

x	variables	
i	integer literals	
τ, σ	$::=$	types
	\mathbb{Z}	
	void	
	$\tau_1 \rightarrow \tau_2$	
	(τ)	S
e	$::=$	annotated terms
	u^τ	
u	$::=$	raw terms
	x	
	i	
	$\lambda(x : \tau).e$	bind x in e
	$e_1 e_2$	
	$e_1 p e_2$	
	if0 (e_1, e_2, e_3)	
	let $x = e$ in u	bind x in u
	halt e	
	(u)	S
p	$::=$	primitives
	$+$	
	$-$	
Γ	$::=$	contexts
	$\Gamma, x : \tau$	

$\boxed{\Gamma \vdash_T e : \tau}$ annotated typing

$$\frac{\Gamma \vdash_T u : \tau}{\Gamma \vdash_T u^\tau : \tau} \quad \text{T_ANT_ANN}$$

$\boxed{\Gamma \vdash_T u : \tau}$ typing

$$\frac{\Gamma(x) = \tau}{\Gamma \vdash_T x : \tau} \quad \text{T_TERM_VAR}$$

$$\frac{}{\Gamma \vdash_T i : \mathbb{Z}} \quad \text{T_TERM_INT}$$

$$\frac{\Gamma, x_1 : \tau_1 \vdash_T e : \tau_2}{\Gamma \vdash_T \lambda(x_1 : \tau_1).e : \tau_1 \rightarrow \tau_2} \quad \text{T_TERM_LAM}$$

$$\frac{\Gamma \vdash_T e_1 : \tau_1 \rightarrow \tau_2 \quad \Gamma \vdash_T e_2 : \tau_1}{\Gamma \vdash_T e_1 e_2 : \tau_2} \quad \text{T_TERM_APP}$$

$$\frac{\Gamma \vdash_T e_1 : \mathbb{Z} \quad \Gamma \vdash_T e_2 : \mathbb{Z}}{\Gamma \vdash_T e_1 p e_2 : \mathbb{Z}} \quad \text{T_TERM_PRIM}$$

$$\frac{\Gamma \vdash_{\text{T}} e_1 : \mathbb{Z} \quad \Gamma \vdash_{\text{T}} e_2 : \tau \quad \Gamma \vdash_{\text{T}} e_3 : \tau}{\Gamma \vdash_{\text{T}} \text{if0}(e_1, e_2, e_3) : \tau} \quad \text{T_TERM_IF0}$$

$\boxed{\Gamma \vdash_{\text{K}} e : \tau}$ annotated typing

$$\frac{\Gamma \vdash_{\text{K}} u : \tau}{\Gamma \vdash_{\text{K}} u^\tau : \tau} \quad \text{K_ANT_ANN}$$

$\boxed{\Gamma \vdash_{\text{K}} u : \tau}$ typing

$$\frac{\Gamma(x) = \tau}{\Gamma \vdash_{\text{K}} x : \tau} \quad \text{K_TERM_VAR}$$

$$\frac{}{\Gamma \vdash_{\text{K}} i : \mathbb{Z}} \quad \text{K_TERM_INT}$$

$$\frac{\Gamma, x : \tau \vdash_{\text{K}} e : \text{void}}{\Gamma \vdash_{\text{K}} \lambda(x : \tau).e : \tau \rightarrow \text{void}} \quad \text{K_TERM_LAM}$$

$$\frac{\Gamma \vdash_{\text{K}} e : \tau \quad \Gamma, x : \tau \vdash_{\text{K}} u : \text{void}}{\Gamma \vdash_{\text{K}} \text{let } x = e \text{ in } u : \text{void}} \quad \text{K_TERM_LET}$$

$$\frac{\Gamma \vdash_{\text{K}} e_1 : \mathbb{Z} \quad \Gamma \vdash_{\text{K}} e_2 : \mathbb{Z}}{\Gamma \vdash_{\text{K}} e_1 p e_2 : \mathbb{Z}} \quad \text{K_TERM_PRIM}$$

$$\frac{\Gamma \vdash_{\text{K}} e' : \tau \rightarrow \text{void} \quad \Gamma \vdash_{\text{K}} e : \tau}{\Gamma \vdash_{\text{K}} e' e : \text{void}} \quad \text{K_TERM_APP}$$

$$\frac{\Gamma \vdash_{\text{K}} e : \mathbb{Z} \quad \Gamma \vdash_{\text{K}} e_1 : \text{void} \quad \Gamma \vdash_{\text{K}} e_2 : \text{void}}{\Gamma \vdash_{\text{K}} \text{if0}(e, e_1, e_2) : \text{void}} \quad \text{K_TERM_IF0}$$

$$\frac{\Gamma \vdash_{\text{K}} e : \tau}{\Gamma \vdash_{\text{K}} \text{halt } e : \text{void}} \quad \text{K_TERM_HALT}$$

Definition rules: 16 good 0 bad

Definition rule clauses: 39 good 0 bad