```
type variables
       variables
\boldsymbol{x}
i
       integer literals
\tau, \sigma
                 ::=
                                                                                 types
                            \alpha
                            \mathbb{Z}
                           void
                            \tau_1 \rightarrow \tau_2
                                                        bind \alpha in \tau
                            \forall \alpha.\tau
                            \tau_1 \times \tau_2
                                                         S
                            (\tau)
                                                                                 annotated values
v
                            u^{\tau}
                                                                                 values
                            \boldsymbol{x}
                           \lambda(x:\tau).v
                                                         \mathsf{bind}\ x\ \mathsf{in}\ v
                           \lambda(x:\tau).e
                                                         \mathsf{bind}\;x\;\mathsf{in}\;e
                            v_1 v_2
                            v_1 \times v_2
                            v\,\cdot \mathbf{1}
                            v\,\cdot {\tt r}
                            v_1 p v_2
                           \mathsf{ifO}(\mathit{v}_1,\mathit{v}_2,\mathit{v}_3)
                                                         S
                            (u)
                                                                                 primitives
                 ::=
p
d
                                                                                 \frac{1}{2}
                 ::=
                            v
                            v \cdot \mathbf{1}
                            v\,\cdot {\tt r}
                            v_1 p v_2
                                                                                 _{
m terms}
                 ::=
                            let x = d in e \quad bind x in e
                            v'(v)
                           \mathsf{ifO}(\mathit{v},\mathit{e}_1,\mathit{e}_2)
                            \mathsf{halt}\,[\tau]v
\Delta
                 ::=
                                                                                  type contexts
```

 Δ, α

::=

Γ

value contexts

 $\Gamma, x : \tau$

 $\Delta \vdash_{\mathrm{F}} \tau$ type formation

$$\begin{array}{ll} \frac{\alpha \in \Delta}{\Delta \vdash_{F} \alpha} & F_TYPE_VAR \\ \\ \frac{\Delta \vdash_{F} \mathbb{Z}}{\Delta \vdash_{F} \tau_{1}} & F_TYPE_INT \\ \\ \frac{\Delta \vdash_{F} \tau_{1}}{\Delta \vdash_{F} \tau_{2}} & F_TYPE_ARR \\ \\ \frac{\Delta, \alpha \vdash_{F} \tau}{\Delta \vdash_{F} \forall \alpha. \tau} & F_TYPE_ALL \\ \\ \frac{\Delta \vdash_{F} \tau_{1}}{\Delta \vdash_{F} \tau_{2}} & F_TYPE_PROD \\ \\ \end{array}$$

 $\Delta; \Gamma \vdash_{\mathcal{F}} v : \tau$ annotated typing

$$\frac{\Delta; \Gamma \vdash_{\mathcal{F}} u : \tau}{\Delta; \Gamma \vdash_{\mathcal{F}} u^{\tau} : \tau} \quad \mathcal{F}_{-\mathsf{ANV_ANN}}$$

 $\Delta \vdash_{\mathrm{F}} \tau$

 $\Delta; \Gamma \vdash_{\mathrm{F}} u : \tau \mid \text{typing}$

$$\frac{\Gamma(x) = \tau}{\Delta; \Gamma \vdash_{\mathrm{F}} x : \tau} \quad \text{F_-VALUE_VAR}$$

$$\frac{\Delta \vdash_{\mathrm{F}} \tau_{1}}{\Delta; \Gamma \vdash_{\mathrm{F}} v_{1} : \tau_{1} \vdash_{\mathrm{F}} v : \tau_{2}} \quad \text{F_-VALUE_INT}$$

$$\frac{\Delta \vdash_{\mathrm{F}} \tau_{1}}{\Delta; \Gamma \vdash_{\mathrm{F}} \lambda(x_{1} : \tau_{1}) . v : \tau_{1} \to \tau_{2}} \quad \text{F_-VALUE_LAM}$$

$$\frac{\Delta; \Gamma \vdash_{\mathrm{F}} v_{1} : \tau_{1} \to \tau_{2}}{\Delta; \Gamma \vdash_{\mathrm{F}} v_{2} : \tau_{1}} \quad \text{F_-VALUE_APP}$$

$$\frac{\Delta; \Gamma \vdash_{\mathrm{F}} v_{1} : \tau_{1}}{\Delta; \Gamma \vdash_{\mathrm{F}} v_{1} : \tau_{2}} \quad \text{F_-VALUE_APP}$$

$$\frac{\Delta; \Gamma \vdash_{\mathrm{F}} v_{1} : \tau_{1}}{\Delta; \Gamma \vdash_{\mathrm{F}} v_{1} \times v_{2} : \tau_{1} \times \tau_{2}} \quad \text{F_-VALUE_PAIR}$$

$$\frac{\Delta; \Gamma \vdash_{\mathrm{F}} v : \tau_{1} \times \tau_{2}}{\Delta; \Gamma \vdash_{\mathrm{F}} v : \tau_{1} \times \tau_{2}} \quad \text{F_-VALUE_PRL}$$

$$\frac{\Delta; \Gamma \vdash_{\mathrm{F}} v : \tau_{1} \times \tau_{2}}{\Delta; \Gamma \vdash_{\mathrm{F}} v : \tau_{2} \times \tau_{2}} \quad \text{F_-VALUE_PRR}$$

$$\frac{\Delta; \Gamma \vdash_{\mathrm{F}} v : \tau_{1} \times \tau_{2}}{\Delta; \Gamma \vdash_{\mathrm{F}} v : \tau_{2} : \mathbb{Z}} \quad \text{F_-VALUE_PRIM}$$

$$\begin{array}{c} \Delta; \Gamma \vdash_{\mathrm{F}} v_1 : \mathbb{Z} \\ \Delta; \Gamma \vdash_{\mathrm{F}} v_2 : \tau \\ \Delta; \Gamma \vdash_{\mathrm{F}} v_3 : \tau \\ \hline \Delta; \Gamma \vdash_{\mathrm{F}} \mathrm{if0}(v_1, v_2, v_3) : \tau \end{array} \quad \mathrm{F_VALUE_IF0}$$

 $\Delta \vdash_{\mathrm{K}} \tau$ type formation

$$\begin{split} \frac{\alpha \in \Delta}{\Delta \vdash_{\mathrm{K}} \alpha} & \quad \mathrm{K_TYPE_VAR} \\ \\ \frac{\Delta \vdash_{\mathrm{K}} \mathbb{Z}}{\Delta \vdash_{\mathrm{K}} \tau} & \quad \mathrm{K_TYPE_INT} \\ \\ \frac{\Delta \vdash_{\mathrm{K}} \tau}{\Delta \vdash_{\mathrm{K}} \tau \to \mathtt{void}} & \quad \mathrm{K_TYPE_ARR} \\ \\ \frac{\Delta \vdash_{\mathrm{K}} \tau_1}{\Delta \vdash_{\mathrm{K}} \tau_2} & \quad \mathrm{K_TYPE_PROD} \\ \\ \frac{\Delta \vdash_{\mathrm{K}} \tau_1}{\Delta \vdash_{\mathrm{K}} \tau_1 \times \tau_2} & \quad \mathrm{K_TYPE_PROD} \end{split}$$

 $\Delta; \Gamma \vdash_{\mathsf{K}} v : \tau$ annotated typing

$$\frac{\Delta; \Gamma \vdash_{\mathsf{K}} u : \tau}{\Delta; \Gamma \vdash_{\mathsf{K}} u^{\tau} : \tau} \quad \mathsf{K_ANV_ANN}$$

 $\Delta; \Gamma \vdash_{\mathrm{K}} u : \tau$ typing

$$\begin{split} \frac{\Delta \vdash_{\mathsf{K}} \tau}{\Gamma(x) &= \tau} &\quad \mathsf{K}_{\mathsf{L}} \mathsf{VALUE}_{\mathsf{L}} \mathsf{VAR} \\ \frac{\Gamma(x) &= \tau}{\Delta; \Gamma \vdash_{\mathsf{K}} x : \tau} &\quad \mathsf{K}_{\mathsf{L}} \mathsf{VALUE}_{\mathsf{L}} \mathsf{INT} \\ \\ \frac{\Delta; \Gamma \vdash_{\mathsf{K}} i : \mathbb{Z}}{\Delta; \Gamma \vdash_{\mathsf{K}} i : \tau} &\quad \mathsf{K}_{\mathsf{L}} \mathsf{VALUE}_{\mathsf{L}} \mathsf{INT} \\ \\ \frac{\Delta; \Gamma \vdash_{\mathsf{K}} \lambda(x : \tau).e : \tau \to \mathsf{void}}{\Delta; \Gamma \vdash_{\mathsf{K}} v_1 : \tau_1} &\quad \mathsf{K}_{\mathsf{L}} \mathsf{VALUE}_{\mathsf{L}} \mathsf{AM} \\ \frac{\Delta; \Gamma \vdash_{\mathsf{K}} v_1 : \tau_1}{\Delta; \Gamma \vdash_{\mathsf{K}} v_2 : \tau_2} &\quad \mathsf{K}_{\mathsf{L}} \mathsf{VALUE}_{\mathsf{L}} \mathsf{PAIR} \end{split}$$

 $\Delta; \Gamma \vdash_{\mathrm{K}} e$ term formation

$$\begin{array}{ll} \Delta;\Gamma\vdash_{\mathbf{K}}v:\tau\\ \frac{\Delta;\Gamma,x:\tau\vdash_{\mathbf{K}}e}{\Delta;\Gamma,x:\tau\vdash_{\mathbf{K}}e} & \mathrm{K_TERM_LET} \\ \\ \frac{\Delta;\Gamma\vdash_{\mathbf{K}}v:\tau_{1}\times\tau_{2}}{\Delta;\Gamma,x:\tau_{1}\vdash_{\mathbf{K}}e}\\ \\ \frac{\Delta;\Gamma\vdash_{\mathbf{K}}v:\tau_{1}\times\tau_{2}}{\Delta;\Gamma\vdash_{\mathbf{K}}\det x=v\cdot \mathrm{lin}\,e} & \mathrm{K_TERM_PRL} \\ \\ \frac{\Delta;\Gamma\vdash_{\mathbf{K}}v:\tau_{1}\times\tau_{2}}{\Delta;\Gamma,x:\tau_{2}\vdash_{\mathbf{K}}e} & \mathrm{K_TERM_PRR} \\ \\ \frac{\Delta;\Gamma\vdash_{\mathbf{K}}v:\tau_{1}\times\tau_{2}}{\Delta;\Gamma\vdash_{\mathbf{K}}\ker x=v\cdot \mathrm{rin}\,e} & \mathrm{K_TERM_PRR} \\ \\ \frac{\Delta;\Gamma\vdash_{\mathbf{K}}v_{1}:\mathbb{Z}}{\Delta;\Gamma\vdash_{\mathbf{K}}v_{2}:\mathbb{Z}}\\ \\ \frac{\Delta;\Gamma\vdash_{\mathbf{K}}v_{2}:\mathbb{Z}}{\Delta;\Gamma,x:\mathbb{Z}\vdash_{\mathbf{K}}e} & \mathrm{K_TERM_PRIM} \\ \end{array}$$

$$\begin{array}{l} \Delta;\Gamma\vdash_{\mathbf{K}}v':\tau\to \mathtt{void}\\ \Delta;\Gamma\vdash_{\mathbf{K}}v:\tau\\ \hline \Delta;\Gamma\vdash_{\mathbf{K}}v'(v) & \mathbf{K}_{\mathsf{-}\mathsf{TERM_APP}}\\ \\ \Delta;\Gamma\vdash_{\mathbf{K}}v:\mathbb{Z}\\ \Delta;\Gamma\vdash_{\mathbf{K}}e_1\\ \hline \Delta;\Gamma\vdash_{\mathbf{K}}e_2\\ \hline \Delta;\Gamma\vdash_{\mathbf{K}}\mathsf{if0}(v,e_1,e_2) & \mathbf{K}_{\mathsf{-}\mathsf{TERM_HALT}}\\ \hline \Delta;\Gamma\vdash_{\mathbf{K}}v:\tau\\ \hline \Delta;\Gamma\vdash_{\mathbf{K}}\mathsf{halt}\left[\tau\right]v & \mathbf{K}_{\mathsf{-}\mathsf{TERM_HALT}} \end{array}$$

Definition rules: 31 good 0 bad Definition rule clauses: 78 good 0 bad