## TESTING BY DUALIZATION

## Yishuai Li

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Supervisor of Dissertation

Benjamin C. Pierce, Professor of Computer and Information Science

Graduate Group Chairperson

Mayur Naik, Professor of Computer and Information Science

Dissertation Committee

Steve Zdancewic, Professor of Computer and Information Science Boon Thau Loo, Professor of Computer and Information Science Rajeev Alur, Professor of Computer and Information Science Leonidas Lampropoulos, Assistant Professor of Computer Science, University of Maryland

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# ACKNOWLEDGEMENT

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# ABSTRACT

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## Yishuai Li

# Benjamin C. Pierce

Software engineering requires rigorous testing to guarantee the product's quality. Semantic testing of functional correctness is challenged by nondeterminism in systems' behavior, which makes testers difficult to write and reason about.

This thesis presents a language-based technique for testing interactive systems. I propose a theory for specifying and validating systems' nondeterministic behaviors, with guaranteed soundness and correctness. I then apply the theory to testing practices, and show how to derive specifications into interactive tester programs. I also introduce a language design for producing test inputs that can effectively detect and reproduce systems' invalid behaviors.

I evaluate the methodology by specifying and testing real-world systems such as web servers and file synchronizers, demonstrating the derived testers' ability to find disagreements between the specification and the implementation.

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## CHAPTER 1

### INTRODUCTION

Software engineering requires rigorous testing of rapidly evolving programs, which costs manpower comparable to developing the product itself [37]. To guarantee programs' compliance with their specifications, we need testers that can tell compliant implementations from violating ones.

This thesis studies the testing of interactive systems' semantics: The system under test (SUT) interacts with the tester by sending and receiving messages, and the tester determines whether the messages sent by the SUT are valid with respect to the protocol specification.

This chapter provides a brief view of interactive testing (Section 1.1), explains why nondeterminism makes this problem difficult (Sections 1.2–1.3), discusses the field of existing works (Section 1.4), and summarizes the contributions of this thesis in addressing the challenges caused by nondeterminism (Section 1.5).

### 1.1. Interactive Testing

Suppose we want to test a web server that supports GET and PUT methods. The server is a stateful program written as a recursive function:<sup>12</sup>

```
CoFixpoint server (data: key \rightarrow value) := request \leftarrow recv;; match request with | GET k \Rightarrow send (data k);; server data | PUT k v \Rightarrow send Done ;; server (data [k \mapsto v]) end.
```

Here the server function iterates over a parameter called data, which is a key-value store. In each iteration, the server receives a request and computes its response. It then sends back the response and recurses with the updated data.

<sup>&</sup>lt;sup>1</sup>Syntax " $x \leftarrow f$ ; y" encodes a monadic program that binds the result of computation f as variable x in continuation f. For example, to receive a request is to bind the result of recv as variable request in the remaining program that performs pattern matching on it.

<sup>&</sup>lt;sup>2</sup>Syntax "data  $[k\mapsto v]$ " represents a key-value store where k is mapped to v, and all other keys are mapped by data. That is, for all k' that are not equal to k, (data  $[k\mapsto v]$ ) k' is equal to (data k').

We can write a tester client that interacts with the server and determines whether it behaves correctly:

This tester implements a reference server internally that computes the expected behavior. The behavior is then compared against that produced by the SUT. The tester rejects the SUT upon any difference from the computed expectation.

The above tester can be viewed as two modules: (i) a *test harness* that interacts with the server and produces transactions of sends and receives, and (ii) a *validator* that determines whether the transactions are valid or not:

```
(* Compute the expected response and next state of the server. *)
Definition serverSpec request data :=
  match request with
  | GET k \Rightarrow (data k, data)
  | PUT k v \Rightarrow (Done , data [k \mapsto v])
  end.
(* Validate the transaction against the stateful specification. *)
Definition validate spec request response data :=
  let (expect, next) := spec request data in
  if response =? expect then Success next else Failure.
(* Produce transactions for the validator. *)
CoFixpoint harness validator state :=
  request ← random;;
  send request;;
  response ← recv;;
  if validator request response state is Success next
  then harness validator next
  else reject.
Definition tester := harness (validate serverSpec).
```

This testing method works for deterministic systems, whose behavior can be precisely computed from their inputs. But, many systems are allowed to behave nondeterministically. For example, systems may implement various hash algorithms, or buffer network packets in different ways. The following sections discuss nondeterminism by partitioning it in two ways, and explains how they pose challenges to the validator and the test harness.

### 1.2. Internal and external nondeterminism

When people talk to each other, voice is transmitted over substances like air or metal. When testers interact with the SUT, messages are transmitted via the runtime environment. The specification might allow SUTs to behave differently from each other, just like people speaking in different accents; we call it *internal nondeterminism*. The runtime environment might affect the transmission of messages, just like solids transmit voice faster than liquids and gases; we call it *external nondeterminism*.

#### 1.2.1. Internal nondeterminism

Within the SUT, correct behavior may be underspecified. Consider web browsing as an example: If a client has cached a local copy of some resource, then when fetching updates for the resource, the client can ask the server not to send the resource's contents if it is the same as the cached copy. To achieve this, an HTTP server may generate a short string, called an "entity tag" (ETag) [14], identifying the content of some resource, and send it to the client:

The next time the client requests the same resource, it can include the ETag in the GET request, informing the server not to send the content if its ETag still matches:

```
/* Client: */
GET /target HTTP/1.1 HTTP/1.1 304 Not Modified
If-None-Match: "tag-foo"
```

If the ETag does not match, the server responds with code 200 and the updated content as

usual.

Similarly, if a client wants to modify the server's resource atomically by compare-and-swap, it can include the ETag in the PUT request as an If-Match precondition, which instructs the server to only update the content if its current ETag matches:

```
/* Client: */
PUT /target HTTP/1.1 HTTP/1.1 204 No Content

If-Match: "tag-foo"
... content (A) ...

/* Client: */
GET /target HTTP/1.1 HTTP/1.1 200 OK
ETag: "tag-bar"
... content (A) ...
```

If the ETag does not match, then the server should not perform the requested operation, and should reject with code 412:

Whether a server's response should be judged valid or not depends on the ETag it generated when creating the resource. If the tester doesn't know the server's internal state (e.g., before receiving any 200 response that includes an ETag), and cannot enumerate all of them (as ETags can be arbitrary strings), then it needs to maintain a space of all possible values, and narrow the space upon further interactions with the server. For example, "If the server has revealed some resource's ETag as "tag-foo", then it must not reject requests targeting this resource conditioned over If-Match: "tag-foo", until the resource has been modified"; and "Had the server previously rejected an If-Match request, it must reject the same request until its target has been modified."

This idea of remembering matched and mismatched ETags is implemented in Figure 1.1.

```
Definition validate request response
            (data
                        : key \rightarrow value)
            (tag_is
                        : key 	o Maybe etag)
            (tag_is_not: key \rightarrow list etag) :=
  match request, response with
  | PUT k t v, NoContent \Rightarrow
    if t \in tag\_is\_not k then Failure
    else if (tag_is k =? Unknown) || strong_match (tag_is k) t
    then (* Now the tester knows that the data in [k]
           * is updated to [v], but its new ETag is unknown. *)
      Success (data
                            [k \mapsto v],
                tag_is
                            [k \mapsto Unknown],
                tag_is_not [k \mapsto []]
    else Failure
  | PUT k t v, PreconditionFailed \Rightarrow
    if strong_match (tag_is k) t then Failure
    else (* Now the tester knows that the ETag of [k]
           * is other than [t]. *)
      Success (data, tag_is, tag_is_not [k → t::(tag_is_not k)])
  | GET k t, NotModified \Rightarrow
    if t \in tag_is_not then Failure
    else if (tag_is k =? Unknown) || weak_match (tag_is k) t
    then (* Now the tester knows that the ETag of [k]
           * is equal to [t]. *)
      Success (data, tag_is [k \mapsto Known t], tag_is_not)
    else Failure
  | GET k t0, OK t v \Rightarrow
    if weak_match (tag_is k) t0 then Failure
    else if data k =? v
    then (* Now the tester knows the ETag of [k]. *)
      Success (data, tag_is [k → Known t], tag_is_not)
    else Failure
  | \_, \_ \Rightarrow Failure
  end.
```

Figure 1.1: Ad hoc tester for HTTP/1.1 conditional requests. PUT k t v represents a PUT request that changes k's value into v only if its ETag matches t; GET k t is a GET request for k's value only if its ETag does not match t; OK t v indicates that the request target's value is v and its ETag is t.

For each key, the validator maintains three internal states: (i) The value stored in data, (ii) the corresponding resource's ETag, if known by the tester, stored in tag\_is, and (iii) ETags that are known to not match the resource's, stored in tag\_is\_not. Each pair of request and response contributes to the validator's knowledge of the target resource. The tester rejects the SUT if the observed behavior does not match the knowledge gained in previous interactions.

Even simple nondeterminism like ETags requires such careful design of the validator, based on thorough comprehension of the specification. We need to construct the validator in a scalable way for more complex protocols.

#### 1.2.2. External nondeterminism

To discuss the nondeterminism caused by the environment, we need to define the environment concept in testing scenario.

**Definition 1.1** (Environment, input, output, and observations). *Environment* is the substance that the tester and the SUT interact with. *Input* is the subset of the environment that the tester can manipulate. *Output* is the subset of the environment that the SUT can alter. *Observation* is the tester's view of the environment.

When testing servers, the environment is the network stack between the client and the server. The input is the sequence of requests sent by the client, and the output is the sequence of responses sent by the server. The responses are transmitted via the network, until reaching the client side as observations.

The tester shown in Section 1.1 runs one client at a time. It waits for the response before sending the next request, as shown in Figure 1.2. Such tester's observation is guaranteed identical to the SUT's output, so it only needs to scan the requests and responses with one stateful validator.

To reveal the server's behavior upon concurrent requests, the tester needs to simulate multiple clients, sending new requests before receiving previous responses. The network delay

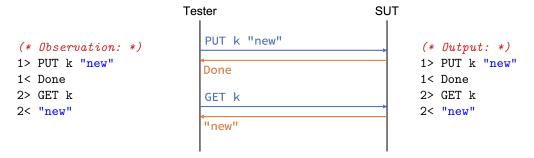


Figure 1.2: With no concurrency, the observation is identical to the output.

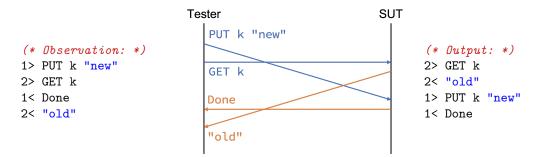


Figure 1.3: Acceptable: The observation can be explained by a valid output reordered by the network environment.

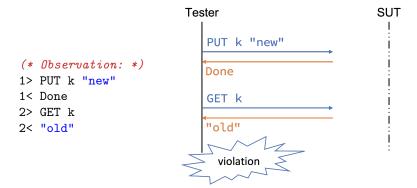


Figure 1.4: Unacceptable: The tester received the Done response before sending the GET request, thus the SUT must have processed the PUT request before the GET request. Therefore, the "old" response is invalid.

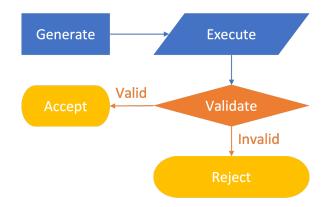


Figure 1.5: Simple tester architecture without shrinking.

might cause the server to receive requests in a different order from that on the tester side. Vice versa, responses sent by the server might be reordered before arriving at the tester, as shown in Figure 1.3. Such tester's observation can be explained by various outputs on the SUT side. The validator needs to consider all possible outputs that can explain such observation, and see if anyone of them complies with the specification. If no valid output can explain the observation, then the tester should reject the SUT, as shown in Figure 1.4.

We need to construct a tester that can handle external nondeterminism systematically, and provide a generic way for reasoning on the environment.

#### 1.3. Test harness and inter-execution nondeterminism

A good tester consists of (i) a validator that accurately determines whether its observations are valid or not, and (ii) a test harness that can reveal invalid observations effectively. Section 1.2 has explained the challenges in the validator. Here we discuss the test harness.

### 1.3.1. Test harness

Intuitively, a tester generates test input and launches the test execution. It then validates the observation and accepts/rejects the SUT, as shown in Figure 1.5.

However, to achieve better coverage, a randomized generator might produce huge test input [19]. Suppose the tester has revealed an invalid observation after thousands of interactions; such a report provides limited intuition of where the bug was introduced. To help

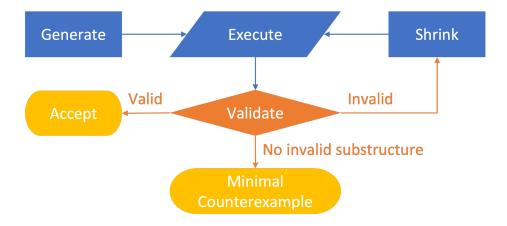


Figure 1.6: Tester architecture with shrinking mechanism.

developers locate the bug more effectively, the tester should present a minimal counterexample that can reproduce the violation. This is done by shrinking the failing input and rerunning the test with the input's substructures. As shown in Figure 1.6, if a test input has no substructure that can cause any failure, then we report it as the minimal counterexample.

The test harness consists of generator, shrinker, and executor. This thesis studies the generator and the shrinker that produce the test input.

Interesting test inputs are those that are more likely to reveal invalid observations. Such subset is usually sparse and cannot be enumerated within reasonable budget e.g. in Subsection 1.2.1, request ETags that match the target resources'. The tester needs to manipulate the inputs' distribution, by implementing heuristics that emphasize certain input patterns, which is challenged by another form of nondeterminism discussed as follows.

# 1.3.2. Inter-execution nondeterminism

Consider HTTP/1.1, where requests may be conditioned over timestamps. If a client has cached a version with a certain timestamp, then it can send the timestamp as If-Modified-Since precondition. The server should not transmit the request target's content if its Last-Modified timestamp is not newer than the precondition's:

/\* Client: \*/

In this scenario, an interesting candidate for the If-Modified-Since precondition in a test case is the Last-Modified timestamp of a previous response. To emphasize this request pattern, the tester needs to implement heuristics that generate test inputs based on previous observations.

HTTP/1.1 304 Not Modified

In case the tester has revealed invalid observations from the server, it needs to rerun the test with shrunk input. The timestamps on the server might be different from the previous execution, so an interesting timestamp in a previous run might become trivial in this run.

The uncertainty that a system may perform differently among executions is called *inter-execution nondeterminism*. Such nondeterminism poses challenges to the input minimization process: To preserve the input pattern, the shrunk HTTP/1.1 request should use the timestamps from the new execution. We need to implement a generic shrinking mechanism that can reproduce the heuristics in the test generator's design.

#### 1.4. State of the Art

This section explains the context for this thesis. I discuss the state of the art in the field of testing, and describe their limitations in addressing the challenges posed by nondeterminism.

## 1.4.1. Property-based testing: QuickCheck

Property-based testing [16] is a testing methodology for validating semantic properties of programs' behavior. The properties are specified as executable boolean predicates over the behavior. To check whether an SUT satisfies a specification, the tester generates test input and executes the SUT with the generated input. The tester then observes the SUT's behavior, and computes the predicates with the observations.

Practices of property-based testing include QuickCheck for Haskell [10] and its variant QuickChick for Coq [23]. These tools can generate random inputs that satisfy logical conditions [24] and integrate with fuzz testing [25] and combinatorial testing [17], and have tested real-world systems like telecoms software [5] and Dropbox [20].

# 1.4.2. Model-based testing: TorXakis

Instead of specifying predicates over systems' behavior, model-based testing [9] defines an abstract model that produces valid behavior. When a tester observes an SUT's behavior, it checks whether the behavior is producible by the specification model.

Practical tools for model-based testing include TorXakis [36], whose modelling language is inspired by Language of Temporal Ordering Specification (LOTOS) [8], the ISO standard for specifying distributed systems. The tool can compile process algebra specifications into tester programs, and can be used for testing dropbox [35].

#### 1.4.3. Limitations

In property-based testing, internal and external nondeterminism makes predicates difficult to write, as discussed in Section 1.2. TorXakis provides limited support for internal nondeterminism, allowing the specification to enumerate all possible values of internal choices. This works for scenarios where the space of choices is small *e.g.* within a dozen. When testing ETags in Subsection 1.2.1, it's infeasible to include a list of all strings in the specification.

To handle inter-execution nondeterminism in QuickCheck, Hughes [19] introduced abstract representations for generating and shrinking test inputs that can adapt to different runtime observations. His technique works for synchronous interactions that blocks the tester to wait for observations, and lacks support for asynchronous testing where the SUT's output may be indefinitely delayed by the environment.

#### 1.5. Contribution

This thesis addresses the challenges in testing caused by various forms of nondeterminism. I introduce symbolic languages for specifying the protocol and representing test input, and dualize the specification into the tester's (1) validator, (2) generator, and (3) shrinker:

1. The specification is written as a reference implementation—a nondeterministic program that exhibits all possible behaviors allowed by the protocol. Internal and external nondeterminism are represented by symbolic variables, and the space of nondeterministic behavior is defined by all possible assignments to the variables.

For internal nondeterminism, the validator computes the symbolic representation of the SUT's output. The symbolic output expectation is then *unified* against the tester's observations, reducing the problem of validating observations to constraint solving.

For external nondeterminism, I introduce a model that specifies the environment. The environment model describes the relation between the SUT's output and the tester's observations. By composing the environment model with the reference implementation, we get a tester-side specification that defines the space of valid observations.

2. Test generation heuristics are defined as computations from observations to the next input. To specify such heuristics in a generic way, I introduce intermediate representations for observations and test inputs, which are protocol-independent.

Heuristics in this framework produce symbolic test inputs that are parameterized over observations. During execution, the test harness computes the concrete input by *instantiating* the symbolic input's arguments with runtime observations.

3. The language for test inputs is designed with inter-execution nondeterminism in mind.

By instantiating the inputs' symbolic intermediate representation with different observations, the test harness gets different test inputs but preserves the pattern.

To minimize counterexamples, the test harness only needs to shrink the inputs' symbolic representation. When rerunning the test, the shrunk input is reinstantiated with the new observations, thus reproduces the heuristics by the test generator.

Thesis claim Symbolic abstract representation can address challenges in testing interactive systems with uncertain behavior. Specifying protocols with symbolic reference implementation enables validating observations of systems with internal and external nondeterminism. Representing test input and observations symbolically allows generating and shrinking interesting test cases despite inter-execution nondeterminism. Combining these methods result in a rigorous tester that can capture protocol violations effectively.

This claim is supported by the following publications:

- 1. From C to Interaction Trees: Specifying, Verifying, and Testing a Networked Server [22], with Nicolas Koh, Yao Li, Li-yao Xia, Lennart Beringer, Wolf Honoré, William Mansky, Benjamin C. Pierce, and Steve Zdancewic, where I developed a tester program based on a swap server's specification written as ITrees [39], and evaluated the tester's effectiveness by mutation testing.
- 2. Verifying an HTTP Key-Value Server with Interaction Trees and VST [41], with Hengchu Zhang, Wolf Honoré, Nicolas Koh, Yao Li, Li-yao Xia, Lennart Beringer, William Mansky, Benjamin C. Pierce, and Steve Zdancewic, where I developed the top-level specification for HTTP/1.1, and derived a tester client that revealed liveness and interrupt-handling bugs in our HTTP server, despite it was formally verified.
- 3. Model-Based Testing of Networked Applications [26], which describes my technique of specifying HTTP/1.1 with symbolic reference implementations, and from the specification, automatically deriving a tester program that can find bugs in Apache and Nginx.

Outline This thesis is structured as follows: Chapter 2 presents a theory for synchronous testing, introduces a language family for representing validators, and shows how to reason about their correctness. Chapter 3 applies the validator theory to an integer machine model that exhibits internal nondeterminism, showing how to derive validators automatically from protocol specifications. Chapter 4 transitions from synchronous testing to asynchronous testing, addressing external nondeterminism by specifying the environment. Chapter 5 presents a mechanism for generating and shrinking test inputs that address inter-execution nondeterminism. To evaluate the techniques I proposed in this thesis, Chapter 6 applies them to testing web servers and file synchronizers. I then compare my technique with related works in Chapter 7, and discuss future directions in Chapter 8.

## CHAPTER 2

## VALIDATOR THEORY

This chapter provides a theoretic view of synchronous testing that involve internal nondeterminsm. Section 2.1 defines the basic concepts in testing. Section 2.2 introduces a language family for writing protocol specifications and validators. Section 2.3 shows how to reason on validators' soundness and completeness with respect to the specification.

# 2.1. Concepts

Testers are programs that determine whether implementations are compliant or not, based on its observations. This section defines the basic concepts and notations in interactive testing.

**Definition 2.1** (Implementations and Traces). *Implementations* are programs that can interact with their environment. *Traces* are the implementations' inputs and outputs during execution. "Implementation i can produce trace t" is written as " $i \stackrel{t}{\longrightarrow}$ ".

This chapter focuses on synchronous testing that assumes no external nondeterminism. Here the tester's observation is identical to the implementation's output, so the tester-side trace is the same as that on the implementation side. Asynchronous testing will be discussed in Chapter 4.

**Definition 2.2** (Specification, Validity, and Compliance). A *specification* is a description of valid traces. "Trace t is *valid* per specification s" is written as "valid $_s$  t".

An implementation i complies with a specification s (written as "comply<sub>s</sub> i") if it only produces traces that are valid per the specification:

$$\mathsf{comply}_s\ i \quad \triangleq \quad \forall t, (i \stackrel{t}{\longrightarrow}) \implies \mathsf{valid}_s\ t$$

**Definition 2.3** (Tester components and correctness). A tester consists of (i) a validator that

accepts or rejects traces (written as "accept<sub>v</sub> t" and "¬accept<sub>v</sub> t"), and (ii) a test harness that triggers different traces with various inputs.

A tester is *correct* if its acceptances and rejections are sound and complete. A tester is rejection-sound if it only rejects non-compliant implementations; it is rejection-complete if it can reject all non-compliant implementations, provided sufficient time of execution.<sup>1</sup>

The tester's correctness is based on its components' properties: A rejection-sound tester requires its validator to be rejection-sound; A rejection-complete tester consists of (i) a rejection-complete validator and (ii) an exhaustive test harness that can eventually trigger invalid traces. The validators' soundness and completeness are defined as follows:

**Definition 2.4** (Correctness of validators). A validator v is rejection-sound with respect to specification s (written as "v sound Rej") if it only rejects traces that are invalid per s:

$$v \operatorname{\mathsf{sound}}_s^{\operatorname{\mathsf{Rej}}} \quad \triangleq \quad \forall t, \neg \operatorname{\mathsf{accept}}_v t \implies \neg \operatorname{\mathsf{valid}}_s t$$

A validator v is rejection-complete with respect to specification s (written as "v complete s") if it rejects all behaviors that are invalid per s:

$$v \; \mathsf{complete}_s^{\mathsf{Rej}} \quad \triangleq \quad \forall t, \neg \mathsf{valid}_s \; t \implies \neg \mathsf{accept}_v \; t$$

The rest of this chapter shows how to construct specifications and validators, and how to prove the validators' correctness with respect to the specifications.

# 2.2. QAC language family

In this section, I introduce the "query-answer-choice" (QAC) language family for writing specifications and validators for network protocols that involve internal nondeterminism.

<sup>&</sup>lt;sup>1</sup>The semantics of "soundness" and "completeness" vary among contexts. This thesis inherits terminologies from existing literature [34], but explicitly uses "rejection-" prefix for clarity. "Rejection soundness" is equivalent to "acceptance completeness", and vice versa.

## 2.2.1. Specifying protocols with server models

Network protocols can be specified with "reference implementations" *i.e.* model programs that exhibit the space of valid behaviors. For client-server systems such as WWW, we can specify networked servers as programs that receive queries and compute the responses. Here I model the server programs with a data structure called state monad.

**Definition 2.5** (State monad). Let S be the state type, A be the result type, then type  $(S \to A \times S)$  represents a computation that, given a pre-state, yields a result and the post state. This computation is pronounced a "state monad with state type S and result type S".

For example, let the state be a key-value mapping  $(K \to V)$ , then we can define get and put computations as follows:

$$\mathtt{get}: K \to ((K \to V) \to V \times (K \to V)) \tag{1}$$

$$get(k)(f) \triangleq (f(k), f) \tag{2}$$

$$put: K \times V \to ((K \to V) \to () \times (K \to V)) \tag{3}$$

$$put(k,v)(f) \triangleq ((), f[k \mapsto v]) \tag{4}$$

These function definitions should be read as:

- 1. The get function takes a key as argument, and constructs a state monad with state type  $(K \to V)$  and result type V.
- 2. Given argument k of type K, get(k) takes a mapping f as pre-state and yields the mapped value f(k) as result. The post state is the original mapping f unchanged.
- 3. The put function takes a key-value pair as argument, and constructs a state monad with state type  $(K \to V)$  and result type "()" (unit type, which corresponds to void return type in C/Java functions).

4. Given argument (k, v) of type  $(K \times V)$ ,  $\operatorname{put}(k, v)$  takes a mapping f as pre-state and substitutes its value at key k with v. The post state is the substituted mapping  $f[k \mapsto v]$ .

Now we can define the server model in terms of state monad:

**Definition 2.6** (Deterministic server model). A deterministic server is an infinite loop whose loop body takes a query and produces a response. The server definition consists of the loop body and a current state:

$$\mathsf{DeterministicServer} \triangleq \exists S, (Q \to S \to A \times S) \times S$$

This type definition is pronounced as: A deterministic server has an initial state of some type S. Its loop body takes a request of type Q and computes a state monad with state type S and result type A, where type A represents the response.

Notice that the server's state type is existentially quantified [29], while its query and response types are not. This is because a protocol specification only defines the space of valid traces, and doesn't require the implementation's internal state to be a specific type.

An instance of server model is written as:

pack 
$$S = \sigma$$
 with (sstep,  $state_0$ )

This expression is pronounced as: The server state is of type  $\sigma$ . Its loop body is function sstep (which has type  $Q \to \sigma \to A \times \sigma$ ) and its initial state is  $state_0$  (which has type  $\sigma$ ).

For example, consider a compare-and-set (CMP-SET) protocol: The server stores a number n. If the client sends a request that is smaller than S, then the server responds with 0. Otherwise, the server sets n to the request and responds with 1:

```
int n = 0;
while (true) {
```

```
int request = recv();
if (request <= n) send(0);
else { n = request; send(1); }
}</pre>
```

Such a server can be modelled as:

$$\operatorname{pack} S = \mathbb{Z} \text{ with } (\lambda(q)(n) \Rightarrow \begin{cases} (0,s) & q \leq n \\ (1,q) & \text{otherwise} \end{cases},$$
 
$$0)$$

In general, servers' responses and transitions might depend on choices that are invisible to the testers, so called internal nondeterminism, as discussed in Subsection 1.2.1. I represent the space of nondeterministic behaviors by parameterizing it over the server's internal choice.

**Definition 2.7** (Nondeterministic server model). A nondeterministic server is an infinite loop whose loop body takes a query and an internal choice to produce a responses. The nondeterministic server definition extends Definition 2.6 with a choice argument of type C:

Server 
$$\triangleq \exists S, (Q \times C \rightarrow S \rightarrow A \times S) \times S$$

Consider changing the aforementioned CMP-SET into compare-and-reset (CMP-RST): When the request is greater than S, the server may reset S to any arbitrary number:

```
int arbitrary();
int n = 0;
while (true) {
  int request = recv();
  if (request <= n) send(0);
  else { n = arbitrary(); send(1); }
}</pre>
```

Its corresponding server model can be written as:

$$\operatorname{pack} S = \mathbb{Z} \text{ with } (\lambda(q,c)(n) \Rightarrow \begin{cases} (0,n) & q \leq n \\ (1,c) & \text{otherwise} \end{cases},$$

This model represents the space of uncertain behavior with the internal choice parameter of type integer. For any value  $(c : \mathbb{Z})$ , the server is allowed to reset S to c.

#### 2.2.2. Valid traces of a server model

By specifying protocols with server models, we can now instantiate the trace validity notation "valid<sub>s</sub> t" in Definition 2.2 in terms of operational semantics.

**Definition 2.8** (Server transitions). Upon request q and choice c, server model s can step to s' yielding response a (written " $s ext{} ext{}$ 

$$\begin{split} s & \xrightarrow[c]{(q,a)} s' & \triangleq & \operatorname{stepServer}(q,c)(s) = (a,s') \\ & \operatorname{stepServer}: Q \times C \to \operatorname{Server} \to A \times \operatorname{Server} \\ & \operatorname{stepServer}(q,c)(s) \triangleq \\ & \operatorname{let}\left(\operatorname{pack} S = \sigma \text{ with } (\operatorname{sstep},state)\right) = s \text{ in} \\ & \operatorname{let}\left(a,state'\right) = \operatorname{sstep}(q,c)(state) \text{ in} \\ & (a,\operatorname{pack} S = \sigma \text{ with } (\operatorname{sstep},state')) \end{split}$$

The stepServer function takes a query and a choice and computes a state monad with state type Server and result type A, by pattern matching on argument (s : Server). Let  $\sigma$  be the server state type of s, sstep be the loop body, and  $(state : \sigma)$  be the current state of s, then

stepServer(q, c)(s) computes the result (a : A) and the post state  $(state' : \sigma)$  using the sstep function, and substitutes the server's pre-step state with the post-step state'.

**Definition 2.9** (Trace validity in QAC). In the QAC language family, a trace is a sequence of  $Q \times A$  pairs. When specifying a protocol with a Server model, a trace t is valid per specification s if and only if it can be *produced* by the server model:

$$\mathsf{valid}_s \ t \quad \triangleq \quad \exists s', s \xrightarrow{t} s'$$

Here the producibility relation in Section 2.1 is expanded with an argument s' representing the post-transition state, pronounced "specification s can produce trace t and step to specification s'":

1. A server model can produce an empty trace and step to itself:

$$s \xrightarrow{\varepsilon} s$$

2. A server model can produce a non-empty trace if it can produce the head of the trace, and step to some server model that produces the tail of the trace:

$$s \xrightarrow{t+(q,a)} s_2 \triangleq \exists s_1, c, s \xrightarrow{t} s_1 \land s_1 \xrightarrow{(q,a)} s_2$$

#### 2.2.3. Validating traces

The validator takes a trace and determines whether it is valid per the protocol specification.

**Definition 2.10** (Validator). A validator is an infinite loop whose loop body takes a pair of query and response and determines whether it is valid or not. The validator iterates over a state of some type V. Given a  $Q \times A$  pair, the loop body may return a next validator

state or return nothing, written as type "option V":

$$\begin{array}{ll} \mathsf{Validator} & \triangleq & \exists V, (Q \times A \to V \to \mathsf{option} \; V) \times V \\ \\ \mathsf{option} \; X & \triangleq & \mathsf{Some} \; (x : X) \mid \mathsf{None} \end{array}$$

For example, a validator for the CMP-SET protocol is written as:

$$\operatorname{pack} V = \mathbb{Z} \text{ with } (\lambda(q,a)(v) \Rightarrow \begin{cases} \text{if } a \text{ is } 1 \text{ then Some } v \text{ else None} & q \leq v \\ \\ \text{if } a \text{ is } 1 \text{ then Some } q \text{ else None} & \text{otherwise} \end{cases},$$

Here the validator state the same as the server model's. The loop body computes the expected response and compares it with the observed response. If they are the same, then the next server state is used as the next validator state. Otherwise, the function returns None, indicating that the response is invalid.

Having defined the validator type, we can now instantiate the trace acception notation "accept, t" in Definition 2.3 in terms of operational semantics.

**Definition 2.11** (Validator transitions). Validator v can consume request q and response a and step to v' (written " $v \xrightarrow{(q,a)} v'$ ") if and only if the post validator can be computed by the stepValidator function:

$$\begin{array}{ll} v \xrightarrow{(q,a)} v' & \triangleq & \mathrm{stepValidator}(q,a)(v) = \mathrm{Some} \ v' \\ & \mathrm{stepValidator} : Q \times A \to \mathrm{Validator} \to \mathrm{option} \ \mathrm{Validator} \\ & \mathrm{stepValidator}(q,a)(\mathrm{pack} \ V = \beta \ \mathrm{with} \ (\mathrm{vstep}, state)) \\ & \triangleq \begin{cases} \mathrm{Some} \ (\mathrm{pack} \ V = \beta \ \mathrm{with} \ (\mathrm{vstep}, state')) & \mathrm{vstep}(q,a, state) = \mathrm{Some} \ state' \\ \mathrm{None} & \mathrm{vstep}(q,a, state) = \mathrm{None} \end{cases} \end{array}$$

The stepValidator function takes a query and a response, and computes the validator transition by pattern matching on argument  $(v : \mathsf{Validator})$ . Let  $\beta$  be the validator state type of v, vstep be the loop body, and  $(state : \beta)$  be the current state of v, then  $\mathsf{stepValidator}(q, a)(v)$  calls the vstep function to validate the  $Q \times A$  pair. If the pair is valid, then vstep returns a post-validation state', which replaces the validator's current state. Otherwise, the validator halts with None.

**Definition 2.12** (Trace acceptance in QAC). A validator accepts a trace if it cosumes the entire trace:

$$\mathsf{accept}_v, t \quad \triangleq \quad \exists v', v \xrightarrow{t} v'$$

1. A validator can consume an empty trace and step to itself:

$$v \xrightarrow{\varepsilon} v$$

2. A validator consumes a non-empty trace if it can consume the head of the trace, and step to some validator that consumes the tail of the trace:

$$v \xrightarrow{t+(q,a)} v_2 \quad \triangleq \quad \exists v_1, v \xrightarrow{t} v_1 \land v_1 \xrightarrow{(q,a)} v_2$$

# 2.3. Soundness and completeness of validators

We can now phrase the correctness properties in Section 2.1 in terms of the QAC language family:

1. A rejection-sound (*i.e.* acceptance-complete) validator consumes all traces that are producible by the protocol specification:

$$\begin{array}{cccc} v \; \mathsf{sound}_s^{\mathsf{Rej}} & \triangleq & \forall t, \neg \mathsf{accept}_v \; t \implies \neg \mathsf{valid}_s \; t \\ & \triangleq & \forall t, (\exists s', s \xrightarrow{t} s') \implies \exists v', v \xrightarrow{t} v' \end{array}$$

2. A rejection-complete (*i.e.* acceptance-sound) validator only consumes traces that are producible by the protocol specification:

$$\begin{array}{cccc} v \; \mathsf{complete}_s^{\mathsf{Rej}} & \triangleq & \forall t, \neg \mathsf{valid}_s \; t \implies \neg \mathsf{accept}_v \; t \\ & \triangleq & \forall t, (\exists v', v \xrightarrow{t} v') \implies \exists s', s \xrightarrow{t} s' \end{array}$$

Both the specification and the validator are infinite loops. To show that the validator consumes the same space of traces as the specification produces, we need to show the correspondence between each server and validator step. This is done by introducing some loop invariant between the server and validator states, and show that it is preserved by the server's and the validator's loop body.

This section shows how to prove that validator pack  $V = \beta$  with (vstep,  $v_0$ ) is sound and complete with respect to the server model pack  $S = \sigma$  with (sstep,  $s_0$ ). The core of the proof is the loop invariant defined as a binary relation between the validator state  $\beta$  and the server state  $\sigma$ . Notation " $(v \sim s)$ " is pronounced "validator state v simulates server state s".

#### 2.3.1. Proving rejection soundness

To prove that any trace producible by the server is consumable by the validator, I perform forward induction on the server's execution path, and show that every step has a corresponding validator step:

• The initial server state  $s_0$  simulates the initial validator state  $v_0$ :

$$v_0 \sim s_0$$
 (RejSound-Init)

• Any server step  $s ext{ } ext{} ext{}$ 

post-execution state s':

$$\forall (q:Q)(c:C)(a:A)(s,s':\sigma)(v:\beta), \tag{RejSound-Step}$$
 
$$s \xrightarrow[c]{(q,a)} s' \wedge v \sim s$$
 
$$\implies \exists (v':\beta), \ v \xrightarrow[c]{(q,a)} v' \wedge v' \sim s'$$



Here syntax " $s \xrightarrow[c]{(q,a)} s'$ " and " $v \xrightarrow[c]{(q,a)} v'$ " are simplified from Definition 2.8 and Definition 2.11, representing the server and validator instances by their states. This is because their state types  $\sigma$ ,  $\beta$  and step functions sstep, vstep remain constant over the transitions.

# 2.3.2. Proving rejection completeness

Rejection completeness says that any trace consumable by the validator is producible by the server model. I construct the server's execution path  $s \xrightarrow{t} s'$  by backward induction of the validation path  $v \xrightarrow{t} v'$ :

• Any accepting validator step  $v \xrightarrow{(q,a)} v'$  has some server state s' that reflects the post-validation state v':

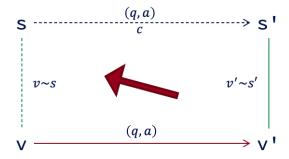
$$\forall (q:Q)(a:A)(v,v':\beta), v \xrightarrow{(q,a)} v'$$
 (RejComplete-End) 
$$\Longrightarrow \exists s': \sigma, v' \sim s'$$

This gives us a final server state from which we can construct the server's execution

path inductively.

• Any accepting validator step  $v \xrightarrow{(q,a)} v'$  whose post-validation state v' reflects some post-execution server state s' has a corresponding server step from a pre-execution state s that reflects the pre-validation state v:

$$\forall (q:Q)(a:A)(v,v':\beta)(s':\sigma), \tag{RejComplete-Step}$$
 
$$\mathsf{vstep}(q,a,v) = \mathsf{Some}\ v' \wedge v' \sim s'$$
 
$$\implies \exists (s:\sigma)(c:C), \mathsf{sstep}(q,c,s) = (a,s') \wedge v \sim s$$



This allows us to inducively construct an execution path starting from some server state that reflects the initial validator state  $v_0$ . To show the existence of an execution path that starts from the initial server state  $s_0$ , we need the following hypothesis:

• The initial validator state  $v_0$  only reflects the initial server state  $s_0$ :

$$\{s \mid v_0 \sim s\} = \{s_0\}$$
 (RejComplete-Init)

Rejection soundness is proven by forward induction, while rejection completeness is proven by backward induction. This is because the choice C is known from the server step, but unknown from the validator step: Given a validator step, we cannot predict "what choices the server will make in the future", but can analyze "what choices the server might have made in the past". This proof strategy is formalized in the Coq proof assistant, and will be

demonstrated with an example in Section 3.3.

# CHAPTER 3

### SYNCHRONOUS VALIDATOR BY DUALIZATION

As discussed in Section 1.2, nondeterminism makes validators difficult to write. To address this challenge, I construct validators *automatically* from the specification. The key idea is to encode the specification with a programming language, and *dualize* the specification program into the validator.

This chapter demonstrates the dualization technique with a programming language in the QAC family. Section 3.1 introduces the Prog language for encoding specifications. Specification written in Prog are dualized into validators in Section 3.2, with correctness proven in Section 3.3.

# 3.1. Encoding Specifications

Constructing the validator automatically requires analyzing the computations of the specification program. The QAC language family in Section 2.2 only provides a state monad interface for server models, which is insufficient for performing structural analysis. This section introduces a programming language for encoding specifications.

For readability, I demonstrate the dualization technique on a subset of QAC server models called integer machine model, featuring random-access memory (RAM) and arithmetic operations. To test real-world systems like web servers, I'll employ a more complex specification language in Chapter 4.

#### 3.1.1. Integer machine model

The server state of an integer machine model is a key-value mapping that resembles a RAM.

The addresses are natural numbers, and the data are integers. The initial server state has

zero data in all addresses:

$$s_0 : \mathbb{N} \to \mathbb{Z}$$
  
 $s_0 = (\_ \mapsto 0)$   
 $i.e. \ \forall (k : \mathbb{N}), s_0!k = 0$ 

Here syntax "s!k" is pronounced "data stored in address !k of memory s".

The server's query, response, and choices (Q, A, C) are of type integer. At the beginning of each server loop, the internal choice is written to address !0, and the query is written to address !1. The server then performs some computation  $f: (\mathbb{N} \to \mathbb{Z}) \to (\mathbb{N} \to \mathbb{Z})$  that manipulates the memory, and then sends back the value stored in address !1 as the response:

$$\mathsf{sstep}_f(q,c)(s) \quad \triangleq \quad \mathsf{let} \ s_1 = s[0 \mapsto c] \ \mathsf{in}$$
 
$$\mathsf{let} \ s_2 = s_1[1 \mapsto q] \ \mathsf{in}$$
 
$$\mathsf{let} \ s_3 = f(s_2) \ \mathsf{in}$$
 
$$(s_3!1,s_3)$$

Each memory-manipulating computation f defines an instance of the integer machine model:

pack 
$$S = \mathbb{N} \to \mathbb{Z}$$
 with  $(\mathsf{sstep}_f, s_0)$ 

Dualizing an integer machine model requires structural analysis of its memory manipulation. Next I'll introduce a programming language to encode computations  $(\mathbb{N} \to \mathbb{Z}) \to (\mathbb{N} \to \mathbb{Z})$ .

## 3.1.2. The Prog modelling language

**Syntax** A program in the Prog language may read and write at any address of the memory, perform arithmetic operations, and make conditional branches:

$$\begin{array}{lll} \mathsf{Prog} & \triangleq & \mathsf{return} & & \mathsf{end} \ \mathsf{computation} \\ & | \ !dst \coloneqq \mathsf{SExp}; \mathsf{Prog} & & \mathsf{write} \ \mathsf{to} \ \mathsf{address} \ dst \in \mathbb{N} \\ & | \ \mathsf{if} \ \mathsf{SExp} \leq \mathsf{SExp} \ \mathsf{then} \ \mathsf{Prog} \ \mathsf{else} \ \mathsf{Prog} & \mathsf{conditional} \ \mathsf{branch} \\ & \mathsf{SExp} & \triangleq \ \mathbb{Z} & \mathsf{constant} \ \mathsf{integer} \\ & | \ !src & \mathsf{read} \ \mathsf{from} \ \mathsf{address} \ \mathit{src} \in \mathbb{N} \\ & | \ \mathsf{SExp} \ \mathit{op} \ \mathsf{SExp} & \mathsf{op} \ \mathsf{o$$

For example, the following program computes the absolute value of data stored in !1, and stores it in address !1:

$$\begin{array}{ll} \text{if} & !1 \leq 0 \\ \\ \text{then} & !1 \leftarrow (0-!1); \text{ return} \\ \\ \text{else} & \text{return} \end{array}$$

**Semantics** Each program  $(p: \mathsf{Prog})$  specifies a computation on the integer machine:

$$\begin{aligned} \operatorname{eval} : \operatorname{Prog} & \to (\mathbb{N} \to \mathbb{Z}) \to (\mathbb{N} \to \mathbb{Z}) \\ & = \begin{cases} s & p \text{ is return} \\ & = \operatorname{eval}(p')(s[dst \mapsto e^s]) & p \text{ is } !dst \coloneqq e; p' \\ & = \operatorname{eval}(\operatorname{if} e_1{}^s \le e_2{}^s \text{ then } p_1 \text{ else } p_2)(s) & p \text{ is if } e_1 \le e_2 \text{ then } p_1 \text{ else } p_2 \end{cases} \\ & e \text{ is } z : \mathbb{Z} \\ & e \text{ is } !src \\ & e_1{}^s \text{ op } e_2{}^s & e \text{ is } e_1 \text{ op } e_2 \end{cases}$$

Here " $e^s$ " is pronounced "evaluating server expression ( $e : \mathsf{SExp}$ ) on memory ( $s : \mathbb{N} \to \mathbb{Z}$ )".

It substitutes all occurrences of "!src" with the data stored in address !src of memory s.

Syntax " $s[k \mapsto v]$ " is pronounced "writing value v to address !k of memory s". It produces a new memory that maps address !k to v, while other addresses remain unchanged from s:

$$s[k \mapsto v] \triangleq k' \mapsto \begin{cases} v & k' = k \\ s!k' & k' \neq k \end{cases}$$

**From Prog to server model** Every program in the **Prog** language corresponds to a server model that performs the computations it specifies:

$$\begin{split} \mathsf{serverOf} : \mathsf{Prog} &\to \mathsf{Server} \\ \\ \mathsf{serverOf}(p) &\triangleq \mathsf{pack} \ S = \mathbb{N} \to \mathbb{Z} \ \mathsf{with} \ (\mathsf{sstep}_{\mathsf{eval}(p)}, s_0) \end{split}$$

For example, the CMP-RST protocol in Subsection 2.2.1 can be constructed by applying serverOf to the following program:

if 
$$!1 \le !2$$
 then  $!1 := 0$ ; return (1)

else 
$$!1 := 1; !2 := !0;$$
 return (2)

The constructed server stores its data n in address !2. When the query stored in !1 is less than or equal to !2 (case 1), the server writes 0 to address !1 as response, and leaves the data untouched in address !2. For queries greater than !2 (case 2), the server writes 1 as response, and updates the data in !2 with the internal choice stored in !0.

Based on specifications written in the Prog language, we can now construct the validator automatically by dualization.

## 3.2. Dualizing Specification Programs

This section presents an algorithm that constructs a validator from the specification program:

$$\mathsf{validatorOf}:\mathsf{Prog}\to\mathsf{Validator}$$

For every program p, validatorOf(p) determines whether a trace is producible by serverOf(p):

$$\forall (p: \mathsf{Prog})(t: \mathsf{list}\; (Q \times A),$$
 
$$(\mathsf{validatorOf}(p) \xrightarrow{t}) \iff (\mathsf{serverOf}(p) \xrightarrow{t})$$

More specifically, given a trace of  $Q \times A$  pairs, the validator determines whether there exists a sequences of internal choices C that explains how the server produces the trace in Definition 2.9.

The idea is similar to the tester in Section 1.1, which validates the trace by executing the serverSpec, and comparing the expected response against the tester's observation.

However, executing a nondeterministic specification does not produce a specific expectation of response, but a space of responses parameterized over the internal choices. Therefore, upon observing a response A, the validator should determine whether there exists a choice C that leads the specification to produce this response.

This reduces the trace validation problem to constraint solving. The validator maintains a set of constraints that unify the responses produced by the specification against the responses observed from the implementation.

More specifically, the validator executes the Prog model and represents internal choices with symbolic variables. These variables are carried along the program execution, so the expected responses are computed as symbolic expressions that might depend on those variables. The validator then constrains that the symbolic response is equal to the concrete observation.

To achieve this goal, the validator stores a symbolic variables for each address of the server model. It also remembers all the constraints added upon observation. These information are called "validation states":

$$(\mathbb{N} \to \mathsf{var}) \times \mathsf{set} \ \mathsf{constraint}$$

Here the constraints are relations between validator expressions (VExps) that may depend on symbolic variables:

$$\begin{array}{lll} \mathsf{constraint} & \triangleq & \mathsf{VExp} \; \mathit{cmp} \; \mathsf{VExp} & \mathit{cmp} \in \{<, \leq, =\} \\ \\ \mathsf{VExp} & \triangleq \; \mathbb{Z} & \mathsf{constant} \; \mathsf{integer} \\ & | \; \#x & \mathsf{variable} \; x \in \mathsf{var} \\ & | \; \mathsf{VExp} \; \mathit{op} \; \mathsf{VExp} & \mathit{op} \in \{+, -, \times, \div\} \end{array}$$

The VExp type replaces SExp's address constructor !src with variable constructor #x. This allows the validator to constrain the values of the same address at different times e.g. the internal choice stored in !0 in different iterations. The validation state maps each address to its current representing variable ( $\mathbb{N} \to \text{var}$ ), which updates as the validator symbolically executes the server program.

Notice that the server program in Subsection 3.1.2 has conditional branches. When executing the specification program, the branch condition might depend on the internal choices, which is invisible to the validator. As a result, the validator doesn't know the exact branch taken by the specification, so it maintains multiple validation states, one for each possible execution path:

set 
$$((\mathbb{N} \to \mathsf{var}) \times \mathsf{set} \; \mathsf{constraint})$$

The initial state of the validator is a single validation state that corresponds to the specification's initial state:

$$\{( \mapsto \#0, \{\#0=0\})\}$$

Here the initial validation state says "all addresses are mapped to variable #0, and the value of variable #0 is constrained to be zero". This reflects the initial server state that maps all addresses to zero value.

The validator's loop body is derived by dualzing the server model:

- 1. When the server performs a write operation !dst := exp, the validator creates a fresh variable x to represent the new value stored in address !dst, and adds a constraint that says x's value is equal to that of exp. This rule also applies to writing the request to address !1 before executing the program.
- 2. When the server makes a nondeterministic branch if e₁ ≤ e₂ then p₁ else p₂, consider both cases: (a) If p₁ was taken, then the validator should add a constraint e₁ ≤ e₂; or
  (b) If p₂ was taken, then the validator should add constraint e₂ < e₁.</li>
- 3. Before executing the program, the server writes the internal choice c to address !0. Accordingly, the validator creates a fresh variable to represent the new value stored in address !0, without adding any constraint.
- 4. After executing the program, the server sends back the value stored in !1 as response.

  Accordingly, the validator adds a constraint that says the variable representing address
  !1 is equal to the observed response.
- 5. When the constraints of a validation state become unsatisfiable, it indicates that the server model cannot explain the observation. This is because either (i) the observation is invalid *i.e.* not producible by the server model, or (ii) the observation is valid, but was produced by a different execution path of the server model.
- 6. The validator accepts the trace if it can be produced by any execution path of the server model. Since each execution path corresponds to a validation state, the validator only needs to remove the unsatisfiable state from the set of states. If the set of validation states becomes empty, it indicates that the observation cannot be explained by any

$$\text{vstep}_p(q,a)(v) \qquad \triangleq \text{let } v' = v_0 \leftarrow v; \\ \text{vstep}_p'(q,a)(v_0) \qquad \text{in} \\ \text{if } v' \text{ is } \varnothing \text{ then None else Some } v' \qquad (6) \\ \text{vstep}_p'(q,a)(v_0) \qquad \triangleq \text{let } v_1 = \text{havoc}(0,v_0) \text{ in} \\ \text{let } v_2 = \text{write}(1,q,v_1) \text{ in} \\ (vs_3,cs_3) \leftarrow \text{exec}(p,v_2); \\ \text{let } cs_4 = cs_3 \cup \{\#(vs_3!1) = a\} \text{ in} \qquad (4) \\ \text{if solvable } cs_4 \text{ then } \{(vs_3,cs_4)\} \text{ else } \varnothing \qquad (5) \\ \begin{cases} \{(vs,cs)\} \\ \text{exec}(p',\text{write}(d,e,(vs,cs))) & \text{if } p \text{ is return} \\ \text{let } v_1 = (vs,cs \cup \{e_1^{vs} \leq e_2^{vs}\}) \text{ in} \\ \text{let } v_2 = (vs,cs \cup \{e_2^{vs} < e_1^{vs}\}) \text{ in} \\ \text{exec}(p_1,v_1) \cup \text{exec}(p_2,v_2) \qquad (2) & \text{then } p_1 \text{ else } p_2) \end{cases} \\ \text{write}(d,e,(vs,cs)) \triangleq \text{let } x_e = \text{fresh } (vs,cs) \text{ in} \qquad (1) \\ (vs[d \mapsto x_e],cs \cup \{\#x_e = e^{vs}\}) \\ \text{havoc}(d,(vs,cs)) \triangleq \text{let } x_c = \text{fresh } (vs,cs) \text{ in } (vs[d \mapsto x_c],cs) \end{cases} \qquad (3)$$

Figure 3.1: Dualizing server model into validator, with derivation rules annotated.

execution path of the specification, so the validator should reject the trace.

This mechanism is formalized in Figure 3.1. Here the notation " $v_0 \leftarrow v$ ;  $\mathsf{vstep}_p'(q, a)(v_0)$ " is a monadic bind for sets: Let  $\mathsf{vstep}_p'$  map each element  $v_0$  in v to a set of validation states  $(\mathsf{vstep}_p'(q, a)(v_0) : \mathsf{set}\ ((\mathbb{N} \to \mathsf{var}) \times \mathsf{set}\ \mathsf{constraint}))$ , and return the union of all result sets as v'.

The validator adds constraints in three circumstances: Rule 1 says the write operation updates the destination with the source expression; Rule 2 guards the branch condition to match its corresponding execution path; Rule 4 unifies the server's symbolic response against the concrete response observed from the implementation.

The constraints added in Rule 1 and Rule 2 are translated from the specification program. Given a server expression ( $e : \mathsf{SExp}$ ) from the source expression or the branch condition, syntax  $e^{vs}$  translates it into a validator expression  $\mathsf{VExp}$  using the validation state vs, by

replacing its addresses with the corresponding variables:

$$e^{vs} \triangleq \begin{cases} n & e \text{ is } z : \mathbb{Z} \\ \#(vs!src) & e \text{ is } !src \\ e_1^{vs} \text{ op } e_2^{vs} & e \text{ is } e_1 \text{ op } e_2 \end{cases}$$

The validator assumes a constraint solver that can determine whether a set of constraints is satisfiable, *i.e.* whether there exists an *assignment* of variables ( $var \rightarrow \mathbb{Z}$ ) that satisfy all the constraints:

$$\forall cs, \text{solvable } cs \iff \exists (asgn: \text{var} \to \mathbb{Z}), asgn \text{ satisfies } cs$$
 
$$asgn \text{ satisfies } cs \triangleq \forall (e_1 \ cmp \ e_2) \in cs, e_1{}^{asgn} \ cmp \ e_2{}^{asgn}$$
 
$$e \text{ is } z : \mathbb{Z}$$
 
$$e^{asgn} \triangleq \begin{cases} z & e \text{ is } z : \mathbb{Z} \\ asgn!x & e \text{ is } \#x \\ e_1{}^{asgn} \ op \ e_2{}^{asgn} & e \text{ is } e_1 \ op \ e_2 \end{cases}$$

Here " $e^{asgn}$ " is pronounced "evaluating validator expression (e: VExp) with assignment ( $asgn: var \to \mathbb{Z}$ )". It substitutes all occurences of "#x" with their assigned value (asgn!x).

Now we have the algorithm that constructs the validator from the specification program p:

$$\mbox{validatorOf}(p) \ \triangleq \ \ \mbox{pack } V = \mbox{set } ((\mathbb{N} \to \mbox{var}) \times \mbox{set constraint}) \mbox{ with}$$
 
$$(\mbox{vstep}_p, \{(\quad \mapsto \#0, \{\#0 = 0\})\})$$

For example, to construct a validator for the CMP-RST protocol in Subsection 2.2.1, we

```
pack V = \operatorname{set} ((\mathbb{N} \to \operatorname{var}) \times \operatorname{set} \operatorname{constraint}) with
 (\lambda(q,a)(v) \Rightarrow \text{let } v' = (vs_0,cs_0) \leftarrow v;
                                         let vs_1 = vs_0[0 \mapsto \mathsf{fresh}\ (vs_0, cs_0)]
                                                                                                              (1)
                                                                                                        in
                                        let x_q = fresh (vs_1, cs_0)
                                                                                                        in
                                         let vs_2 = vs_1[1 \mapsto x_q]
                                                                                                        in
                                         let cs_2 = cs_0 \cup \{ \#x_q = q \}
                                                                                                        in
                                         let cs_{3a0} = cs_2 \cup \{\#(vs_2!1) \le \#(vs_2!2)\} in
                                                                                                               (2a)
                                         let x_{3a1} = fresh (vs_2, cs_{3a0})
                                                                                                        in
                                         let vs_{3a1} = vs_2[1 \mapsto x_{3a1}]
                                                                                                        in
                                         let cs_{3a1} = cs_{3a0} \cup \{ \#x_{3a1} = 0 \}
                                                                                                        in
                                         let cs_{3b0} = cs_2 \cup \{\#(vs_2!2) < \#(vs_2!1)\}
                                                                                                               (2b)
                                                                                                        in
                                         let x_{3b1} = fresh (vs_2, cs_{3b0})
                                                                                                        in
                                         let vs_{3b1} = vs_2[1 \mapsto x_{3b1}]
                                                                                                        in
                                         let <math>cs_{3b1} = cs_{3b0} \cup \{\#x_{3b1} = 1\}
                                                                                                        in
                                         let x_{3b2} = \text{fresh}(vs_{3b1}, cs_{3b1})
                                                                                                        in
                                         let vs_{3b2} = vs_{3b1}[2 \mapsto x_{3b2}]
                                                                                                        in
                                         let cs_{3b2} = cs_{3b1} \cup \{\#x_{3b2} = \#(vs_{3b2}!1)\} in
                                         ((vs_4, cs_4) \leftarrow \{(vs_{3a1}, cs_{3a1}), (vs_{3b2}, cs_{3b2})\};
                                         let cs_5 = cs_4 \cup \{\#(vs_4!1) = a\}
                                         if solvable cs_5 then \{(vs_4, cs_5)\} else \varnothing
                            if v' is \varnothing then None else Some v'
 , \{(\_ \mapsto \#0, \{\#0 = 0\})\}
                                                                                                                      )
```

Figure 3.2: Validator for CMP-RST automatically derived from its specification in Prog. This program consists of three parts: (1) symbolizing the query and internal choice before executing the model, (2) considering both branches in the model program, propagating a validation state for each branch, and (3) filtering the validation states by constraint satisfiability, removing invalid states.

first specify it in Prog as:

if 
$$!1 \le !2$$
 then  $!1 \leftarrow 0$ ; return else  $!1 \leftarrow 0$ ;  $!2 \leftarrow !0$ ; return

This program stores the data n in address !2. If the request is less than or equal to n, then the program writes response 0 to address !1, and leaves the data unchanged; Otherwise, it writes 1 as response, and updates address !2 with the internal choice in !0.

We then apply function validatorOf to this Prog-based specification, resulting in a validator as shown in Figure 3.2. Validators constructed in this way are proven correct in the next section.

### 3.3. Correctness Proof

So far I have introduced the Prog language for writing specifications and shown how to construct a validator from it. This section shows how to prove the soundness and completeness of all validators dualized from Prog-based specifications:

$$\begin{split} \forall p: \mathsf{Prog}, \, \mathsf{let} \, s &= \mathsf{serverOf}(p) \, \, \mathsf{in} \\ &= \mathsf{validatorOf}(p) \, \, \mathsf{in} \\ &= v \, \mathsf{sound}_s^{\mathsf{Rej}} \wedge v \, \mathsf{complete}_s^{\mathsf{Rej}} \\ &= i.e. \, \, \forall t: \mathsf{list} \, (Q \times A), \\ &= \mathsf{valid}_s \, t \, \Longleftrightarrow \, \mathsf{accept}_v \, t \\ &= i.e. \, \, \exists s', s \stackrel{t}{\longrightarrow} s' \, \Longleftrightarrow \, \exists v', v \stackrel{t}{\longrightarrow} v' \end{split}$$

To apply the proof techniques in Section 2.3, I design the loop invariant in Subsection 3.3.1. I then use the invariant to prove the hypotheses for soundness and completeness in Subsection 3.3.2 and Subsection 3.3.3, respectively.

### 3.3.1. Designing loop invariant

Let  $\beta = \mathsf{set}\ ((\mathbb{N} \to \mathsf{var}) \times \mathsf{set}\ \mathsf{constraint})$  be the validator state type, and  $\sigma = \mathbb{N} \to \mathbb{Z}$  be the server state type, then the loop invariant  $(v : \beta) \sim (s : \sigma)$  is a binary relation between the validator state v and the server state s. To define this relation, I first discuss the semantics of validator states.

The validator state is a set of validation states that consist of an address-variable mapping and a set of constraints over the variables. Each validation state defines a space of server states. A validator accepts a trace if it has a validation state whose constraints are satisfiable, which indicates the existence of a server that produces the trace. A corresponding server state can be constructed from any assignment that satisfies the validation state's constraints:

$$vs^{asgn} \triangleq addr \mapsto asgn!(vs!addr)$$

Let  $(vs : \mathbb{N} \to \mathsf{var})$  be a mapping in the validation state,  $(asgn : \mathsf{var} \to \mathbb{Z})$  be an assignment of variables, then  $(vs^{asgn} : \mathbb{N} \to \mathbb{Z})$  is a server state that maps each address !addr to the value assigned by asgn to the address' corresponding variable in vs.

**Definition 3.1** (Loop invariant for Prog-based validators). Validator state v reflects server state s (written " $v \sim s$ ") if the server state lies within the space of servers defined by some validation state (vs, cs)  $\in v$ . That is, there exists an assignment that relates the server state and the validation state:

$$v \sim s \quad \triangleq \quad \exists (vs, cs) \in v, \; \exists asgn,$$
 
$$asgn \; {\sf satisfies} \; cs \; \wedge \; vs^{asgn} = s$$

Having defined the loop invariant, we only need to instantiate the hypotheses in Subsection 2.3.1–2.3.2 with Prog-based definitions. The rest of this section proves the hypotheses for establishing validators' soundness and completeness. The entire proof is formalized in

the Coq proof assitant.

# 3.3.2. Proving rejection soundness

Lemma 3.1 (RejSound-Init).

If: 
$$vs = (\_ \mapsto \#0)$$
  $cs = \{\#0 = 0\}$   $s = (\_ \mapsto 0)$   
Then:  $\{(vs, cs)\} \sim s$ 

*Proof.* Since (vs, cs) is the only element in the validator state, we only need to show that:

$$\exists (asgn: \mathsf{var} \to \mathbb{Z}), \quad asgn \text{ satisfies } cs \ \land \ vs^{asgn} = s$$

By constructing the assignment as:

$$asgn = (\_ \mapsto 0)$$

We have:

$$\#0^{asgn} = 0$$

Thus:

 $asgn \ {\it satisfies} \ cs$ 

We also know that:

$$\forall k, asgn!(vs!k) = 0 = (s!k)$$

Thus:

$$vs^{asgn} = s$$

Lemma 3.2 (RejSound-Step).

$$\forall (q, c, a : \mathbb{Z})(s, s' : \sigma)(v : \beta),$$

$$s \xrightarrow{(q,a)} s' \wedge v \sim s$$

$$\Longrightarrow \exists v' : \beta, \ v \xrightarrow{(q,a)} v' \wedge v' \sim s'$$

*Proof.* The invariant  $v \sim s$  tells us that v contains a pre-validation state that reflects the pre-step server state s:

$$\exists (vs, cs) \in v, \ \exists asgn, \quad asgn \ \text{satisfies} \ cs \ \land \ vs^{asgn} = s$$

The  $\mathsf{vstep}_p'$  function in Figure 3.1 leads to a set of post-validation states. We need to show that some state in it reflects the post-step server state s':

The server's internal choice c was provided, so we know the server's entire execution path. By induction on the Prog syntax, we can choose the right post-validation state (vs', cs') by computing each branch condition, and deduct the satisfying assignment asgn' by computing each write operation's source value and destination variable.

### 3.3.3. Proving rejection completeness

Lemma 3.3 (RejComplete-End).

$$\forall (q, a : \mathbb{Z})(v, v' : \beta), v \xrightarrow{(q, a)} v'$$

$$\Longrightarrow \exists s' : \sigma, v' \sim s'$$

*Proof.* Since the  $\mathsf{vstep}_p$  function in Figure 3.1 checks the nonemptiness of the result, we know that v' must be nonempty. Consider validation state  $(vs', cs') \in v'$ . Since  $\mathsf{vstep}_p'$  checks that

(solvable cs'), we know that:

 $\exists asgn, \quad asgn \text{ satisfies } cs'$ 

Let:

$$s' = vs' \stackrel{asgn}{=}$$

Then we have:

$$(vs',cs') \in v' \land asgn \text{ satisfies } cs' \land vs' \ ^{asgn} = s'$$
 
$$i.e. \ v' \sim s'$$

Lemma 3.4 (RejComplete-Step).

$$\begin{split} \forall (q,a:\mathbb{Z})(v,v':\beta)(s':\sigma), \\ v & \stackrel{(q,a)}{\longrightarrow} v' \ \land \ v' \sim s' \\ & \Longrightarrow \ \exists (s:\sigma)(c:\mathbb{Z}), \ s \stackrel{(q,a)}{\underset{c}{\longrightarrow}} s' \ \land \ v \sim s \end{split}$$

*Proof.* We first construct the pre-step server state  $(s:\sigma\mid v\sim s)$ . We then compute the internal choice c and prove the server step  $s\xrightarrow[c]{(q,a)} s'$ .

The definition of  $v' \sim s'$  says:

$$\exists (vs', cs') \in v', \ \exists asgn, \quad asgn \ {\sf satisfies} \ cs' \ \land \ vs' \ ^{asgn} = s'$$

From the definition of  $\mathsf{vstep}_p$ , we know that:

$$\exists (vs, cs) \in v, \quad (vs', cs') \in \mathsf{vstep}_p'(q, a)(vs, cs)$$

Since  $\mathsf{vstep}_p'$  monotonically increases the set of constraints, we have  $\mathit{cs} \subseteq \mathit{cs}'$ . Therefore:

$$asgn$$
 satisfies  $cs$ 

Let:

$$s = vs^{asgn}$$

Then we have:

$$(vs,cs) \in v \quad \wedge \quad asgn \ {\rm satisfies} \ cs \quad \wedge \quad vs^{asgn} = s$$
 
$$i.e. \ v \sim s$$

From the definition of  $\mathsf{vstep}_p'$ , the validator first creates a fresh variable to represent the server's internal choice, so we can deduct the internal choice from the assignment:

$$x_c = \text{fresh}(vs, cs)$$
  $c = asgn!x_c$ 

Now we need to show that the server's loop body  $\mathsf{sstep}_p(q,c)(s)$  results in response a and post-execution state s'. Since the post-validation state v' simulates s' and guarantees the response to be a, we only need to prove the post-execution state to be s'.

We have known that:

$$s = vs^{asgn}$$
  $s' = vs'^{asgn}$   $(vs, cs) \xrightarrow{(q,a)} (vs', cs')$ 

Therefore, we can prove  $s \xrightarrow[c]{(q,a)} s'$  by induction on the Prog syntax, showing that every write or branch operation preserves asgn's ability to unify the server state with the validation state. This leads the post-execution state to be unifiable against vs' using asgn, thus to be

s'.

The core of this proof is to find the internal choice c for server step  $s {q,a \choose c} s'$ . The choice was computed with the assignment deducted from the loop invariant. The assignment contains the value of all symbolic variables, which includes all choices made by the server, past and future. The loop invariant requires the assignment to explain the past choices, but cannot predict future choices. Therefore, we can only infer the server step from the validator step using backward induction.

## Lemma 3.5 (RejComplete-Init).

If: 
$$vs = (\_ \mapsto \#0)$$
  $cs = \{\#0 \equiv 0\}$   $s_0 = (\_ \mapsto 0)$   
Then:  $\{s \mid \{(vs, cs)\} \sim s\} = \{s_0\}$ 

*Proof.* The requirement for s says:

$$\exists asgn : \mathsf{var} \to \mathbb{Z}, \quad asgn \text{ satisfies } cs \quad \land \quad vs^{asgn} = s$$

The constraint satisfaction tells us that:

$$asgn!0 = 0$$

We then have:

$$\forall k : \mathbb{N}, \quad s!k = asgn!(vs!k) = asgn!0 = 0 = s_0!k$$

Therefore,  $s_0$  is the only server state that (vs, cs) simulates.

Now we have proven that all Prog-based validators satisfy the hypotheses defined in Subsection 2.3.1–2.3.2, and we can conclude that the validators constructed by dualization are sound and complete. Next I'll show how to apply this dualization technique to test real-world

programs.

### CHAPTER 4

#### ASYNCHRONOUS TESTER BY DUALIZATION

So far I've introduced the theory of validating synchronous interactions using the QAC language family, and shown how to construct validators by dualization with a simple Prog language.

However, in real-world testing practices, there are more problems to consider. For example: How to interact with the SUT via multiple channels? How to handle external nondeterminism?

As discussed in Subsection 1.2.2, a networked server's response may be delayed by the network environment, and an asynchronous tester may send other requests rather than waiting for the response. Therefore, we cannot view the trace as a sequence of  $Q \times A$  pairs like we did in Definition 2.9, and the state monad in the QAC language family becomes insufficient for defining the space of asynchronous interactions.

This chapter applies the idea of dualization to testing asynchronous systems. I transition from the QAC language family to the ITree specification language, which allows modelling asynchronous interactions. The ITree-based specifications are derived into tester programs that can interact with the SUT and reveal potential defects.

Figure 4.1 illustrates the derivation framework from ITrees to testers. Section 4.1 introduces the ITree language that encodes each box in the framework. Section 4.2 and Sec-

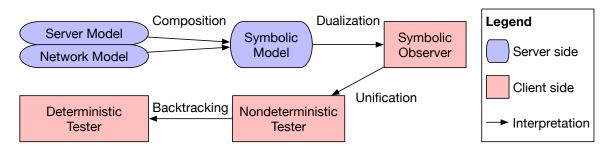


Figure 4.1: Deriving tester program from specification

tion 4.3 address internal and external nondeterminism in the ITree context, and interprets the "server model" into a "nondeterministic tester". Section 4.4 then explains how to execute the nondterministic tester model as an interactive tester program that runs on deterministic machines.

## 4.1. From QAC to Interaction Trees

To write specifications for protocols' rich semantics, I employed "interaction tree" (ITree), a generic data structure for representing interactive programs in the Coq programming language, introduced by Xia et al. [39]. I provide a brief introduction to the ITree specification language in Subsection 4.1.1.

ITrees allow specifying protocols as monadic programs that model valid implementations' possible behavior. In Subsection 4.1.2, I show how to embed specifications in the QAC family in terms of interaction trees.

The derivation from server specifications to interactive testers is by *interpreting* ITree programs, which corresponds to the arrows in Figure 4.1. In Subsection 4.1.3, I explain the mechanism of interpretation by deriving testers from deterministic server models. The rest of this chapter then shows how to handle nondeterminism when interpreting ITrees.

#### 4.1.1. Language definition

Consider an echo program, which keeps reading some data and writing it out verbatim, until reaching EOF. We can represent the program in Coq, with a reference in C as:

Here the behavior after getchar depends on the value actually read. The monadic computation in Coq can be desugared into:

```
CoInductive itreeM (E: Type \rightarrow Type) (R: Type) := Ret : R \rightarrow itreeM E R | Trigger : E R \rightarrow itreeM E R | Bind : \forall {X : Type}, itreeM E X \rightarrow (X \rightarrow itreeM E R) \rightarrow itreeM E R.
```

Figure 4.2: Mock definition of interaction trees.

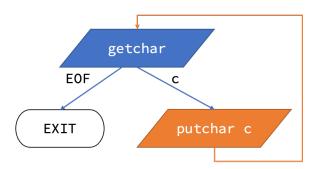


Figure 4.3: Interaction tree for echo program

```
CoFixpoint echo := Bind getchar  (\lambda \ c \ \Rightarrow \ \text{if c is EOF} \\ \text{then EXIT} \\ \text{else Bind (putchar c)} \\ (\lambda \ \_ \ \Rightarrow \ \text{echo})
```

Such continuation-passing style can be represented as a tree of interactions. To help readers better understand the interaction tree language, I first provide a modified version of it that better shows its tree structure, and then explain the actual type definition used in practice.

Mock interaction trees As shown in Figure 4.2, a mock interaction tree (itreeM) has two kinds of leaves, Ret and Trigger, and has internal nodes constructed by Bind:

• (Ret r) represents a pure computation that yields a value r. In the echo example, EXIT halts the program with return value zero:

```
Definition EXIT := Ret 0.
```

• (Trigger e) performs an impure event e and returns its result. Here (e: E R) is an event whose result is of type R. For example, getchar has result type char, and putchar's result type is unit (which corresponds to void in C/C++, or () in Haskell). These effective programs are constructed by triggering standard I/O events:

```
CoInductive itree (E: Type \rightarrow Type) (R: Type) := Pure : R \rightarrow itree E R | Impure : \forall {X : Type}, E X \rightarrow (X \rightarrow itree E R) \rightarrow itree E R.
```

Figure 4.4: Formal definition of interaction trees (simplified)

```
Variant stdioE: Type → Type := (* event type *)

GetChar: stdioE char

| PutChar: char → stdioE unit.

Definition getchar : itreeM stdioE char := Trigger GetChar.

Definition putchar (c: char) : itreeM stdioE unit := Trigger (PutChar c).
```

• (Bind m k) binds the return value of m to the continuation function k. It first runs program m until it returns some value of type X. The return value (x: X) then instantiates k into the following computation (k x: itreeM E R). This corresponds to the monadic (;;) syntax:

```
Notation "x \leftarrow m1;; m2" := (Bind m1 (\lambda x \Rightarrow m2)).
Notation "m1;; m2" := (Bind m1 (\lambda \Rightarrow m2)).
```

As illustrated in Figure 4.3, each possible return value x is an edge that leads to the child it instantiates, *i.e.*, (k x). In this way, the Ret and Trigger nodes are connected into a tree structure.

The mock interaction tree provides an intuitive continuation-passing structure for representing impure programs. However, to implement dualization effectively, we need to revise the language definition of monadic binding.

Practical interaction trees Instead of binding a program to a continuation, ITree binds a single impure event, as shown in Figure 4.4. I use (Impure e k) to replace (Bind (Trigger e) k) representations in itreeM. A Pure computation cannot be bound to a continuation, and must be the leaf of an ITree.<sup>1</sup>

The Ret, Trigger, and Bind constructors introduced in itreeM have equivalent representa-

<sup>&</sup>lt;sup>1</sup>For readability, the "practical" ITree definition is a simplified version from Xia et al. [39]. Here Pure and Impure correspond to the Ret and Vis constructors. I dropped the (Tau: itree E R  $\rightarrow$  itree E R) constructor, which carries no semantics and is used for satisfying Coq's guardedness condition.

tions in itree, so we can still write programs in the monadic syntax:

```
Definition ret {E R} : R \rightarrow itree E R := Pure.

Definition trigger {E R} (e: E R) : itree E R := Impure e Pure.

CoFixpoint bind {X E R} (m: itree E X) (f: X \rightarrow itree E R) : itree E R := match m with | Pure x \Rightarrow f x | Impure e k \Rightarrow Impure e (\lambda r \Rightarrow bind (k r) f) end.

Notation "x \leftarrow m1;; m2" := (bind m1 (\lambda x \Rightarrow m2)).

Notation "m1;; m2" := (bind m1 (\lambda _- \Rightarrow m2)).

CoFixpoint translateM {E R} (m: itreeM E R) : itree E R := match m with | Ret r \Rightarrow ret r | Trigger e \Rightarrow trigger e | Bind m1 k \Rightarrow x \leftarrow translateM m1;; translateM (k x) end.
```

### 4.1.2. QAC in ITrees

The ITree specification language is a superset of the QAC language family. Any server model in Subsection 2.2.1 can be translated into an interaction tree that receives requests and sends responses.

The deterministic server's event type is defined as follows:

Here ioE is a parameterized event that takes types I and O as arguments. Type qaE is an instance of I/O event that receives requests of type Q and sends responses of type A.

Given a loop body sstep and an initial state s, we can define the interaction tree of the server model as a recursive program:

```
CoFixpoint detServer (sstep: \mathbb{Q} \to \sigma \to \mathbb{A} * \sigma) (s: \sigma): itree qaE void := \mathbb{Q} \leftarrow \text{trigger Recv}; let (a, s') := sstep q s in trigger (Send a);; detServer sstep s'.
```

The server program iterates over state (s:  $\sigma$ ). In each iteration, it receives a request (q: Q) and computes the response (a: A) using the state monad function sstep. It then sends back the response and recurses with the post state (s':  $\sigma$ ).

To specify a nondeterministic server with internal choices of type C, I introduce another event to represent its internal choices.

```
Variant choiceE: Type \rightarrow Type := Choice: choiceE C. (* make an internal choice *)

Definition qacE: Type \rightarrow Type := qaE \oplus choiceE.
```

Here qacE is a sum type of qaE and choiceE events, meaning that the server's events are either sending/receiving messages or making internal choices.

At the beginning of each iteration, the nondeterministic server makes an internal choice (c: C) as the seed of its sstep function:

```
CoFixpoint server (sstep: \mathbb{Q} \to \mathbb{C} \to \sigma \to \mathbb{A} * \sigma) (s: \sigma): itree qacE void := c \leftarrow trigger Choice;; q \leftarrow trigger Recv;; let (a, s') := sstep q c s in trigger (Send a);; server sstep s'.
```

Such server models can be derived into tester programs by interpretation.

#### 4.1.3. Interpreting interaction trees

To interpret an ITree is to specify the operational semantics of its events. For example, the tester program in Section 1.1 can be constructed by interpreting a deterministic server model in Subsection 4.1.2.

**Tester event type** An interactive tester generates requests and sends them to the SUT, receives responses, and validates its observation against the specification:

This type definition is pronounced as: "The tester receives responses A as input, sends requests Q as output, generates requests to send, or throws an exception when it detects a violation in its observations.

**Dualizing server events** The tester is constructed by dualizing the server specification's behavior: When the specification receives a request, the tester generates a request and sends it to the SUT; When the specification sends a response, the tester expects to receive the response from the SUT. We can write this correspondence as a function from server events to the tester's behaviors:

The dualize function takes an event and yields an ITree program. It maps the server's receive event to the tester's generate and send operations, and vice versa, maps the server's send event to the tester's receive operation. If the tester's received response differs from that specified by the server model, then the tester throws an exception to indicate a violation it detected.

**Applying event handlers** The dualize function is also called a handler. It produces an ITree that has the same result type as its argument event. Therefore, we can construct the tester by substituting the server's events with the operations defined by the handler function:

```
CoFixpoint interp {E F T} (handler: \forall {R}, E R \rightarrow itree F R) (m: itree E T) : itree F T := match m with | Pure r \Rightarrow Pure r | Impure e k \Rightarrow x \leftarrow f e;; interp handler (k x) end.

Definition tester (sstep: Q \rightarrow \sigma \rightarrow A * \sigma) (s: \sigma) : itree testE void :=
```

interp dualize (detServer sstep s).

Applying the dualization handler to the server model gives us an ITree program that performs tester interactions. The tester keeps generating, sending and receiving messages until observing an unexpected response when it throws an exception and rejects the SUT. It is semantically equivalent to the tester in Section 1.1.

To derive testers from nondeterministic server models, I design more complex tester events and handlers, as discussed in the following sections.

## 4.2. Handling Internal Nondeterminism

This section applies the idea of dualization in Chapter 3 to the ITree context, showing how to address internal nondeterminism by symbolic evaluation based on ITree specifications. It covers the derivation path from "symbolic model" to "nondeterministic tester" in Figure 4.1, using HTTP/1.1 entity tags introduced in Subsection 1.2.1 as an example.

As discussed in Section 3.1, dualization requires refining the representation of the server's computation *e.g.* encoding its branches over symbolic conditions. This is done by designing ITrees' event types in Subsection 4.2.1 and specifying the server's behavior with a symbolic model.

The server specification is derived into a tester client by *interpreting* interaction trees. To interpret is to define semantic rules that transform one ITree program into another, and corresponds to the arrows in Figure 4.1. Subsection 4.1.3 explains the interpretation of ITrees.

The interpretation from symbolic model to the nondeterministic tester model is implemented in two phases, illustrated as "dualization" and "unification" arrows in Figure 4.1: Subsection 4.2.2 dualizes the server's behavior into the tester client's, resulting in a "symbolic observer" that encodes symbolic evaluation as primitive events. Subsection 4.2.3 then instantiates the primitive events into pure computations that unify concrete observations against

their symbolic representations.

#### 4.2.1. Symbolic server model

The server specification is an ITree program that exhibits all valid behavior of the protocol. I combine the Prog language in Subsection 3.1.2 with the simplistic ITree example in Subsection 4.1.2.

**Network packet type** Instead of receiving requests and sending responses, the server receives and sends *packets* that carry routing information. This allows us to specify the server's interaction against concurrent clients in Section 4.3. A packet consists of headers that indicate its source and destination, and a payload of either a request or a response:

```
Notation connection := N. (* N for natural number *)
Record packet Q A := {
  Source : endpoint;
  Destination : endpoint;
  Payload : Q + A
}.
```

This type definition says: the packet type is parameterized over the Q and A types that represent its request and response. Its Source and Destination fields each records an endpoint represented as a natural number. Its Payload type is the sum of request and response.

Here's an example trace of network packets:

```
Context get: string \rightarrow request.
Context ok : string \rightarrow response.
Definition server_end: endpoint := 0.
Example trace: list (packet request response) :=
  [ { Source
                := 1;
      Destination := server_end;
      Payload := inl (get "/index.html")
    }
  ; { Source
               := server_end;
      Destination := 1;
              := inr (ok "Hello!")
      Payload
    }
  ].
```

This trace encodes a transaction between client 1 and the server (represented as endpoint 0).

The client sends a GET request to fetch the resource in path "/index.html", and the server responds with 200 OK and content "Hello!". The inl and inr are constructors for sum types:

```
Context inl: \forall {X Y}, X \rightarrow X + Y. Context inr: \forall {X Y}, Y \rightarrow X + Y.
```

Symbolic representation To specify systems' nondeterministic behavior, the Prog language in Subsection 3.1.2 encodes data as symbolic expressions SExp, so that the responses and branch conditions may depend on internal choices. I do the same for ITree specifications, by symbolizing the choice events and branch conditions. Take my HTTP specification [26] as an example. Its choice event has symbolic expression as result type:

```
Variant comparison := Strong | Weak.

Variant exp: Type \rightarrow Type :=
Const : string \rightarrow exp string
| Var : var \rightarrow exp string
| Compare : string \rightarrow exp string \rightarrow comparison \rightarrow exp bool.

Variant choiceE: Type \rightarrow Type :=
Choice: choiceE (exp string).
```

Here I instantiate the choiceE in Subsection 4.1.1 with symbolic return type (exp string), pronounced "expression of type string". In this example, I use strings to represent entity tags (ETags) that HTTP servers may generate, which was discussed in Subsection 1.2.1. The type interface can be adjusted to other protocols under test.

Symbolic expressions may be constructed as constant values, as variables, or with operators.

Here is an example of expressions of type string:

```
Context x y : var.

Example expressions: list (exp string) :=
  [ Const "foo"
  ; Var x
  ; Compare "bar" (Var y) Weak
  ].
```

The Compare constructor takes an expression of type string and compares it against a constant string. (Compare t tx cmp) represents the ETag comparison between t and tx, using "strong

```
1
      Notation \sigma := (path \rightarrow resource).
2
3
      Context OK PreconditionFailed : symbolic_response.
4
      Context process: request \rightarrow \sigma \rightarrow itree smE (symbolic_response * \sigma).
 5
      CoFixpoint server_http (state: \sigma) :=
6
        pq ← trigger Recv;;
 7
8
        let respond_with a :=
9
          trigger (Send { Source
                                         := server_conn
10
                          ; Destination := pq.(Source)
                                      := inr a } ) in
11
                          ; Payload
12
                             := request_of pq
        let q : request
                                                       in
                             := q.(Content)
13
        let v : string
                                                       in
14
                             := q.(TargetPath)
        let k : path
                                                       in
15
        let t : string
                             := if_match q
                                                       in
16
        let tx: exp string := (state k).(ETag)
                                                       in
17
        IFX (Compare t tx Strong)
18
        THEN
          if q.(Method) is Put
19
20
          then
21
            tx' ← or (trigger Choice)
22
                        (Pure (Const EmptyString));;
23
            let state' := state [k \mapsto \{Content := v; ETag := tx'\}] in
24
            respond_with OK;;
25
            server_http state
26
                                  (* handling other kinds of requests *)
27
             (a, state') ← process q state;;
28
            respond_with a;;
29
            server_http state'
30
        ELSE
31
          respond_with PreconditionFailed;;
32
          server_http s.
```

Figure 4.5: Server model for HTTP conditional requests

comparison" or "weak comparison" mechanism<sup>2</sup> specified by cmp. The constant ETag is provided by the request, and the symbolic one comes from the server state.

Figure 4.5 shows an ITree model for If-Match requests (Subsection 1.2.1). The server state  $\sigma$  [LYS: I used  $\sigma$  to represent the server state in QAC, so keeping this notation.] maps each

<sup>&</sup>lt;sup>2</sup>HTTP/1.1 servers may choose to generate ETags as "strong validators" (with uniqueness guarantee) or "weak validators" (for potentially better performance). Weak validators have prefix W/ while strong validators do not. When handling compare-and-swap operations such as PUT requests conditioned over If-Match in Subsection 1.2.1, the server should evaluate its precondition with "strong comparison" that don't allow weak validators (e.g. W/"foo") to match any ETag including itself. For GET requests conditioned over If-None-Match, the server may evaluate with "weak comparison" where a weak validator like W/"bar" matches itself and also matches strong validator "bar", but doesn't match W/"foo" or "foo".

path to its corresponding "resource"—file content and metadata like ETag. The server first evaluates the request's If-Match condition by "strong comparison" as required by HTTP. If the request's ETag matches its target's, then the server updates the target's contents with the request payload. The target's new ETag tx' is permitted to be any value, so the model represents it as Choice event.

Notice that the server model exhibits three kinds of branches:

- 1. The if branch in Line 19 is provided by ITree's embedding language Coq, and takes a boolean value as condition;
- 2. The IFX branch in Line 17 constructs an ITree that nondeterministically branches over a condition written as a symbolic expression of type bool:

```
Variant branchE: Type → Type :=
  Decide: exp bool → branchE bool.

Notation "IFX condition THEN x ELSE y" :=
  (b ← trigger (Decide condition);;
  if b then x else y).
```

3. The or operator in Line 21 takes two ITrees as possible branches and constructs an ITree that may nondeterministically take either branch:

```
Variant nondetE: Type → Type :=
  Or: nondetE bool.

Definition or {E R} (x y: itree E R) : itree E R :=
  b ← trigger Or;;
  if b then x else y.
```

These three kinds of branch conditions play different roles in the specification, and will be handled differently during testing:

1. The "pure" if condition is used for deterministic branches like (q.(Method) is Put) in the example. Here q is a "concrete request"—a request that doesn't involve symbolic variables, as opposed to "symbolic" ones—generated by the client and sent to the server, so its method is known by the tester and needn't be symbolically evaluated.

- 2. The "symbolic" IFX condition here plays a similar rule as the if branches in the Prog language: Which branch to take depends on the server's internal choices, so the tester needs to consider both cases.
- 3. The or branch defines multiple control flows the server may take. In the HTTP example, the server may generate an ETag for the resource's new content, but is not obliged to do so. It may choose to generate no ETags instead, using (Pure (Const EmptyString)) as an alternative to (trigger Choice).

In addition to IFX branch conditions, the symbolic expressions may also appear in the server's responses. For example, after generating an ETag in Line 21 of Figure 4.5, the server may receive a GET request and send the ETag to the client:

Suppose the server generated the ETag as expression (Var x), then we can use the expression to construct the symbolic response in the specification, rather than determining its concrete value. The mechanism of producing expressions for ETags is explained in Subsection 4.2.2.

Now we can define the specification's event type smE. The symbolic server model receives concrete requests and sends symbolic responses, so its event is defined as:

```
Definition symbolic_packet := packet request symbolic_response. 
 Definition qaE := ioE symbolic_packet symbolic_packet. 
 Notation smE := (qaE \oplus nondetE \oplus choiceE \oplus branchE).
```

The "Symbolic Model" in Figure 4.1 is an ITree constructed by applying the server\_http function to an initial state:

```
1 Notation oE := (observeE \oplus nondetE \oplus choiceE \oplus constraintE).
3 Definition observe {R} (e: smE R) : itree oE R :=
4
      match e with
5
      Recv
                   ⇒ trigger FromObserver
6
      | Send px \Rightarrow p \leftarrow trigger ToObserver;;
7
                      trigger (Guard px p)
8
      | Decide bx ⇒ or (trigger (Unify bx true);; ret true)
9
                          (trigger (Unify bx false);; ret false)
10
      | Or
                   \Rightarrow trigger Or
11
      | Choice
                   \Rightarrow trigger Choice
12
      end.
13
14 Definition observer_http: itree oE void :=
15
      interp observe sm_http.
```

Figure 4.6: Dualizing symbolic model into symbolic observer.

```
Definition sm_http: itree smE void :=
  server_http init_state.
```

The rest of this section will explain the interpretations from this symbolic model.

## 4.2.2. Dualizing symbolic model

This subsection takes the symbolic model composed in Subsection 4.2.1 and dualizes its interactions, which corresponds to the "Dualization" arrow in Figure 4.1. It applies the idea of derivation rules (1)–(4) for Prog (Section 3.2) to models written as ITrees.

This interpretation phase produces a symbolic observer that models the tester's observation and validation behavior. The observer sends a request when the server wants to receive one, and receives a response when the server wants to send one. It also creates constraints over the server's internal choices based on its observations.

Figure 4.6 shows the dualization algorithm. It interprets the symbolic model's events with the observe handler, whose types are explained as follows:

The tester observes a trace of concrete packets, so observer's interactions return concrete requests and responses, as opposed to the symbolic model whose responses are symbolic.

```
Definition concrete_packet := packet request concrete_response.
```

```
Variant observeE : Type → Type :=
FromObserver : observeE concrete_packet
```

| ToObserver : observeE concrete\_packet.

Notice that the observer's send and receive events both return the packet sent or received, unlike the server model whose Send event takes the sent packet as argument. This is because the tester needs to generate the request packet to send, and the event's result value represents that generated and sent packet.

As discussed in Section 3.2, when the server sends a symbolic response or branches over a symbolic condition, the tester needs to create symbolic constraints accordingly. The observer introduces "constraint events" to represent the creation of constraints primitively.

```
\begin{tabular}{lll} Variant & constraintE : Type $\rightarrow$ Type := \\ & Guard : packet $\rightarrow$ concrete_packet $\rightarrow$ constraintE unit \\ & | Unify : exp bool $\rightarrow$ bool $\rightarrow$ constraintE unit. \\ \end{tabular}
```

Here (Guard px p) creates a constraint that the symbolic packet px emitted by the specification matches the concrete packet p observed during runtime. (Unify bx b) creates a constraint that unifies the symbolic branch condition bx with boolean value b. These constraints will be solved in Subsection 4.2.3.

The dualization algorithm in Figure 4.6 does the follows:

- 1. When the symbolic model absorbs a packet in Line 5, the observer generates a request packet;
- 2. When the symbolic model emits a symbolic packet px in Line 6, the observer receives a concrete packet p, and adds a constraint that restricts the symbolic and concrete packets to match each other.
- 3. When the symbolic model branches on a symbolic condition bx in Line 8, the tester accepts the observation if it can be explained by any branch. This is done by constructing the observer as a nondeterministic program that has both branches, using the or combinator. For each branch, the observer adds a constraint that the symbolic

condition matches the chosen branch.

- 4. Nondeterministic branches in Line 10 are preserved in this interpretation phase, and will be resolved in Section 4.4.
- 5. Internal choices in Line 11 are addressed by the next phase in Subsection 4.2.3, along with the constraints created in this phase.

The result of dualization is a symbolic observer that models tester behaviors like sending requests and receiving responses. The symbolic observer is a nondeterministic program with primitives events like making choices and adding constraints over the choices.

For example, dualizing Line 17–32 in Figure 4.5 results in an observer program as shown in Figure 4.7. The next subsection interprets the observer's primitive Guard and Unify events into pure computations of symbolic evaluation.

#### 4.2.3. Symbolic evaluation

This subsection takes the symbolic observer produced in Subsection 4.2.2 and solves the constraints it has created. The constraints unify symbolic packets and branch conditions against the concrete observations. The tester should accept the SUT if the constraints are satisfiable.

As shown in Figure 4.8, the unification algorithm evaluates the primitive symbolic events into a stateful checker program, which reflects the Prog-based validator in Section 3.2. The interpreter maintains a validation state V which stores the symbolic variables and the constraints over them. The derivation rules are as follows:

- 1. When the server makes an internal choice in Line 8, the tester creates a fresh variable and adds it to the validation state.
- 2. When the observer creates a constraint in Line 10, the tester adds the constraint to the validation state, and solves the new set of constraints. If the constraints become unsatisfiable, then the tester Throws an exception that indicates the current execution

```
Example observer_body: itree oE void :=
 let guard_response a :=
   p ← trigger ToObserver;;
    trigger (Guard { Source
                                 := server_conn
                   ; Destination := pq.(Source)
                   ; Payload
                                := inr a } ) in
 let bx: exp bool := Compare t tx Strong in
 or (
     trigger (Unify (Compare bx true));;
     if q.(Method) is Put
     then
        tx' \leftarrow or (trigger Choice)
                  (Pure (Const EmptyString));;
        let state' := state [k \mapsto \{Content := v; ETag := tx'\}] in
        guard_response OK;;
        interp observe (server_http state')
        (a, state') ← interp observe (process q state);;
        guard_response a;;
        interp observe (server_http state')
     trigger (Unify (Compare bx false));;
     guard_response PreconditionFailed;;
     interp observe (server_http s)
     ).
```

Figure 4.7: Symbolic observer example.

```
1 Notation ntE := (observeE \oplus nondetE \oplus exceptE).
2
3 Definition V: Type := list var * list (constraintE unit).
4
5 Definition unify {R} (e: oE R) (v: V) : itree ntE (V * R) :=
6
      let (xs, cs) := v in
7
      match e with
8
      | Choice \Rightarrow let x: var := fresh v in
9
                   ret (x::xs, cs, Var x)
10
      | (constraint: unifyE) \Rightarrow let cs' := constraint::cs in
11
                                   if solvable cs'
12
                                   then ret (xs, cs', tt)
13
                                   else Trigger (Throw ("Conflict: " ++ print cs'))
14
                         \Rightarrow b \leftarrow trigger Or;; ret (v, b)
15
      | (oe: observeE) \Rightarrow r \leftarrow trigger oe;; ret (v, r)
16
      end.
17
18 Definition nondet_tester_http: itree ntE void :=
19
      (_, vd) ← interp_state unify observer_http initV;;
20
      match vd in void with end.
```

Figure 4.8: Resolving symbolic constraints.

branch cannot accept the observations:

```
Variable exceptE: Type \rightarrow Type := Throw: \forall {X}, string \rightarrow exceptE X.
```

3. The observer is a nondeterministic program with multiple execution paths, constructed by Or events in Line 14. The tester accepts the observation if any of the branches does not throw an exception. These branches will be handled in the next section, along with the observer's send/receive interactions in Line 15.

Notice that the unify function interprets a symbolic observer's event (oE R) into a function of type ( $V \rightarrow itree\ tE\ (V * R)$ ), which is also called a state monad transformer. It takes a pre-validation state (v:V) and computes an ITree that yields the observer event's corresponding result (r:R) along with a post-validation state (v:V). This stateful interpretation process is implemented by a variant of interp called interp\_state:

```
CoFixpoint interp_state {E F V R}  (\text{handler: } \forall \ \{X\}, \ E \ X \to V \to \text{itree F (V * X))} \\ (\text{m: itree E R) (v: V)} \\ : \text{ itree F (V * R) :=} \\ \text{match m with} \\ | \ \text{Pure r } \Rightarrow \text{ret (v, r)} \\ | \ \text{Impure e k } \Rightarrow \ '(\text{v', r}) \leftarrow \text{handler e v;} \\ \text{interp\_state handler (k r) v'} \\ \text{end.}
```

So far I have interpreted the symbolic model into a tester model that observes incoming and outgoing packets, nondeterministically branches, and in some cases throws exceptions. Next I'll explain how to extend the symbolic model to address external nondeterminism.

## 4.3. Handling External Nondeterminism

As introduced in Subsection 1.2.2, the environment might affect the transmission of messages, so called external nondeterminism. The tester should take the environment into account when validating its observations.

This section explains how to address external nondeterminism by specifying the environment, with the networked server example. It corresponds to the "Composition" arrow in Figure 4.1. Subsection 4.3.1 defines a model for concurrent TCP connections. Subsection 4.3.2 then

composes the network model with the server specification, yielding a tester-side specification that defines the space of valid observations.

#### 4.3.1. Modelling the network

When testing servers over the network, request and response packets may be indefinitely delayed. As a result, messages from one end might arrive at the other end in a different order from that they were sent.

The space of network reorderings can be modelled by a *network model*, a conceptual program for the "network wire". The wire can be viewed as a buffer, which absorbs packets and later emits them:

```
Variant netE: Type → Type := (* network event type *)
Emit : packet → netE unit
| Absorb: netE packet.
```

After absorbing a packet, the wire may emit it immediately or after absorbing/emitting other packets. Such choices are modelled by nondeterministic Or branches:

```
Variant nondetE: Type → Type := (* nondeterministic branch *)
Or: nondetE bool.

Definition or {E R} `{nondetE -< E} (x y: itree E R) : itree E R := b ← trigger Or;;
if b then x else y.</pre>
```

Here (or x y) creates a nondeterministic program that may behave as either x or y. The nondetE here is a special case of choiceE defined in Subsection 4.1.1 with boolean space of choices, but they'll be handled differently during test derivation. The type signature  $\{E\ R\}$  `{nondetE -< E} says the (or) combinator can apply to ITrees whose event E is a super-event of nondetE, and with arbitrary return type R. For example, arguments x and y can be of type (itree (netE  $\oplus$  nondetE) void).

For example, the network model for concurrent TCP connections is defined in Figure 4.9. The model captures TCP's feature of maintaining the order within each connection, but packets in different connections might be reordered arbitrarily. When the wire chooses a packet to send, the candidate must be the oldest in its connection.

```
Fixpoint pick_one (1: list packet) : itree nondetE (option packet) :=
  if l is p::l'
  then or (Ret (Some p)) (pick_one 1')
  else ret None.
{\tt Definition\ oldest\_in\_each\_conn\ :\ list\ packet\ \to\ list\ packet\ :=\ \dots}
(* filter the oldest packet in each connection *)
CoFixpoint tcp (buffer: list packet) : itree (netE 

nondetE) void :=
  let absorb := pkt ← trigger Absorb;;
                tcp (buffer ++ [pkt])
                                              in
  let emit p := trigger (Emit p);;
                 tcp (remove pkt buffer)
  let pkts
              := oldest_in_each_conn buffer in
  opkt \( \to \) pick_one pkts;;
  if opkt is Some pkt
  then emit pkt
  else absorb.
```

Figure 4.9: Network model for concurrent TCP connections. The model is an infinite program iterating over a buffer of all packets en route. In each iteration, the model either absorbs or emits some packet, depending on the current buffer state and the choice made in pick\_one. Any absorbed packet is appended to the end of buffer. When emitting a packet, the model may choose a connection and send the oldest packet in it.

Notice the pick\_one function, which might return (i) Some p or (ii) None. The network model then (i) emits packet p or (ii) absorbs a packet into buffer.

- When the given list pkts is empty, pick\_one always returns None, because the wire has no packet in the buffer, and must absorb some packet before emitting anything.
- Given a non-empty linked list (p::1'), with p as head and 1' as tail, pick\_one might return (Some p), meaning the wire can emit that packet; or it might return None, meaning the wire can still absorb packets into the buffer.

Such network model reflects the TCP environment, where messages are never lost but might be indefinitely delayed. In the next subsection, I'll demonstrate how to compose the server and network models into a client-side observation model.

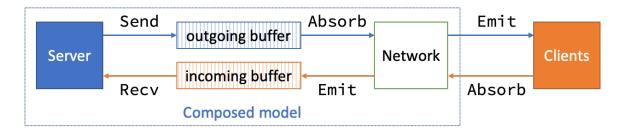


Figure 4.10: Network composition architecture

### 4.3.2. Network composition

The network connects the server on one end to the clients on other ends. When one end sends some message, the network model absorbs it and later emits it to the destination.

To compose a server model with a network model is to pair the server's Send and Recv events with the network's Absorb and Emit events. Since the network model is nondeterministic, it might not be ready to absorb packets sent by the server. The network might also emit a packet before the server is ready to receive it.

To handle the asynchronicity among the server and network events, I insert message buffers between them. As shown in Figure 4.10, the *incoming buffer* stores the packets emitted by the network but not yet consumed by the server's Recv events, and the *outgoing buffer* stores the packets sent by the server but not yet absorbed by the network.

The server and the clients are the opposite ends of the network. Each packet has routing fields that indicate its source and destination. When the network emits a packet, we need to determine whether the packet is emitted to the server's incoming buffer or to the clients, by inspecting its destination:

```
CoFixpoint compose \{E\} (srv: itree (qaE \oplus E) void)
                                                                     (* server model *)
1
 2
                  (\texttt{net} \; : \; \texttt{itree} \; (\texttt{netE} \; \oplus \; \texttt{nondetE}) \; \, \texttt{void})
                                                                     (* network model *)
3
                  (bi bo: list packet)
                                                  (* incoming and outgoing buffers *)
                 : itree (netE \oplus nondetE \oplus E) void :=
4
 5
      let step_net :=
 6
         match net with
 7
         | Impure (Absorb|) knet ⇒
 8
           match bo with
9
           | pkt::bo' ⇒ compose srv (knet pkt) bi bo'
10
                        ⇒ pkt ← trigger Absorb;;
           | []
11
                            compose srv (knet pkt) bi bo
12
           end
13
         | Impure (Emit pkt|) knet \Rightarrow
14
           if toServer pkt
15
           then compose srv (knet tt) (bi++[pkt]) bo
16
           else trigger (Emit pkt);;
17
                 compose srv (knet tt) bi bo
18
         | Impure (|Or) knet \Rightarrow b \leftarrow trigger Or;;
19
                                 compose srv (knet b) bi bo
20
         | Pure vd \Rightarrow match vd in void with end
21
         end
22
       in
23
      match srv with
24
       | Impure (Recv|) ksrv \Rightarrow
25
         match bi with
26
         | pkt::bi' ⇒ compose (ksrv pkt) net bi' bo
27
         | [] \Rightarrow step_net
28
         end
29
       | Impure (Send pkt|) ksrv \Rightarrow
30
         compose (ksrv tt) net bi (bo++[pkt])
31
       | Impure (|e) ksrv \Rightarrow
                                         (* other events performed by the server *)
32
         r \leftarrow trigger e;; compose (ksrv r) net bi bo
33
       | Pure vd \Rightarrow match vd in void with end
34
       end.
```

Figure 4.11: Network composition algorithm. When the server wants to send a packet in Line 29, the packet is appended to the outgoing buffer until absorbed by the network in Line 9, and eventually emitted to the client in Line 16. Conversely, packets sent by clients are absorbed by the network in Line 10, emitted to the server's incoming buffer in Line 15, until the server consumes it in Line 26.

Now we can define the composition algorithm formally, as shown in Figure 4.11. In this example, we reuse the qaE definition in Subsection 4.1.1, and let the Q and A both be the packet type. The composed ITree takes the server and network models as parameters, and makes steps in the two ITrees in certain order.

The composed model exhibits to the client three kinds of events: (i) Network operations (netE) where packets are emitted to or absorbed from clients, (ii) Nondetermistic branches (nondetE) made by the network model, and (iii) Other events {E} performed by the server model e.g. internal choices (choiceE) in Subsection 4.1.1.

Notice that this algorithm schedules the server at a higher priority than the network model. The composed model only steps into the network model when the server is starved in Line 27, by calling the step\_net process defined in Line 5. Such design is to avoid divergence of the derived tester program, which I'll further explain in Section 4.4.

So far I've shown how to specify systems that exhibit external nondeterminism. By specifying the environment and composing it with the implementation-side specification, we can describe the space of valid observations. The rest of this chapter will show how to derive tester programs from the observer-side specification.

# 4.4. Executing Tester Model

This section takes the nondetermistic tester model derived in Subsection 4.2.3 and transforms it into an interactive program. Subsection 4.4.1 handles the nondeterministic branches via backtrack execution, and produces a deterministic tester model. Subsection 4.4.2 then interprets the deterministic tester into IO program that interacts with the SUT.

# 4.4.1. Backtrack execution

This subsection explains how to run the nondeterministic tester on a deterministic machine. It reflects the derivation rules (5) and (6) for Prog in Section 3.2, and constructs the "Backtracking" arrow in Figure 4.1.

The deterministic tester implements a client that sends and receives concrete packets:

Notice that the ClientRecv event might return (Some pkt), indicating that the SUT has sent a packet pkt to the tester; or it might return None, when the SUT is silent or its sent packet hasn't arrived at the tester side. This allows the tester to perform non-blocking interactions, instead of waiting for the SUT which might cause starvation.

Figure 4.12 shows the backtracking algorithm. It interacts with the SUT and checks whether the observations can be explained by the nondeterministic tester model. That is, checking whether the tester has an execution path that matches its interactions. This is done by maintaining a list of all possible branches in the tester, and checking if any of them accepts the observation.

The tester exhibits two kinds of randomness: (1) When sending a request packet to the SUT, it generates the packet randomly with GenPacket; (2) When the nondeterministic tester model branches, the deterministic tester randomly picks one branch to evaluate, using GenBool:

```
Variant genE: Type → Type :=
  GenPacket : genE concrete_packet
| GenBool : genE bool.
```

The execution rule is defined as follows:

- 1. When the tester nondeterministically branches in Line 9, randomly pick a branch (k b) to evaluate, and push the other branch (k (negb b)) to the list of other possible cases.
- 2. When the current tester throws an exception in Line 11, it indicates that the current execution path rejects the observations. The tester should try to explain its observations with other branches of the tester model. If the others list is empty, it indicates that the observation is beyond the specification's producible behavior, so the tester should reject the SUT.

```
Notation tE := (clientE \oplus genE \oplus exceptE).
 2
3 CoFixpoint backtrack (current:
                                            itree ntE void)
                           (others: list (itree ntE void))
4
5
                : itree tE void :=
6
      match current with
 7
      | Impure e k \Rightarrow
        match e with
8
9
        | (|Or|)
                            \Rightarrow b \leftarrow trigger GenBool;;
10
                                backtrack (k b) (k (negb b)::others)
11
        | (||Throw msg)
                            \Rightarrow match others with
                                | other::ot' \Rightarrow backtrack other ot'
12
13
                                1 []
                                              ⇒ trigger (Throw msg)
14
                                end
15
        | (FromObserver|) ⇒ q ← trigger GenPacket;;
16
                                trigger (ClientSend q);;
17
                                let others' := expect FromObserver q others in
18
                                backtrack (k q) others'
19
        | (ToObserver|)
                            \Rightarrow
20
           oa \( \text{trigger ClientRecv;;} \)
21
           match oa with
22
           | Some oa ⇒ let others' := expect ToObserver a others in
23
                         backtrack (k a) others'
24
           | None
             match others with
25
             | other::ot' ⇒ backtrack other (ot'++[current]) (* postpone *)
26
27
             I []
                           \Rightarrow backtrack m
                                                []
                                                                    (* retry *)
28
             end
29
           end
30
        end
31
      | Pure vd ⇒ match vd in void with end
32
33
34 Definition tester_http: itree tE void :=
35
      backtrack nondet_tester_http [].
```

Figure 4.12: Backtrack execution of nondeterministic tester.

```
CoFixpoint match_observe {R} (e: observeE R) (r: R)
1
2
                                   (m: itree ntE (V * void))
3
               : itree ntE (V * void) :=
4
     match m with
5
      | Impure (oe|) k \Rightarrow
6
        match oe, e with
7
        | FromObserver, FromObserver
8
        | ToObserver \Rightarrow k r
9
        | _, _ ⇒ trigger (Throw ("Expect " ++ print oe
10
                                ++ " but observed " ++ print e))
11
12
      | Impure (|e0|) k | Impure (||e0) k \Rightarrow
13
        r0 ← trigger e0;;
14
        match_observe e r (k r0)
15
      | Pure (_, vd) ⇒ match vd in void with end
16
17
18
   Definition expect {R} (e: observeE R) (r: R)
19
      : list (itree ntE (V * void)) \rightarrow list (itree ntE (V * void))
20
      := map (match_observe e r).
```

Figure 4.13: Matching tester model against existing observation.

3. When the tester wants to observe a packet *from* itself, it generates a packet and sends it to the SUT in Line 16.

Notice that if the current branch is rejected and the tester backtracks to other branches, the sent packet cannot be recalled from the environment. Therefore, all other branches should be matched against this send event as well. This is done by the expect function.

As shown in Figure 4.13, (expect e r 1) matches every tester in list 1 against the observation e that has return value r. For each element  $m \in 1$ , if m's first observer event oe matches the observation e (Line 7 and Line 8), then match\_observe instantiates the tester's continuation function k with the observed result r. Otherwise, the tester throws an exception in Line 9, indicating that this branch cannot explain the observation because they performed different events.

4. When the current tester wants to observe a packet to itself, it triggers the ClientRecv event in Line 20. If a packet has indeed arrived, then it instantiates the current branch as well as other possible branches, in the same way as discussed in Rule (3).

If the tester hasn't received a packet from the SUT (Line 24), it doesn't reject the SUT, because the expected packet might be delayed in the environment. If there are other branches to evaluate (Line 26), then the tester postpones the current branch by appending it to the back of the queue. Otherwise, if the current branch is the only one that hasn't rejected, then the tester retries the receive interaction.

Notice that if the SUT keeps silent, then the tester will starve but won't reject, because (i) such silence is indistinguishable from the SUT sending a packet but delayed by the environment, and (ii) the SUT hasn't *exhibited* any violations against the specification. The starvation issue is addressed in Subsection 4.4.2.

The backtracking algorithm also explains the network composition design in Figure 4.11, where the server model is scheduled at a higher priority than the network model: Suppose the SUT has produced some invalid output, then every branch of the tester should reject its observation by throwing an exception. However, the network model is always ready to absorb packets. Evaluating the network model lazily prevents the composed symbolic model from having infinitely many absorbing branches. This allows the derived tester to converge to rejection upon violation.

Now we have derived the specification into a deterministic tester model in ITree. The tester's events reflect actual computations of a client program. In the next subsection, I'll translate the ITree model into a binary executable that runs on silicon and metal.

# 4.4.2. From ITree model to IO program

The deterministic tester model derived in Figure 4.12 is an ITree program that never returns (its result type void has no elements). It represents a client program that keeps interacting with the SUT until it reveals a violation and throws an exception.

In practice, if the tester hasn't found any violation after performing a certain amount of interactions, then it accepts the SUT. This is done by executing the ITree until reaching a certain depth.

```
1 Fixpoint execute (fuel: nat) (m: itree tE void) : IO bool :=
2
      match fuel with
                                              (* accept if out of fuel *)
3
      1 0
                 \Rightarrow ret true
4
      | S fuel' \Rightarrow
 5
        match m with
6
        | Impure e k \Rightarrow
7
           match e with
8
           | (||Throw _)
                               ⇒ ret false (* reject upon exception *)
9
           | (ClientSend q|) ⇒ client_send q;;
10
                                  execute fuel' (k tt)
11
           | (ClientRecv|)
                               ⇒ oa ← client_recv;;
12
                                  execute fuel' (k oa)
13
           | (|GenPacket|)
                               ⇒ pkt ← gen_packet;;
14
                                  execute fuel' (k pkt)
15
           | (|GenBool|)
                               \Rightarrow b \leftarrow ORandom.bool;;
16
                                  execute fuel' (k b)
17
18
        | Pure vd \Rightarrow match vd in void with end
19
        end
20
      end.
21
22
   Definition test_http: IO bool :=
23
      execute bigNumber tester_http.
```

Figure 4.14: Interpreting ITree tester to IO monad.

As shown in Figure 4.14, the execute function takes an argument fuel that indicates the remaining depth to explore in the ITree. If the execution ran out of fuel (Line 3), then the test accepts; If the tester model throws an exception (Line 8), then the test rejects. Otherwise, it translates the ITree's primitive events into IO computations in Coq [LYS: Cite Li-yao's SimpleIO library], which are eventually extracted into OCaml programs that can be compiled into executables that can communicate with the SUT over the operating system's network stack.

This concludes my validation methodology. In this chapter, I have shown how to test real-world systems that exhibit internal and external nondeterminism. I applied the dualization theory in Chapter 2 to address internal nondetermism, and handled external nondeterminism by specifying the environment's space of uncertainty. The specification is derived into an executable tester program, by multiple phases of interpretations. The derivation framework is built on the ITree specification language, but the method is applicable to other languages

that allow destructing and analyzing the model programs.

So far I have answered "how to tell compliant implementations from violating ones". The next chapter will answer "how to generate and shrink test input that reveal violations effectively", and unveil the techniques behind gen\_packet in Line 13 of Figure 4.14.

# CHAPTER 5

### TEST HARNESS DESIGN

A tester consists of a validator and a test harness. Chapters 2 and 4 have explained the validator's theory and practices. This chapter presents a language-based design for test harnesses. I'll show how to generate and shrink test inputs effectively, addressing interexecution nondeterminism.

Section 5.1 provides a brief overview of how test harnesses work. Section 5.2 explains how to write heuristics to generate interesting test inputs. Section 5.3 then shows how to keep the test inputs interesting among different executions in the shrinking process.

### 5.1. Overview

This section introduces the abstract architecture of an interactive tester, using the networked server as an example. I'll present a naïve implementation of the test harness, which will be improved in the following sections.

The test harness interacts with the environment and provides the observations for the validator. The validator may represent requests and responses as abstract datatypes for the convenience of specification. The test harness translates these abstract representations into bytes transmitted on the underlying channel.

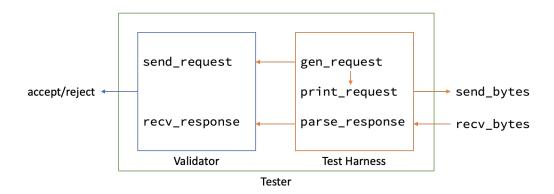


Figure 5.1: Tester architecture outline.

```
1 Definition gen_packet: IO concrete_packet :=
2
      src
                   ← random_conn;;
3
      method
                    ← oneof [Get; Put];;
4
      target
                    ← random_path;;
5
      precondition \( \to \) oneof [IfMatch, IfNoneMatch];;
6
                    \leftarrow \texttt{random\_etag;;}
      etag
7
      payload
                    ← random_string;;
8
      ret { Source
                         := src;
9
            Destination := server_conn;
10
            Data
                         := inr { Method
                                               := method;
11
                                   TargetPath := target;
12
                                               := [(precondition, etag)];
                                   Headers
13
                                   Pavload
                                               := payload
14
                                 }
15
          }.
```

Figure 5.2: Naïve generator for HTTP requests.

As shown in Figure 5.1, when the validator wants to observe a sent request, the harness generates the request and encodes it into bytes to send. Conversely, when the validator wants to observe a received response, the harness receives bytes from the environment and decodes it into abstract messages.

The generator is a randomized program that produces test inputs. One example is the gen\_packet function in Figure 4.14. The HTTP packets generator can be naïvely implementation as shown in Figure 5.2. It fills in the request's fields with arbitrary values, and has limited coverage of the SUT's behavior. This is because the request target and ETags are both generated randomly, and thus unlikely to hit the server's resource, resulting in 404 Not Found and 412 Precondition Failed in almost all cases.

To reveal more interesting behavior from the SUT, we should tune the generator's distribution to emphasize certain patterns of the test input. For example, if the tester knows what paths have the server stored resources, then it can generate more paths that correspond to existent resources; if the tester has observed some ETags generated by the server, then it can include these ETags in future requests. In the next section, I'll explain how to implement such heuristics in ITree-based testers.

### 5.2. Heuristics for Test Generation

This section implements heuristics for generating test inputs. I'll use the HTTP tester as an example to show how to make requests more interesting, by parameterizing them over the model state (Subsection 5.2.1) and the trace (Subsection 5.2.2).

# 5.2.1. State-based heuristics

The model state may instruct the test generator to produce more interesting test inputs. For example, consider the random\_path generator in Line 4 of Figure 5.2. One way to improve it is to generate more paths that have corresponding resources on the server:

Here I modify the server model's state type  $\sigma$  from (path  $\rightarrow$  resource) in Figure 4.5 into (list (path \* resource)), which has the same expressiveness but allows the generator to access the list of all paths in the server state. The generator chooses from these existent paths in 90% of the cases, as assigned by the freq combinator. The remaining 10% are still generated randomly, to discover how the SUT handles nonexistent paths.

For the gen\_packet generator in Figure 5.2, replacing its random\_path with the improved gen\_path would generate more interesting request targets. This requires the gen\_packet to carry the server state to instantiate gen\_path.

As shown in Figure 4.12, the GenPacket generator is triggered when the tester wants to observe a packet from itself to the SUT. fig:symbolic-observer then shows that such FromObserver expectation happens when the symbolic model Emits a packet. Such Emit event only happens when the server wants to receive a packet in Figure 4.10. The Recv events are triggered by the server model in Figure 4.5, which iterates over the server state  $\sigma$ .

Therefore, I extend the server's Recv event type to include the server state:

```
Variant qaE: Type \rightarrow Type := Recv : \sigma \rightarrow qaE packet | Send : packet \rightarrow qaE unit.
```

Now when the server wants to receive a request, it triggers (Recv state), where (state:  $\sigma$ ) contains the server's paths and resources at that point. The state argument is then carried to the generator, by adding parameters to the event types along the interpretation:

```
Variant netE: Type \rightarrow Type := Emit : packet \rightarrow netE unit | Absorb: \sigma \rightarrow netE packet.

Variant observeE : Type \rightarrow Type := FromObserver : \sigma \rightarrow observeE concrete_packet | ToObserver : observeE concrete_packet.

Variant genE: Type \rightarrow Type := GenPacket : \sigma \rightarrow genE concrete_packet | GenBool : genE bool.

Definition gen_packet: \sigma \rightarrow IO concrete_packet.
```

As a result, when instantiating the (GenPacket state) event in Figure 4.14, we can feed the gen\_packet function with argument state, so that gen\_path can generate interesting paths based on the server state.

#### 5.2.2. Trace-based heuristics

When the SUT makes internal choices e.g. generating ETags, the specification represents them as symbolic variables. These variables' concrete value are not stored in the specification state, but may be observed during execution. For example, when an HTTP server responds to a GET request, it might include the resource's ETag as shown in Subsection 1.2.1.

To improve the generator in Figure 5.2, we can generate interesting ETags based on the trace produced during execution. The trace is a list of packets sent and received by the tester, and the packets' payloads may include responses that have an ETag field. The gen\_etag function emphasizes ETags that were observed in the trace, which are more likely to match those generated by the SUT:

```
Definition gen_etag (trace: list concrete_packet) : IO string :=
  let etags: list string := tags_of trace in
```

```
freq [(90, oneof etags);
     (10, random_etag)].
```

To utilize this improved generator for ETags, the tester needs to record the trace of packets sent and received. This is done by modifying the execute function in Figure 4.14, adding an accumulator as the recursion parameter:

```
Fixpoint execute (fuel: nat) (trace: list concrete_packet)
                   (m: itree tE void) : IO bool :=
  match fuel with
  | S fuel' \Rightarrow
    match m with
    | Impure e k \Rightarrow
      match e with
      | (ClientSend q|) ⇒ client_send q;;
                              execute fuel' (trace ++ [q]) (k tt)
      | (ClientRecv|)
                         \Rightarrow oa \leftarrow client_recv;;
                              let trace' := match oa with
                                              | Some a \Rightarrow trace ++ [a]
                                              | None \Rightarrow trace
                                              end in
                              execute fuel' trace' (k oa)
      | (|GenPacket state|) ⇒ pkt ← gen_packet state trace;;
                                  execute fuel' trace (k pkt)
      ... (* similar to Figure 4.14 *)
```

When the tester sends or receives a packet, the packet is appended to the runtime trace.

Then the gen\_packet generator can take the trace accumulated so far, and feed it to the ETag generator:

```
Definition gen_packet (state: \sigma) (trace: list concrete_packet) := target \leftarrow gen_path state;; etag \leftarrow gen_etag trace;; ... (* same as Figure 5.2 *)
```

Now I've shown how to generate interesting test inputs by implementing state-based and trace-based heuristics. The next section explains how to shrink the test inputs while keeping them interesting, addressing inter-execution nondeterminism.

# 5.3. Shrinking Interactive Tests

Suppose we have generated a test input that has caused invalid observations of the SUT. The generated counterexample consists of (1) signals that are essential to triggering violations,

and (2) *noises* that do not contribute to revealing such violations. We need to shrink the counterexample by removing its noises and keeping its signals.

For interactive testing, the test input is a sequence of request messages. An intuitive way of shrinking is to remove some requests from the original sequence and rerun the test. However, rerunning an interesting request might produce trivial results, due to inter-execution nondeterminism discussed in Subsection 1.3.2.

To prevent turning signals into noises when rerunning the test, I shrink the heurestics instead of shrinking the generated test input. Subsection 5.3.1 introduces the architecture for interactive shrinking, then Subsection 5.3.2 explains the language design beneath that addresses inter-execution nondeterminism.

#### 5.3.1. Architecture

I propose a generic framework for generating and shrinking interactive tests. The key idea is to introduce an abstract representation for test inputs that embed trace-based heuristics. When shrinking the counterexample, the test harness picks a substructure of the abstract representation, and computes the corresponding test input using the new runtime trace.

For example, when generating a timestamp, instead of producing concrete value e.g. "Tue, 24 May 2022 06:35 the generator returns an abstract representation that says "use the timestamp observed in the last response". When rerunning the test, the timestamp is computed from the new trace e.g. "Wed, 25 May 2022 06:35:50 GMT".

The test generation and shrinking framework is shown in Figure 5.3. It refines the test harness box in Figure 5.1, and involves four languages, from right to left:

- 1. Byte representation, in which the tester interacts with the environment. This can be network packets, file contents, or other serialized data produced and observed by the tester.
- 2. Intermediate representation (IR), a generic language that abstracts the byte represen-

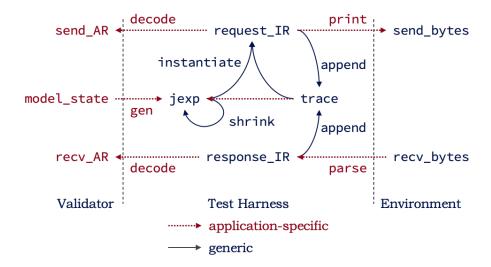


Figure 5.3: Test harness architecture.

tation as structured data. The test harness parses byte observations and records its trace in terms of the IR, which allows representing trace-based heuristics as a generic language i.e. J-expressions.

3. J-expression (Jexp), a symbolic abstraction of the IR. The IR corresponds to concrete inputs and outputs, whereas Jexp defines a computation from trace to IR. The generator provides test inputs in terms of Jexps; The test harness *instantiates* the generated Jexps into request IR, and *prints* them into byte representation.

When shrinking test inputs, the test harness shrinks the sequence of Jexps. The shrunk Jexps are then instantiated by the new trace during runtime.

The intermediate representation and J-expression will be further explained in Subsection 5.3.2.

4. Application representation (AR), including the request (Q), response (A), and state (S) types used for specifying the protocol. Specification writers can choose the type interface at their convenience, provided the request and response types are embeddable into the IR.

```
\begin{split} \mathsf{JSON}^\mathsf{T} &\triangleq \mathsf{T} \mid \{\mathsf{object}^\mathsf{T}\} \mid [\mathsf{array}^\mathsf{T}] \mid \mathsf{string} \mid \mathbb{Z} \mid \mathbb{B} \mid \mathsf{null} \\ \mathsf{object}^\mathsf{T} &\triangleq \varepsilon \mid \mathsf{"string"} : \mathsf{JSON}^\mathsf{T}, \mathsf{object}^\mathsf{T} \\ \mathsf{array}^\mathsf{T} &\triangleq \varepsilon \mid \mathsf{JSON}^\mathsf{T}, \mathsf{array}^\mathsf{T} \\ \mathsf{IR} &\triangleq \mathsf{JSON}^\mathsf{IR} \\ \mathsf{Jexp} &\triangleq \mathsf{JSON}^\mathsf{label}.\mathsf{Jpath}.\mathsf{function} \\ \mathsf{where} \; label \in \mathbb{N}, function \in \mathsf{IR} \to \mathsf{IR} \\ \mathsf{Jpath} &\triangleq \mathsf{this} \mid \mathsf{Jpath}\#index \mid \mathsf{Jpath}@field \\ \mathsf{where} \; index \in \mathbb{N}, field \in \mathsf{string} \end{split}
```

Figure 5.4: Intermediate representation and J-expression.

```
Notation labelT := nat.
Definition traceT := list (labelT * IR).

Context q1 q2 a1 a2 : IR.

Example labelled_trace: traceT :=
[(1, q1); (3, q2); (4, a2); (2, a1)].

Tester

q1

q2

a2

a1
```

Figure 5.5: Labelled trace example.

The testing framework implements protocol-independent mechanisms like recording the trace and shrinking counterexamples, based on the generic IR and Jexp languages. It can be used for testing various protocols, provided application-specific translations from IR to AR and between IR and bytes. The test developer needs to tune the generator that produces Jexps, encoding their domain knowledge as state-based and trace-based heuristics.

### 5.3.2. Abstract representation languages

I choose JSON as the IR in this framework, which allows syntax trees to be arbitrarily wide and deep, and provides sufficient expressiveness for encoding message data types in general.

The J-expression is an extension of JSON that can encode trace-based heuristics. As shown in Figure 5.4, a Jexp may include syntax (*label.Jpath.function*) that represents trace-based heuristics, specified as:

1. The *label* refers to an IR in the trace that the heuristics computes with. The test harness records the trace as a list of labelled messages, where requests are labelled odd,

```
(* a2 = *)
                                 Example second_file_mode: jpath :=
 "files": [
                                   this @ "files" # 2 @ "mode".
    {
      "name": "foo",
                                 Example mode_add_write (j: IR) : IR :=
      "mode": 755
                                   match j with
   },
                                    | JSON_Number n \Rightarrow
                                      JSON_Number (mode_bits_or 200 n)
      "name": "bar",
                                    I \rightarrow j
      "mode": 500
                                    end.
   }
 ],
                                 Example id (j: IR) : IR := j.
  "exitCode": 0
```

Figure 5.6: IR, Jpath, and heuristics function example.

and their responses are labelled as the next even number. Labelling messages allows locating them in the trace despite shrinking and inter-execution nondeterminism.

For example, consider the trace in Figure 5.5: If a trace-based heuristics is interested in q2's response a2, then it can be encoded as "compute the test input based on message labelled 4":

```
Context get_label: labelT \rightarrow traceT \rightarrow IR.

Compute get_label 4 labelled_trace.

(* = a2 : IR *)
```

Suppose the test input is shrunk by removing q1, the label for q2 remains unchanged as 3, so label 4 corresponds to the new response to q2:

```
Example new_trace: traceT :=
  [(3, q2); (4, a2')].

Compute get_label 4 new_trace.
(* = a2' : IR *)
```

As a result, the trace-based heuristics are preserved and adapted to new executions during the shrinking process.

2. The Jpath is a path in the IR's syntax tree, and refers to a substructure of the IR that the heuristics uses.

For example, suppose request q2 lists files in a directory using the POSIX 1s command, and its response a2 is encoded as the IR shown in Figure 5.6. The response IR is a JSON object whose "files" field is an array of objects, each has a "name" and a "mode" field. A heuristics can refer to the second file's mode bits by Jpath (this@"files"#2@"mode"), which will guide the test harness to locate its corresponding value:

```
Context get_jpath: jpath \rightarrow IR \rightarrow IR. Compute get_jpath second_file_mode a2. (* = JSON_Number 500 : IR *)
```

3. The function has type ( $IR \rightarrow IR$ ), and defines the computation based on the sub-IR located by the Jpath.

Consider the mode bits located in the previous example: If the heuristics wants to add write permission to the mode bits, it can do so with the mode\_add\_write function in Figure 5.6, which produces mode 700. Some heuristics might use the sub-IR 500 as-is, using the identity function id.

J-expression provides a generic interface for test developers to implement trace-based heuristics. For the aforementioned file system example, the tester can generate a request that changes the mode bits of an observed file, with the following Jexp:

```
(* e5 = *)
{
   "command": "chmod",
   "args": [
    4.(this@"files"#2@"mode").mode_add_write,
    4.(this@"files"#2@"name").id
]
}
```

To instantiate Jexps into request IR, the test harness substitutes all occurences of (l.p.f) in the Jexp with its corresponding IR computed from the runtime trace:

```
Definition eval (1: labelT) (p: jpath) (f: IR \rightarrow IR) (t: traceT) : IR := let a: IR := get_label 1 t in let j: IR := get_jpath p a in f j.
```

For example, given the runtime trace in Figure 5.5, with a2 is defined in Figure 5.4, the the above Jexp is instantiated into the following request:

```
(* instantiate e5 labelled_trace = *)
{
  "command": "chmod",
  "args": [ 700, "bar" ]
}
```

However, when rerunning the test, the new\_trace has a different response associated with label 4. The new response a2' might have fewer than 2 files in its payload. Moreover, the response a2' might have not appeared in the trace, due to delays in the environment.

To instantiate the original Jexp in such situations, I loosen the get\_jpath and get\_label functions when evaluating the heuristics:

1. When evaluating a Jpath starting with p#n, if p corresponds to an array with fewer than n elements, or the array's n-th element cannot properly evaluate the remaining path, then try continuing the evaluation with any other element in the array.

For example, consider evaluating (this@3#"bar") on the following IR's:

Here j2 doesn't have a third element, and j3's third element doesn't have field "bar". In these cases, get\_jpath chooses other elements in the two arrays, resulting in value 22 for j2, and 31 for j3.

2. When evaluating label 1 and Jpath p on a trace, if the message labelled 1 does not exist in the trace, or cannot evaluate Jpath p properly, then try continuing the evaluation with any other IR in the trace.

For example, consider evaluating J-expression 6. (this#20"foo").id on the following

traces:

```
Definition t1: traceT :=
  [(1,q1); (2,j2); (5,q2)].

Definition t2: traceT :=
  [(3,q1); (4,j3); (5,q2); (6,a2)].
```

Here t1 doesn't have a message labelled 6, probably caused by environment delays; t2 has label 6 but its corresponding message is an object rather than an array expected by the Jexp. In these cases, eval chooses other messages in the trace to evaluate, resulting in value 21 for t1, and 33 for t2.

By introducing loose evaluation of J-expressions, my test harness allows partial instantiation of heuristics when the runtime trace is less than satisfying.

So far I have shown how to generate and shrink interactive test inputs and address interexecution nondeterminism. In the next chapter, I'll combine this test harness design with the validator practice in Chapter 4, and evaluate these techniques by testing real-world systems like HTTP servers and file synchronizers.

# CHAPTER 6

### **EVALUATION**

This chapter evaluates the testing methodology presented in this thesis, by deriving testers from specifications and running them against systems under test.

I conduct the experiments on two kinds of systems, HTTP/1.1 server (Section 6.1) and file synchronizer (Section 6.2). The research questions are: (1) Qualitative: Is the tester useful to finding invalid behavior in the SUT? and (2) Quantitative: Can the tester reveal those invalid behavior quickly?

# 6.1. Testing Web Servers

This thesis is motivated by the Deep Specification project [3], whose goal is to build systems with rigorous guarantee of functional correctness, studying HTTP as an example. I formalized a subset of HTTP/1.1 specification, featuring WebDAV requests GET, PUT, and POST [11], ETag preconditions [14], and forward proxying [13].

From the protocol specification written as ITrees, I derived a tester client that sends and receives network packets. Subsection 6.1.1 explains the system under test and the experiment setup. Subsection 6.1.2 and Subsection 6.1.3 then describe the evaluation results qualitatively and quantitatively.

# 6.1.1. Systems Under Test

I ran the derived tester against three server implementations:

- Apache HTTP Server [12], which is among the most popular servers on the World Wide Web [28, 38]. I used the latest release 2.4.46, and edited its configuration file to enable WebDAV and proxy modules.
- Nginx [33], the other most popular server. The experiment was conducted on the latest release 1.19.10, with only WebDAV module enabled, because Nginx doesn't

fully support forward proxying like Apache does.

• DeepWeb server developed in collaboration with Zhang et al. [41], supporting GET and POST requests. The server's functional correctness was formally verified, showing our methodology of specifying systems in testable and verifiable ways.

The tests were performed on a laptop computer (with Intel Core i7 CPU at 3.1 GHz, 16GB LPDDR3 memory at 2133MHz, and macOS 10.15.7). The Apache and Nginx servers were deployed as Docker instances, using the same host machine as the tester runs on. Our simple server was compiled into an executable binary, and also ran on localhost.

The tester communicates with the server via POSIX system calls, in the same way as over Internet except using address 127.0.0.1. The round-trip time (RTT) of local loopback is  $0.08 \pm 0.04$  microsecond (at 90% confidence).

## 6.1.2. Qualitative Result

Apache My tester rejected the Apache HTTP Server, which uses strong comparison for PUT requests conditioned over If-None-Match, while RFC 7232 specified that If-None-Match preconditions must be evaluated with weak comparison. [BCP: What are strong and weak comparison? [LYS: ETag jargons.]] I reported this bug to the developers, and figured out that Apache was conforming with an obsoleted HTTP/1.1 standard [15]. The latest standard has changed the semantics of If-None-Match preconditions, but Apache didn't update the logic correspondingly.

To further evaluate the tester's performance in finding other violations, I fixed the precondition bug by deleting 13 lines of source code and recompiling the container.

The tester accepted the fixed implementation, which can be explained in two ways: (1) The server now complies with the specification, or (2) The server has a bug that the tester cannot detect. To provide more confidence that (1) is the case, I ran the tester against servers with

known bugs, created by mutating the Apache source code manually.<sup>1</sup>

The tester rejected all 20 bugs, located in various modules of the Apache server: core, http, dav, and proxy. They appear both in control flow (e.g., early return of handler function, skipped precondition check) and in data values (e.g., calling functions with wrong parameters, flipping bits in computations, accessing buffer off by one byte). Some mutants took the tester longer time to reveal than others, which will be discussed in Subsection 6.1.3.

Nginx When testing Nginx, I found that its WebDAV module did not check the If-Match and If-None-Match preconditions of PUT requests. I then browsed the Nginx bug tracker and found a ticket opened by Haverbeke [18], reporting the same issue with If-Unmodified-Since preconditions.

This issue has been recognized by the developers in 2016 but never resolved. One possible reason is that the current architecture of Nginx makes it difficult for the WebDAV module to utilize the precondition checker in the HTTP core module.

A fix to this bug would involve either restructuring the modules or copying source code from one module to another, unlike simply removing bad code in Apache, so I only tested mutants for the latter.

**DeepWeb** My test derivation framework was developed in parallel with the DeepWeb server. After my collaborators finished the formal proof of the server's functional correctness, I tested the server with my derived tester. The tester has revealed a liveness issue—when a client pipelines more than one requests in a single connection, the server may hang without processing the latter requests.

This liveness bug was out of scope for the server's functional correctness, which only requires the server not to send invalid messages. Such partial correctness may be trivially satisfied by a silent implementation that never responds. My experiments has shown this limitation

<sup>&</sup>lt;sup>1</sup>I didn't use automatic mutant generators because (i) Existing tools could not mutate all modules I'm interested in; and (ii) The automatically generated mutants could not cause semantic violations against my protocol specification.



Figure 6.1: Cost of detecting bug in each server implementation. The left box with median line is the tester's execution time before rejecting the server, which includes interacting with the server and checking its responses. The right bar with median circle is the number of HTTP/1.1 messages sent and received by the tester before finding the bug. Results beyond 25%-75% are covered by whiskers.

in formal verification, and guided the debugging of the server implementation.

These results show that my tester is capable of finding different kinds of bugs in server implementations, within and beyond functional correctness. Next I'll evaluate how long the tester takes to reveal bugs.

### [LYS: Under construction:]

# 6.1.3. Quantitative Result

To answer Research Question (2) at the beginning of this chapter, I measure the execution time and network interactions taken to reject vanilla Apache and its mutants, as shown in Figure 6.1. The 20 mutants are named after the module where I inserted the bug. The tester rejected all the buggy implementations within 1 minute, and in most cases, within 1 second. This does not include the time for shrinking the counterexample.

Some bugs took longer time to find, and they usually required more interactions to reveal.

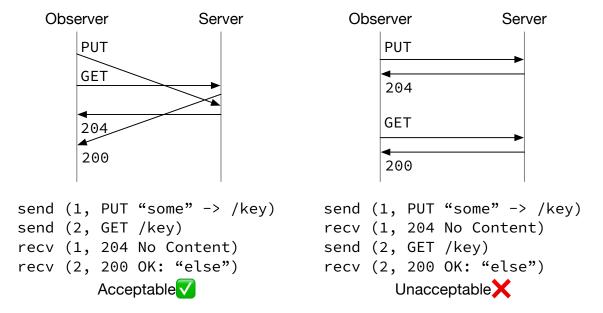


Figure 6.2: GET-after-PUT bug pattern in Apache mutants. The trace on the left does not convince the tester that the server is buggy, because there exists a certain network delay that explains why the PUT request was not reflected in the 200 response. When the trace is ordered as shown on the right, the tester cannot imagine any network reordering that causes such observation, thus must reject the server.

This may be caused by (1) The counter-example has a certain pattern that my generator didn't optimize for, or (2) The tester did produce a counter-example, but failed to reject the wrong behavior. I determine the real cause by analyzing the bugs and their counterexamples:

Mutants 19 and 20 are related to the WebDAV module, which handles PUT requests
that modify the target's contents. The buggy servers wrote to a different target from
that requested, but responds a successful status to the client.

The tester cannot tell that the server is faulty until it queries the target's latest contents and observes an unexpected value. To reject the server with full confidence, these observations must be made in a certain order, as shown in Figure 6.2.

 Mutant 18 is similar to the bug in vanilla Apache: the server should have responded with 304 Not Modified, but sent back 200 OK instead. To reveal such violation, a minimal counterexample consists of 4 messages:

- 1. GET request,
- 2. 200 OK response with some ETag "x",
- 3. GET request conditioned over If-None-Match: "x", and
- 4. 200 OK response, indicating that the ETag "x" did not match itself.

Notice that (2) must be observed before (3), otherwise the tester will not reject the server, with a similar reason as Figure 6.2.

• Mutant 5 causes the server to skip some code in the core module, and send nonscence messages when it should respond with 404 Not Found. The counterexample can be as small as one GET request on a non-existential target, followed by a non-404, non-200 response. However, my tester generates request targets within a small range, so the requests' targets are likely to be created by the tester's previous PUT requests.

Narrowing the range of test case generation might improve the performance in aforementioned Mutants 18–20, but Mutant 5 shows that it could also degrade the performance of finding some bugs.

• The mutants in proxy module caused the server to forward wrong requests or responses.

To test servers' forward proxying functionality, the tester consists of clients and origin servers, both derived by dualization. When the origin server part of the tester accepts a connection from the proxy, it does not know for which client the proxy is forwarding requests. Therefore, the tester needs to check the requests sent by all clients, and make sure none of them matches the forwarded proxy request.

The more client connections the tester has created, the longer it takes the tester to check all connections before rejecting a buggy proxy.

These examples show that the time-consuming issue of some mutants are likely caused by the generators' heuristics. Cases like Mutant 5 can be optimized by state-based heuristics

```
Inductive node := 

File : content \rightarrow node 

| Directory : list (name*node) \rightarrow node.

Context read : path \rightarrow node \rightarrow option content. 

Context write: path \rightarrow content \rightarrow node \rightarrow option node. 

Context mkdir: path \rightarrow node \rightarrow option node. 

Context ls : path \rightarrow node \rightarrow list name. 

Context rm : path \rightarrow node \rightarrow option node.
```

Figure 6.3: File system specification.

in Subsection 5.2.1; Proxy-related bugs can be more easily found by trace-based heuristics in Subsection 5.2.2; For Mutants 18–20, the requests should be sent at specific time periods so that the resulting trace is unacceptable per specification, which is discussed in Chapter 8.

# 6.2. Testing file synchronizer

To demonstrate the generality of my specification-based testing methodology, I applied it to file synchronizers. Subsection 6.2.1 introduces my specification of the file system and synchronization semantics. From these specifications, I derived a tester program for the Unison file synchronizer [30], with results shown in Subsection 6.2.2.

### 6.2.1. System Under Test

A file synchronizer manipulates the file system to reconcile updates in different replicas [6]. To check a synchronizer's correctness, the tester needs to update replicas, launch the synchronization process, and observe the propagated updates.

My specification consists of two parts:

1. A file system model represented as a tree, where the leaves are files and the branches are directories. As shown in Figure 6.3, the file system model is a simplified abstraction from the POSIX file interface, ignoring metadata and file permissions. Specifying more aspects of the file system is discussed in Chapter 8.

Based on the file system model, I specified five basic file operations the tester may perform: (i) reading contents from a file, (ii) writing contents to a file, (iii) creating a

new directory, (iv) listing entries under a directory, and (v) removing a file or directory recursively.

Some file operations may fail *e.g.* when reading from a path that refers to a directory. These failures are represented as return value (None: option \_) in the node functions.

2. A file synchronizer model that syncs updates between two replicas, implementing the reconcilation algorithm by Balasubramaniam and Pierce [6]:

```
Definition \sigma := node*node*node.
```

```
Context reconcile: \sigma \rightarrow \sigma.
```

Notice that the reconcile function manipulates three replicas. This is because the synchronizations might be partial: Upon write-write and write-delete conflicts, the synchronizer does not propagate the conflicting updates, and leaves the dirty files untouched in both replicas.

The third parameter of the reconcile function represents the subset of the two replicas that were synchronized: (reconcile (a,b,g)) syncs replicas a and b based on their previous consensus g. The consensus is initially empty, and updated when a change in one replica is propagated to another, or the two replicas have made identical changes.

Having specified the file system interface and the reconcilation semantics, I modelled the SUT as a deterministic QA server described in Definition 2.6. As shown in Figure 6.4, the request type Q can be file operations or the synchronization command; the response type A carries the return value of file system queries, or the transactions' exit code. For example, when synchronizing the two replicas, code 1 indicates partial synchronization with conflicts unresolved, and code 2 means the synchronizer has crashed due to uncaught exceptions or interruptions.

The QA model for the file system+synchronizer was dualized into a tester program that makes system calls to manipulate files, launch the synchronizer, and observe the updates. The system calls are made one at a time, and the file synchronizer is run as a foreground

```
(* file operations *)
  Variant F :=
 Fls
         (p: path)
| Fread (p: path)
| Fwrite (p: path) (c: content)
| Fmkdir (p: path)
| Frm
         (p: path).
Variant R := R1 | R2. (* replicas
Variant Q :=
                     (* query type
  QFile (r: R) (f: F)
| QSync.
                      (* response type *)
Variant A :=
        (1: list name)
| Aread (c: content)
                      (* exit code
| Aexit (z: Z).
```

Figure 6.4: Query and response types for testing file synchronizer.

process that blocks other interactions. Testing the synchronizer as a nonblocking background process is discussed in Chapter 8.

# 6.2.2. Experiment Results

The tester has revealed two features of the Unison file synchronizer, and I reported them to the developers. By analyzing the program's behavior, the developers determined that Unison did not violate its specification, which allows a wider set of behavior than my specification defines. The revealed features are as follows:

Synchronizing read-only directories When the tester creates a directory in one replica with read and execution permission (mode 500) and calls the synchronization command, Unison crashed without creating the corresponding directory in the other replica.

The crashing behavior only occurs on macOS, and is caused by Unison's mechanism for propagating changes: When copying directory foo from replica A to replica B, the synchronizer first creates a temporary directory "B/.unison.foo.xxxx.unison.tmp", and then renames it to "B/foo". The rename implementation in macOS requires write permission to proceed, so the change was not propagated.

This issue is not considered a violation in Unison or macOS, because: (1) Unison is allowed to halt without propagating an expected change, as long as its exit code has indicated an error, and no unexpected change was propagated. (2) The POSIX specification [21] says the rename function may require write access to the directory.

Despite being compliant to the specification, this feature in Unison is considered a defect, as it disables synchronization of read-only files and directories. A potential fix might be substituting rename with other system calls.

This defect was revealed by accident: My file system specification in Figure 6.3 does not mention file permissions, so I defaulted to mode 755. However, when implementing the test executor, I made a typo that wrote the permission as hexadecimal 0x755 while it should be octal 0o755. This caused the created directory to have mode bits 525, which triggered the aforementioned behavior.

This experiment shows that my current abstraction of the file system is worth expanding to include more information like file permissions, which might reveal other features of the file synchronizer.

The experiment also reveals a challenge in specifying programs, that the underlying operating system might also pose uncertainty to the program's behavior. Such external nondeterminism may be handled by parameterizing the program's specification over the OS's, in a similar way as composing the server model with the network model in Section 4.3.

Detecting write-delete conflict Suppose replicas A and B have a synchronized file foo.txt. If the tester deletes A/foo.txt and writes to B/foo.txt, then according to the specification, the synchronizer should detect this conflict and halt with exit code 1. During the tests, Unison did not notice that B/foo.txt was changed, and decided to propagate the deletion from replica A to replica B.

This behavior is caused by Unison's "fastcheck" feature that improves the performance at the risk of ignoring conflicts. With fastcheck enabled by default on \*nix systems, the synchronizer detects file modifications by checking if their timestamps have changed. When the tester writes to the files with short intervals, the timestamps might remain unchanged, so the synchronizer treats the written file as unmodified. Such behavior can be avoided by updating the file contents after a longer interval.

Notice that although Unison decided to propagate the file deletion, it does check the file contents before deleting it. As a result, the Unison process crashed and complained that B/foo.txt was modified during synchronization.

If the fastcheck feature was disabled, then Unison can detect the conflict by comparing the file contents bit-by-bit. It'll propagate no updates and leave the two replicas as-is, which results the same as enabling fastcheck but at lower performance.

This experiment shows that the executor may affect the test result by interacting with the SUT slowly or quickly. It is worth expanding the test harness to allow different configurations for executing the tests.

So far I have demonstrated the effectiveness of my testing methodology, by deriving testers that can reveal violations and interesting caveats in real-world systems like web servers and file synchronizers. In the following chapters, I'll discuss related works in specifying and testing interactive systems, as well as potential improvements that can be made.

### CHAPTER 7

### RELATED WORK

The area of automated testing is well-studied, diverse, and difficult to navigate [1]. This chapter explores methodologies in specifying and testing interactive systems. I focus on techniques that have been practised in testing real-world programs. Section 7.1 compares different specification techniques and their derived validators. Section 7.2 then discusses practices in developing test harnesses.

# 7.1. From Specifications to Validators

Different testing scenarios exhibit various challenges that motivate the specification design. This section partitions the validation techniques by the languages used for developing the specifications.

# 7.1.1. State machine specification: Quviq QuickCheck

Property-based testing with QuickCheck has been well adopted in industrial contexts [19]. The specification is a boolean function over traces *i.e.* the validator. My solutions to addressing internal and external nondeterminism are inspired by practices in QuickCheck.

Internal nondeterminism My HTTP/1.1 specification was initially written as a Quick-Check property. Before handling preconditions like If-Match and If-None-Match, the validator implements a deterministic server model and compares its behavior with the observations, as shown in the validate function in Section 1.1. When expanding the specification to cover conditional requests, I implemented the ad hoc validator by manually translating the trace into tester-side knowledge, as shown in Figure 1.1.

The complexity in describing "what behavior is valid" motivates me to rephrase the specification. I applied the idea of model-based testing [9], and specified the protocol in terms of "how to produce valid behavior". My specification represented internal nondeterminism with symbolic variables. The validator then checks whether the trace is producible by the symbolic specification, by reducing the producibility problem to constraint solving.

External nondeterminism Hughes et al. [20] have used QuickCheck to test Dropbox. The specification does not involve internal nondeterminism, but does handle external nondeterminism that local nodes may communicate with the server at any time. This is done by introducing "conjectured events" to represent the possible communications. The validator checks if the conjectured events can be inserted to somewhere in the trace to make it producible by the model.

To specify servers' allowed observations delayed by the network, Koh et al. [22] introduced the concept of "network refinement". The network may scramble the traces by delaying some messages after others, with one exception: If the client has received response A before it sends request Q, then by causality, the server-side trace must have sent response A before receiving request Q. Upon observing a client-side trace T, our QuickCheck validator searches for a server-side trace that (i) can be reasonably scrambled into trace T, and (ii) complies with the protocol specification.

My network model design in Section 4.3 was inspired by these idea of conjecturing the environment's behavior. Instead of inserting conjectured communication events or reordering the trace, I specified the network as an independent module and composed it with the server specification. This provides more flexibility in specifying the environment *e.g.* limiting the buffer size or the number of concurrent connections, and allows reusing the network models for specifying other protocols on top of it.

### 7.1.2. Process algebra: LOTOS and TorXakis

Language of Termporal Ordering Specification (LOTOS) [8] is the ISO standard for specifying OSI protocols. It defines distributed concurrent systems as *processes* that interact via *channels*. Using a formal language strongly inspired by LOTOS, Tretmans and van de Laar [35] implemented a test generation tool called TorXakis, and used it for testing Dropbox.

TorXakis supports internal nondeterminism by defining a process for each possible value.

This requires the space of invisible values to be finite. In comparison, I represented invisible values as symbolic variables, and employed constraint solving that can handle inifitite space of data like strings and integers.

As for external nondeterminism, TorXakis hardcodes all channels between each pair of processes, assuming no new process joins the system. Whereas in my network model, "channels" are the "source" and "destination" fields of network packets, which allows specifying a server that exposes its port to infinitely many clients.

### 7.1.3. Transition systems: NetSem and Modbat

Using labelled transition systems (LTS), Bishop et al. [7] have developed rigorous specification for TCP, UDP, and the Sockets API. To handle internal nondeterminism in real-world implementations, they symbolized the model states, which is then evaluated with a special-purpose model symbolic model checker. They focused on developing a post-hoc specification that matches mainstream systems like FreeBSD, Linux, and WinXP, while I aim at finding bugs in rapidly evolving implementations, and borrowed the idea of symbolic evaluation in validating observations.

Artho and Rousset [4] have generated test cases for Java network API, which involves blocking and non-blocking communications. Their abstract model was based on extended finite state machines (EFSM), and could capture bugs in the network library <code>java.nio</code>. Their validator rejects the SUT upon unexpected exceptions or observations that fail its <code>encoded</code> assertions. In comparison, assertions in my validator are <code>derived</code> from the abstract model, which covers full functional correctness of the SUT.

### 7.2. Test Harnesses

This section explores techniques of generating and shrinking test inputs. Subsection 7.2.1 compares different heuristics used by test generators; Subsection 7.2.2 explains existing shrinking techniques for interactive testing scenarios. The executor of test harnesses is beyond the scope of this thesis, and will be discussed in Chapter 8.

#### 7.2.1. Generator Heuristics

In addition to state-based and trace-based heuristics discussed in Section 5.2, other kinds of heuristics can be applied to generating inputs for various testing scenarios.

Constraint-based heuristics The reason for introducing heuristics is to increase the chance of triggering invalid behavior. I specified the heuristics as "how to produce interesting input", while in some cases, it's more convenient to specify "what inputs are interesting". For example, well-typed lambda expressions can be easily defined in terms of typing rules, but are less intuitive to enumerate by a generator.

Narrowing [2] allows generating data that satisfy certain constraints. Lampropoulos et al. [24] have applied the idea of narrowing to the QuickChick testing framework in Coq [23], representing constraints as inductive relations. The relations are compiled into efficient generators that produce satisfying data.

The narrowing generator in QuickChick has been used during my preliminary experiment with HTTP/1.1, where I defined a well-formed relation for HTTP requests to guide the generator. This constraint-based heuristics can be integrated to my testing framework by interpreting QuickChick's Gen (generator) monad into the IO monad used by the test harness.

Coverage-based heuristics Another strategy to increase the chance of revealing invalid behavior is to cover more execution paths of the SUT. This idea is applied to fuzz testing [27], with popular implementations AFL [40] and Honggfuzz [32], and combined with property-based testing by Lampropoulos et al. [25].

Coverage-based testers mutate the test inputs and observe the programs' execution paths. An input is considered interesting if it causes the program to traverse a previously unvisited path. The interesting inputs will be mutated and rerun to cover potentially more paths.

To track the program's execution paths, coverage-based heuristics need to instrument the SUT during compilation, making it inapplicable for black-box testing. When fuzzing interactive systems like web servers, the SUT is run in a simulator where the requests are provided

as files instead of network packets. The responses are ignored in fuzz testing, which does not check functional correctness. To produce a trace for validation, the SUT needs to be carefully modified to record its send and receive events. Addressing these challenges would enable coverage-based heuristics to be integrated in interactive testing of systems' functional correctness.

# 7.2.2. Shrinking Interactive Tests

To address inter-execution nondeterminism in Quviq QuickCheck, Hughes [19] introduced the idea of shrinking abstract representations of test input. The tester first generates a *script* using state-based heuristics, and instantiates the script with the tester's runtime state. The scripts can be shrunk and adapted to new runtimes when rerunning the test.

The language design of my test harness is inspired by the QuickCheck approach, and extends it in two dimensions:

- 1. The QuickCheck framework assumes synchronous interactions, where the requests are function calls that immediately return. When testing asynchronous systems *e.g.* networked servers, the responses might be indefinitely delayed by the environment, which would block the QuickCheck tester's state transition.
  - To generate test inputs asynchronously, I implemented a non-blocking algorithm for instantiating scripts into requests. When a dependant observation is absent due to delays or loss by the environment, the test harness tries to instantiate the request using other observations, instead of waiting for the observation from the environment.
- 2. QuickCheck requires the test developer to specify a runtime state to guide the generator, and define the state transition rules for each interaction.
  - In comparison, I proposed trace-based and state-based heuristics as separate concepts. Generators in my testing framework are based on (i) traces recorded automatically during runtime, and (ii) model states exposed by the underlying specifications. The generic intermediate representation of traces lifts the requirement of specifying tran-

sitions for test generation purposes.

### CHAPTER 8

#### CONCLUSION AND FUTURE WORK

This thesis presents a systematic technique for testing interactive systems with uncertain behavior. I propose a theory of dualizing protocol specification into validators, with formal guarantee of soundness and completeness (Chapter 2). To test systems in real-world practices, I applied the dualization theory to the interaction tree specification language, and derived specifications into interactive testing programs (Chapter 4). I then presented a test harness design to generate and shrink interactive test inputs effectively (Chapter 5). The entire methodology is evaluated by revealing programs' incompliant behavior with derived testers (Chapter 6).

To address challenges posed by internal, external, and inter-execution nondeterminisms, I introduced various flavors of symbolic abstract interpretation: Systems' internal choices are represented as symbolic variables and unified against the tester's observations (??, Section 4.2); Possible impacts made by the environment are represented as nondeterministic branches (Section 4.3), and determined by backtrack searching (Section 4.4); The test inputs are generated as symbolic intermediate representations that can adapt to different traces during runtime (Section 5.3).

The technique in this thesis can be expanded in scenario and by combination:

- 1. Specifying and testing other kinds of SUTs in various setups e.g. background monitoring processes, distributed locks, cyber-physical systems etc. These attempts might expose the limitations of my methodology or introduce new challenges in testing.
- 2. Integrating other testing techniques to the framework e.g. tuning the executor to capture time-related violations [31], find bugs with fewer tests by enumerating within a small input space [17], etc. This may enhance my testers' effectiveness or reveal potential improvements that existing techniques can make.

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