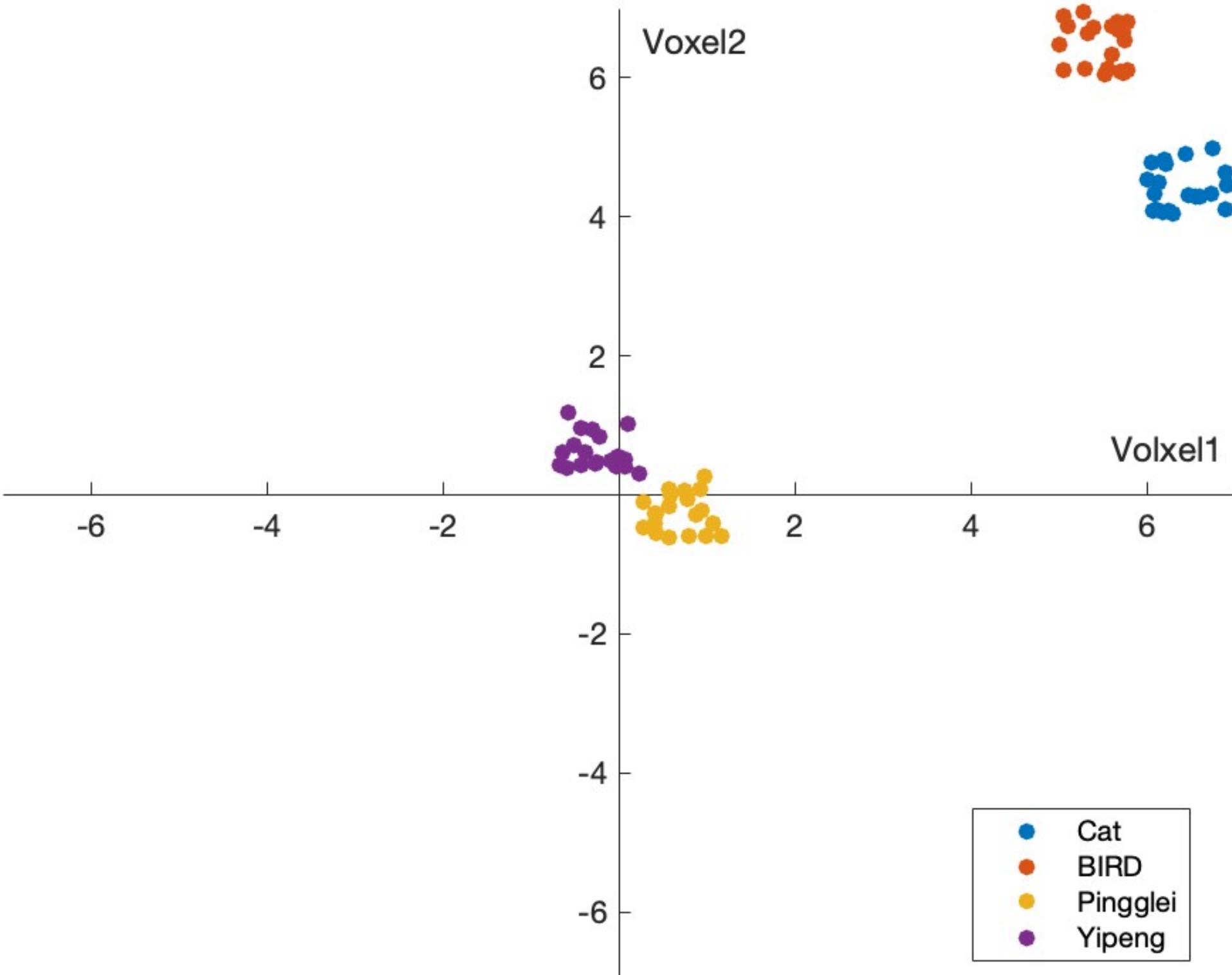


# Why Multivariate Analysis?

Information lost in Univariate analysis



A region's function was identified by determining which task activated it most strongly



what information is represented in a region, in terms of brain states associated with distinct patterns of activity, and how that information is encoded and organized

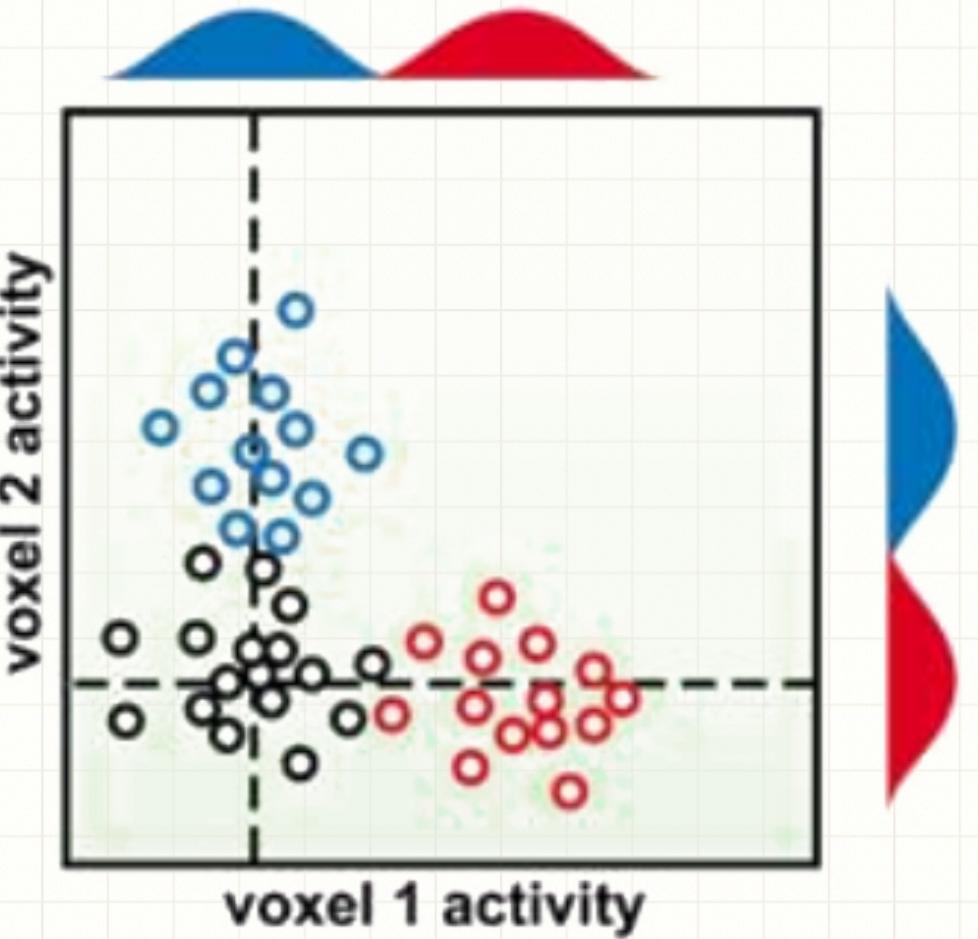
# Why Multivariate Analysis?

Information lost in Univariate analysis

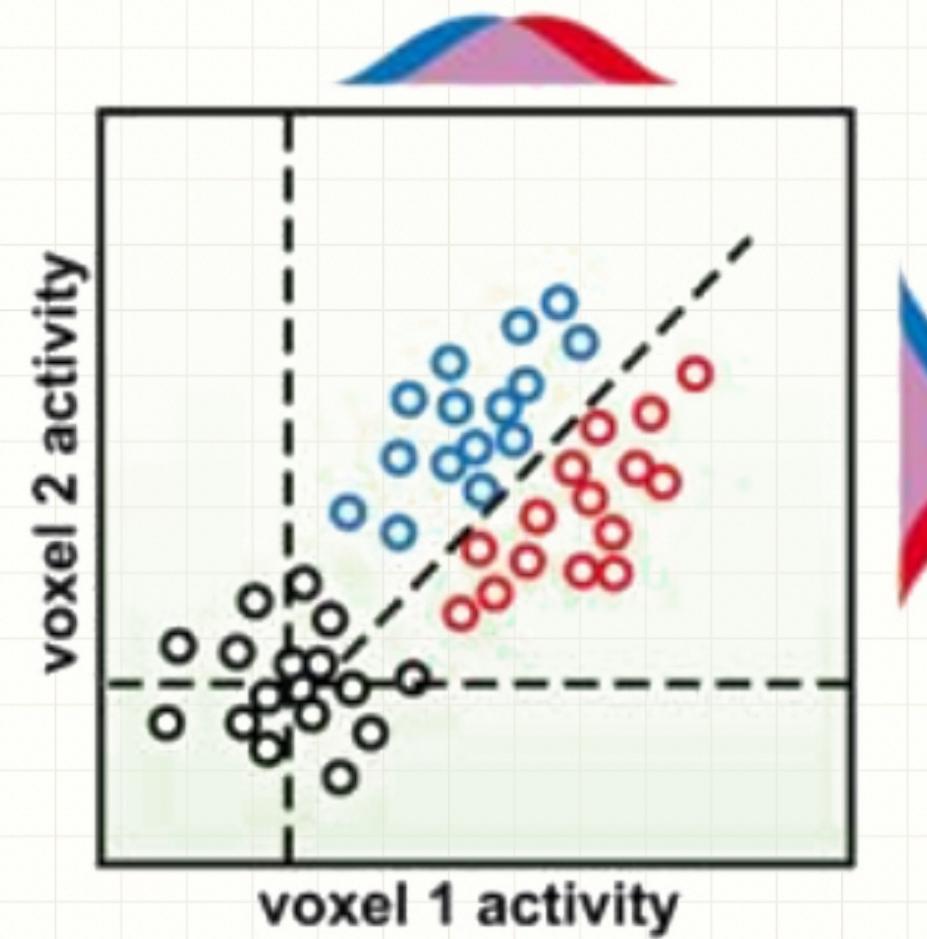


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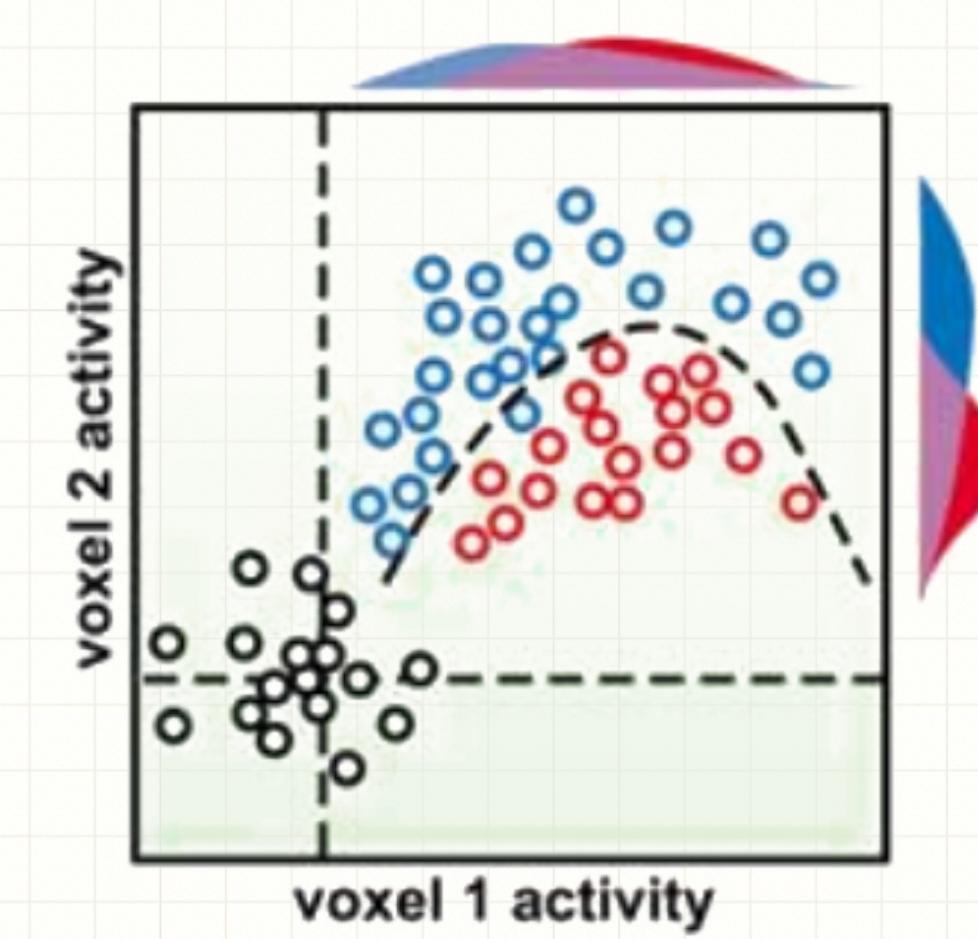
a. Ideal Univariate Situation



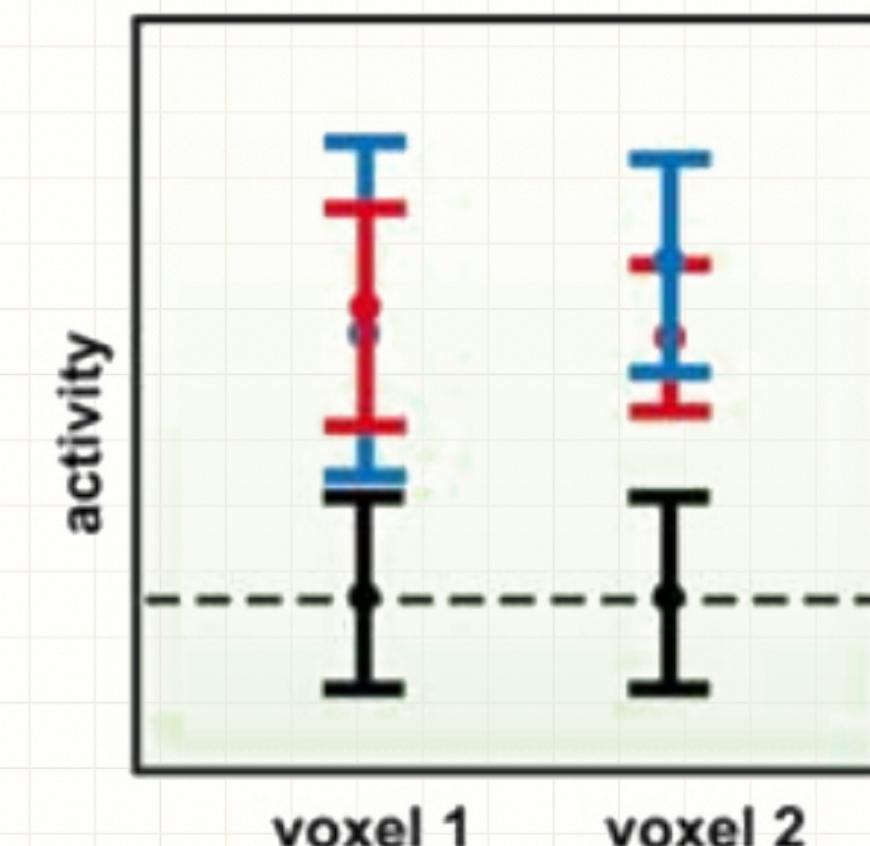
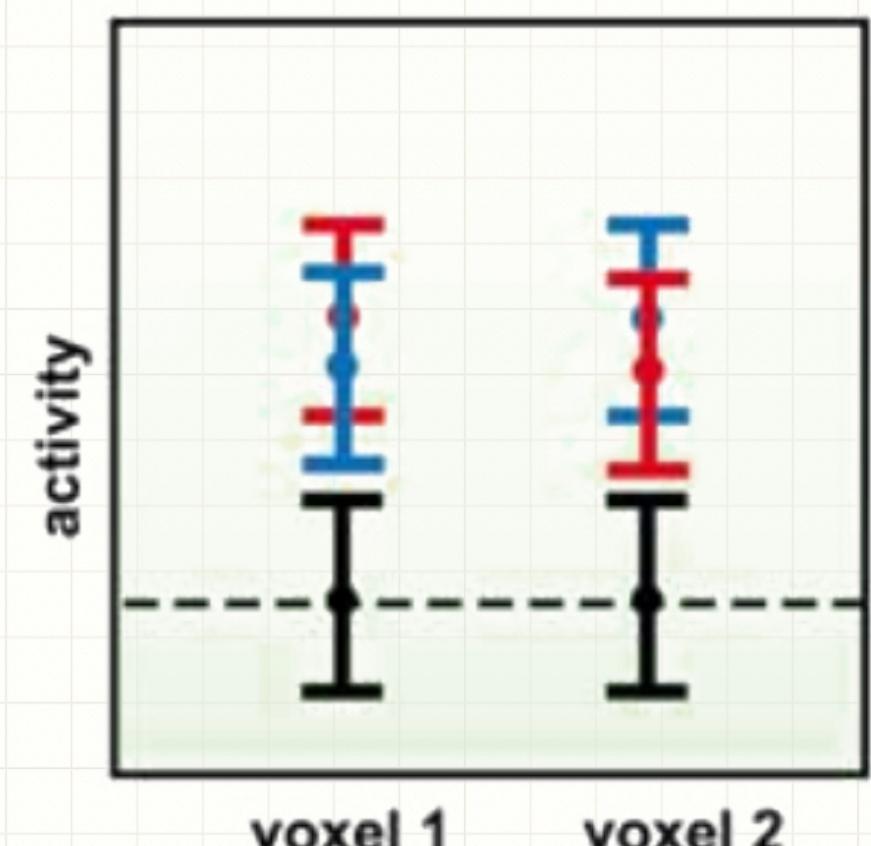
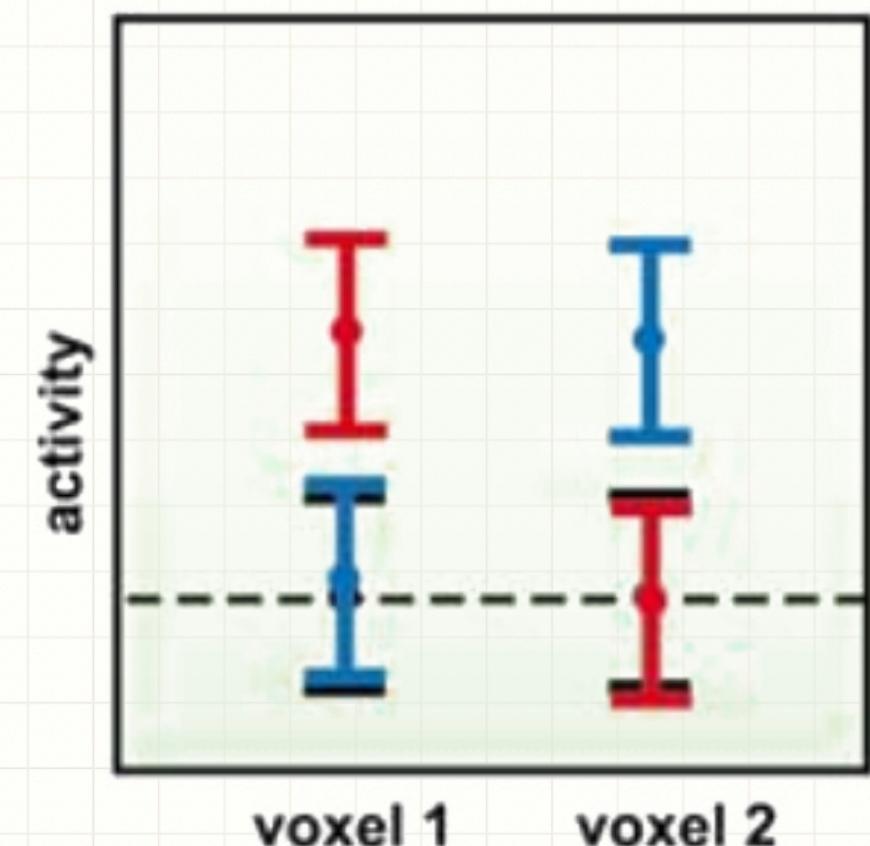
b. Linearly Separable



c. Nonlinearly Separable

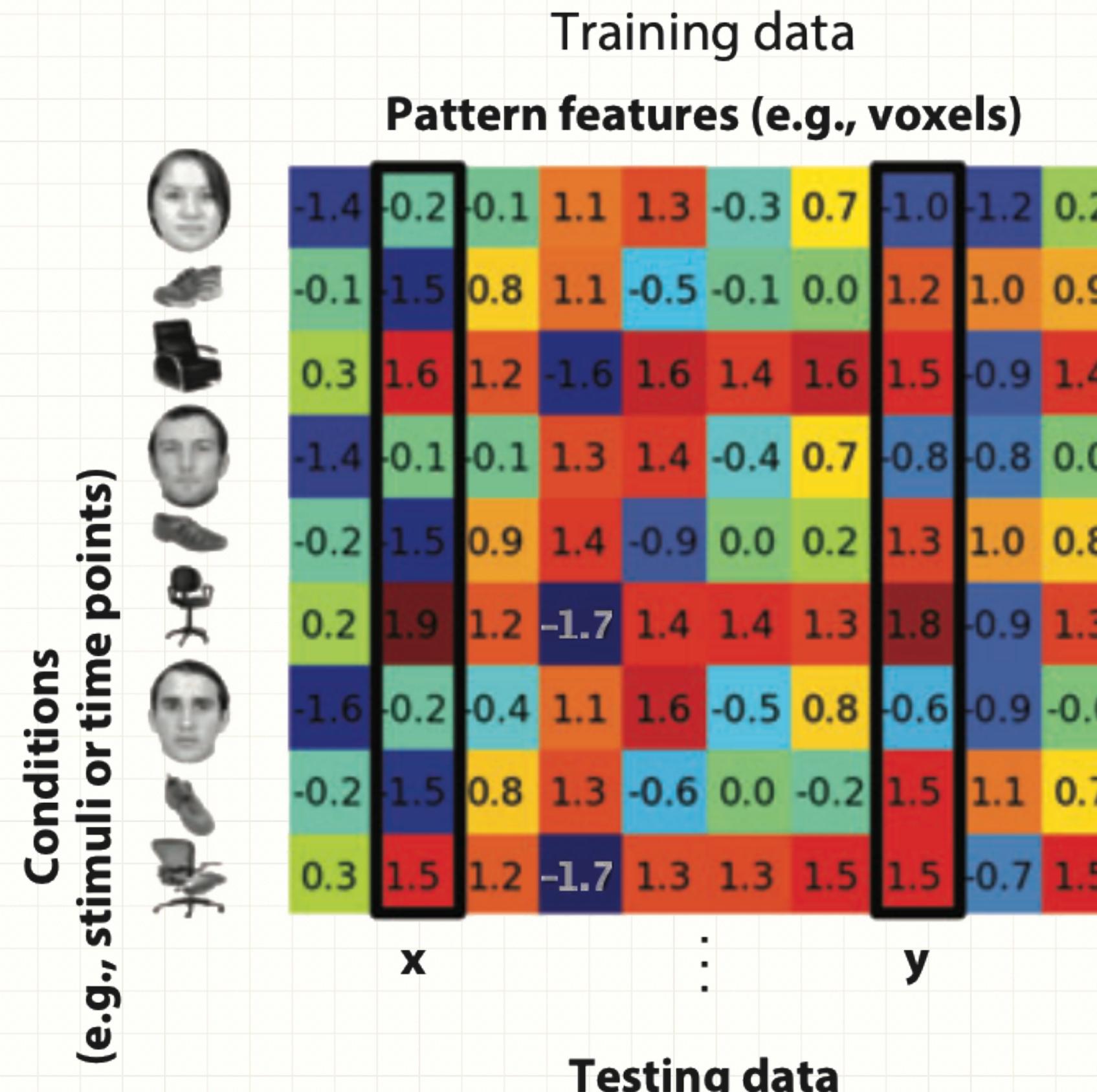


- Condition A
- Condition B
- Baseline

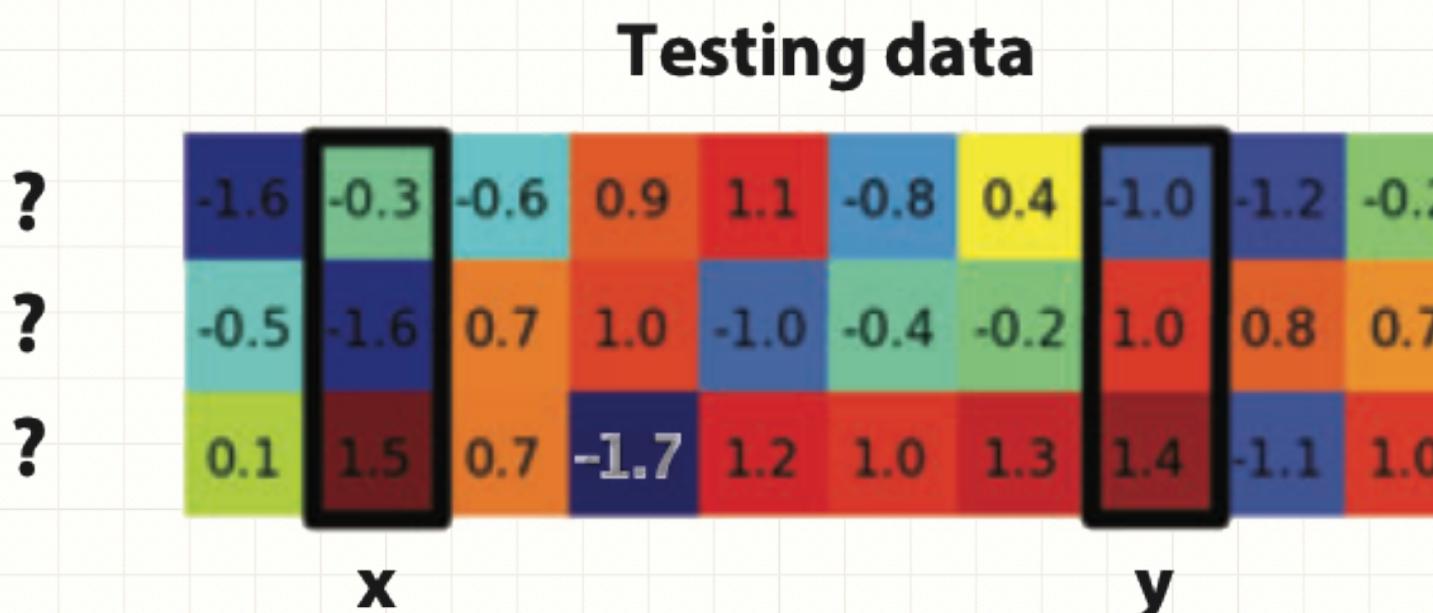
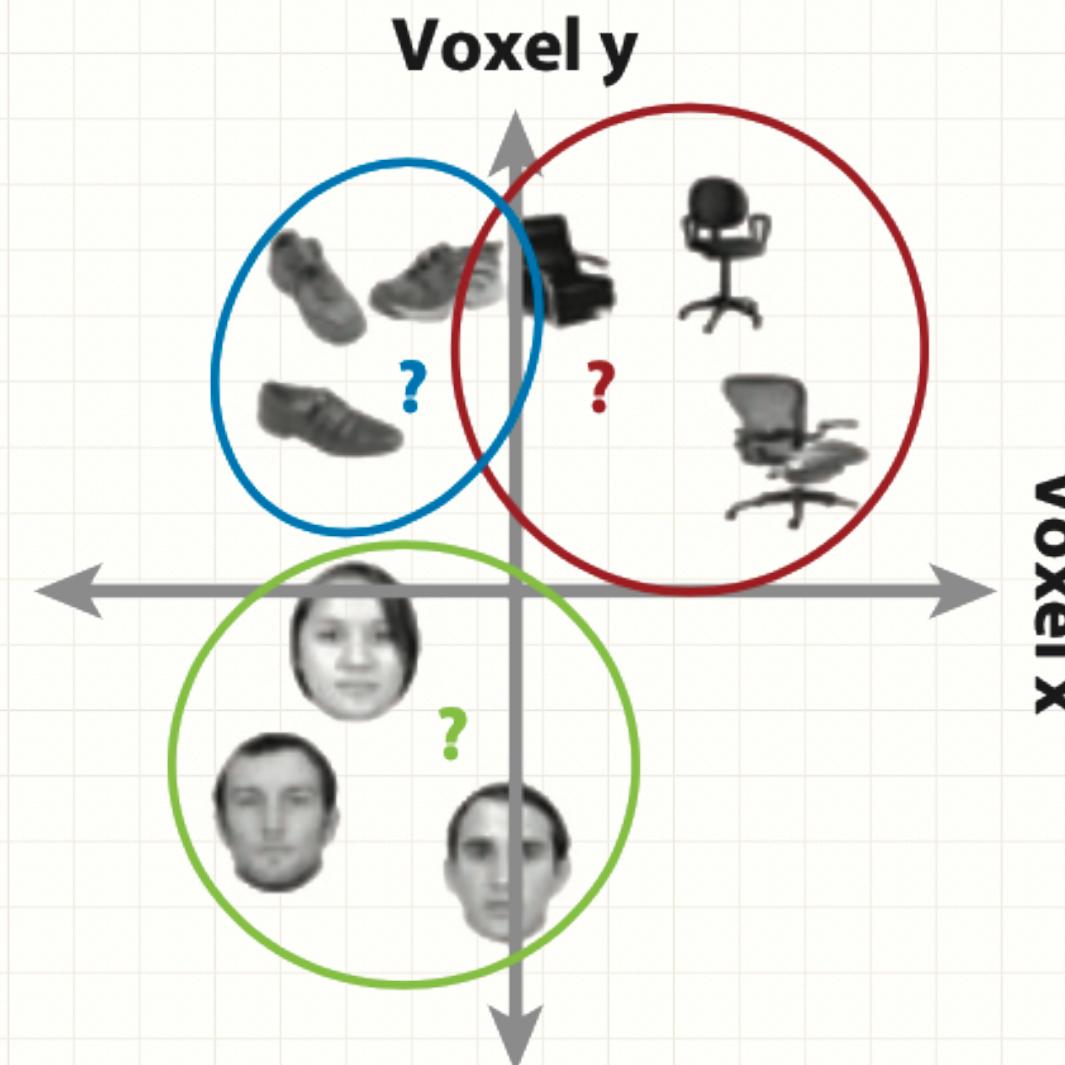


Cox 2003 neuroimage

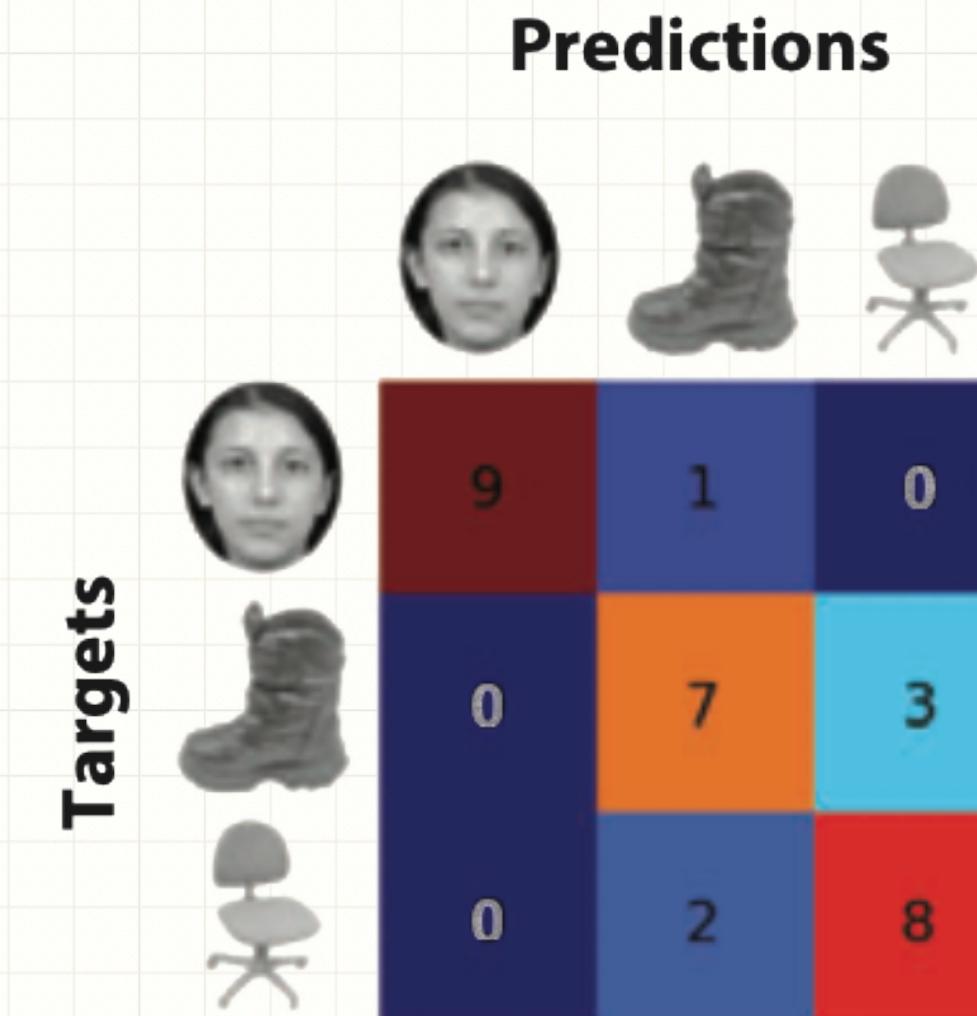
# Multivariate Analysis - Classification



Classification



Classification confusion matrix



# Multivariate Analysis - Classification



- One-nearest-neighbor(1NN): classified a test response vector as the category for the training data vector that was closest in the neural representational space
- Support vector machine(SVM): fine-tune the position of the decision surface on the basis of the vectors that are closest to the surface, i.e., the support vectors, by maximizing the distances from the surface to these borderline cases
- Linear discriminant analysis (LDA), K-nearest-neighbor(KNN)...

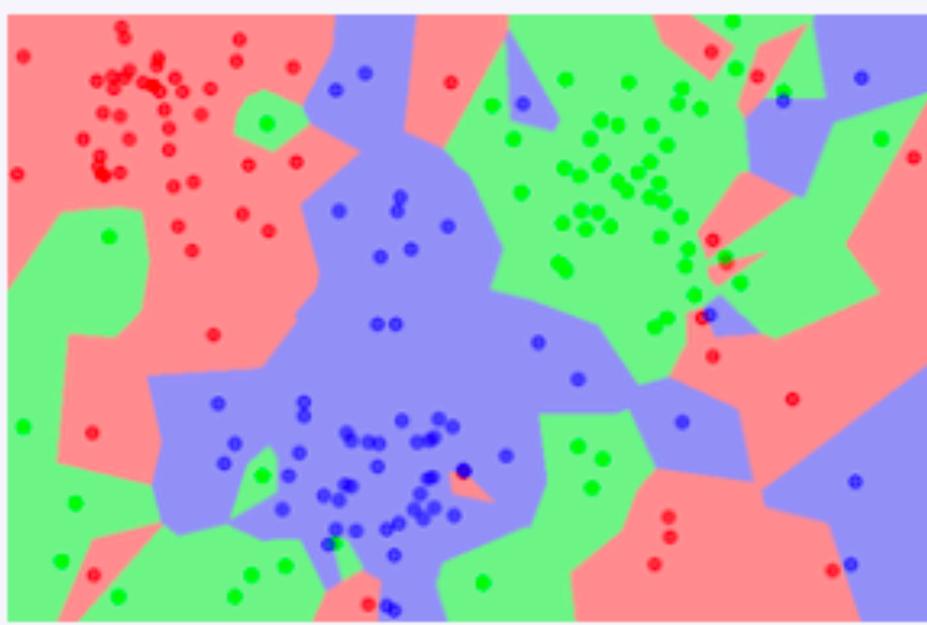


Fig. 2. The 1NN classification map.

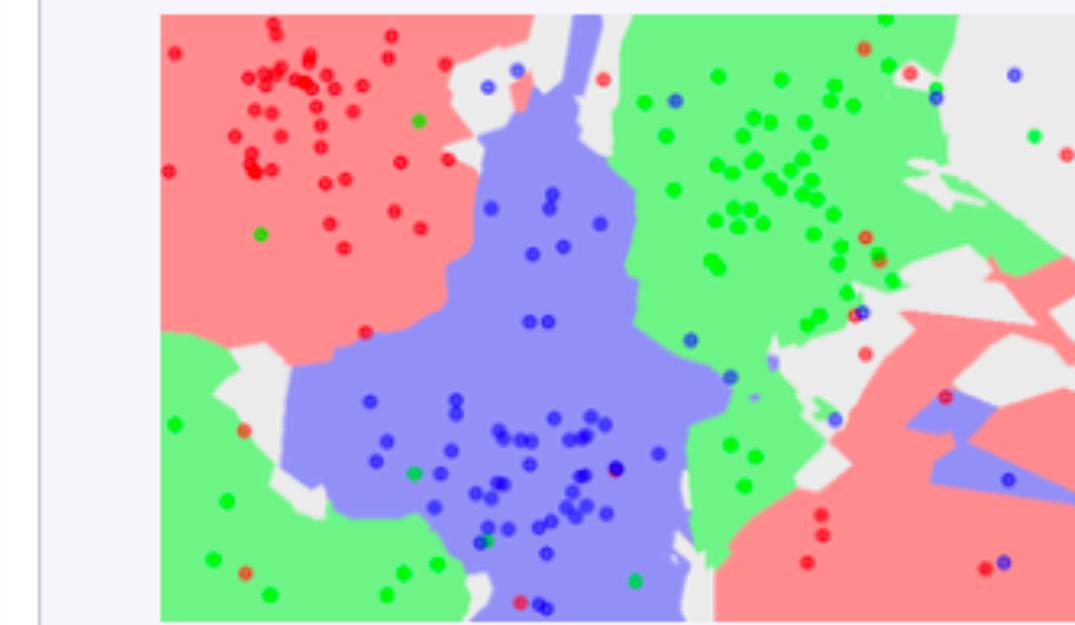
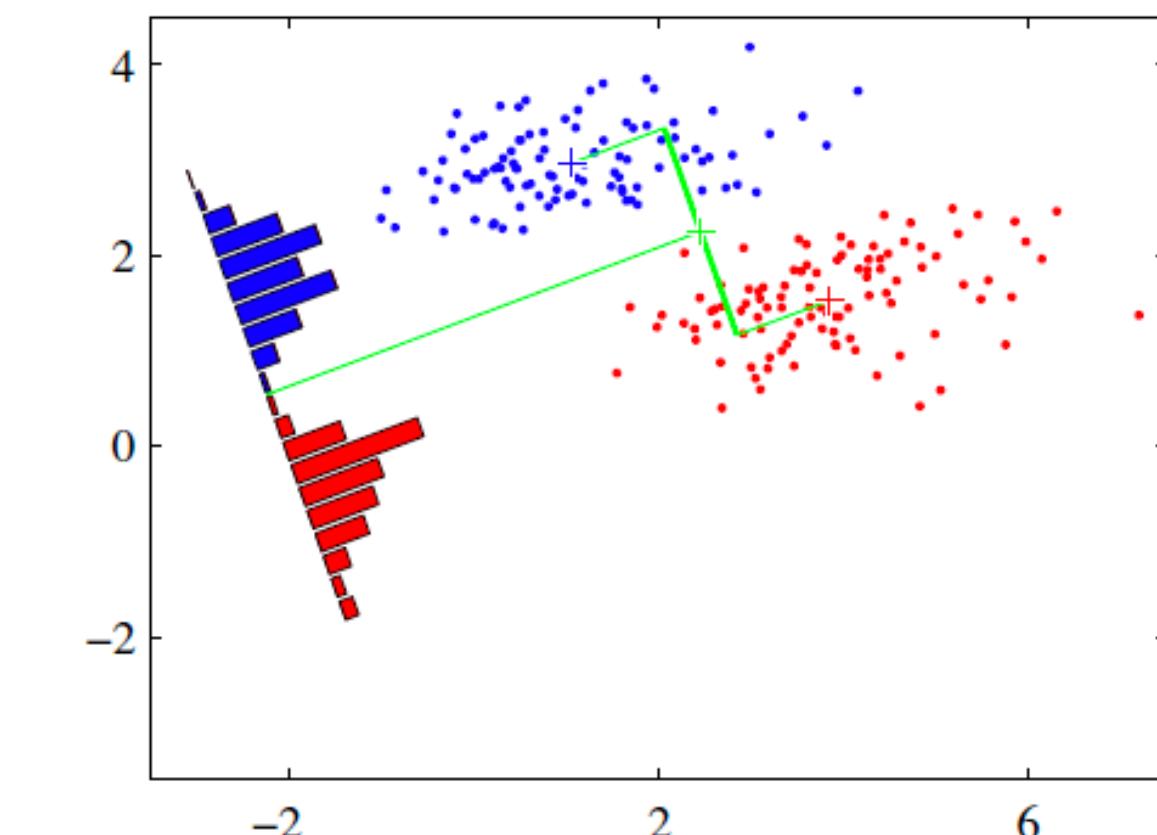
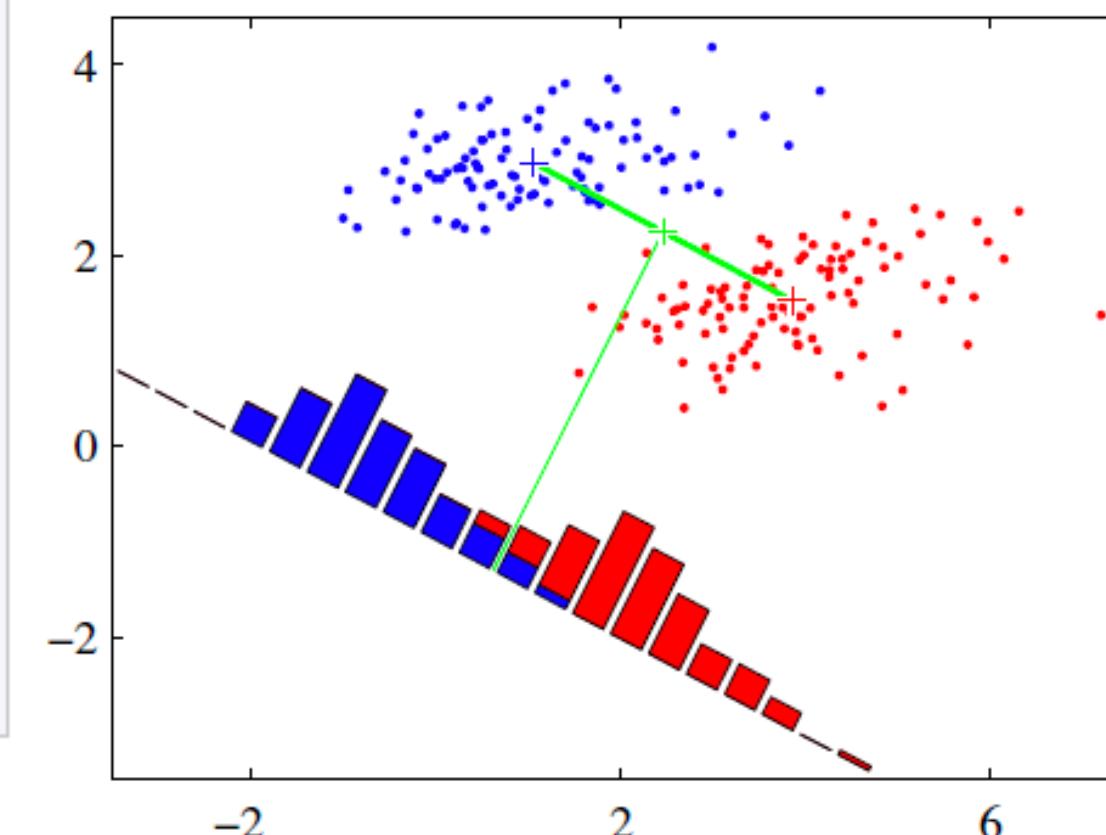


Fig. 3. The 5NN classification map.



# Multivariate Analysis - Classification

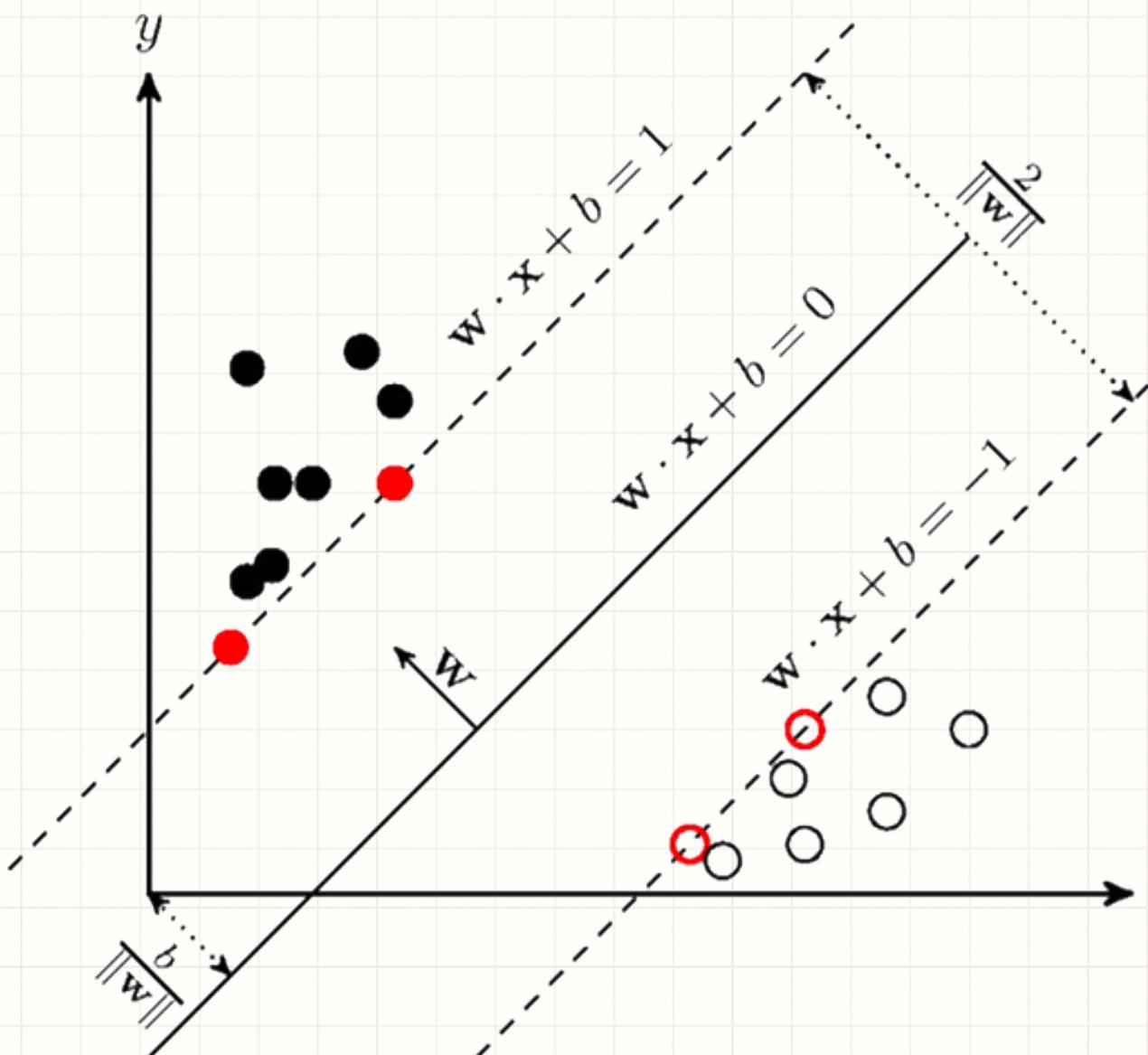
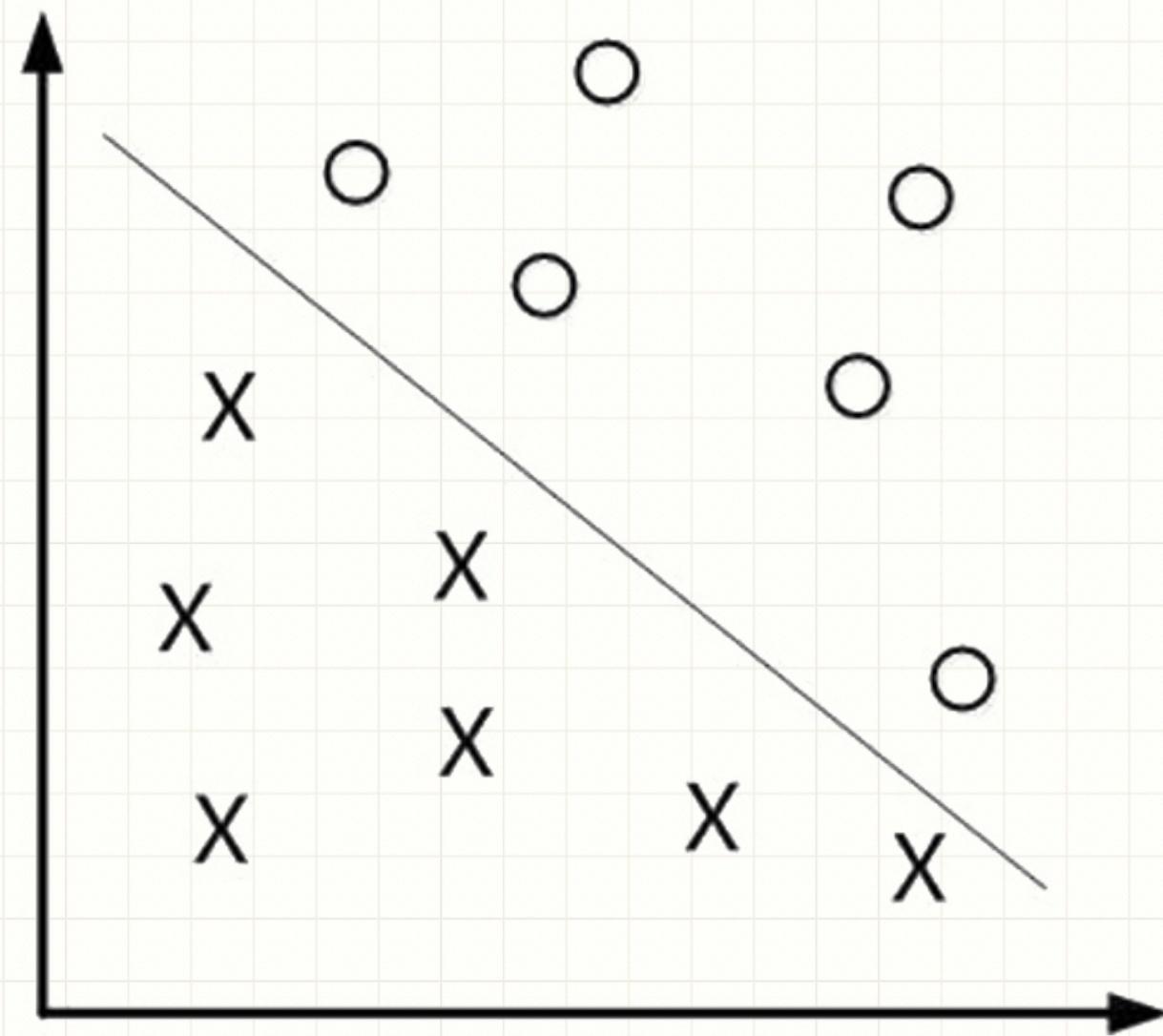


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## SVM的数学模型

一个线性分类器的学习目标便是要在n维的数据空间中找到一个超平面（hyper plane），这个超平面的方程可以表示为：

$$w^T x + b = 0$$



这个超平面可以用分类函数  $f(x) = w^T x + b$  表示，当  $f(x)=0$  的时候， $x$  便是位于超平面上的点，而  $f(x)>0$  的点对应  $y=1$  的数据点， $f(x)$  小于 0 的点对应  $y=-1$  的点

svm PPT来源：刘燮仪

# Multivariate Analysis - Classification



## SVM的数学模型

在超平面 $w^T x + b = 0$ 确定的情况下， $|w^T x + b|$ 能够表示点x到距离超平面的远近

定义函数间隔为： $\hat{\gamma} = y(w^T x + b) = yf(x)$

而超平面 $(w, b)$ 关于T中所有样本点 $(x_i, y_i)$ 的函数间隔最小值（其中x是特征，y是结果标签，i表示第i个样本），便为超平面 $(w, b)$ 关于训练数据集T的函数间隔：

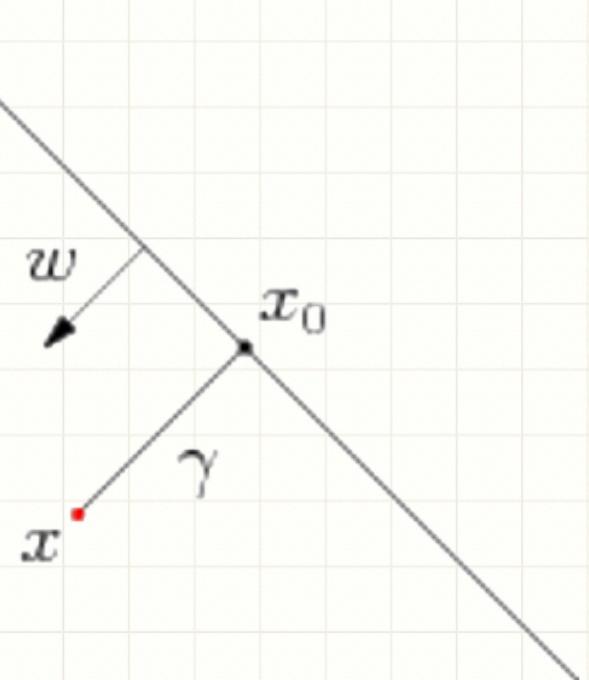
$$\hat{\gamma} = \min_i \hat{\gamma}_i (i = 1, \dots, n)$$

因为 $x_0$ 在超平面上： $w^T x_0 + b = 0 \quad w^T x_0 = -b$

式子  $x = x_0 + \gamma \frac{w}{\|w\|}$  ( $\|w\|$ 为w的二阶范数) 两边同时乘以 $w^T$

根据  $w^T x_0 = -b$  和  $w^T w = \|w\|^2$  得到： $\gamma = \frac{w^T x + b}{\|w\|} = \frac{f(x)}{\|w\|}$

二阶范数：向量元素绝对值的平方和再开方，空间上两个向量矩阵的直线距离



svm PPT来源：刘燮仪

# Multivariate Analysis - Classification



## SVM的数学模型

$$\gamma = \frac{w^T x + b}{\|w\|} = \frac{f(x)}{\|w\|}$$

上式两边乘上对应的类别  $y$ , 即可得出几何间隔:  $\tilde{\gamma} = y\gamma = \frac{\hat{\gamma}}{\|w\|}$

最大间隔分类器 (maximum margin classifier) 的目标函数可以定义为:  $\max \tilde{\gamma}$

如果令函数间隔为1 (方便计算):  $\tilde{\gamma} = \frac{1}{\|w\|}$

目标函数转化为:  $\max \frac{1}{\|w\|}, \quad \text{s.t.}, y_i(w^T x_i + b) \geq 1, i = 1, \dots, n$

求  $\frac{1}{\|w\|}$  的最大值相当于求  $\frac{1}{2} \|w\|^2$  的最小值

定义拉格朗日函数:  $\mathcal{L}(w, b, \alpha) = \frac{1}{2} \|w\|^2 - \sum_{i=1}^n \alpha_i (y_i(w^T x_i + b) - 1)$

svm PPT来源: 刘燮仪

# Multivariate Analysis - Classification



## SVM的数学模型

定义拉格朗日函数:  $\mathcal{L}(w, b, \alpha) = \frac{1}{2} \|w\|^2 - \sum_{i=1}^n \alpha_i (y_i (w^T x_i + b) - 1)$

$$\theta(w) = \max_{\alpha_i \geq 0} \mathcal{L}(w, b, \alpha)$$

$$\min_{w, b} \theta(w) = \min_{w, b} \max_{\alpha_i \geq 0} \mathcal{L}(w, b, \alpha) = p^*$$

$$\max_{\alpha_i \geq 0} \min_{w, b} \mathcal{L}(w, b, \alpha) = d^*$$

KKT条件就是指上面最优化数学模型的标准形式中的最小点  $x^*$  必须满足下面的条件:

1.  $h_j(\mathbf{x}_*) = 0, j = 1, \dots, p, g_k(\mathbf{x}_*) \leq 0, k = 1, \dots, q,$
2.  $\nabla f(\mathbf{x}_*) + \sum_{j=1}^p \lambda_j \nabla h_j(\mathbf{x}_*) + \sum_{k=1}^q \mu_k \nabla g_k(\mathbf{x}_*) = \mathbf{0},$   
 $\lambda_j \neq 0, \mu_k \geq 0, \mu_k g_k(\mathbf{x}_*) = 0$

在满足上述条件下, 问题转换为对偶问题, 首先要让  $L(w, b, \alpha)$  关于  $w$  和  $b$  最小化, 然后求对  $\alpha$  的极大, 最后利用 SMO 算法求解对偶问题中的拉格朗日乘子。

svm PPT来源: 刘燮仪

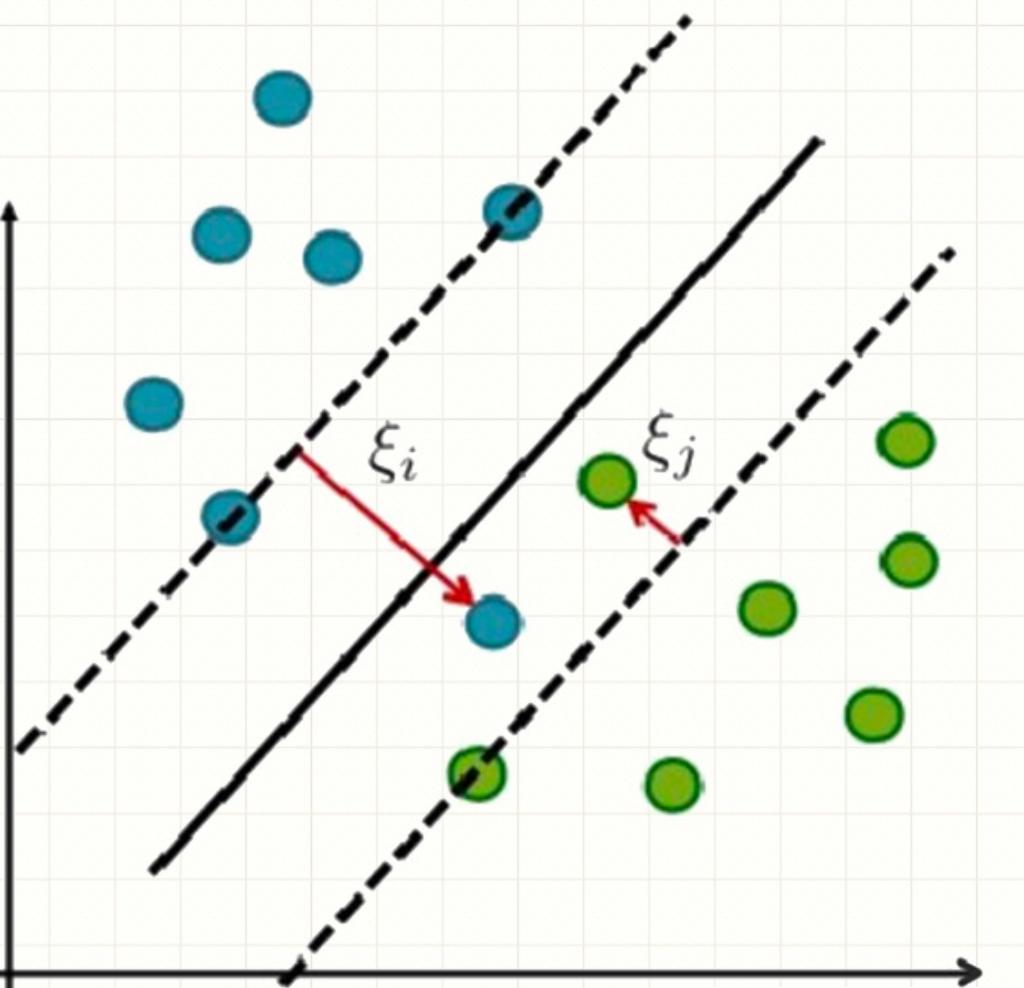
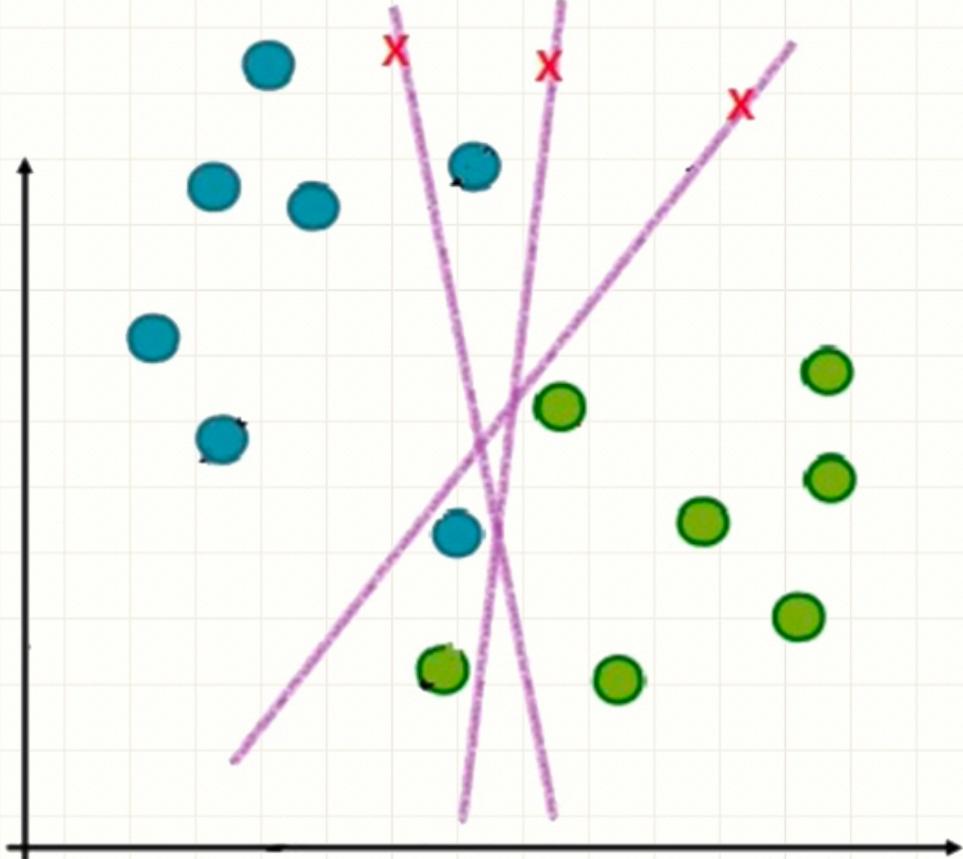
# Multivariate Analysis - Classification



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SVM扩展

不完全线性可分



引入一个松弛变量 $\xi_i$

允许部分样本点不满足约束条件:

$$1 - y_i (\mathbf{w}^T \mathbf{x}_i + b) \leq 0$$

优化目标:

$$\begin{aligned} & \min_{\mathbf{w}, b, \xi \geq 0} \frac{1}{2} \mathbf{w}^\top \mathbf{w} + C \sum_i \xi_i \\ & \text{s.t. } y_i (\mathbf{w}^\top \mathbf{x}_i + b) \geq 1 - \xi_i, \quad i = 1, \dots, n \\ & \xi_i \geq 0 \end{aligned}$$

其中  $C$  是一个大于 0 的常数, 可以理解为错误样本的惩罚程度

构造拉格朗日函数:  $\min_{\mathbf{w}, b, \xi} \max_{\lambda, \mu} L(\mathbf{w}, b, \xi, \lambda, \mu) = \frac{1}{2} \|\mathbf{w}\|^2 + C \sum_{i=1}^n \xi_i + \sum_{i=1}^n \lambda_i [1 - \xi_i - y_i (\mathbf{w}^\top \mathbf{x}_i + b)] - \sum_{i=1}^n \mu_i \xi_i$   
s.t.  $\lambda_i \geq 0 \quad \mu_i \geq 0$

对偶问题转化为:  $\max_{\lambda, \mu} \min_{\mathbf{w}, b, \xi} L(\mathbf{w}, b, \xi, \lambda, \mu)$

svm PPT来源: 刘燮仪

# Multivariate Analysis - Classification



## SVM扩展

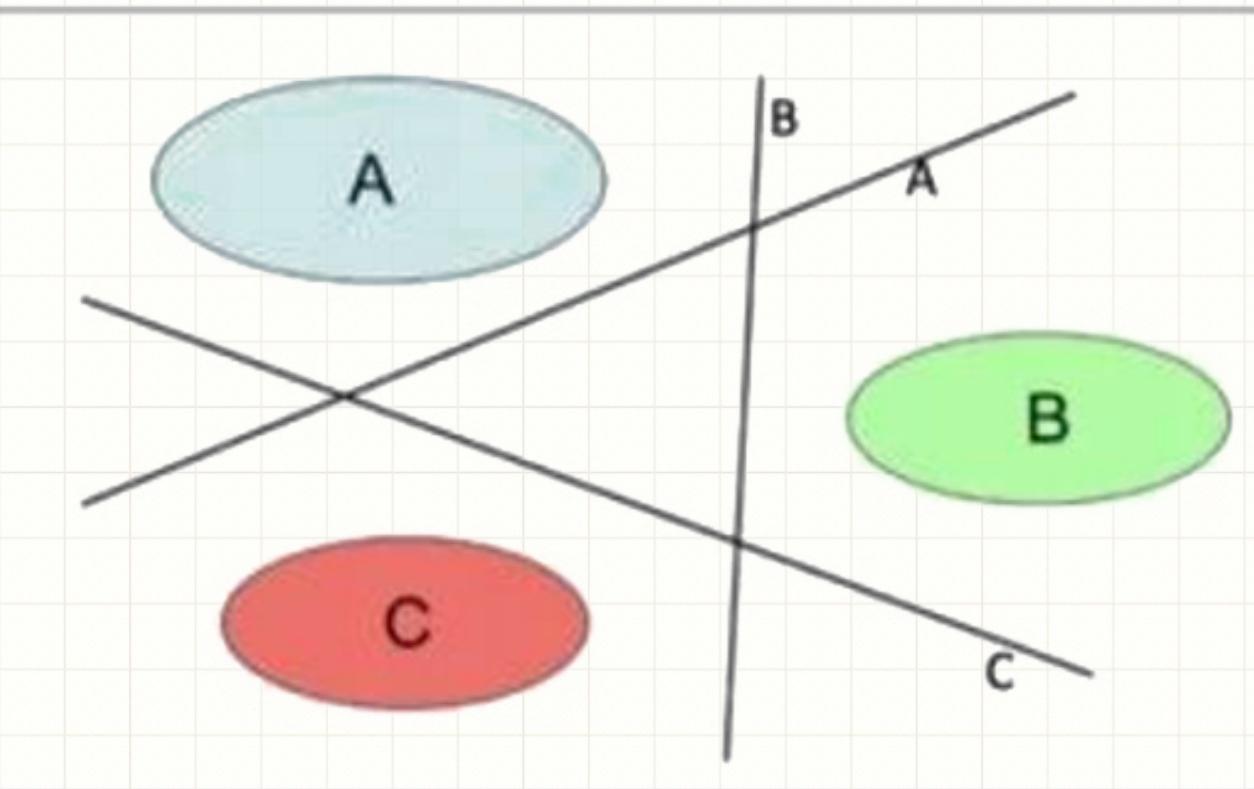
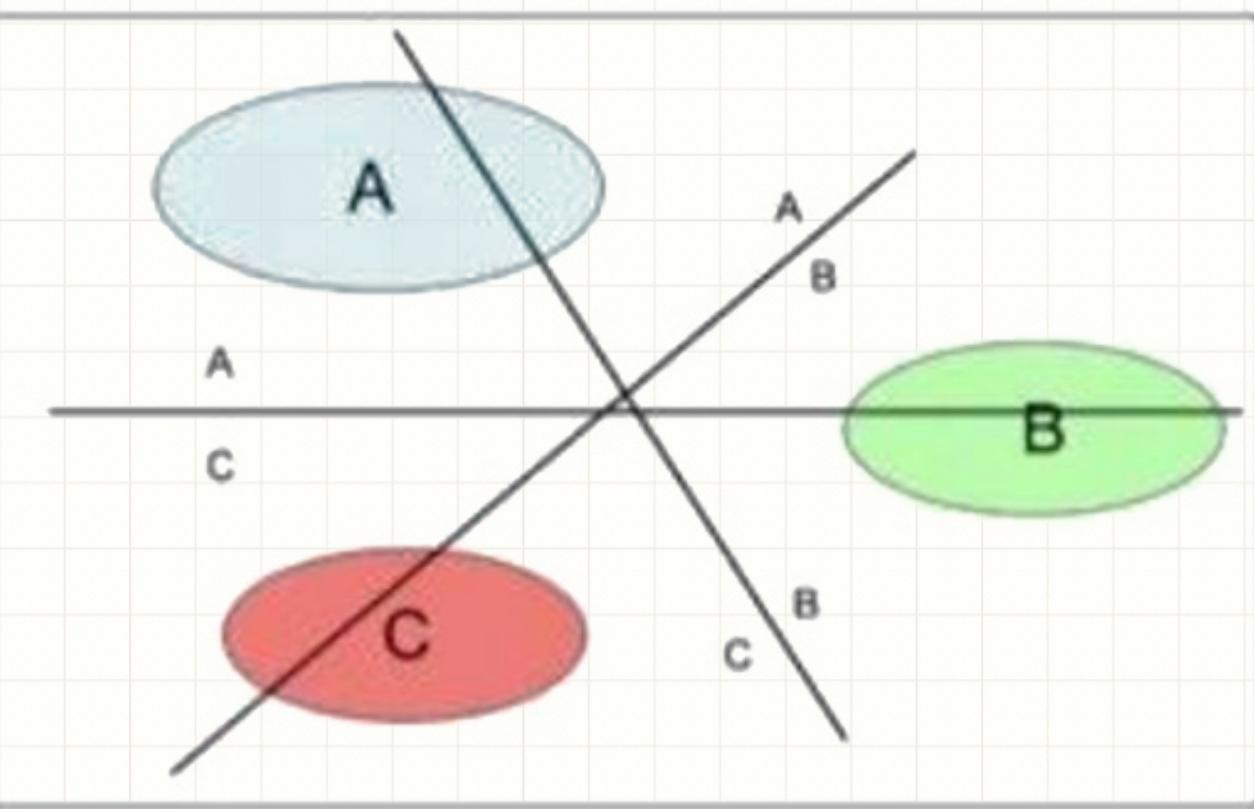
扩展为多分类的方法有：

### 一对一 (one-versus-one, OVO SVMs) 方法:

训练时对于任意两类样本都会训练一个二分类器，最终得到  $k(k-1)/2$  个二分类器，共同组成  $k$  分类器。对未知样本分类时，使用所有的  $k(k-1)/2$  个分类器进行分类，将出现最多的那个类别作为该样本最终的分类结果。

### 一对多 (one-versus-rest, OVR SVMs) 方法:

训练时依次把  $k$  类样本中的某个类别归为一类，其它剩下的归为另一类，使用二分类的SVM训练处一个二分类器，最后把得到的  $k$  个二分类器组成  $k$  分类器。对未知样本分类时，分别用这  $k$  个二分类器进行分类，将分类结果中出现最多的那个类别作为最终的分类结果。



svm PPT来源：刘燮仪

# Multivariate Analysis - Classification



- SVM in Matlab & scikit-learn

## fitcsvm

训练用于一类和二类分类的支持向量机 (SVM) 分类器

### 语法

```
Mdl = fitcsvm(Tbl,ResponseVarName)
Mdl = fitcsvm(Tbl,formula)
Mdl = fitcsvm(Tbl,Y)

Mdl = fitcsvm(X,Y)

Mdl = fitcsvm(___,Name,Value)
```

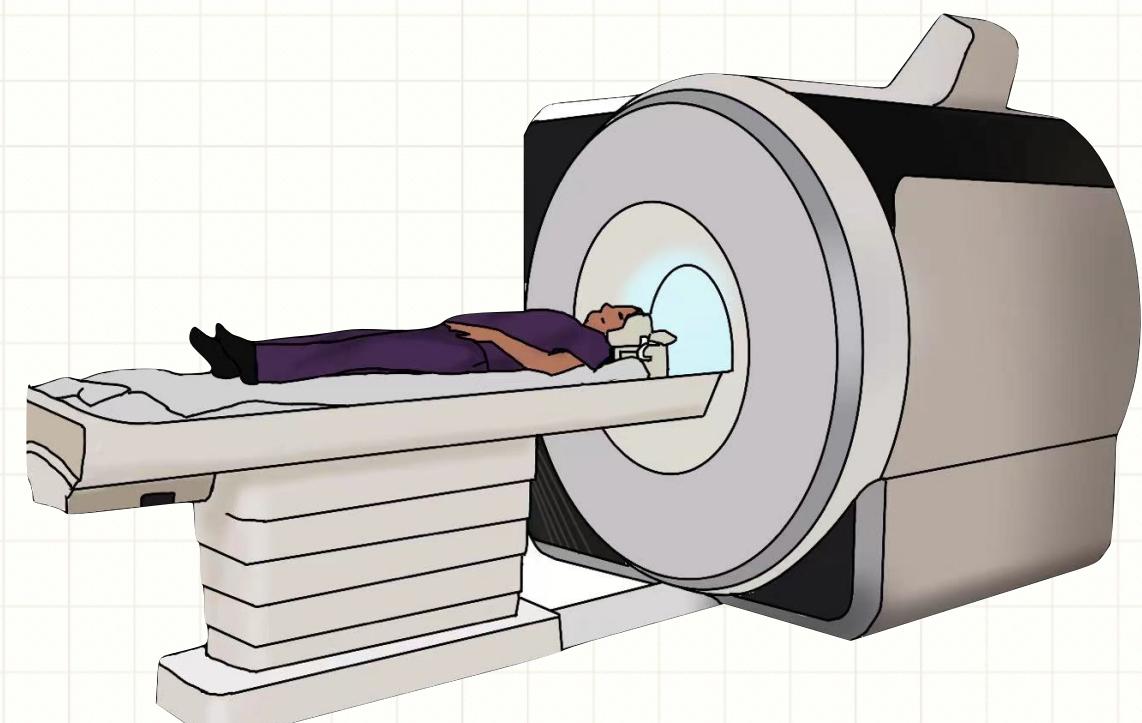
```
from sklearn.svm import LinearSVC
linearsvc = LinearSVC(C=1e9)
linearsvc.fit(X_stand, y)
```

LIBSVM -- A Library for Support Vector Machines

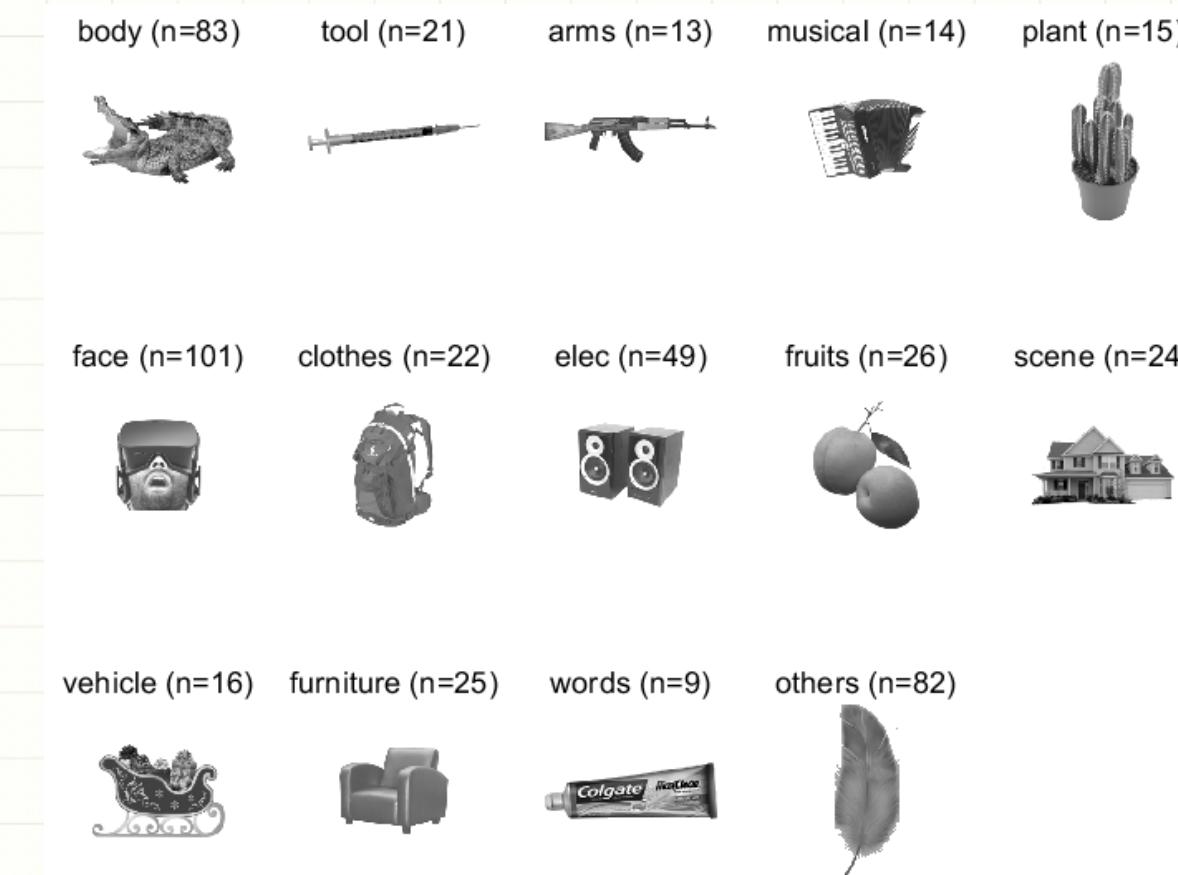
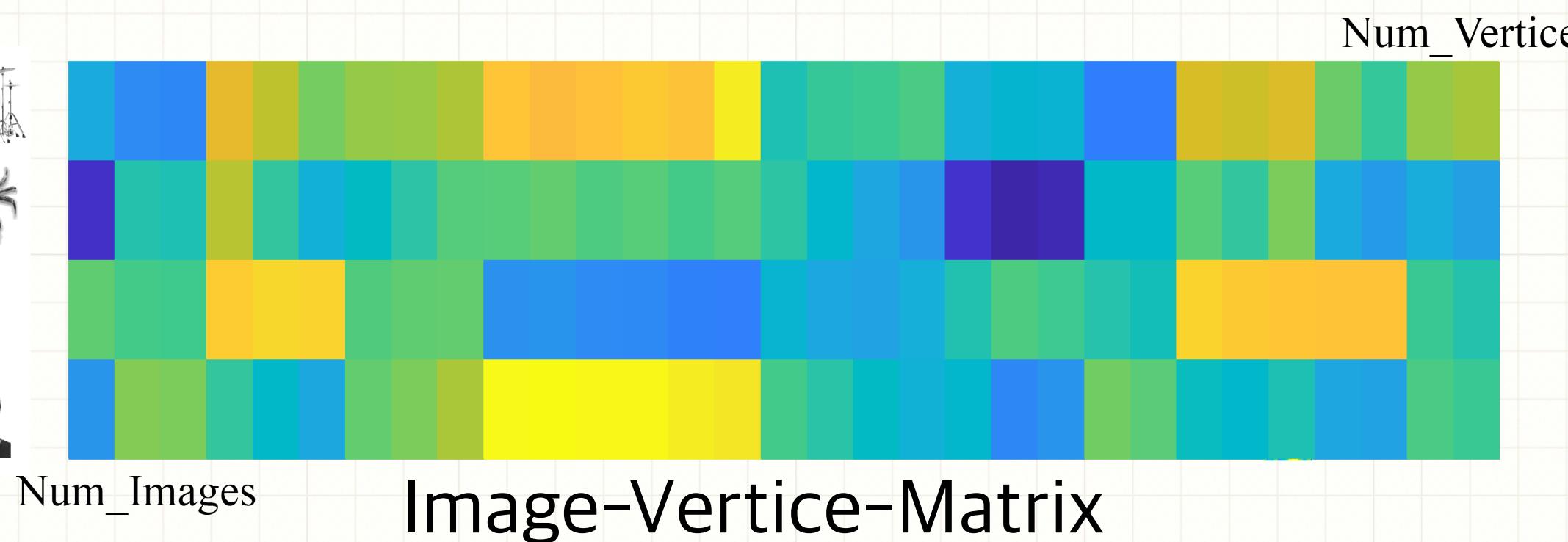
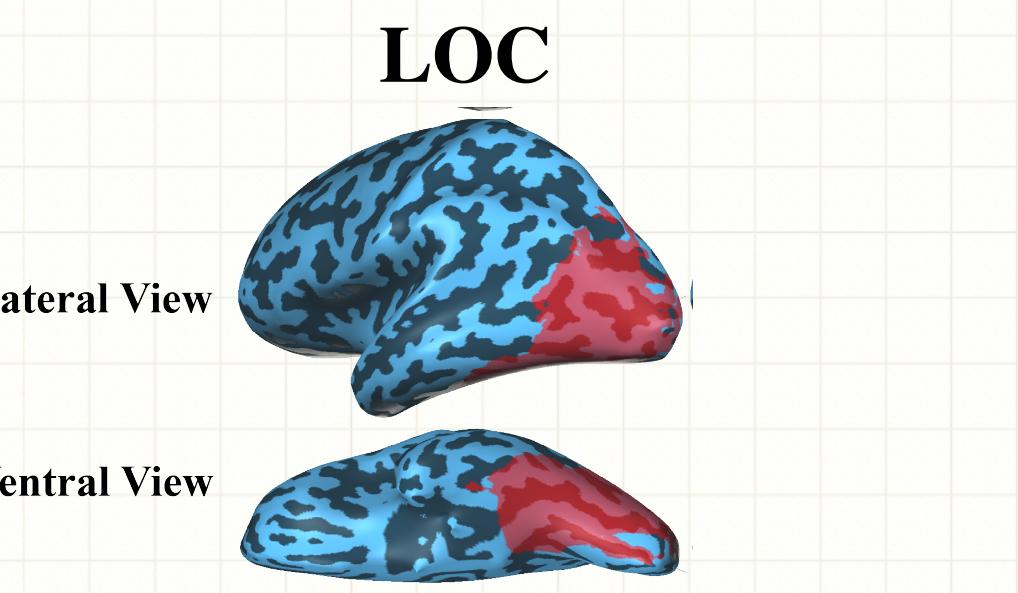
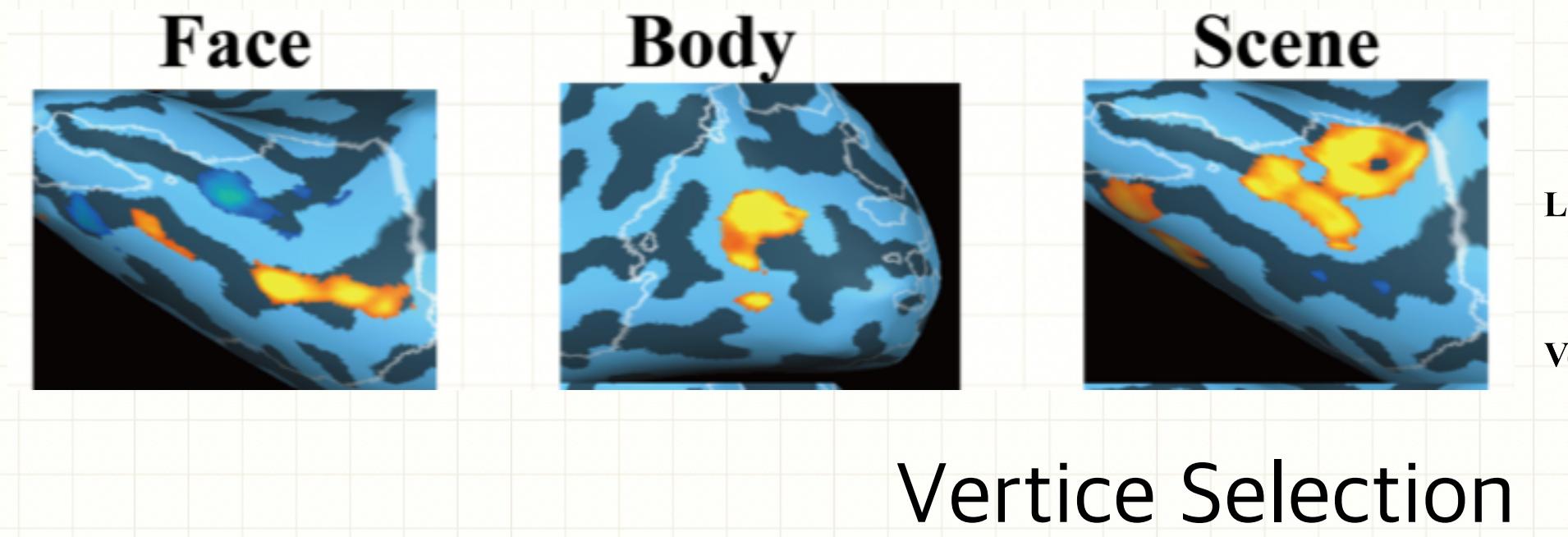
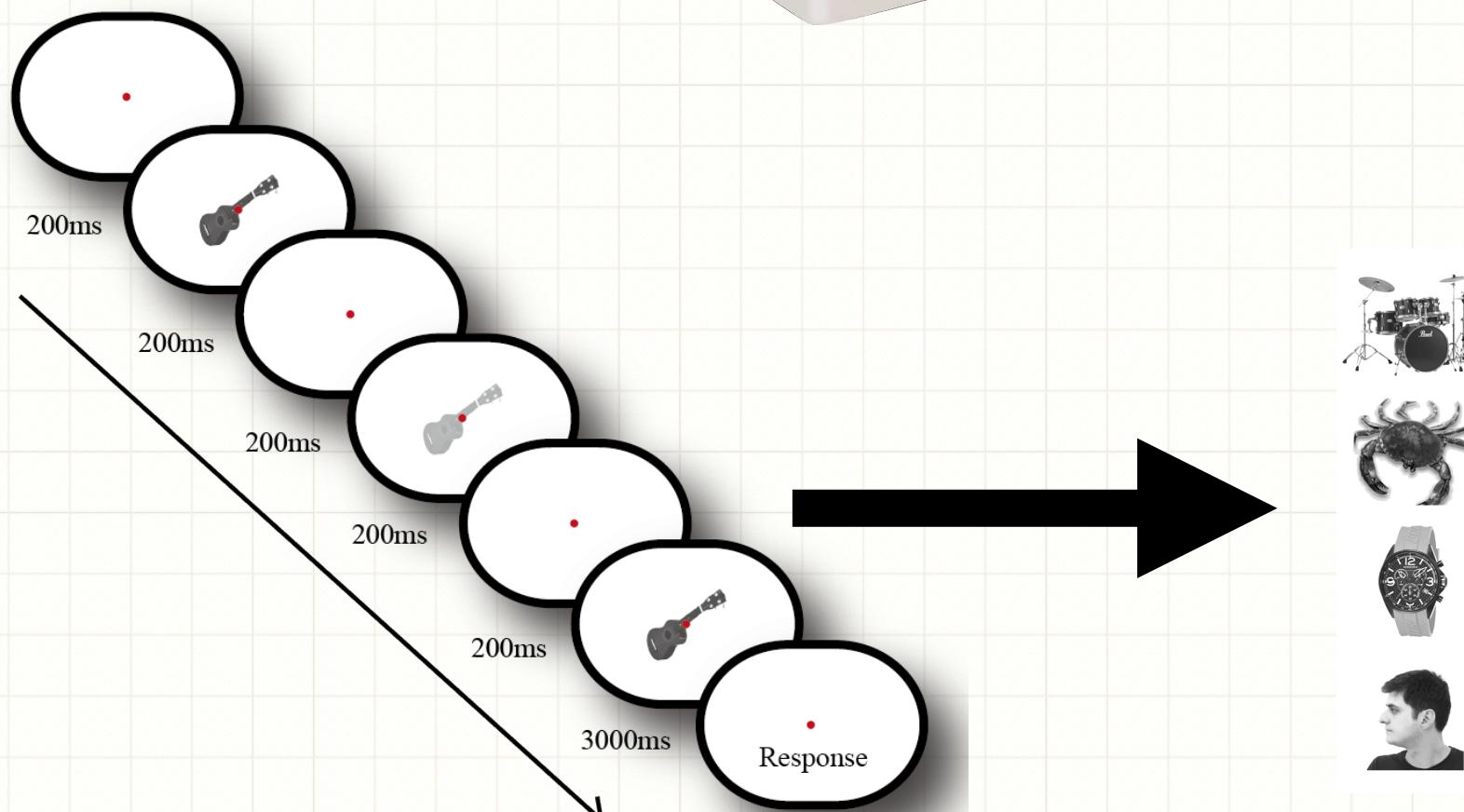
Chih-Chung Chang and [Chih-Jen Lin](#)

# Example Data

1 subjects, passively viewing 500 images, 10 trials per image,  
event-related design



A. Contrast Change Detection



# Multivariate Analysis - Classification



- Q1 - Can we read(decode) image category through the response of non-selective area?
- e.g. Can PPA (scene preferencing area) distinguish Animal & Face?

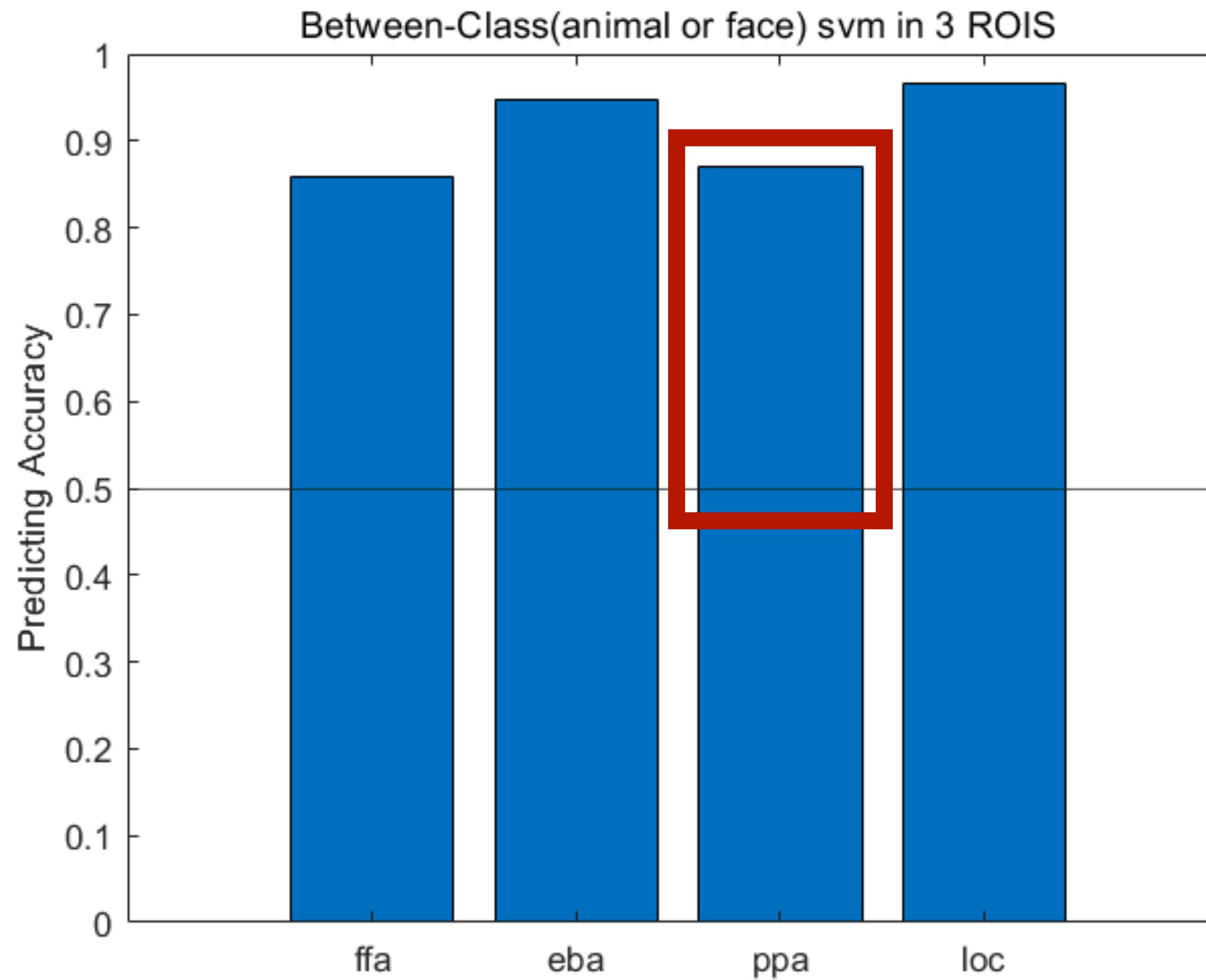
```
%% 2-class svm in 3 rois
interested_idx = [image_category(1).picset, image_category(6).picset]; % decode animal or face?
all_image = length(interested_idx);
leave_out_num = 20;
for bb = 1:boot_times
    animal_idx = image_category(1).picset;
    label_array = zeros(1,all_image);
    label_array(animal_idx)=1; % 1 is animal and 0 is face

    leave_out_idx = randperm(all_image,leave_out_num); % split data into train and test sets
    train_idx = setdiff(1:all_image, leave_out_idx);
    for rr = 1:length(average_beta)
        roi_now = average_beta{rr,2};
        mdl = fitcsvm(average_beta{rr,1}(train_idx, :), label_array(train_idx)); % train a svm model
        predicted_label = predict(mdl, average_beta{rr,1}(leave_out_idx, :)); % predict test data
        predicted_acc(rr,bb) = length(find(predicted_label==label_array(leave_out_idx)))./leave_out_num; %check accuracy
        roi_legend{rr} = roi_now;
    end
end
```

# Multivariate Analysis - Classification



- Q1 - Can we read(decode) image category through the response of non-selective area?
- e.g. Can PPA (scene preferencing area) distinguish Animal & Face?
- —— Yes



# Multivariate Analysis - Classification



- Q2 - Can we read(decode) any categories through the response pattern?
- Decoding 4 categories (animal, face, man-made object, natural object)

```
tic
load('roi_beta.mat') % beta in 3 rois for 6 trials
load("category_label.mat") % category label
% load('toy_data.mat') % beta in LOC for 6 trials

% sort categories into 4 sets
image_category(3).name = 'man-made object';
image_category(3).picset = [image_category(2).picset, image_category(3).picset, image_category(4).picset,
image_category(2)=image_category(6);
image_category(4).name='natural object';
image_category(4).picset = [image_category(5).picset, image_category(9).picset];
image_category(5:end)=[];
category_legend={};
```

# Multivariate Analysis - Classification



- Q2 - Can we read(decode) any categories through the response pattern?
- Decoding 4 categories (animal, face, man-made object, natural object)

```
confuse_matrix = zeros(boot_times, 4, length(image_category), length(image_category));
for bb = 1:boot_times % we do this for boot_times

    % combine 6 trials, and pick data
    pooled_response{1}=[];pooled_response{2}=[];pooled_response{3}=[];pooled_response{4}=[];label_array=[];
    for cc = 1:length(image_category)
        sample_image = randperm(length(image_category(cc).picset), 40);
        image_idx = image_category(cc).picset(sample_image);
        for trial_num = 1:length(roi_beta)
            pooled_response{1} = [ pooled_response{1};roi_beta{trial_num}.ffa(image_idx, :)];
            pooled_response{2} = [ pooled_response{2};roi_beta{trial_num}.eba(image_idx, :)];
            pooled_response{3} = [ pooled_response{3};roi_beta{trial_num}.ppa(image_idx, :)];
            pooled_response{4} = [ pooled_response{4};roi_beta{trial_num}.loc(image_idx, :)];
        end
        label_array = [label_array, cc*ones(1,trial_num*40)];
        category_legend{cc}=image_category(cc).name;
    end
    % split data into train & test sets
    test_idx = randperm(length(label_array),leave_out_num);
    train_idx = setdiff(1:length(label_array), test_idx);
    for rr = 1:4 % do this for 4 rois
        train_data = double(pooled_response{rr}(train_idx, :));
        train_label = label_array(train_idx);
        test_data = double(pooled_response{rr}(test_idx, :));
        test_label = label_array(test_idx);
        % train a multi-label svm model and predict labels for test sets
        model=svmtrain(train_label', train_data);
        [pred, acc, ~] = svmpredict(test_label', test_data,model);
        acc_save(rr,bb)= acc(1); % save accuracy
        % save confuse matrix
        for sample_now = 1:length(test_label)
            confuse_matrix(bb, rr ,test_label(sample_now), pred(sample_now))=confuse_matrix(bb, rr ,test_label(sample_now), pred(sample_now))+1;
        end
    end
    waitbar(bb/boot_times)
end
```

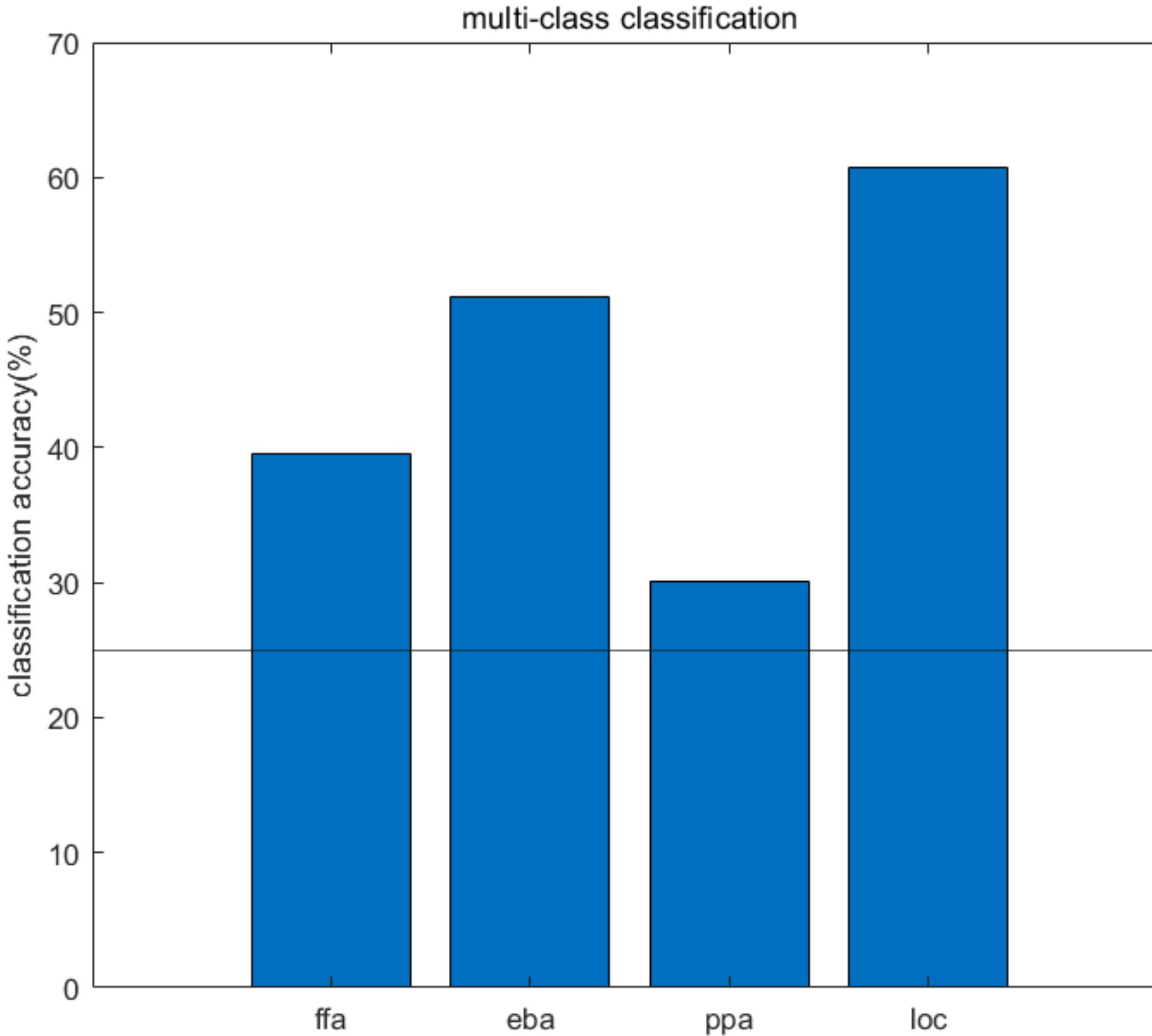
Balance the data

Save decode pattern

# Multivariate Analysis - Classification



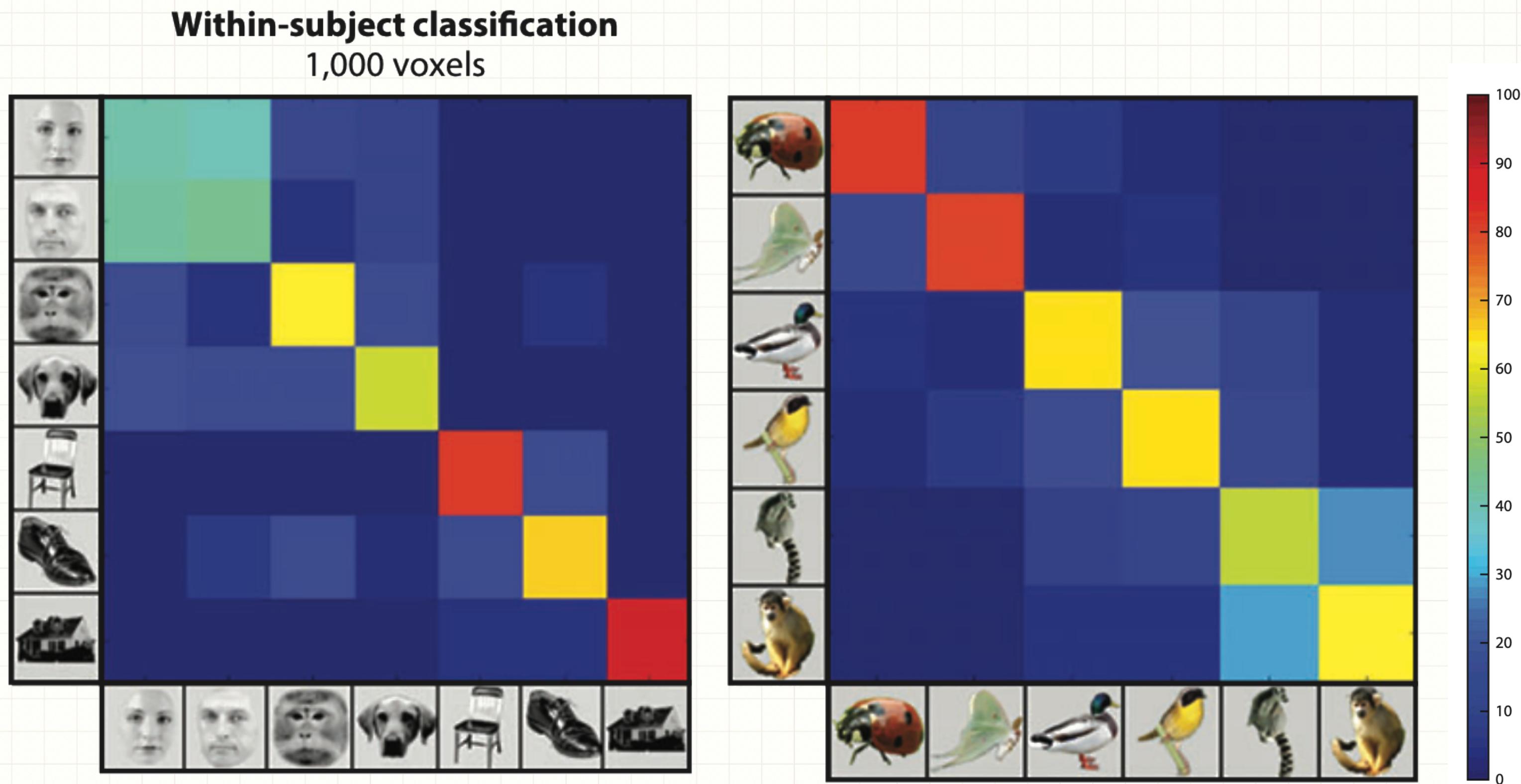
- Q2 - Can we read(decode) any category through the response pattern?
- Decoding 4 categories (animal, face, man-made object, natural object)



# Multivariate Analysis - Classification



- Q3 - Which categories are misidentified as what?
- Confuse Matrix (error pattern) reveals the discriminability between any two categories

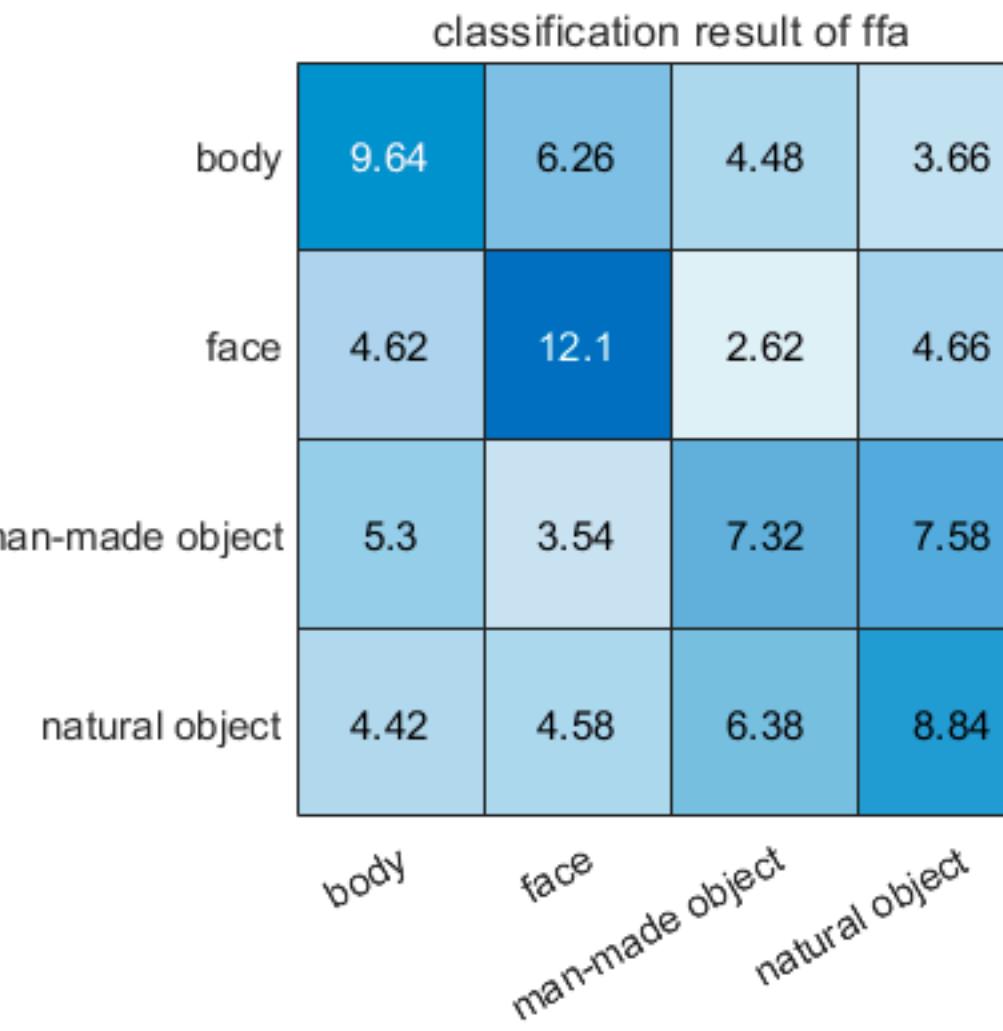


# Multivariate Analysis - Classification

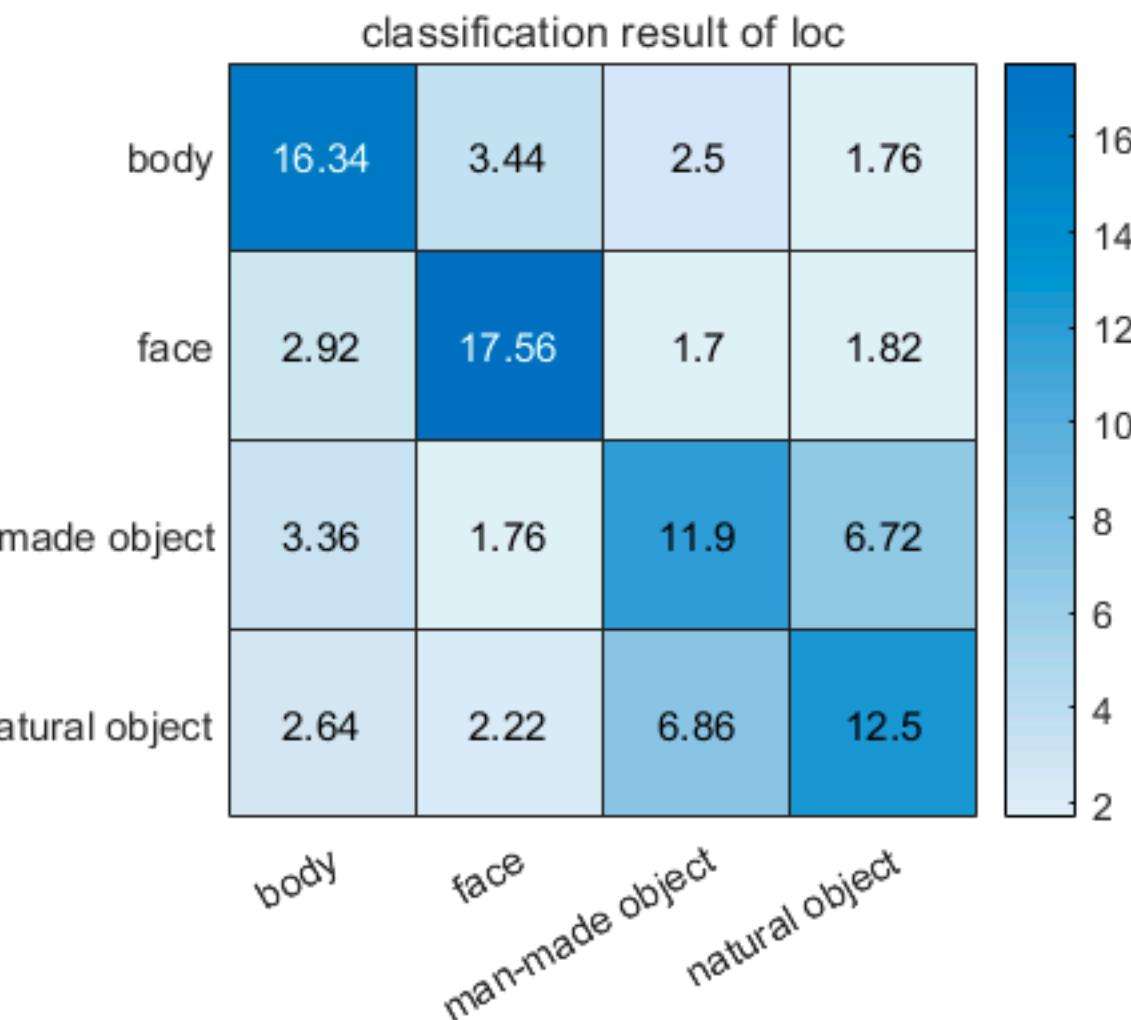
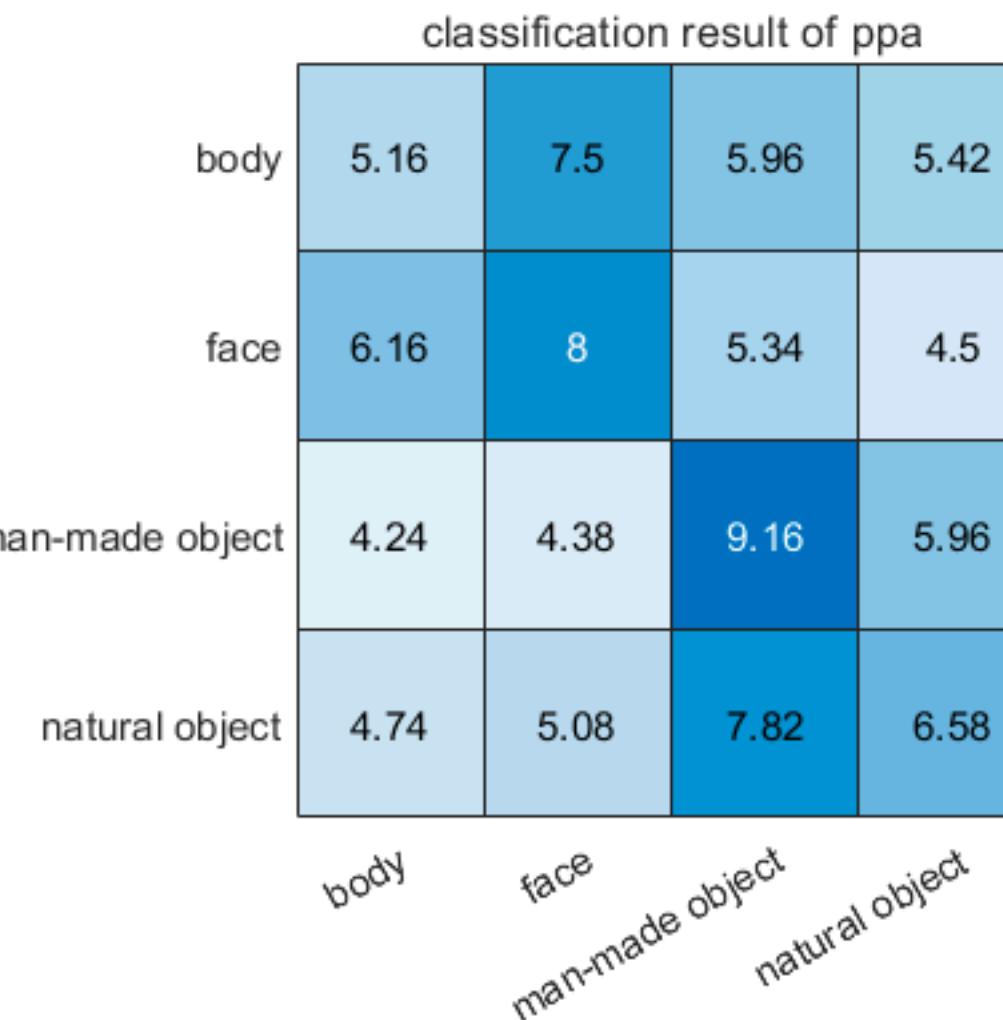
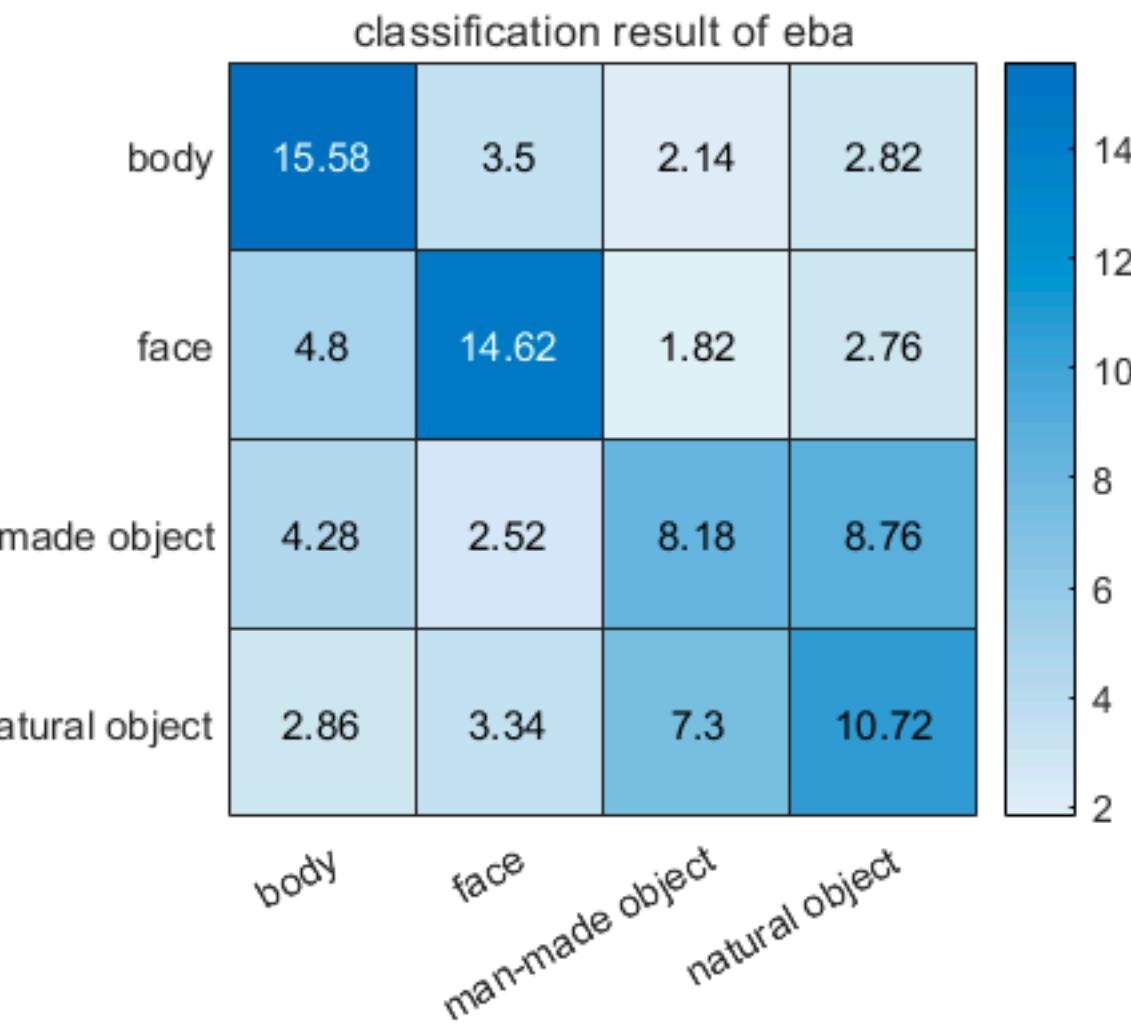


- Q3 - Which categories are misidentified as what?**
- Confuse Matrix (error pattern) reveals the discriminability between any two categories**
- Two subcategories of objects are confused in all areas**
- Discriminability as a measure of distance**

```
[pred, acc, ~] = svmpredict(test_label', test_data,model);
acc_save(rr,bb)= acc(1); % save accuracy
% save confuse matrix
for sample_now = 1:length(test_label)
    confuse_matrix(bb, rr ,test_label(sample_now), pred(sample_now))=confuse_matrix(bb, rr
end
```



multi-label classification



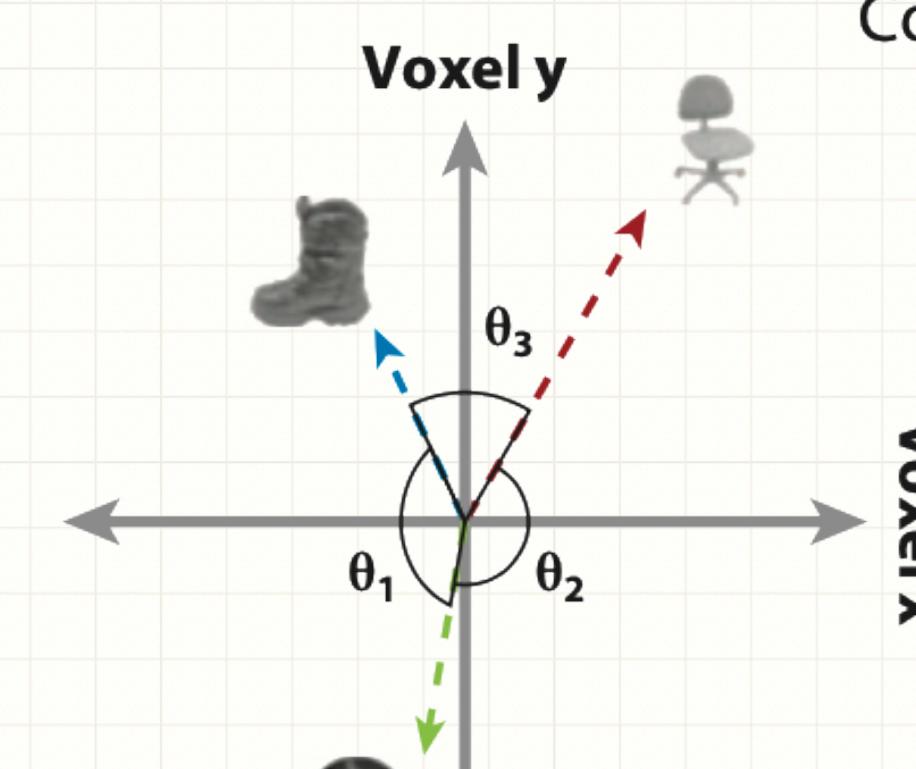
# Multivariate Analysis - Distance

- Discriminability as a measure of **distance**
- Distance between any samples in representation space.

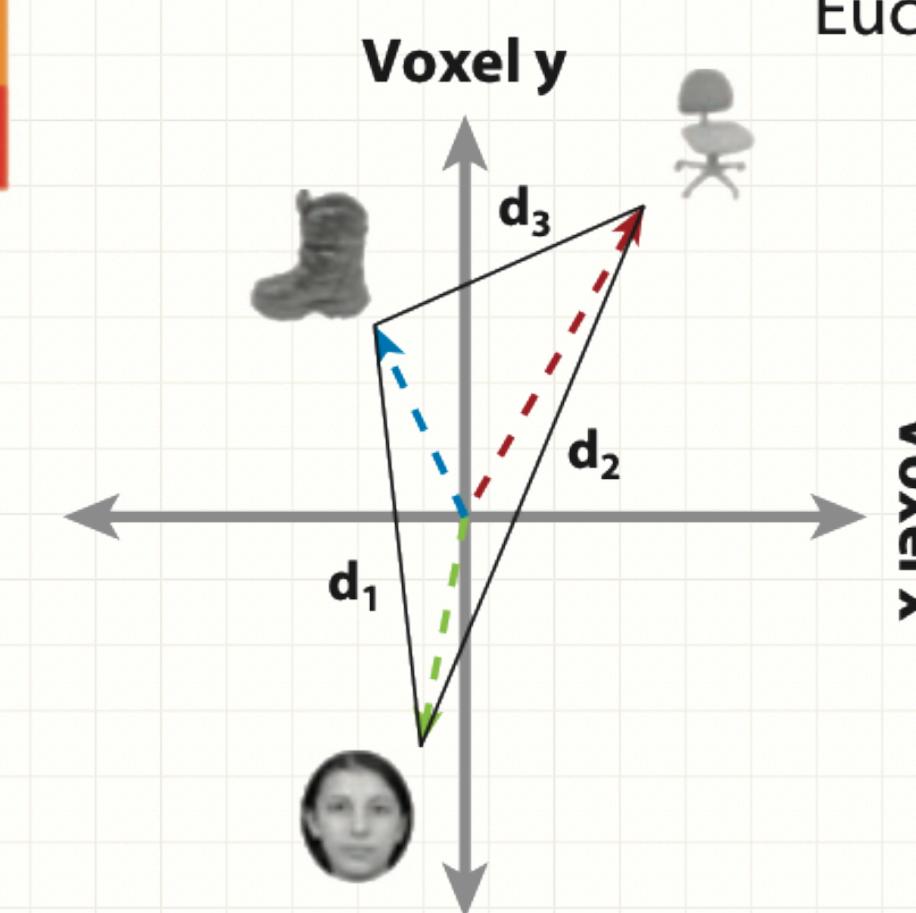
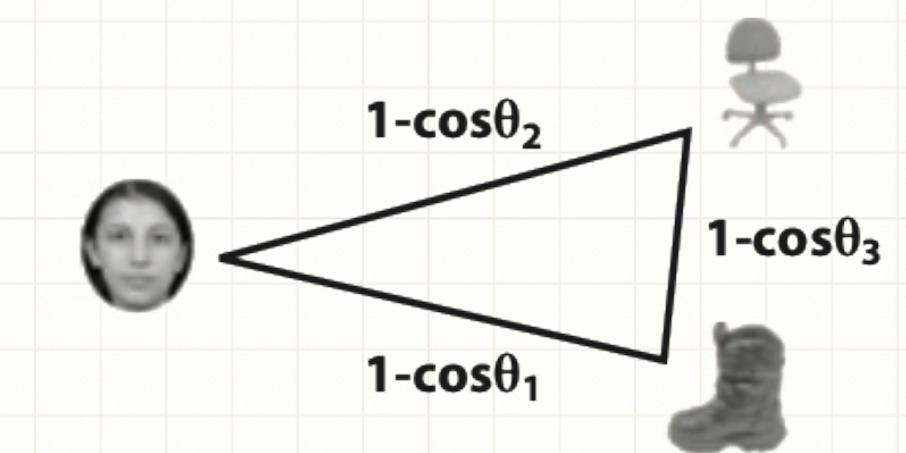
Conditions  
(e.g., stimuli or time points)

		Pattern features (e.g., voxels)									
		x					y				
Condition	Stimulus	-1.6	-0.3	-0.6	0.9	1.1	-0.8	0.4	-1.0	-1.2	-0.2
		-0.5	-1.6	0.7	1.0	-1.0	-0.4	-0.2	1.0	0.8	0.7
		0.1	1.5	0.7	-1.7	1.2	1.0	1.3	1.4	-1.1	1.0

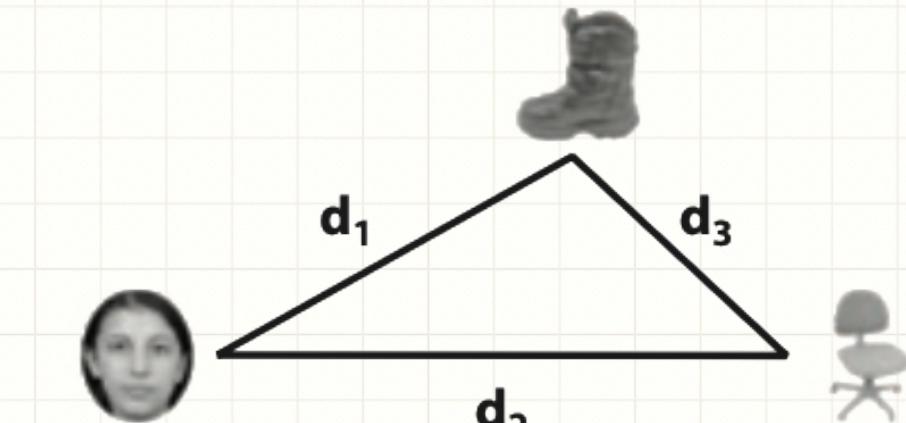
Representational similarity analysis



Cosine distance



Euclidean distance



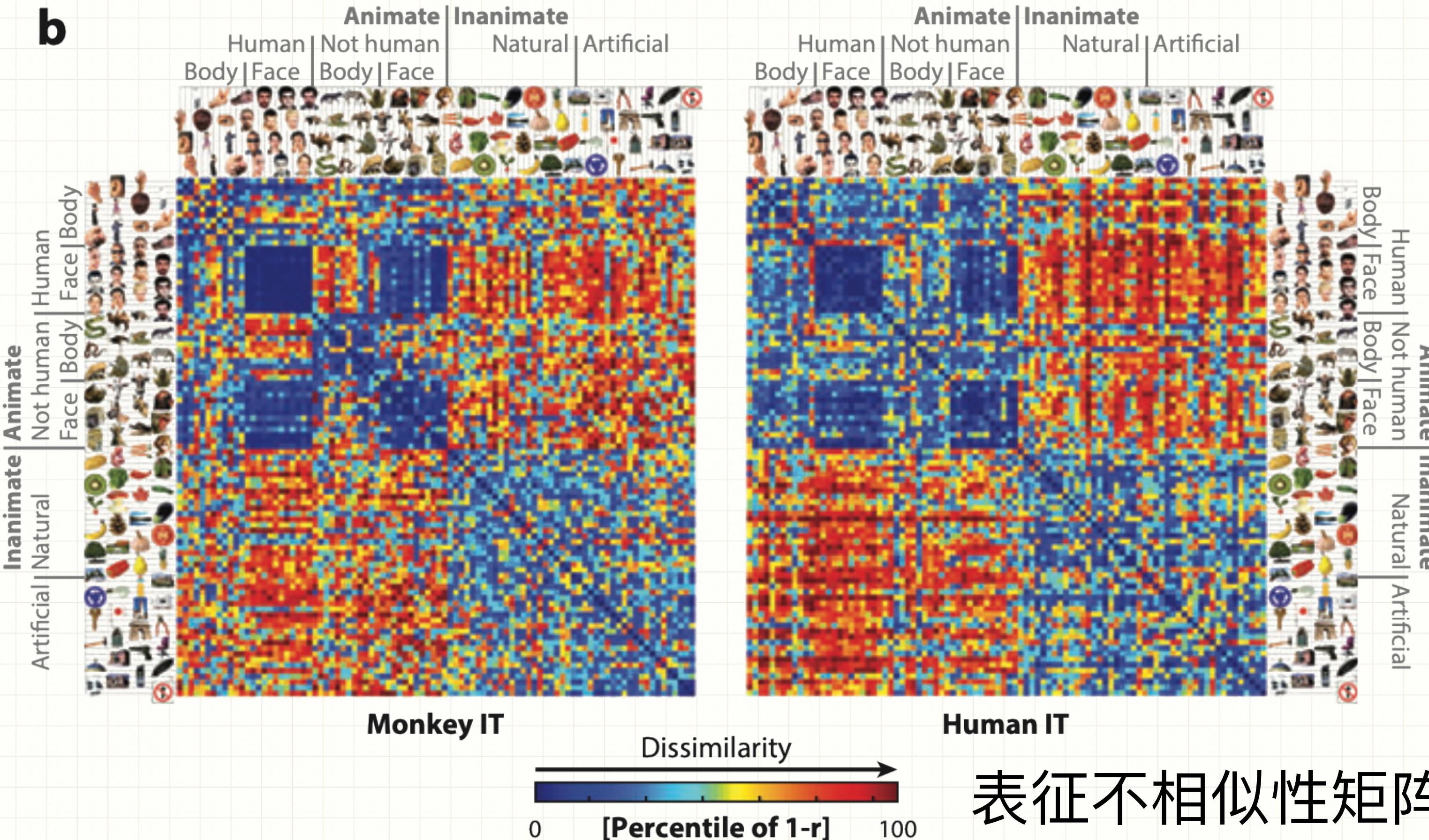
Feature-based  
representational space

Feature-independent  
representational space

# Multivariate Analysis - RSA

## REPRESENTATIONAL SIMILARITY ANALYSIS

- RSA examines the structure of representations within a representational space in terms of distances between response vectors



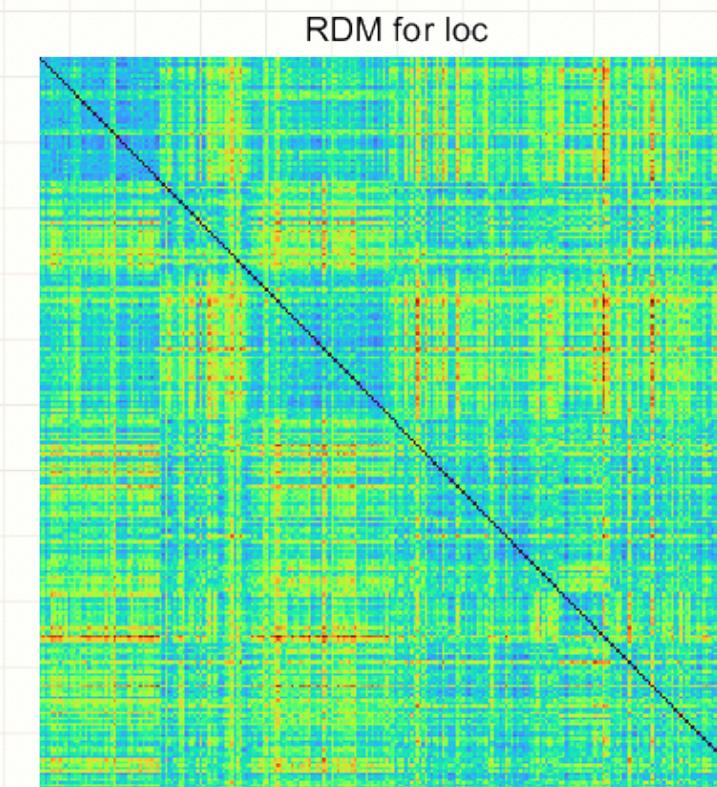
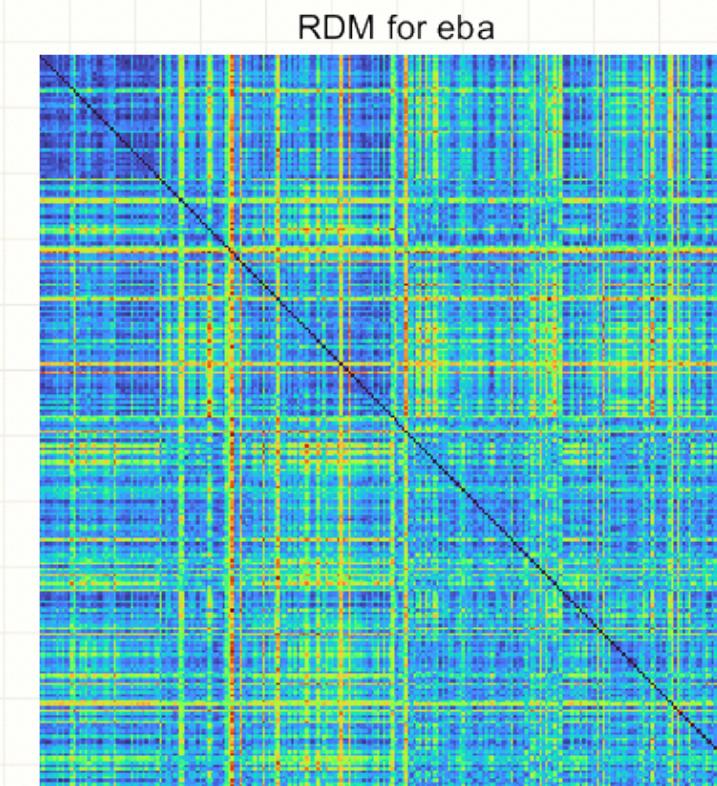
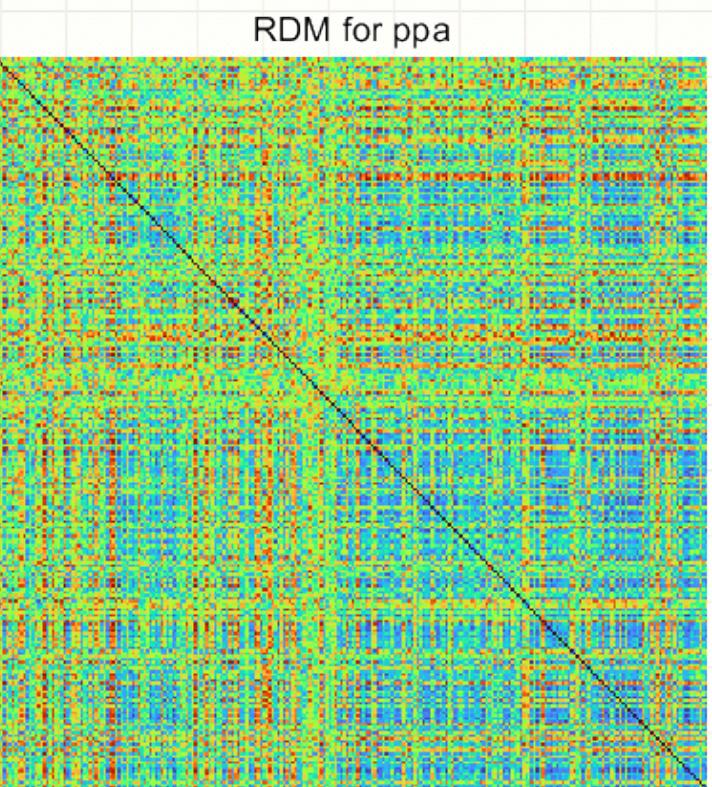
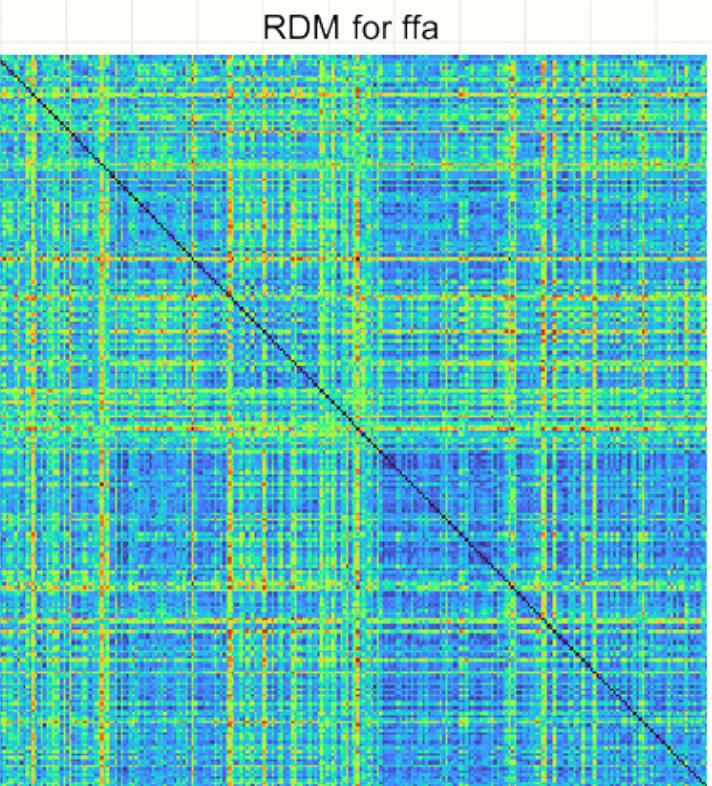
# Multivariate Analysis - RSA

## REPRESENTATIONAL SIMILARITY ANALYSIS

### Draw RDM

```
load('average_roi_beta.mat')
load("category_label.mat")
% sort categories
image_idx = [];
for cc = 1:length(image_category)
    image_idx = [image_idx image_category(cc).picset];
end
image_idx = image_idx(1:2:500);
figure
for rr = 1:length(average_beta)
    subplot(2,2,rr)
    beta_now = average_beta{rr,1};
    beta_now = beta_now(image_idx, :);
    pd = squareform(pdist(beta_now, 'correlation'));

    imagesc(pd)
    title(['RDM for ' roi_legend{rr}'])
    axis off
    colorbar
    pd_save{rr}=pd;
end
```



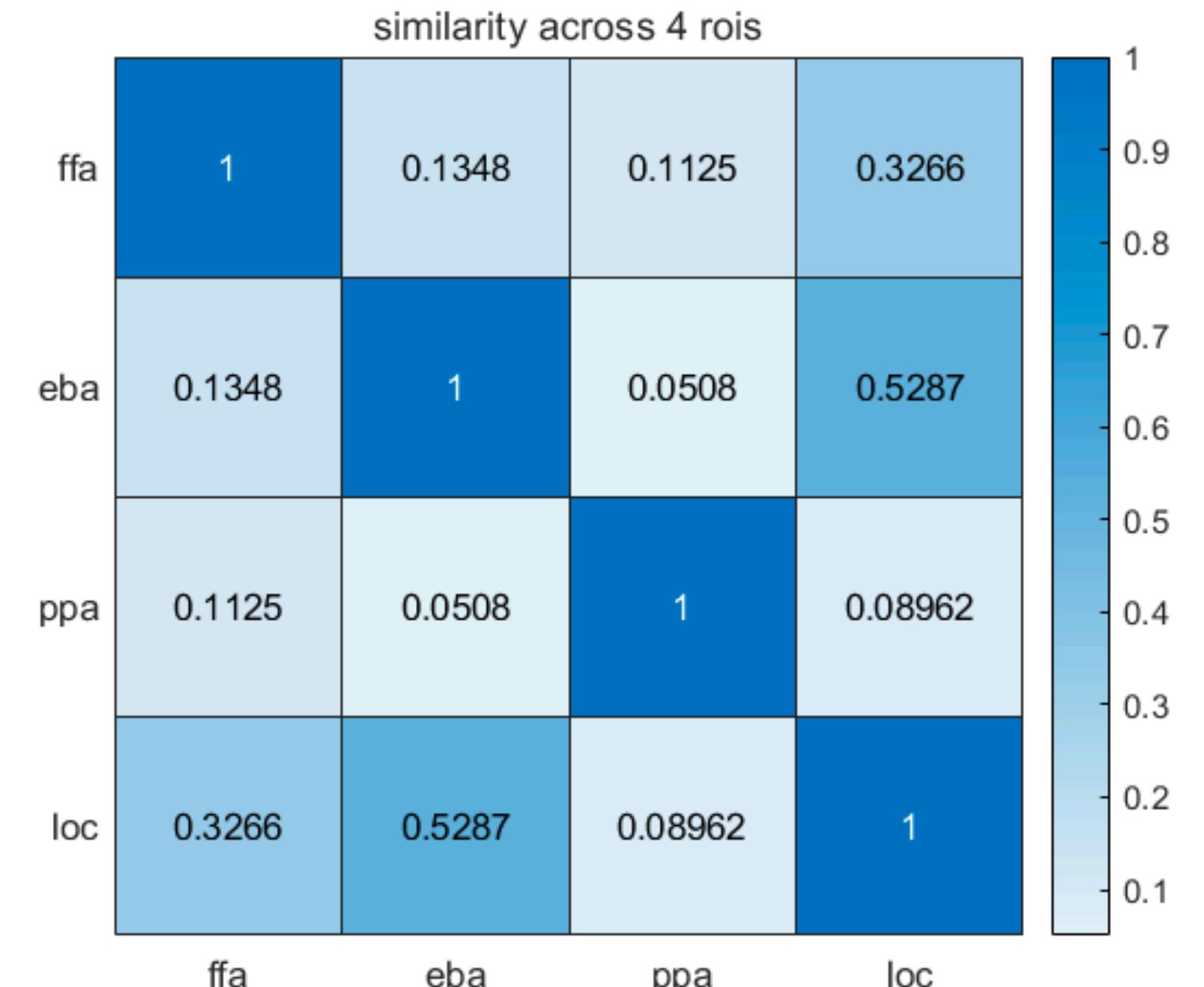
# Multivariate Analysis - RSA



## REPRESENTATIONAL SIMILARITY ANALYSIS

- Compare across systems
- PPA shows a geometry inconsistent with other areas

```
figure
for rx = 1:length(average_beta)
    for ry = 1:length(average_beta)
        rs(rx, ry) = corr(pd_save{rx}(find(tril(ones(size(pd)), -1))), pd_save{ry}(find(tril(ones(size(pd)), -1))));
    end
end
heatmap(roi_legend,roi_legend,rs)
title('similarity across 4 rois')
set(gcf, 'position',[744,653,473,396])
toc
```

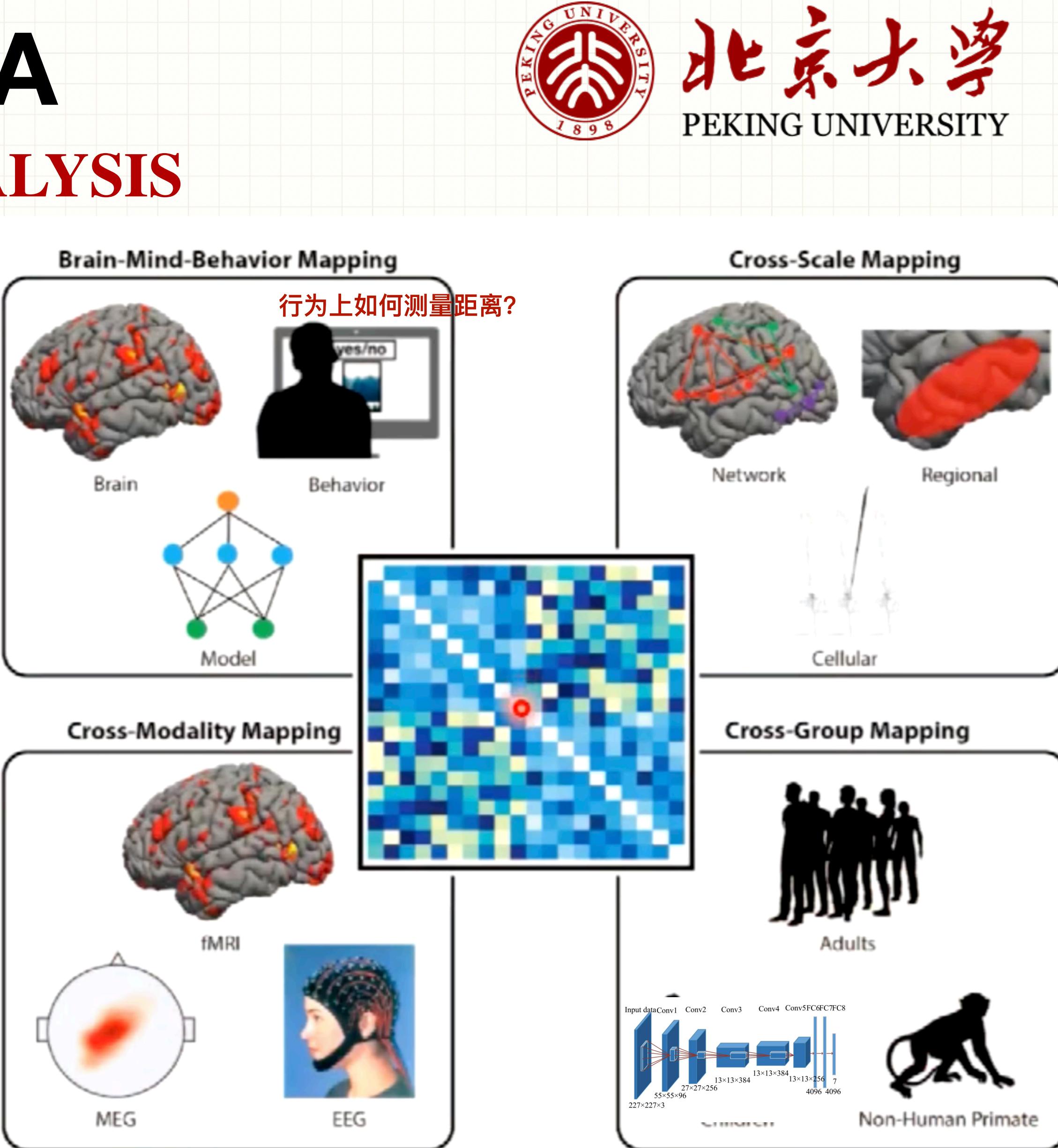


# Multivariate Analysis - RSA

## REPRESENTATIONAL SIMILARITY ANALYSIS

### Pros

1. RSA can reveal that representations in different brain areas differ even if MVP classification is equivalent in those areas
2. By converting the locations of response vectors from a set of feature coordinates to a set of distances between vectors, the geometry of the representational space is now in a format that is not dependent on the feature coordinate axes



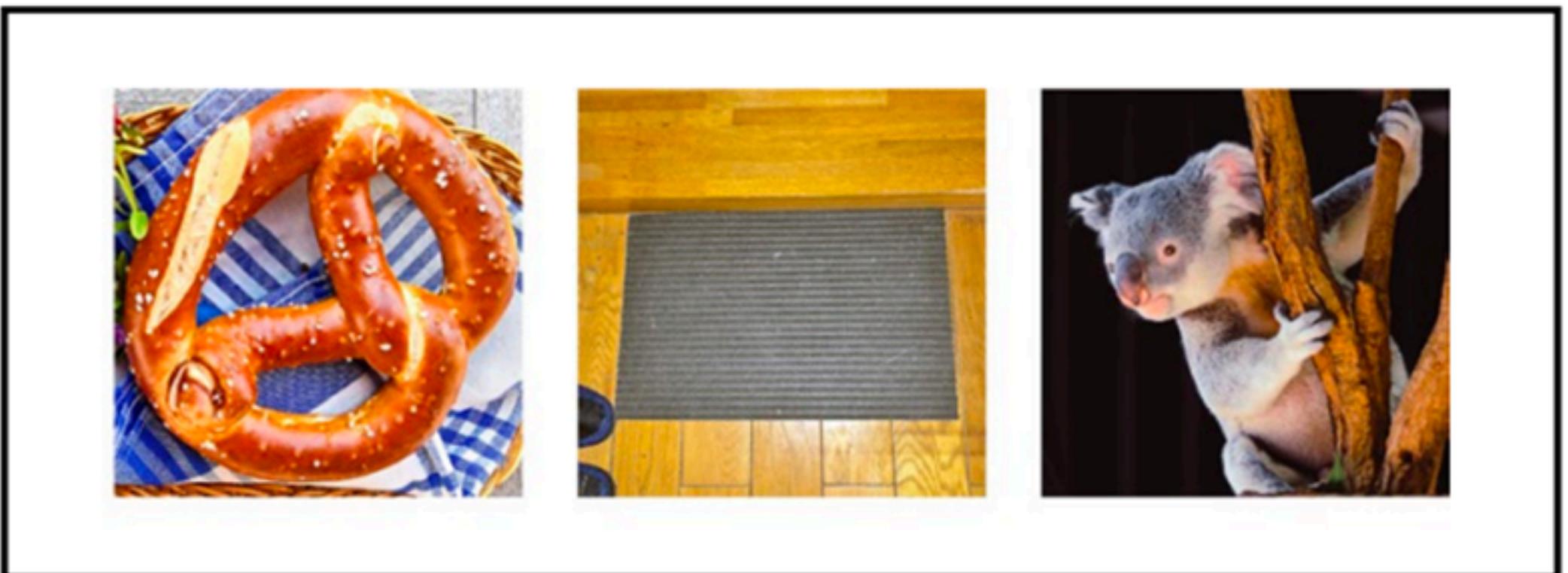
# Multivariate Analysis - RSA

## 行为上测量RSA



a

Which is the odd one out?



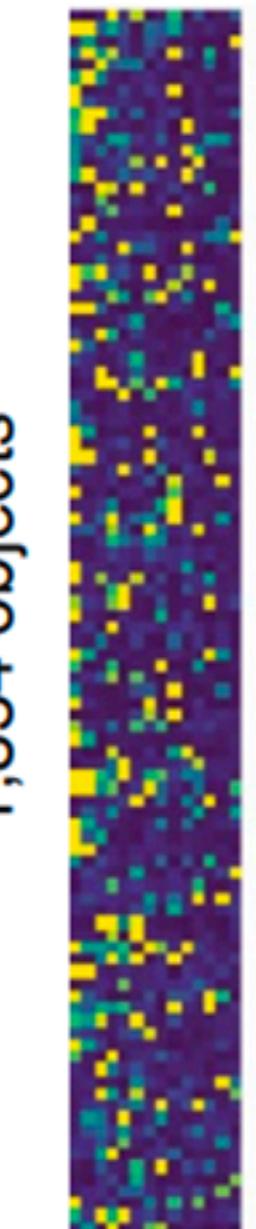
Broad sampling  
of images  
(1,854 objects)



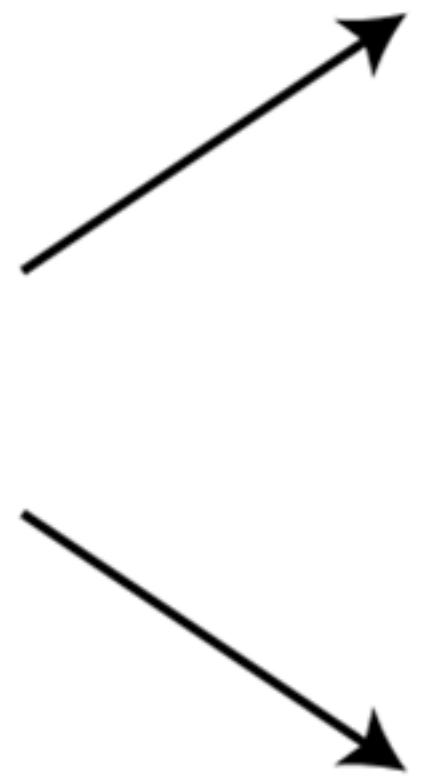
Large-scale  
online crowdsourcing  
( $n = 1.46$  million trials)

b

Representational  
embedding



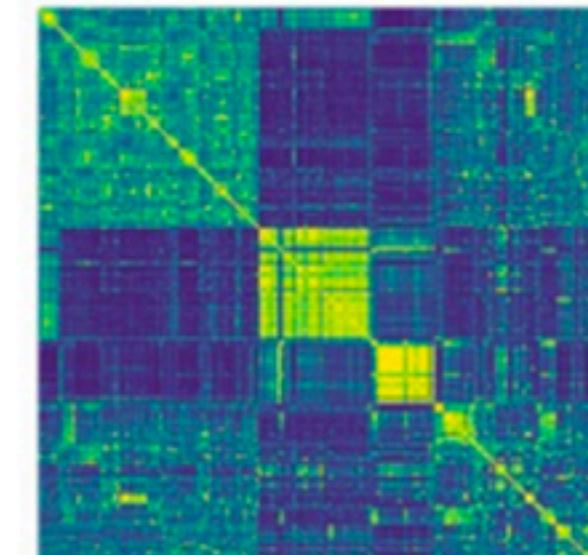
Object  
dimensions



Predicted choice behaviour



Predicted object similarity



1,854 objects

# Multivariate Analysis - RSA

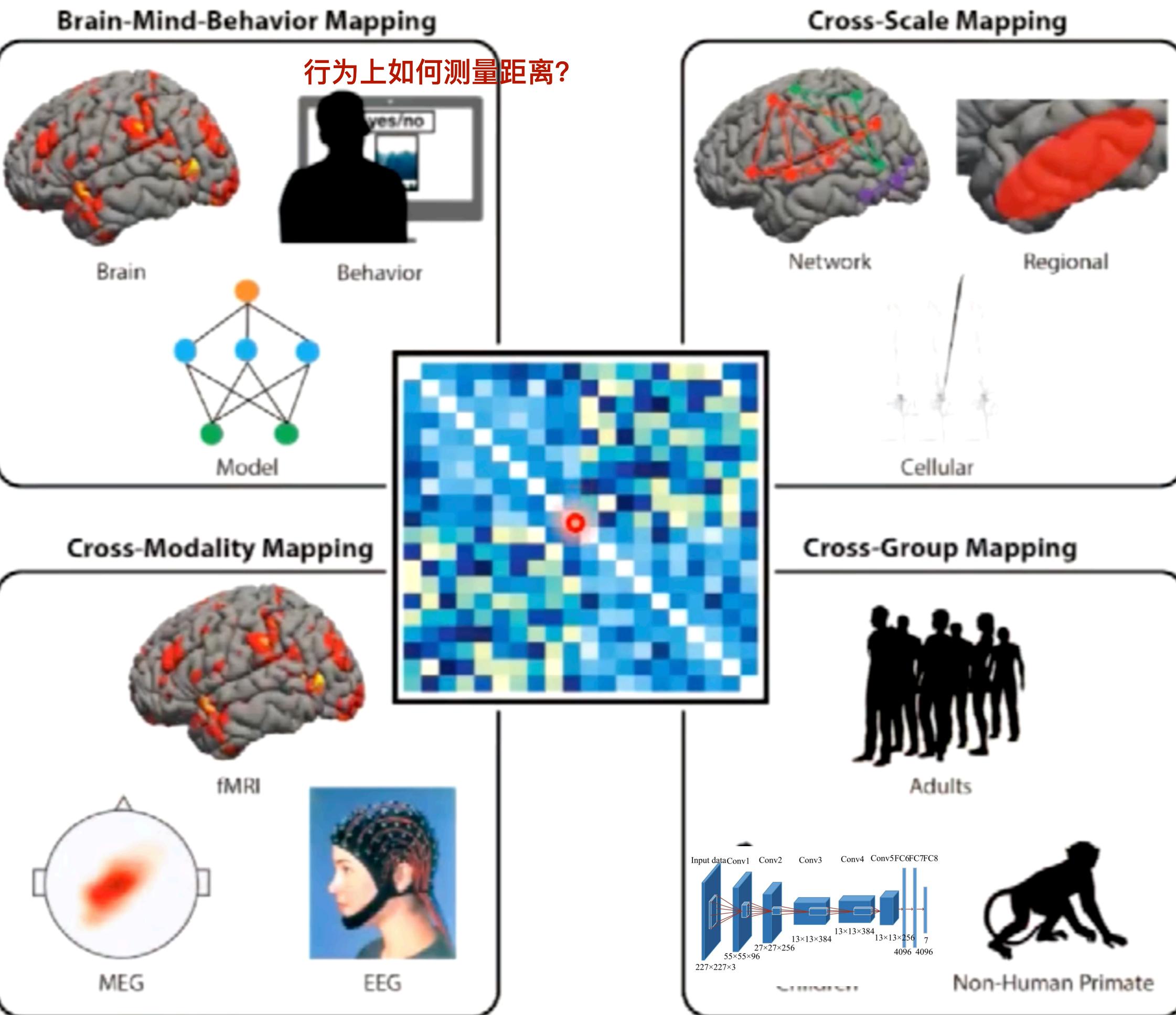
## REPRESENTATIONAL SIMILARITY ANALYSIS



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### Cons

- 1) RSA忽略了物理空间的差异, fMRI 的voxel位置已经不再重要了
- 2) RSA强调了表征差异, 而忽略了表征强度的区别
- 3) 基于Correlation的RSA过分关注所有channel(Voxel, Neuron, etc.)的反应, 可能忽略了少部分channel 的特有表征。



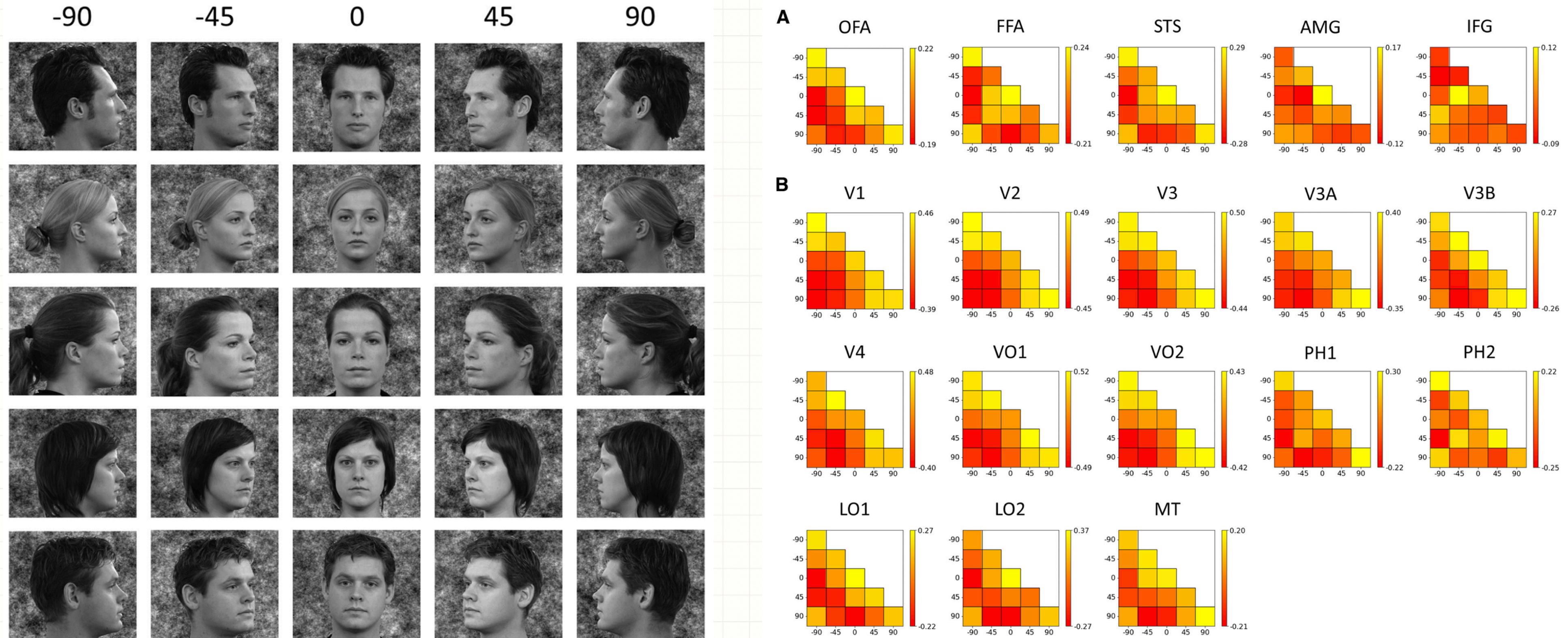
# Multivariate Analysis - RSA



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## REPRESENTATIONAL SIMILARITY ANALYSIS

Example - Use RSA to determine whether the representation of symmetrical viewpoints in face-selective regions is directly linked to the perception and recognition of face identity



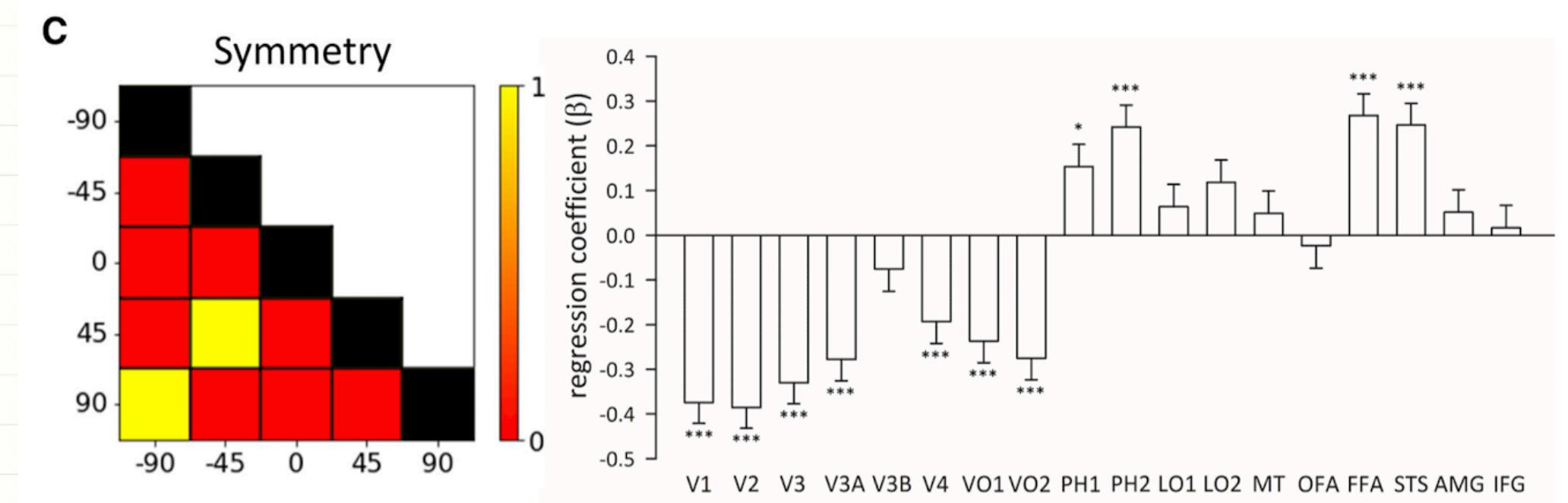
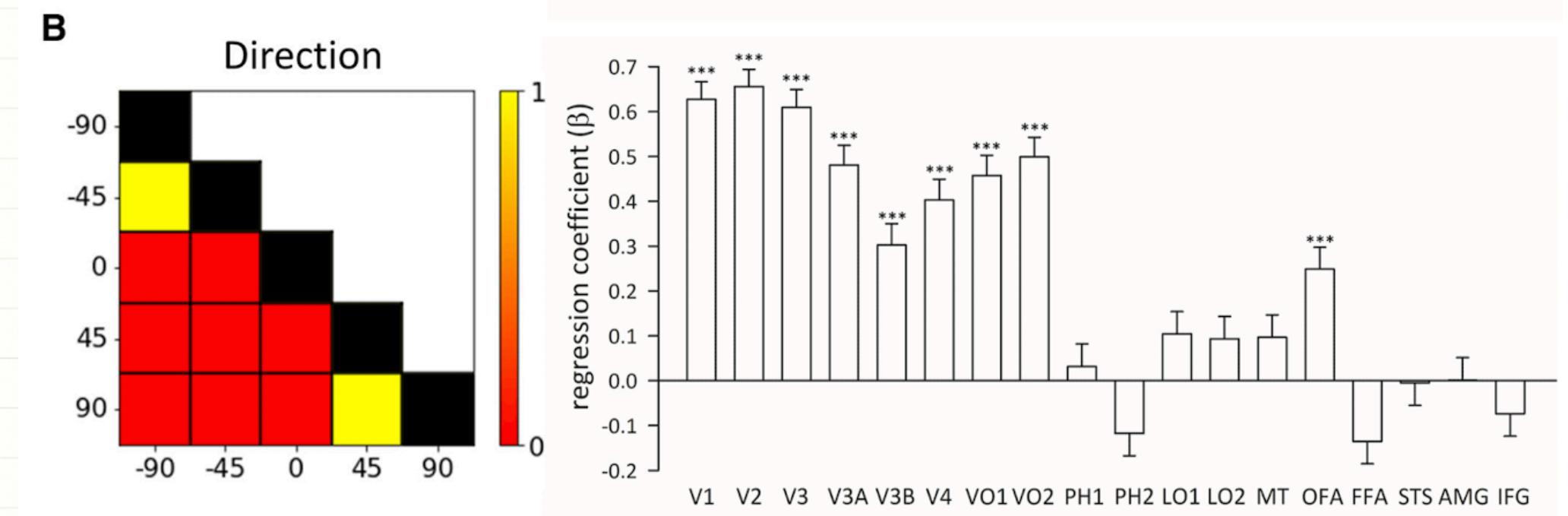
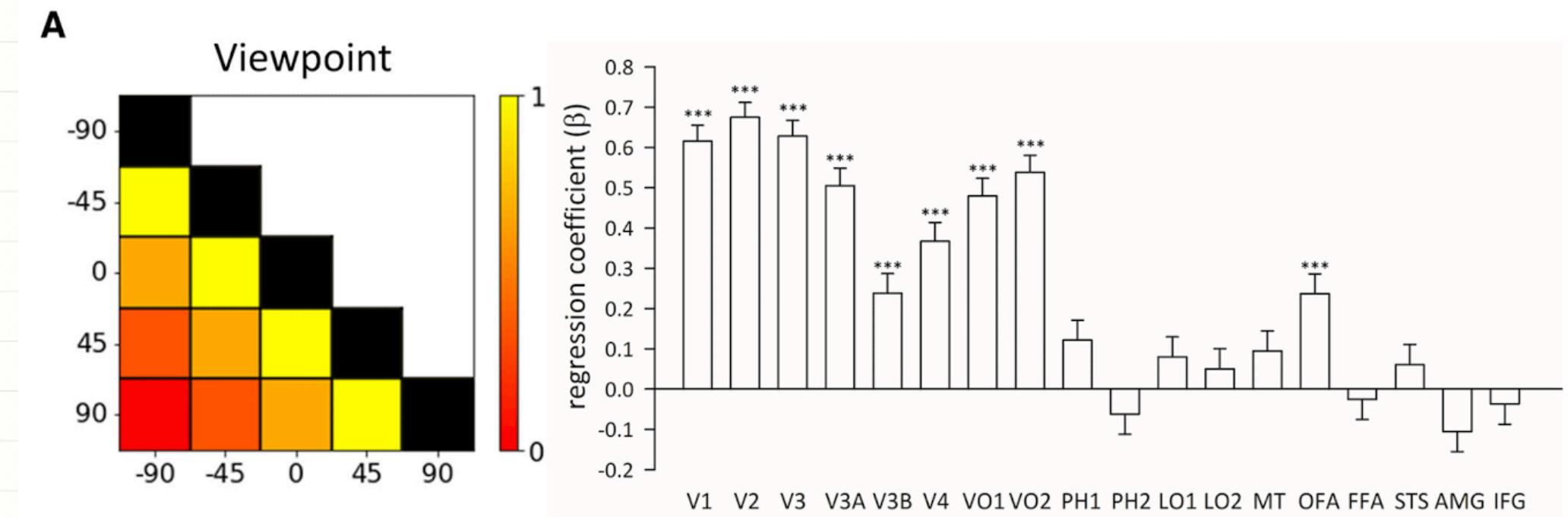
Symmetrical Viewpoint Representations in Face-Selective Regions Convey an Advantage in the Perception and Recognition of Faces

# Multivariate Analysis - RSA

## REPRESENTATIONAL SIMILARITY ANALYSIS

**Example - Use RSA to determine whether the representation of symmetrical viewpoints in face-selective regions is directly linked to the perception and recognition of face identity**

**fMRI - model**



Symmetrical Viewpoint Representations in Face-Selective Regions Convey an Advantage in the Perception and Recognition of Faces

# Multivariate Analysis - RSA

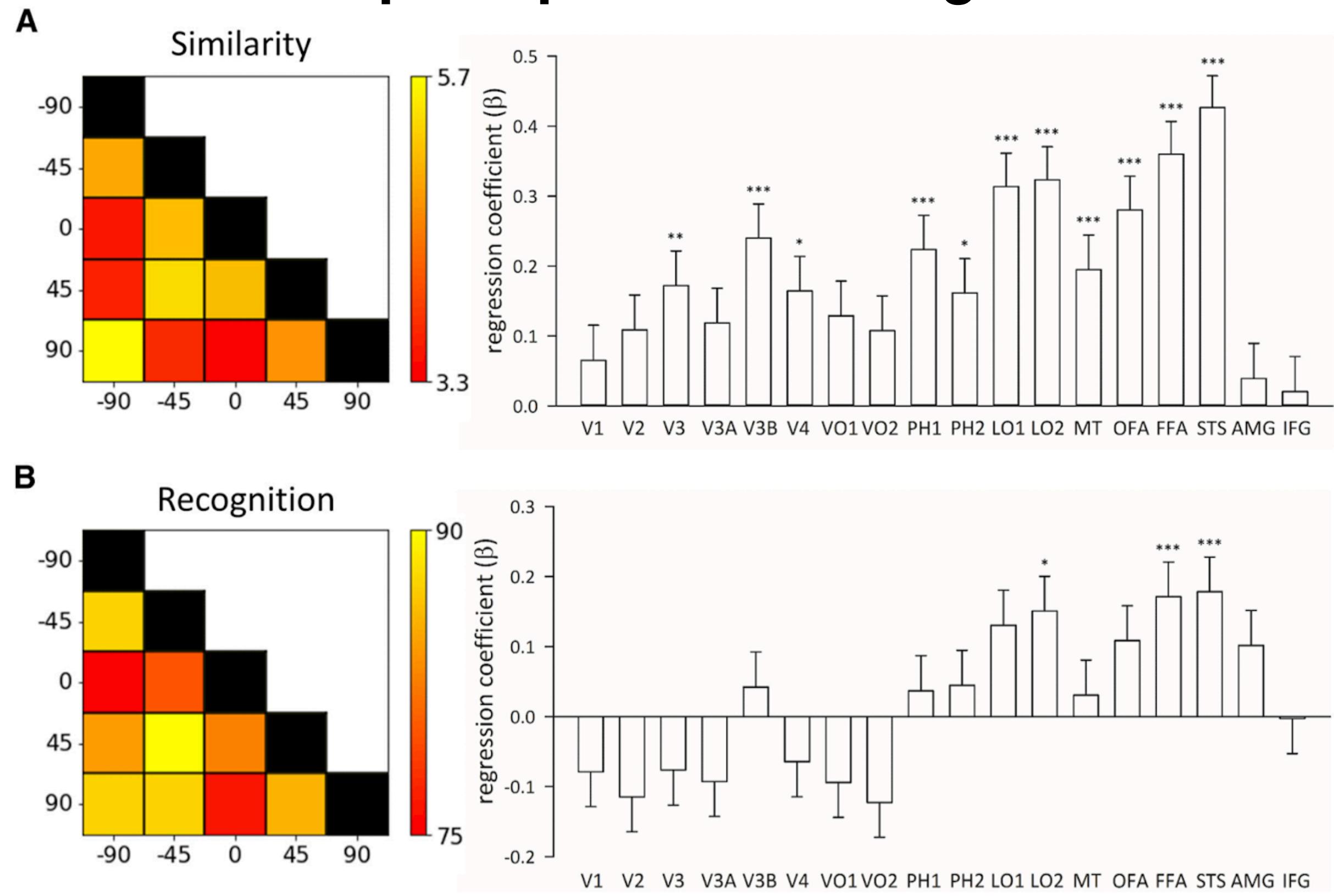
## REPRESENTATIONAL SIMILARITY ANALYSIS



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Example - Use RSA to determine whether the representation of symmetrical viewpoints in face-selective regions is directly linked to the perception and recognition of face identity

fMRI - behavior



Symmetrical Viewpoint Representations in Face-Selective Regions Convey an Advantage in the Perception and Recognition of Faces

# Recommended Reading



## Decoding Neural Representational Spaces Using Multivariate Pattern Analysis

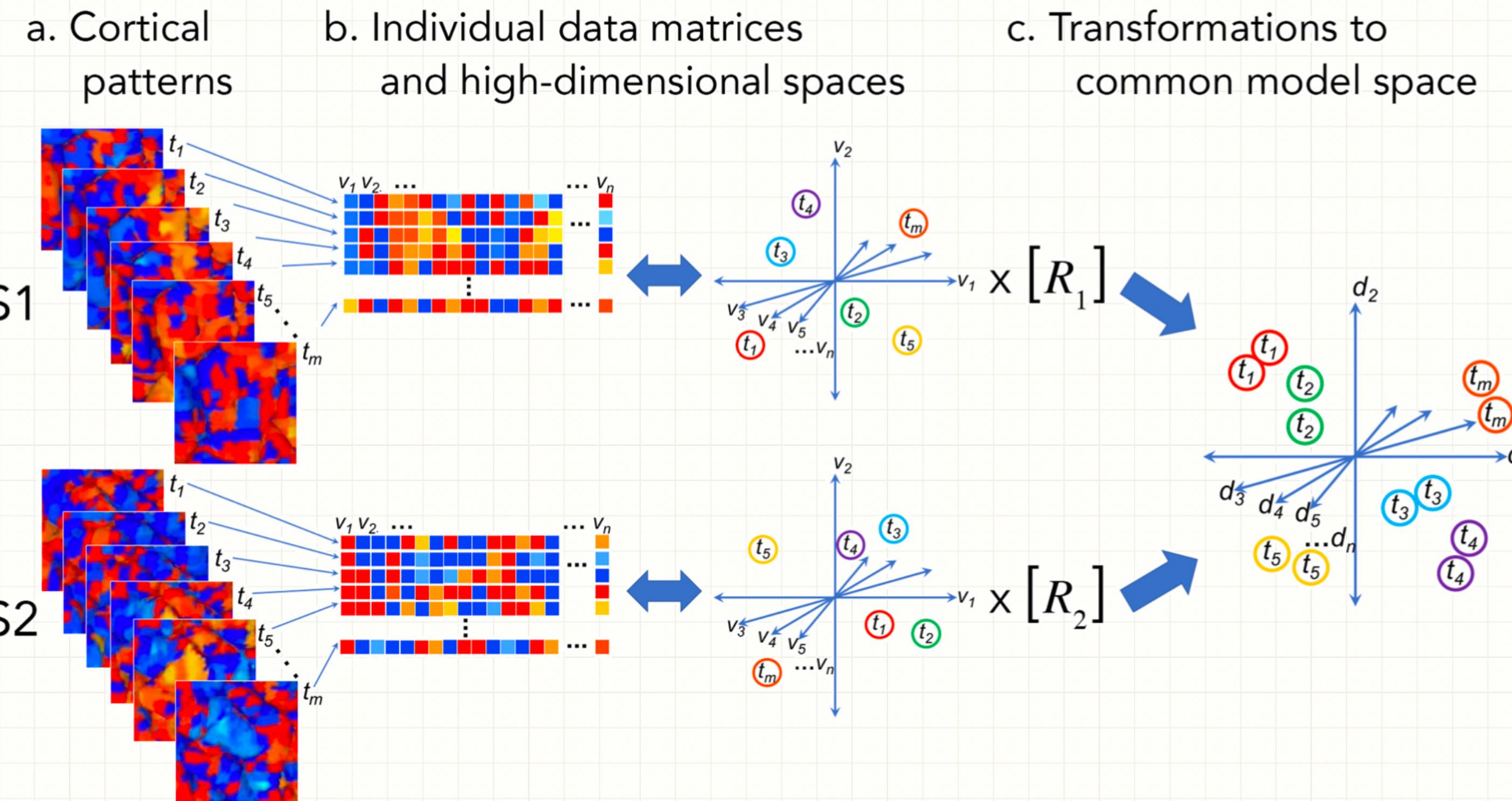
James V. Haxby,<sup>1,2</sup> Andrew C. Connolly,<sup>1</sup>  
and J. Swaroop Guntupalli<sup>1</sup>

<sup>1</sup>Department of Psychological and Brain Sciences, Center for Cognitive Neuroscience,  
Dartmouth College, Hanover, New Hampshire 03755;  
email: james.v.haxby@dartmouth.edu, andrew.c.connolly@dartmouth.edu,  
swaroopgj@gmail.com

<sup>2</sup>Center for Mind/Brain Sciences (CIMeC), University of Trento, Rovereto,  
Trentino 38068, Italy

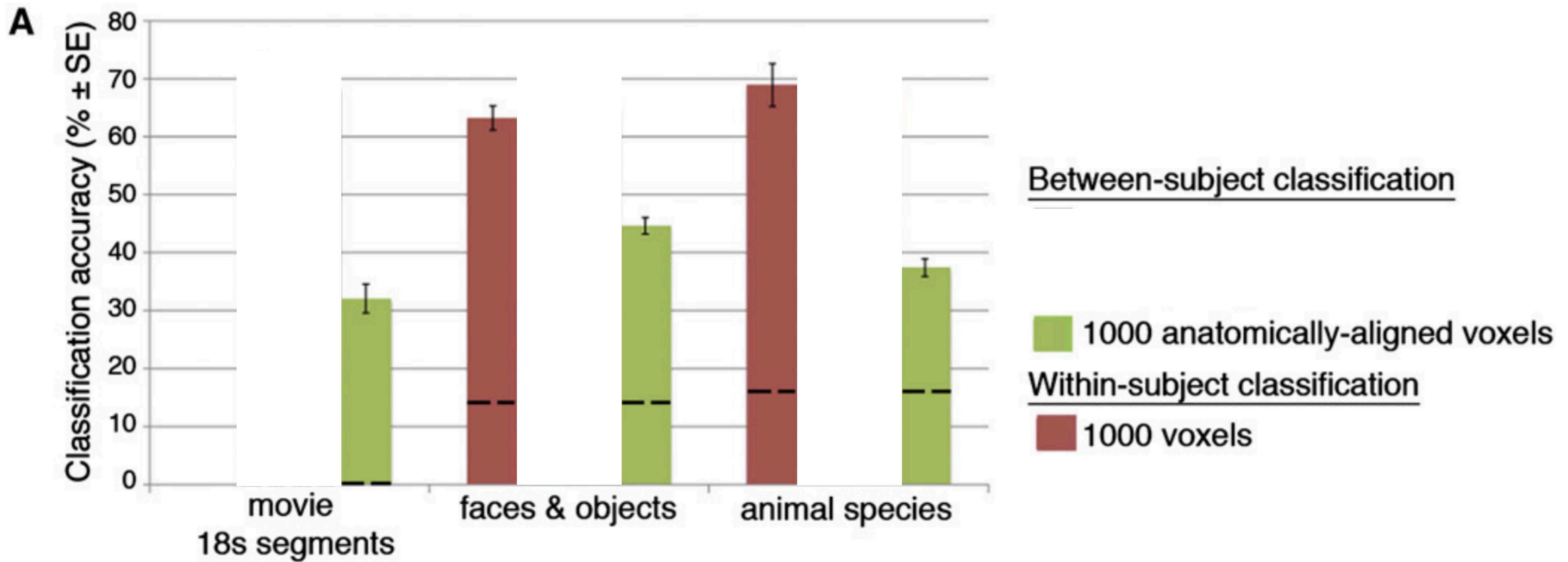
# 功能磁共振中的大脑超配准

## Cortical Hyper-alignment in fMRI



# Cross-Subject MVPA

MVPA performs poorly in cross-subject decoding



Haxby, J. V., Guntupalli, J. S., Connolly, A. C., Halchenko, Y. O., Conroy, B. R., Gobbini, M. I., ... & Ramadge, P. J. (2011). A common, high-dimensional model of the representational space in human ventral temporal cortex. *Neuron*, 72(2), 404-416.

# Cross-Subject MVPA



## Neural mind-reading technique performs poorly in cross-subject decoding

### Actual stimulus

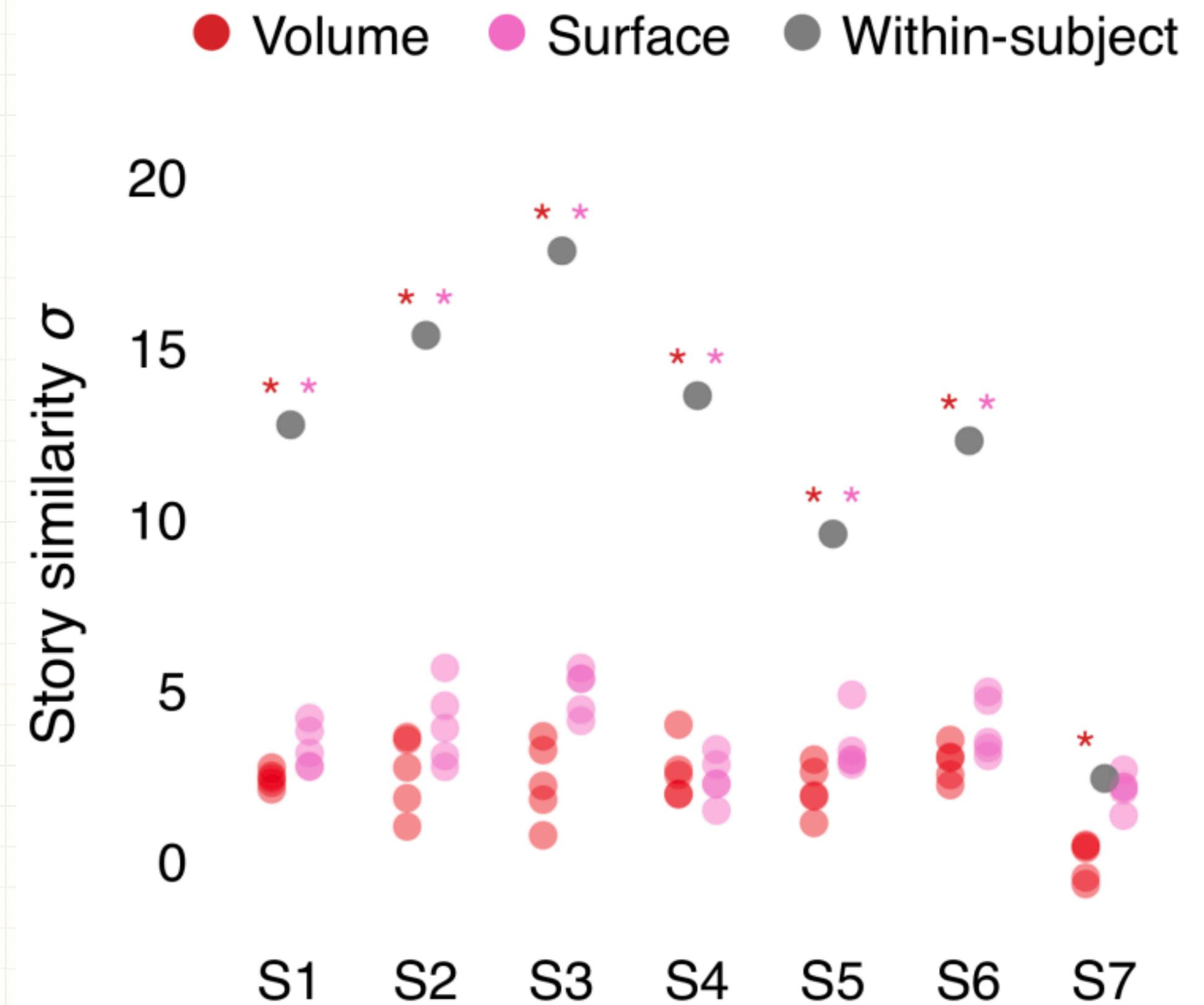
*i got up from the air mattress and pressed my face against the glass of the bedroom window expecting to see eyes staring back at me but instead finding only darkness*

*i didn't know whether to scream cry or run away instead i said leave me alone i don't need your help adam disappeared and i cleaned up alone crying*

### Decoded stimulus

*i just continued to walk up to the window and open the glass i stood on my toes and peered out i didn't see anything and looked up again i saw nothing*

*started to scream and cry and then she just said i told you to leave me alone you can't hurt me i'm sorry and then he stormed off i thought he had left i started to cry*

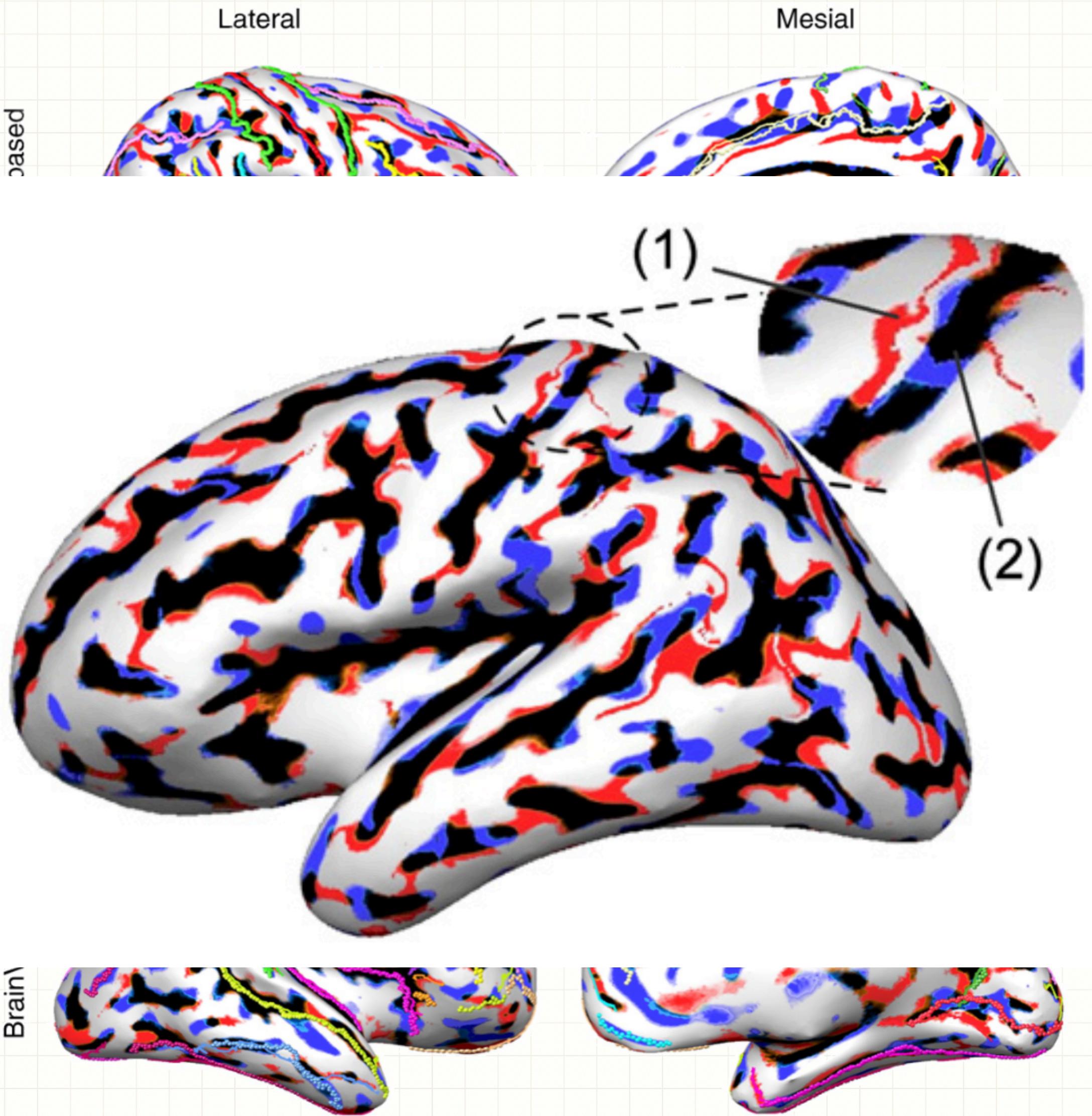


J Tang, A LeBel, S Jain, AG Huth - Nature Neuroscience, 2023

# Cortical registration - Anatomical



- Between subjects registration of the brain is an important issue for group-level analysis in fMRI study.
- Voxel-based method
  - Talairach Space
  - MNI Space
- Surface-based method →
  - Anatomical registration methods can not accurately delineate individual differences in fine-grained cortical architecture



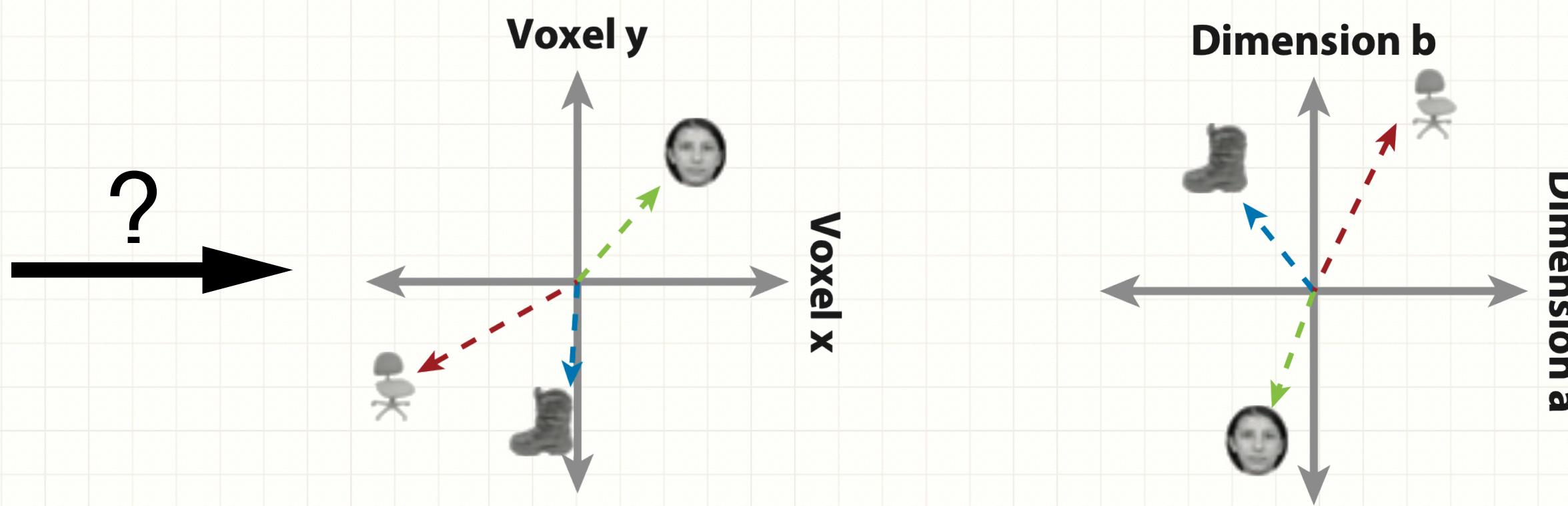
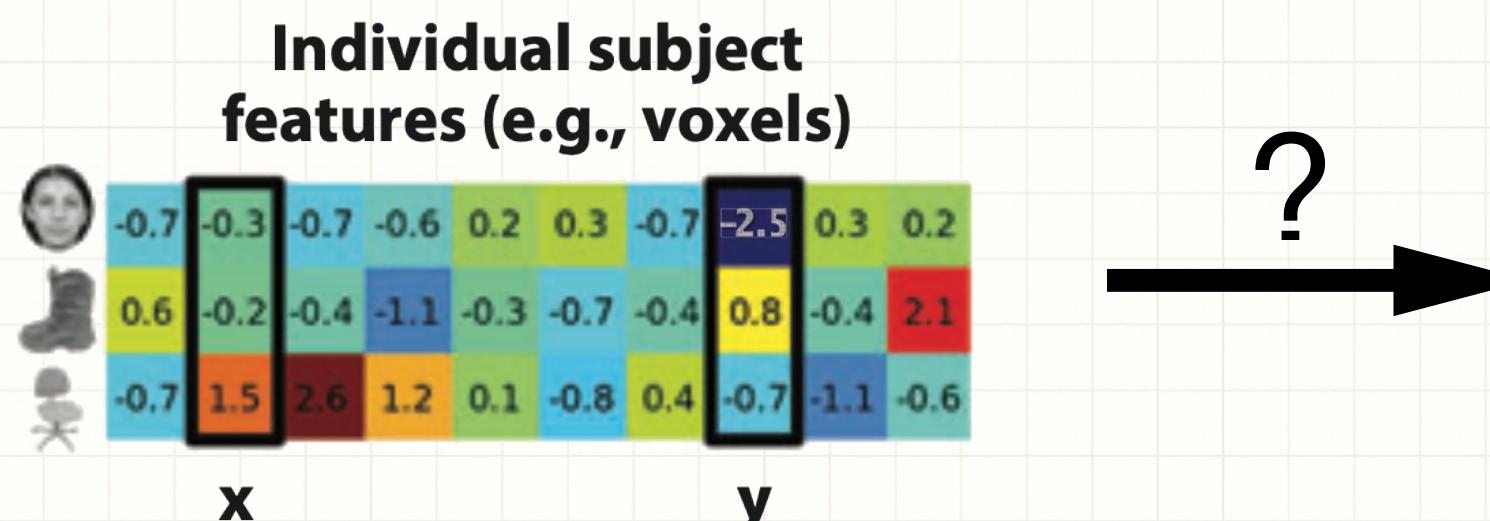
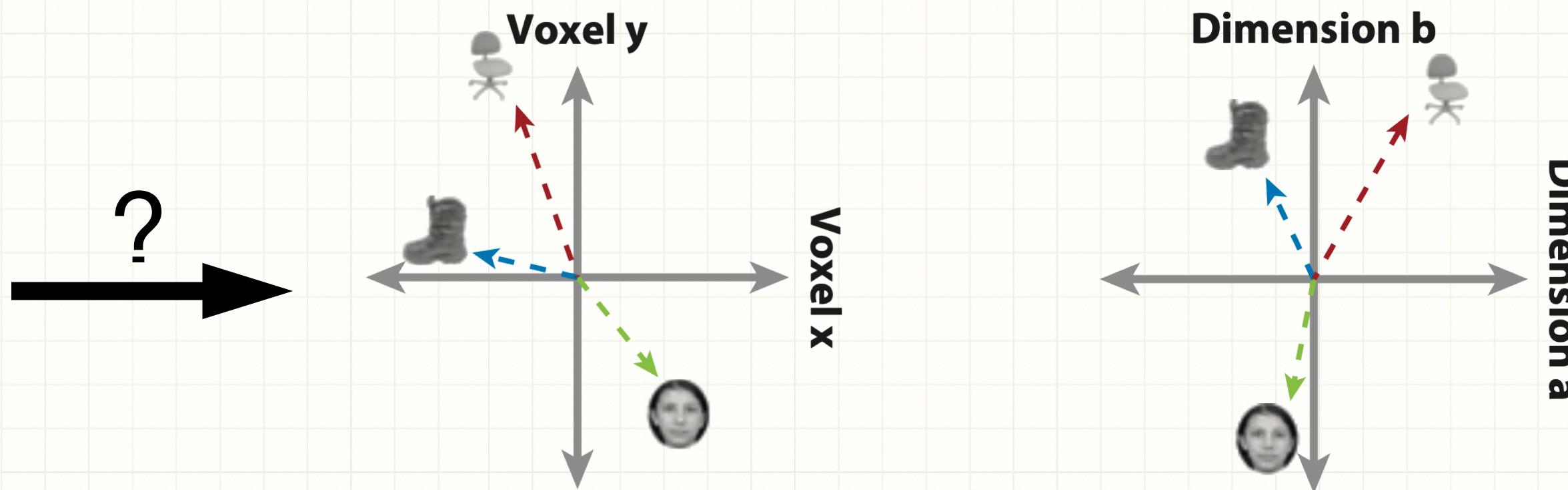
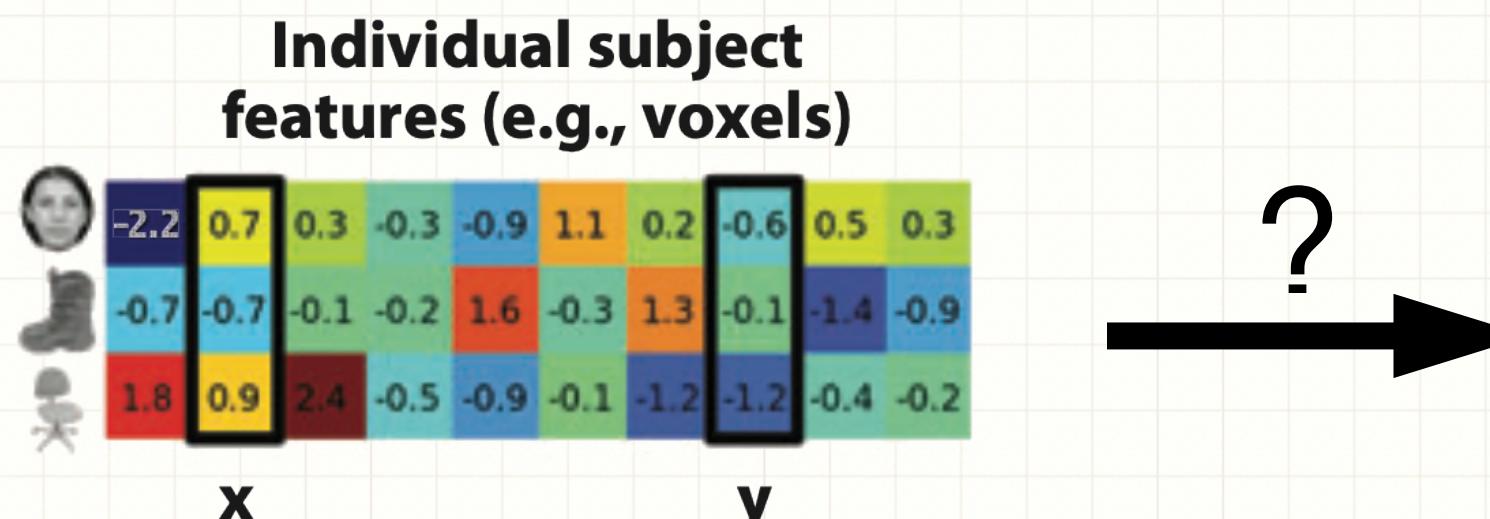
(Pantazis et al., 2010)

# Functional registration: Hyperalignment



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- Cortical response patterns: high-dimensional features
- Multiple subjects: rotate axis based on the shared tuning properties

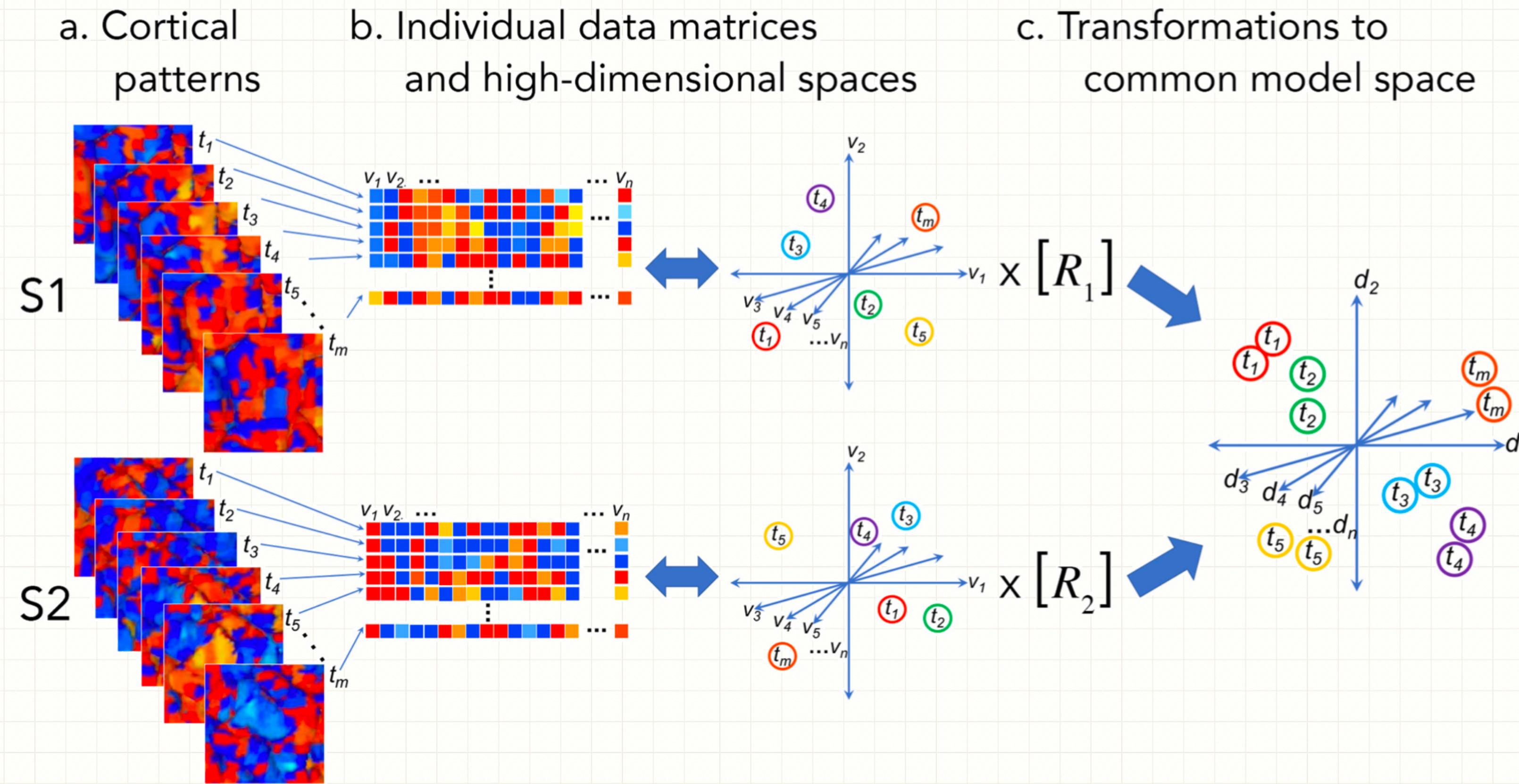


(Haxby et al., 2014)

# Functional registration: Hyperalignment



- Cortical response patterns: high-dimensional features
- Multiple subjects: rotate axis based on the shared tuning properties
- **Hyperalignment: find the orthogonal matrix for high-dimensional axis rotating**



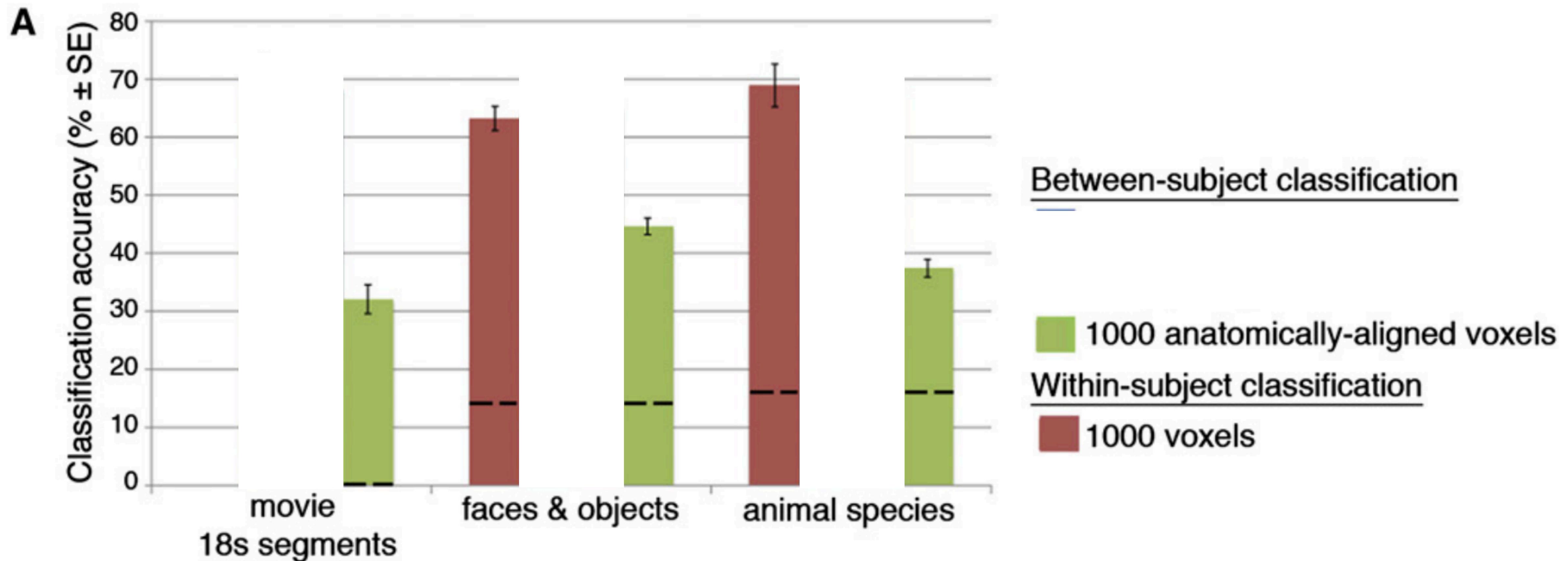
(Haxby et al., 2020)

# Cross-Subject MVPA



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## Improve cross subject mvpa by hyperalignment

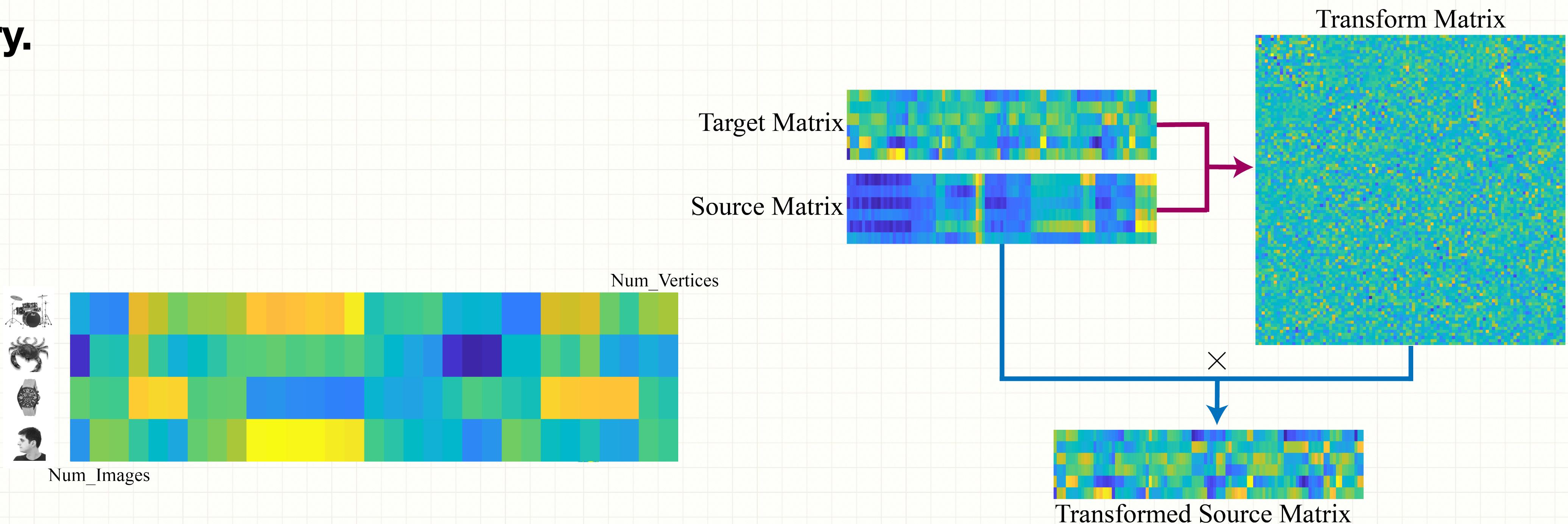


Haxby, J. V., Guntupalli, J. S., Connolly, A. C., Halchenko, Y. O., Conroy, B. R., Gobbini, M. I., ... & Ramadge, P. J. (2011). A common, high-dimensional model of the representational space in human ventral temporal cortex. *Neuron*, 72(2), 404-416.

# Mechanism of HyperAlignment



- Representation Geometry differs for 3 image sets
- The representation of the near-image is the most inconsistent, resulting in the poorest generalization performance.
- Why?
- **procrustes(X,Y) determines a linear transformation (orthogonal rotation) of the points in matrix Y to best conform them to the points in matrix X**
- **The assumption behind procrustes: two systems share the same representation geometry.**



# Progress of HyperAlignment



- Modeling both functional differences and topographic differences by Individualized Neural Tuning (INT) model.

**A** Separating stimulus information  $S$  from response tuning  $T$  in brain responses  $B$

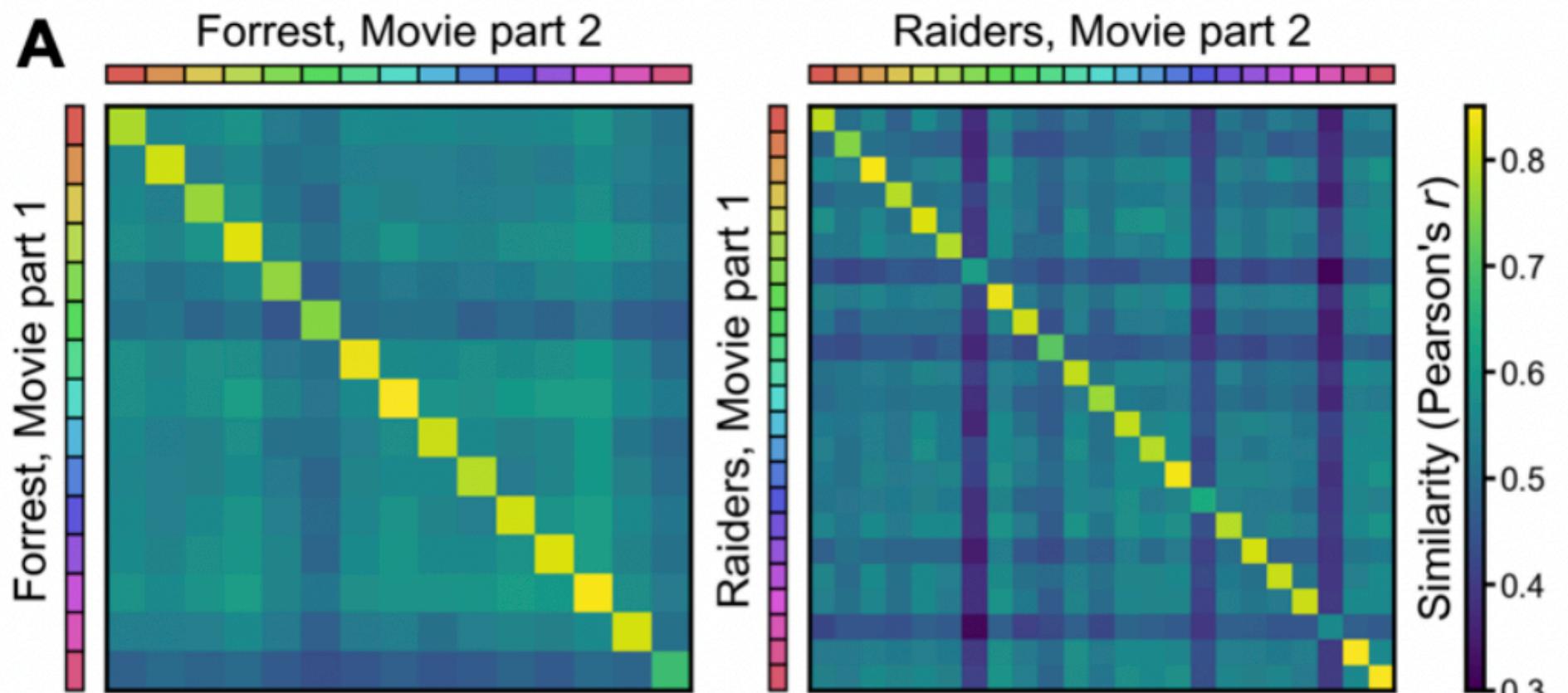
$$t \begin{matrix} v \\ B(p) \end{matrix} = t \begin{matrix} k \\ S \end{matrix} \times \begin{matrix} v \\ T(p) \end{matrix}$$

**B** The same neural response tuning  $T$  underlies different responses  $B$  to different stimuli  $S$

$$\begin{matrix} t_{(1)} & \begin{matrix} v \\ B(p,1) \end{matrix} \\ t_{(2)} & \begin{matrix} v \\ B(p,2) \end{matrix} \end{matrix} = \begin{matrix} t_{(1)} & \begin{matrix} k \\ S_{(1)} \end{matrix} \\ t_{(2)} & \begin{matrix} k \\ S_{(2)} \end{matrix} \end{matrix} \times \begin{matrix} v \\ T(p) \end{matrix}$$

**C** Predicting brain responses  $B$  to new stimuli given  $T$  and the new  $S$

$$t_{(new)} \begin{matrix} v \\ B(p,new) \end{matrix} = t_{(new)} \begin{matrix} k \\ S_{(new)} \end{matrix} \times \begin{matrix} v \\ T(p) \end{matrix}$$

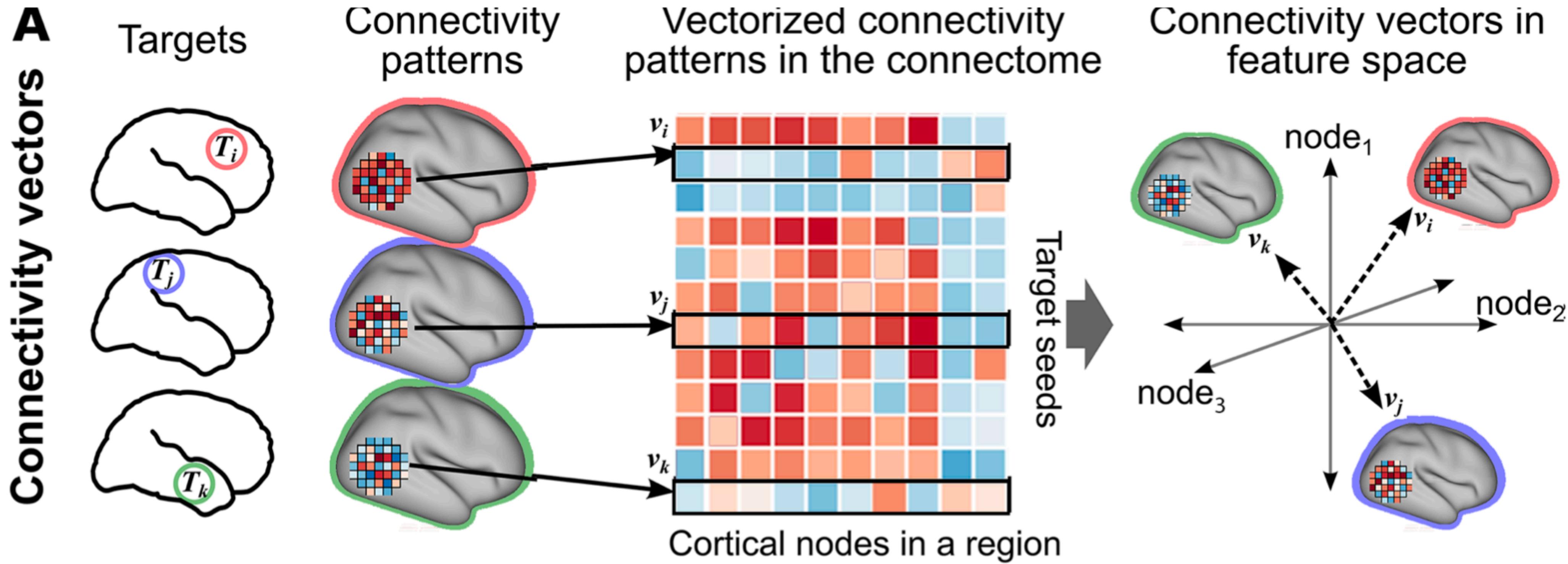


(Ma et al., 2022, bioRxiv)

# Progress of HyperAlignment



- Fine scale connectome hyperalignment



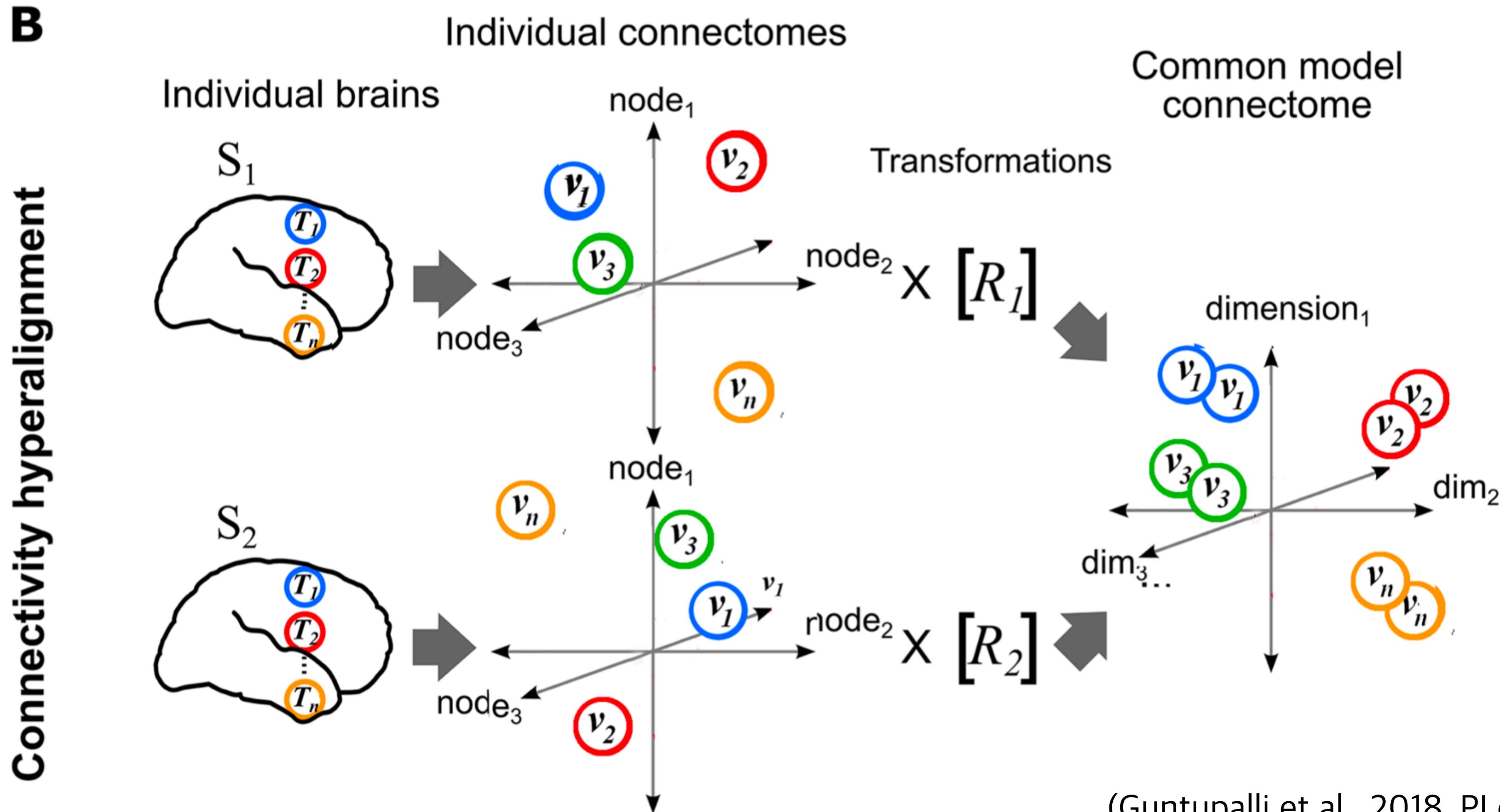
(Guntupalli et al., 2018, PLoS computational biology)

# Progress of HyperAlignment



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- Fine scale connectome hyperalignment



# Progress of HyperAlignment

## Cross-movie prediction of individualized functional topography

Guo Jiahui, Ma Feilong, Samuel A. Nastase, James V. Haxby, M. Ida Gobbini

doi: <https://doi.org/10.1101/2022.11.21.517253>

